Low Complexity Near Optimal Hybrid Detectors for Large-Scale MIMO Uplink Systems Based on Complex Support Vector Regression

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November 2015

A thesis submitted to McGill University in partial fulfillment of the requirements for the degree of Master of Engineering.

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Abstract

This report describes the use of LATEX to format a thesis. A number of topics are covered: content and organization of the thesis, LATEX macros for controlling the thesis layout, formatting mathematical expressions, generating bibliographic references, importing figures and graphs, generating graphs in MATLAB, and formatting tables. The LATEX macros used to format a thesis (and this document) are described.

Acknowledgments

Thesis regulations require that contributions by others in the collection of materials and data, the design and construction of apparatus, the performance of experiments, the analysis of data, and the preparation of the thesis be acknowledged.

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List of Acronyms

16-QAM 16-point Quadrature Amplitude Modulation

3GPP Third Generation Partnership Project
 3GPP2 Third Generation Partnership Project 2
 64-QAM 64-point Quadrature Amplitude Modulation

ADSL Asymmetric Digital Subscriber Line

ARQ Automatic Repeat Request

WPAN Wireless Personal Area Network

Chapter 1

Introduction

1.1 Large MIMO system

One of the biggest challenges the researchers and industry practitioners are facing in wireless communication area is how to bridge the sharp gap between increasing demand of high speed communication of rich multimedia information with high level Quality of Service (QoS) requirements and the limited radio frequency spectrum over a complex space-time varying environment. The promising technology for solving this problem, Multiple Input Multiple Output (MIMO) technology has been of immense research interest over the last several tens of years is incorporated into the emerging wireless broadband standard like 802.11ac [1] and long-term evolution (LTE) [2]. The core idea of MIMO system is to use multiple antennas at both transmitting and receiving end, so that multiplexing gain (multiple parallel spatial data pipelines that can improve spectrum efficiency) and diversity gain (better reliability of communication link) are obtained by exploiting the spatial domain [47]. Large-Scale MIMO system (LS-MIMO) is an upgraded version of conventional MIMO technology employing hundreds of low power low price antennas at base station (BS), that serves several tens of terminals simultaneously. This technology can achieve full potential of conventional MIMO systems including significant link reliability and throughput benefits. Nonetheless, the LS-MIMO systems have been shown to enjoy some distinct advantages that are not available in small-scale MIMO systems such as additional power efficiency as well as system robustness to both unintended man-made interference and intentional jamming. [3] [4].

1.2 Large MIMO detections

The price paid for LS-MIMO system is the increased complexities for signal processing at both transmitting and receiving ends. The uplink detector is one of the key components in a large MIMO system. With orders magnitude more antennas at the BS, benefits and challenges coexist in designing of detection algorithms for the uplink communication of large MIMO systems. On one hand, a large number of receive antennas provide potential of large diversity gains, on the other hand, complexities of the algorithms become crucial to make the system practical.

Vertical Bell Laboratories Layered Space-Time (V-BLAST) architecture for MIMO system can achieve high spectrum efficiency by spatial multiplexing (SM), that is, each transmit antenna transmits independent symbol streams. However the optimal maximum likelihood detector (MLD) for V-BLAST systems that perform exhaustive search over the transmit symbol vector space has a complexity that increases exponentially with the number of transmitted antennas, which is prohibitive for practical applications.

In order to alleviate this problem, linear detectors (LD) such as zero-forcing (ZF) and minimum mean square error (MMSE) aided by successive interference cancellation with optimal ordering (ZF-OSIC, MMSE-OSIC) are exploited in V-BLAST architecture [5] [6] [7], although ZF-OSIC and MMSE-OSIC can provide significant improvement comparing to their LD counterparts, a common drawback of SIC aided LD is the error propagation effect, which can not be eliminated by ordering. That results in inferior performances comparing to MLD [8] [9] [10].

