

## Outline for June 12, 2019

1. Survivor Outer Space Activity (**GOAL**: get students to think about center of mass)
2. Define the center-of-mass

$$\vec{R}_{CM} = \frac{m_1\vec{r}_1 + m_2\vec{r}_2}{m_1 + m_2} \quad (1)$$

3. Small White Board Question: Draw the center of mass for 2 particles
4. Big White Board Question: Show that  $\vec{R}_{CM}$  lies on the line spanned by  $\vec{r} = \vec{r}_2 - \vec{r}_1$ . **HINT**: consider the cross product  $(\vec{R}_{CM} - \vec{r}_1) \times (\vec{r}_2 - \vec{r}_1)$
5. Define  $\vec{F}_1$  and  $\vec{F}_2$  to be the net external forces acting on particle 1 and 2. Define  $\vec{F}_{12}$  and  $\vec{F}_{21}$  to be the internal forces
6. Small White Board Question: Write down Newton's second law for the 2 masses

$$m_1\ddot{\vec{r}}_1 = \vec{F}_{12} + \vec{F}_1 \quad (2)$$

$$m_2\ddot{\vec{r}}_2 = \vec{F}_{21} + \vec{F}_2 \quad (3)$$

7. Small White Board Question: What is the relationship between  $\vec{F}_{21}$  and  $\vec{F}_{12}$  ?

$$\vec{F}_{12} = -\vec{F}_{21} \quad \text{Newton's Third Law} \quad (4)$$

8. Write down some examples of "internal forces"

- gravitaitional
- Coulomb
- Hooke's law

9. Derive Newton's second law for the center of mass

$$(m_1 + m_2)(\ddot{\vec{r}}_1 + \ddot{\vec{r}}_2) = M\ddot{\vec{R}}_{CM} = \vec{F}_{\text{total}} \quad (5)$$

10. What happens when  $\vec{F}_{\text{total}} = 0$ ?
11. Assume  $\vec{F}_{\text{tot}} = 0$ , write  $\vec{F}_{21} = -\vec{F}_{12} = f(r)\hat{r} = -\vec{\nabla}U(r)$  so that we consider a "Central Force"
12. Find Newton's second law for  $\vec{r} = \vec{r}_2 - \vec{r}_1$

$$\frac{m_1m_2}{m_1 + m_2}(\ddot{\vec{r}}_2 - \ddot{\vec{r}}_1) = \mu\ddot{\vec{r}} = f(r)\hat{r} \quad (6)$$