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## MTH 351 LAB 5 John Waczak

```
clear all;  
format long;
```

### 1.

Use a computer algebra system to compute the arclength of  $f(x) = e^x$  from 0 to 1 with 16 digits of accuracy

using Mathematica to perform the integration. I am using the arc length formula:  $a = \int_a^b \sqrt{1 + f'(x)^2} dx$

```
TrueVal = 2.127616414686636;
```

### 2.

See arclength.m for my function definition.

```
r = arclength(0,1,2^10)  
Error = TrueVal-r  
relE = abs(Error)/TrueVal
```

```
r =
```

```
2.127617691971491
```

```
Error =
```

```
-1.277284855216720e-06
```

```
relE =
```

```
6.003360598272336e-07
```

### 3.

See arclength1.m for my function definition

---

```
r1 = arclength2(0, 1, 2^10)
Error1 = TrueVal-r1
relE1 = abs(Error1)/TrueVal
```

```
r1 =
```

```
2.129096187874880
```

```
Error1 =
```

```
-0.001479773188244
```

```
relE1 =
```

```
6.955075069120623e-04
```

## 4.

use newton's method with aprime and arclength to find when the arclength is equal to pi.

```
clear all ;
xold = 1 ;
n = 2^8 ;
tol = 1e-8;
maxiter = 50;
for i = 1:maxiter
    % must subtract pi from arclength as newton's methods wants to
    % find zeros so we must shift entire function to make pi a zero
    x = xold - (arclength(0,xold,n)-pi)/aprime(xold);
    if abs(x-xold)<tol
        i
        break
    end
    xold = x;
end
```

```
i =
```

```
5
```

Thus we can see that it took 9 iterations to find the x value to a tolerance of 1e-8. Now I will verify that the function does truly evaluate to pi

```
arc_pi = arclength(0, xold,n)
diff = abs(arc_pi - pi)
```

---

`arc_pi =`

`3.141592652571839`

`diff =`

`1.017953721316189e-09`

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