## **Homework Set #1**

Due Date: Before class Friday January 25th

1) You (2 points)

- (a) What is your major/minor?
- (b) When do you plan on graduating?
- (c) What do you want to do after graduation? (eg: grad school? if so, what subject? if not, what industry?)
- (d) What do you most want to get out of this course?

2) Solid State Physics (5 points)

- (a) Assume a solid is composed of closely packed atoms. What is the spacing between atoms? Express your result in terms of  $\alpha$ ,  $\alpha_G$ ,  $m_{\text{proton}}$ , and  $m_{\text{electron}}$ .
- (b) If you wanted to study the crystal structure of a solid material with  $Z \sim 10$  using light, what wavelength of photons would you need? Express your result in terms of  $\alpha$ ,  $\alpha_G$ ,  $m_{\text{proton}}$ , and  $m_{\text{electron}}$ .
- (c) Where in the spectrum of EM radiation do these photons lie?

## 3) Strength of Gravity on Earth

(5 points)

- (a) Calculate the local strength of gravity  $g_{local}$  in terms of  $\alpha$ ,  $\alpha_G$ ,  $m_{proton}$ , and  $m_{electron}$ .
- (b) What is your estimated value in mks units?
- (c) How does this compare with the well-known value of 9.8 m/s<sup>2</sup>?

4) Neutron Stars (5 points)

- (a) Estimate the radius, mass, and speed of sound for neutron stars in terms of  $\alpha$ ,  $\alpha_G$ ,  $m_{\text{proton}}$ , and  $m_{\text{electron}}$ . (Assume: A neutron star is a solid made of neutrons and  $m_{\text{proton}} \sim m_{\text{neutron}}$ )
- (b) What are you estimated values in mks units?
- (c) Compare your estimates to actual values for Neutron Stars quoted online.
- (d) Look up  $m_{\text{neutron}}$ . How does this compare with the assumption of  $m_{\text{proton}} \sim m_{\text{neutron}}$ ?

5) 2D Rotations (3 points)

- (a) Show that  $R(\Theta) = e^{I\Theta} = cos(\Theta) + Isin(\Theta)$  where,  $I = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}$
- (b) Show that 2D rotations commute. (ie:  $R(\Theta_1)R(\Theta_2) = R(\Theta_2)R(\Theta_1)$ )

6) 3D Rotations (5 points)

(a) Work out the "algebra" of the generators of 3D rotations  $J_i$ .

Where  $J_3 = \begin{bmatrix} 0 & -i & 0 \\ i & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$ ,

 $J_2 = \begin{bmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{bmatrix}$ 

 $J_1 = \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & -i \\ 0 & i & 0 \end{bmatrix}$ 

(These generators different from the T's derived in class by a factor of i)

- Working out the algebra means calculating the commutation relations  $[J_i, J_j]$ . (b) Let M be a traceless  $2 \times 2$  hermitian matrix and U be a  $2 \times 2$  hermitian matrix with determinant =
- (b) Let M be a traceless  $2 \times 2$  hermitian matrix and U be a  $2 \times 2$  hermitian matrix with determinant = 1. Show that  $M' = U^{\dagger}MU$  is also traceless and hermitian and that is has the same determinant as M.