Sphere Decoder (SD) [11] is the most prominent algorithm that utilizes the lattice structure of MIMO systems, which can achieve optimal performance with relatively much lower complexity comparing to MLD. However, SD has two major shortages that make it problematic to be integrated into a practical systems. The first shortage is SD has various complexities under different signal to noise ratios (SNR), while a constant processing data rate is required for hardware. The second shortage is the complexity of SD still has a lower bound that increases exponentially with the number of transmit antennas and the order of modulation scheme [12]. The fixed complexity sphere decoder (FCSD) [13] makes it possible to achieve near optimal performance with a fixed complexity under different values of SNR. The FCSD inherits the principle of list based searching algorithms, which first generate a list of candidate symbol vectors and then the best candidate is chosen as the solution. The other sub optimal detectors belong to this class include Generalized Parallel

Interference Cancellation (GPIC) [14] and Selection based MMSE-OSIC (sel-MMSE-OSIC) [15]. However, all these list based searching algorithms have the same shortage - their complexities increase exponentially with the number of transmit antennas and the order of modulation scheme [15]. Therefore, such algorithms are prohibitive when it comes to a large number of antennas or a high order modulation scheme, for example in IEEE 802.11ac standard [1], the modulation scheme is 256QAM.

Besides the above detection algorithms designed for conventional MIMO systems, in the last several years, a variety of metaheuristic based local search algorithms invoked from machine learning field [16] have been proposed for large MIMO systems. These algorithms have complexities that are comparable or slightly higher comparing to MMSE detector and near-optimal performance. Such algorithms include likelihood ascend searching (LAS) algorithm and variants [17] [18] [19] and Reactive Tabu search (RTS) algorithms and variants (e.g. Layered Tabu search (LTS) [20], Random Restart Reactive Tabu search (R3TS) [21]). Additionally, there are other algorithms proposed for large MIMO systems including Message passing technique based algorithms (e.g. Belief propagation (BP) detectors based on graphic model and Gaussian Approximation (GA) [22] [23] [24] [25]), Probabilistic Data Association (PDA) based algorithms [26], Monte Carlo sampling technique based algorithms (e.g. Multiple Restart- Mixed Gibbs Sampling (MR-MGS) algorithm [27]) and Element based Lattice Reduction (LR) aided algorithms [28].

Considering MIMO detection from a Combinatorial Optimization (CO) problem view-point, as powerful tool for solving CO problems, methoheuristic algorithms [29] are good choices for designing large MIMO detectors, driven by demand of achieving acceptable performance with significantly lower computational complexity. Besides the metaheuristic algorithms that based on local search strategies which use trajectory methods based on single solution, another class of metaheuristic algorithms is defined as population based. The population based metaheuristic algorithms deal with a population of candidate solutions. Intrinsically the population based metaheuristic algorithms can provide wider and more efficient exploration of search space. The major population based metaheuristic algorithms includes Evolutionary Computation (EC) and Ant Colony Optimization (ACO).

Genetic algorithm (GA) is one kind of EC algorithms, which are designed for CO problems. GA mimics the natural evolution process of a population and is powerful tool in searching a solution that is close enough to global optimum [30].

1.3 Support Vector Regression

Firmly grounded in framework of statistical learning theory or VC (Vapnik–Chervonenkis) theory, the Support Vector (SV) technique has become a powerful tool to solve real world supervised learning problems such as classification, regression and prediction. The SV method is a nonlinear generalization of Generalized Portrait algorithm developed by Vapnik in 1960s [31] [32], which can provide good generalization performance [33].

Interest in SV algorithms boosted since 1990s, promoted by the works of Vapnik and co-workers at AT& T Bell laboratory [34] [35] [36] [37] [38] [39]. Moreover, the kernel based methods [33] were proposed in order to extending the SV algorithms to nonlinear learning cases. The input data samples are mapped into some high dimensional feature space (also called Reproducing Kernel Hilbert Space (RKHS)) and then linear tools are applied to the feature mappings of the input data samples. This is equivalent to transforming the nonlinear learning tasks in the original space into the linear learning tasks in high dimensional feature space. The mathematical notion underlying kernel based methods is that of RKHS [33], in which the inner products of the feature mappings can be simply replaced by the computationally economical kernel functions. Because SV algorithms only deal with the inner products of the the feature mappings. Therefore, by kernel based methods, it is sufficient to use the specific kernel functions based on the RKHS discarding the actual structure of the feature space.

Based on the principle of structural risk minimization [40], the ϵ -SVR [36] [41] solves an original constraint optimization problem (primal objective problem) by transforming it into a Lagrange dual form (dual objective problem), which is a Quadratic Programming (QP) problem. Efficient methods for training SV algorithms which are based on large scale data sets were proposed, which is called decomposition. Decomposition process is performed by decomposing a large QP problem into a sequence of sub QP problems and solve them in an iterative manner [42] [43], Sequential Minimal Optimization (SMO) algorithm [44] is one of well known representatives of decomposition methods.

