

1) If every NP-hard language is in PSPACE-hard then $NP \subseteq PSPACE$. This also would mean SAT is PSPACE-hard, since SAT is in NP-hard it must be in PSPACE. Since SAT is PSPACE-hard & in PSPACE, it is PSPACE-complete. Since it is PSPACE-complete all PSPACE languages can be reduced to SAT. Since SAT is in NP, $PSPACE \subseteq NP$. If $NP \subseteq PSPACE$ and $PSPACE \subseteq NP$ $NP = PSPACE$.

2) An LBA is defined using the 8-tuple $(Q, X, \Sigma, q_0, M_L, M_R, q_f, \delta)$ where:

Q = finite set of states

X = tape alphabet

Σ = input alphabet

M_L = left end marker

M_R = right end marker

q_0 = initial state

q_f = final states

δ = transition function

$A_{LBA} = \{ \langle M, w \rangle \mid M \text{ is an LBA that accepts } w \}$

The maximum amount of ~~transitions~~

LBA configurations is $|Q| \cdot |w| \cdot |X|^{|w|}$. This means

we can solve A_{LBA} in polynomial space. Therefore

$A_{LBA} \in PSPACE$. Now we will reduce a language L

in $PSPACE$ to A_{LBA} to show it is $PSPACE$ -hard.

Since A_{LBA} is in $PSPACE$ & $PSPACE$ -hard.

A_{LBA} is $PSPACE$ -complete