

Übung 2

Problem 1: Signal to Noise Ratio

4 points

A binary signal is sent via a 3 kHz wide channel with a signal to noise ratio of 20 dB. Calculate the maximum data rate.

$$C_s = B \cdot \log_2 (1 + \text{SNR}) \quad // \text{Shannon}$$

C_s - max. data rate

B - Bandwidth

SNR - signal power / noise power

$$\text{SNR}_{\text{dB}} \rightarrow \text{SNR} :$$

$$\text{SNR}_{\text{dB}} = 10 \cdot \log_{10} (\text{SNR})$$

$$20 \text{ dB} = 10 \cdot \log_{10} (\text{SNR})$$

$$2 \text{ dB} = \log_{10} (\text{SNR}) \quad | \quad \text{SNR} = 100$$

$$C_s = 3000 \text{ Hz} \cdot \log_2 (101) \cdot \text{bit}$$

$$= 19974,63 \text{ bit/s}$$

$$= \underline{\underline{20 \text{ kbit/s}}}$$

Problem 2: Maximum Data Rate

4 points

A quaternary signal is sent via a 20 MHz wide channel. The medium experiences interference. We measure a signal to noise ratio of 30 dB. Calculate the maximum data rate that can be achieved over this channel.

$$SNR_{dB} = 30 \text{ dB} \rightarrow SNR = 1000$$

~~for binary signal~~

$$C_s = 20 \text{ MHz} \cdot \log_2(1001) \cdot \text{bit} \quad // \text{Shannon}$$
$$= 199,3 \text{ Mbit/s}$$

Because we have a quaternary signal, instead of a binary signal, the max. data rate has to be multiplied by the factor 2.

$$\Downarrow \quad \underline{\underline{C_s = 398,7 \text{ Mbit/s}}}$$

Problem 3: Noiseless channel

4 points

Specify the maximum data rate that can be achieved over a noiseless 4 kHz wide channel.

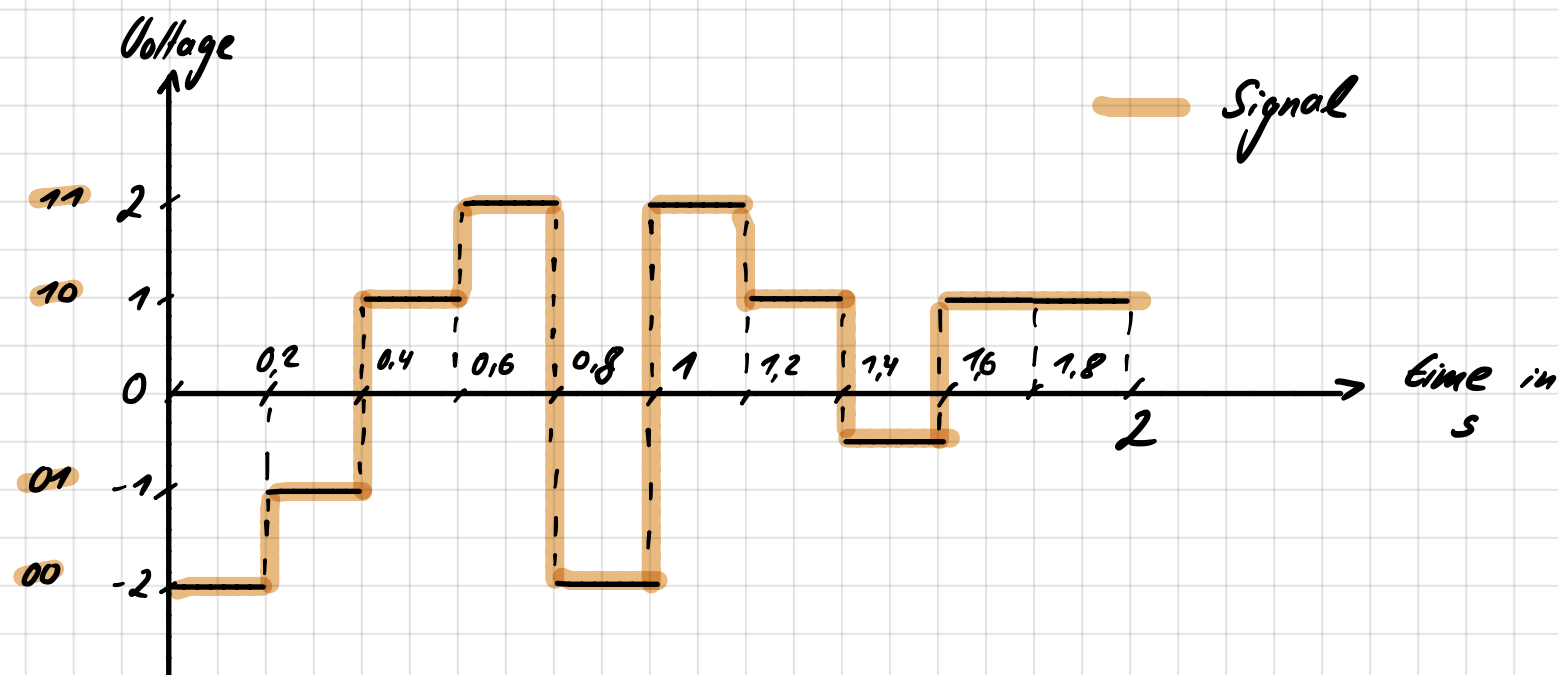
$$C_s = 2 \cdot B \cdot \log_2(n) \quad // \text{Nyquist}$$

$$C_s = 2 \cdot 4000 \text{ Hz} \cdot \log_2(2) \cdot \text{bit}$$
$$= 8000 \text{ bps} = \underline{\underline{8 \text{ kbit/s}}}$$

Problem 4: Multilevel Signals

3 points

Represent the following sequence of bits as a quaternary signal with a baud rate of 5/s in a time-voltage-diagram: 00011011001110011010. Determine the bitrate.



Problem 5: Units

2 points

What is the difference between 1 kb, 1 kB, and 1 KiB?

kb : kilobit , 1 kilobit is always equal to 1000 bit

kB : is ambiguous , could mean a) 1 kB = 1000 byte

b) 1 kB = 1024 byte

KiB : was introduced to erase the ambiguity of kB.

The kibibyte emphasize the use of the binary base

2 1 KiB = 1024 byte

Explain the term baseband and broadband. Why do we need broadband communication? Explain how broadband communication of baseband signals is achieved. Give example application scenarios.

Baseband

=> information is transmitted as a digital signal over the medium.

Therefore encoding procedures are necessary, to define the representation of high (1) and low (0)

Broadband

=> information is transmitted as an analogous signal over the medium.

The use of different frequencies allows to transfer multiple signals at the same time.

Baseband signals on Broadband communication & e.g.

The baseband signal is modulated onto a carrier signal, which has a specific frequency.

Because one baseband signal doesn't use the whole frequency range of the broadband, many baseband signals can be transferred by using different frequency carrier signals.

A good example are radio networks, which use a specific frequency, which you can tune your radio to, so that the signal can be processed by the radio.