Complex valued signal arises in signal processing and digital communication areas etc. Therefore, developing signal processing algorithms which are suitable to be directly applied to complex valued systems is typically natural and concise choice. Furthermore, for MIMO systems, although one can transform the complex valued system model into an equivalent real valued system model, the detection algorithms built based on the complex valued model is more preferable due to the flexibility for signal constellation choice and hardware

implementations [45]. In recent years, a mathematical framework for pure complex valued SV algorithms was developed which can deal with complex valued tasks in signal processing, digital communication and related areas in an elegant and computational efficient manner [46].

1.4 Thesis Contribution

1.5 Thesis Outline

Chapter 2

Theoretical Analysis of Channel Hardening Phenomenon

2.1 System Model

Consider a uncoded complex large MIMO uplink spatial multiplexing (SM) system with N_t users, where each is equipped with transmit antenna. The number of receive antennas at the Base Station (BS) is N_r , $N_r \geq N_t$. Typically large MIMO systems have hundreds of antennas at the BS, as shown in Fig 2.1.

Bit sequences, which are modulated to complex symbols, are transmitted by the users over a flat fading channel. The discrete time model of the system is given by:

$$y = Hs + n, (2.1)$$

where $\mathbf{y} \in \mathbb{C}^{N_r \times 1}$ is the received symbol vector, $\mathbf{s} \in \mathbb{C}^{N_t}$ is the transmitted symbol vector, with components that are mutually independent and taken from a finite signal constellation alphabet \mathbb{O} (e.g. BPSK, 4-QAM, 16-QAM, 64-QAM), $|\mathbb{O}| = M$. The transmitted symbol vectors $\mathbf{s} \in |\mathbb{O}|^{N_t}$, satisfy $\mathbb{E}[\mathbf{s}\mathbf{s}^H] = \mathbf{I}_{N_t}E_s$, where E_s denotes the symbol average energy, $\mathbb{E}[\cdot]$ denotes the expectation operation, \mathbf{I}_{N_t} denotes identity matrix of size $N_r \times N_t$. Furthermore $\mathbf{H} \in \mathbb{C}^{N_r \times N_t}$ denotes the Rayleigh fading channel propagation matrix, each component is independent identically distributed (i.i.d) circularly symmetric complex Gaussian random variable with zero mean and unit variance. Finally, $\mathbf{n} \in \mathbb{C}^{N_r}$ is the additive white Gaussian noise (AWGN) vector with zero mean components and $\mathbb{E}[\mathbf{n}\mathbf{n}^H] = \mathbf{I}_{N_r}N_0$, where N_0 denotes the noise power spectrum density, and hence $\frac{E_s}{N_0}$ is the signal to noise ratio (SNR).

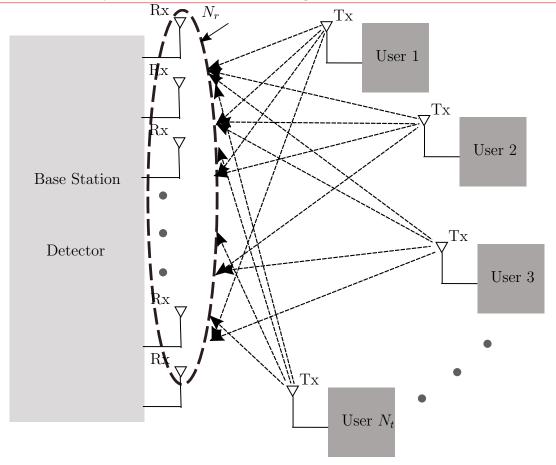


Fig. 2.1 Large MIMO uplink system

The task of a MIMO detector is to estimate the transmit symbol vector \mathbf{s} , based on the knowledge of receive symbol vector \mathbf{y} and channel matrix \mathbf{H} .

The Optimal Maximum Likelihood Detector (MLD) for MIMO system is given by

$$\hat{\mathbf{s}} = \min_{\mathbf{s} \in |\mathbb{O}|^{N_t}} ||\mathbf{y} - \mathbf{H}\mathbf{s}||^2, \tag{2.2}$$

Chapter 3

Complex Support Vector Preliminary Detector (CSVPD) for Large-Scale MIMO Uplink Systems

The key challenge in designing Large-Scale MIMO (LS-MIMO) detectors is to reduce complexities while maintaining high performances. Given the redundant diversity gain potential provided by LS-MIMO [47] that can only be achieved at very high Signal to Noise Ratio (SNR), one may consider to sacrifice the redundant diversity gains in order to reduce complexities. Furthermore, the ML criterion of MIMO detection stated in (2.2) indicates MIMO detection can be naturally classified as a Combinatorial Optimization (CO) problem, that consist of the search for the optimal solution in a discrete and finite set.

