

1) To show that 5SAT is NP-Complete we will reduce 3SAT to 5SAT. To start we'll reduce 3SAT to 4SAT by mapping the clause  $(a \vee b \vee c)$  to  $(a \vee b \vee c \vee d) \wedge (a \vee b \vee c \vee \bar{d})$  where  $d$  is any arbitrary set. If  $(a \vee b \vee c)$  is satisfied then so is  $(a \vee b \vee c \vee d) \wedge (a \vee b \vee c \vee \bar{d})$  and vice-versa. This proves that 4SAT is NP-Complete. Now we will reduce 4SAT to 5SAT using a similar method we will map  $(a \vee b \vee c \vee d)$  to  $(a \vee b \vee c \vee d \vee e) \wedge (a \vee b \vee c \vee d \vee \bar{e})$  since anything that satisfies both  $(a \vee b \vee c \vee d)$  satisfies both  $(a \vee b \vee c \vee d \vee e) \wedge (a \vee b \vee c \vee d \vee \bar{e})$  and vice-versa 5SAT is NP-Complete.

2) To show that LPATH is NP-Complete we will reduce HAMPATH to LPATH. Take  $HAMPATH = \{(G, a, b)\}$  and reduce it to  $(G, a, b, k)$  where  $k$  is the number of nodes in  $G$ . Since  $(G, a, b, k)$  contains a hamiltonian path from  $a$  to  $b$  of length  $k$  & a hamiltonian path is a simple path,  $(G, a, b, k) \in LPATH$  and LPATH is NP-Complete.