Based on the aforementioned situations, the metaheuristics algorithmic frameworks are of intense research interest in LS-MIMO detection in recent years. Metaheuristics refer to the high level algorithmic strategies that guide subordinate heuristics iteratively by combining different intelligent learning operations. Metaheuristics can explore and exploit the searching space efficiently and find near optimal solutions without costing high complexities. The class of algorithms includes but not restrict to Iterative Local Search (ILS), Tabu Search (TS), Simulated Annealing (SA), Genetic Algorithms (GA) and Ant Colony Optimization (ACO).

The single solution based metaheuristics which are also defined as trajectory methods, start from an initial solution and the search process performs on a single solution at any time as a trajectory in the searching space. In resent years, several single solution based metaheuristics algorithms are applied to LS-MIMO detection problem, such as

3 Complex Support Vector Preliminary Detector (CSVPD) for Large-Scale MIMO J. Phinko System Grant States shared by single solution based metaheuristics and gorithms is their performances are influenced by initial solution, the performances are improved when starting from a promising region of searching space

In this chapter, we proposed a complex support vector preliminary detector (CSVPD), which has a complexity comparable with linear detectors but performs much better. The proposed CSVPD can work in the complex valued Large-Scale MIMO (LS-MIMO) systems in an elegant and efficient manner. We exploit the specific widely linear regression model without constant offset, which is suitable for LS-MIMO systems model. Furthermore, based on the analysis of channel hardening phenomenon from Chapter 2 and the recent advances in machine learning field concerning decomposition process for SVM [48], we propose a combined single direction searching strategy in CSVR training process which can approximately maximize the gain of the sub dual objective functions whose work set size are two. The combined single direction searching strategy proposed can achieve a much smaller searching times than the optimal double direction searching while make dual objective function converge using as few iterations as the latter one.

Furthermore, we show that channel hardening phenomenon can be further exploited in CSVPD to reduce the computational complexity and simplify the implementation of the algorithm for LS-MIMO systems. Finally, we compare the performance of CSVPD aided likelihood ascend search (LAS) detector and CSVPD aided parallel interference cancellation with ordering (OPIC) detector with MMSE-LAS and MMSE-OPIC. These results demonstrate the potential of CSVPD to be utilized as a preliminary detector that can improve the LS-MIMO detectors whose performances are influenced by the reliability of initial solutions.

3.1 Brief Introduction to ϵ -Support Vector Regression (ϵ -SVR)

3.1.1 primal Objective Function

Suppose we are given a training data $((\mathbf{x}_1, y_1), (\mathbf{x}_2, y_2), \dots, (\mathbf{x}_L, y_L))$, L denotes the size of the training data set, $\mathbf{x}_i \in \mathbb{R}^V$ denotes input data vector, V is the number of features in \mathbf{x}_i . y_i denotes the output. Let \mathbf{w} denotes regression coefficient vector, $\Phi(\mathbf{x}_i)$ denotes the feature mapping of \mathbf{x}_i , $\mathbf{w}, \Phi(\mathbf{x}_i) \in \mathbb{R}^{\Omega}$, $\Omega \in \mathbb{R}$ denotes the dimension of mapped feature space (For linear model, $\mathbf{x}_i = \Phi(\mathbf{x}_i)$, $\Omega = V$). The regression estimate $g(\mathbf{x}_i)$ (either linear

$$g(\mathbf{x}_i) = \mathbf{w}^T \Phi(\mathbf{x}_i) + b \quad i = 1, 2, \dots, L$$
(3.1)

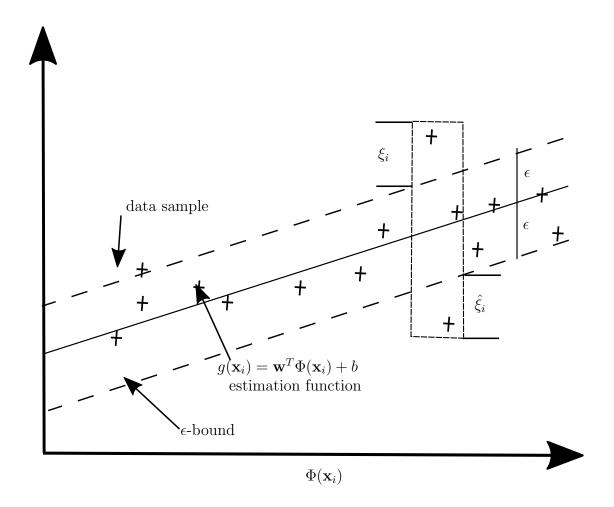


Fig. 3.1 Regression Model of ϵ -SVR

In ϵ -SVR, as shown in Fig 3.1, the solid line represents the regression estimate in 3.1, ϵ controls the precision of the regression, the area between two dash lines (ϵ -bound) is called ϵ -tube. Only the regression estimates that have the deviation larger than ϵ (the data points located outside ϵ -tube in Fig.3.1) denoted by ξ_i and $\hat{\xi}_i$, contribute to the estimation errors. the goal of ϵ -SVR is to minimize the risk introduced by estimate errors while keeping \mathbf{w}

3 Complex Support Vector Preliminary Detector (CSVPD) for Large-Scale MIMO III Plinka Systems regularized risk minimization principle, therefore, the printal constraint optimization problem is formulated as

$$\min_{\mathbf{w}, \xi, \hat{\xi}_i} f(\mathbf{w}, \xi_i, \hat{\xi}_i) = \frac{1}{2} ||\mathbf{w}||^2 + C \sum_{i=1}^{L} (R(\xi_i) + R(\hat{\xi}_i))$$

$$s.t. \begin{cases}
y_i - \mathbf{w}^T \Phi(\mathbf{x}_i) - b \leq \epsilon + \xi_i, i = 1, 2 \cdots, L \\
\mathbf{w}^T \Phi(\mathbf{x}_i) + b - y_i \leq \epsilon + \hat{\xi}_i, i = 1, 2 \cdots, L \\
\epsilon, \xi_i, \hat{\xi}_i \geq 0, i = 1, 2 \cdots, L
\end{cases} \tag{3.2}$$

In (3.2), $\frac{1}{2}||\mathbf{w}||^2$ is the regularization term in order to ensure the flatness of regression model. slack variables ξ_i and $\hat{\xi}_i$ are introduced based on the "soft margin" principle [37] that can cope with the infeasible constraints of the optimization problem and allows the existence of some additive noise to the observations. R(u) denotes the cost function. The simplest cost function is R(u) = u, The choice of the cost function is determined by the statistical distribution of the additive noise [41]. For example if the noise is Gaussian distributed, then the optimal cost function is $R(u) = \frac{1}{2}u^2$. The term $C \sum_{i=1}^{L} (R(\xi_i) + R(\hat{\xi}_i))$ denotes the penalty of the additive noise, $C \in \mathbb{R}$ and $C \geq 0$ that controls the trade off between regularization term and cost function term.

In ϵ -SVR, the objective to exploit slack variables ξ_i and $\hat{\xi}_i$ is to compensate the influences from the outliers that exceed the ϵ -tube which are caused by noise.

3.1.2 Cost Function

The optimal cost function $(R(\xi_i) + R(\hat{\xi}_i))$ in (3.2) can be derived based on maximum likelihood (ML) principle. Assume the data samples \mathbf{x}_i in data set are iid, Let $f_{true}(\mathbf{x}_i)$, $i = 1, 2, \dots, L$ denotes true regression function. the underlying assumption is $y_i = f_{true}(\mathbf{x}_i) + \varepsilon_i$, $i = 1, 2, \dots, L$, ε_i denotes additive noise of the *i*th data sample, with probability density function (pdf) $Pr(\cdot)$. Let $P(\cdot)$ denotes the pdf of y_i . Based on ML principle we want to

$$\max_{f} \prod_{i=1}^{L} P(y_i | f(\mathbf{x}_i)) = \prod_{i=1}^{L} P(f(\mathbf{x}_i) + \varepsilon_i | f(\mathbf{x}_i)) = \prod_{i=1}^{L} Pr(\varepsilon_i) = \prod_{i=1}^{L} Pr(y_i - f(\mathbf{x}_i))$$
(3.3)

$$\max_{f} \sum_{i=1}^{L} \log(Pr(y_i - f(\mathbf{x}_i))), \tag{3.4}$$

maximizing (3.4) is equivalent to minimizing $-\sum_{i=1}^{L} \log(Pr(y_i - f(\mathbf{x}_i)))$, therefore (3.3) is equivalent to

$$\min_{f} - \sum_{i=1}^{L} \log(Pr(y_i - f(\mathbf{x}_i))), \tag{3.5}$$

Let $c(\mathbf{x}_i, y_i, f(\mathbf{x}_i))$ denotes the cost function of *i*th input-out data sample, which is defined as

$$c(\mathbf{x}_i, y_i, f(\mathbf{x}_i)) \propto -\log(P(y_i - f(\mathbf{x}_i))).$$
 (3.6)

Thus (3.5) is equivalent to

$$\min_{f} \quad \sum_{i=1}^{L} c(\mathbf{x}_i, y_i, f(\mathbf{x}_i)), \tag{3.7}$$

In ϵ -SVR, in order to provide more flexibility to precision control, Vapnik's ϵ -insensitive function, as shown in (3.8), is applied to (3.5).

$$|u|_{\epsilon} = \begin{cases} 0 & if \quad |u| < \epsilon \\ |u| - \epsilon & otherwise \end{cases}$$
 (3.8)

Thus the final form of cost function in ϵ -SVR can be written as

$$\tilde{c}(y_i, \mathbf{x}_i, f(\mathbf{x}_i)) \propto -\log(Pr(|y_i - f(\mathbf{x}_i)|_{\epsilon})),$$
 (3.9)

the cost function term is determined according to the distribution of noise. In discrete time model of LS-MIMO systems, noise is AWGN, that is $-\log(Pr(\varepsilon_i)) \propto \frac{1}{2}\varepsilon_i^2$, based on (3.9), the cost function in LS-MIMO SVD defined as

$$c_{LS-MIMO}(\mathbf{x}_i, y_i, f(\mathbf{x}_i)) = \frac{(|y_i - f(\mathbf{x}_i)|_{\epsilon}^2)}{2}, \tag{3.10}$$

3 Complex Support Vector Preliminary Detector (CSVPD) for Large-Scale MLMORUPHINGS Systems ξ_i and $\hat{\xi}_i$ are used to cope with the outliers of ϵ -tube caused by additive noise, that is

$$\xi_i = \max(0, y_i - \mathbf{w}^T \Phi(\mathbf{x}_i) - b - \epsilon)$$
(3.11)

$$\hat{\xi}_i = \max(0, \mathbf{w}^T \Phi(\mathbf{x}_i) + b - y_i - \epsilon). \tag{3.12}$$

Because the deviation between the estimates $g(\mathbf{x}_i)$ and the observation y_i in 3.1 can only exceed the ϵ -tube in one direction, therefore there is at most one of ξ_i and $\hat{\xi}_i$ can be non zero. That is $\xi_i \hat{\xi}_i = 0$.

In conclusion, the cost function term in (3.2) can be defined as $R(u) = \frac{1}{2}u^2$, thus we have

$$R(\xi_i) + R(\hat{\xi}_i) = \frac{1}{2}\xi_i^2 + \frac{1}{2}\hat{\xi}_i^2 = \frac{1}{2}|y_i - f(\mathbf{x}_i)|_{\epsilon}^2$$
(3.13)

3.1.3 Dual Objective Problem

3.2 Combined Single Direction Searching Strategy

Decomposition methods were proposed to solve this QP problem by decomposing it into sub QP problems and solving them iteratively [44]. Therefore, the computational intensive numerical methods can be avoided. Decomposition is performed by sub set selection solver, which refers to a set of algorithms that separate the optimization variables (Lagrange multipliers) into two sets S and N, S is the work set and N contains the remaining optimization variables. In each iteration, only the optimization variables in the work set is updated while keeping other optimization variables fixed. The Sequential Minimal Optimization (SMO) algorithm [44] is an extreme case of the decomposition solvers. An important issue of the sub set selection solvers is the selection of the work set. One strategy is to choose Karush-Kuhn-Tucker (KKT) condition violators, ensuring the final converge [43]. The SMO algorithm restricts the size of the work set to two. A method to train SVM without offset was proposed In [48], with the comparable performance to the SVM with offset. A set of sequential single variable work set selection strategies, which require O(n)searching time are proposed. The optimal double variable work set selection strategy, which performs exhaustively searching, however, requires $O(n^2)$ searching time. The authors demonstrate that with the combination of two different proposed single variable work set selection strategies, convergence can be achieved by a iteration time that is as few as optimal double variable work set selection strategy.

3 Complex Support Vector Preliminary Detector (CSVPD) for Large-Scale MIMO In Plinka System dation of kernel based methods is RKHS which is defined in complex domain, however most of the practitioners are dealing with real data sets. In communication and signal processing area, the channel gains, signals, waveforms etc. are all represented in complex form. Recently, a pure complex SVR & SVM based on complex kernel was proposed in [46], which can deal with the complex data set purely in complex domain. The results in [46] demonstrate the better performance as well as reduced complexity comparing to simply split learning task into two real case by real kernels. Based on this work, we derive a complexity-performance controllable detector for large MIMO systems based on a dual channel complex SVR (CSVR). The detector can work in two parallel real SVR channels which can be solved independently. Moreover, only the real part of kernel matrix is needed in both channels. This means a large amount of computation cost saving can be achieved. Based on the discrete time MIMO channel model, in our regression model, this CSVR-detector is constructed without offset, Therefore, for each real SVR without offset, Two types of combined single optimization variable selection strategy are proposed based on the work in [48]. The proposed combined single optimization variable selection strategy can approximate optimal double optimization variable selection strategy. The former one can achieve as few as iteration time while enjoy significant speed gain in each iteration.

- 3.3 Complex Support Vector Preliminary Detector
- 3.4 Channel Hardening Approximation
- 3.5 CSVPD-LAS versus MMSE-LAS
- 3.6 CSVPD-OPIC versus MMSE-OPIC

Chapter 4

Mathematical Layout Styles

TEX does a marvelous job of setting mathematical formulas, most often choosing pleasing spacing. However, on occasion one should intercede to improve the layout. This chapter defines a few such occasions. In addition, this chapter documents some features of the amsmath package which overcome difficulties in typesetting some mathematical forms. The amsmath package is documented in *The LATEX Companion* [?].

The modified setup is typeset as

$$G(z) = \begin{cases} \frac{P(z)}{1+z^{-1}} & \text{for } p \text{ even,} \\ P(z) & \text{for } p \text{ odd.} \end{cases}$$

$$(4.1)$$

With the modified definitions, we get the following.

$$\mathbf{d}^{(i)} = \hat{\mathbf{v}}^{(i)} - \hat{\tilde{\mathbf{v}}}^{(i)}$$

$$\mathbf{n}^{(i)} = \mathbf{u}^{(i)} - \tilde{\mathbf{v}}^{(i)}$$

$$(4.2)$$

Chapter 5

Tables

5.1 Tables in \LaTeX

Tables of many different sorts can be made with LATEX. This chapter gives suggestions on producing tables, along with a number of examples.

To illustrate these rules, here is a table and the LATEX input which was used to generate it.

5 Tables 17

 Table 5.1
 Filter specifications

Taps	Transition	Stopband	Passband	Stop-band	Ultimate			
(N)	Band	Weighting	Ripple	Rejection	Stop Band			
		(α)	dB	dB	dB			
8			0.06	31	31			
12	\mathbf{A}	1	0.025	48	50			
16			0.008	60	75			
12			0.04	33	36			
16	В	1	0.02	44	48			
24			0.008	60	78			
16		1	0.07	30	36			
24	C	1	0.02	44	49			
32	С	2	0.009	51	60			
48		2	0.006	50	66			
24		1	0.1	30	38			
48	D	2	0.006	50	66			
64			0.002	65	80			
48	Б	2	0.07	32	46			
64	${ m E}$	5	0.025	40	51			

Transition Code Letter	Normalized Transition Band
A	0.14
В	0.10
\mathbf{C}	0.0625
D	0.043
\mathbf{E}	0.023

The normalized transition band is the width of the transition band normalized to 2π ; that is, $(\omega_s - \pi/2)/(2\pi)$.

Appendix A

LATEX Macros

The LaTeX commands and macros used in formatting the title page for this document are shown in this appendix.

A.1 Thesis Preamble

The commands used to create the title page for a thesis are shown below. The McGill University crest is brought in via a macro McGillCrest which allows for setting the size and colour of an imported PostScript file which contains the actual crest. The title page also includes a red separator line.

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