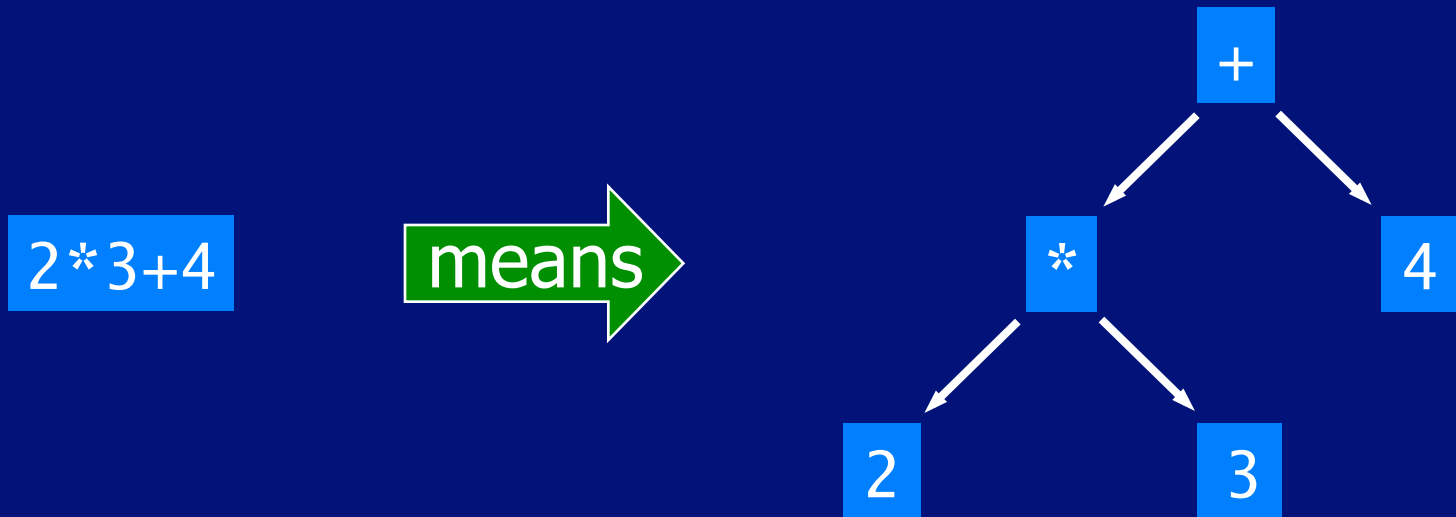


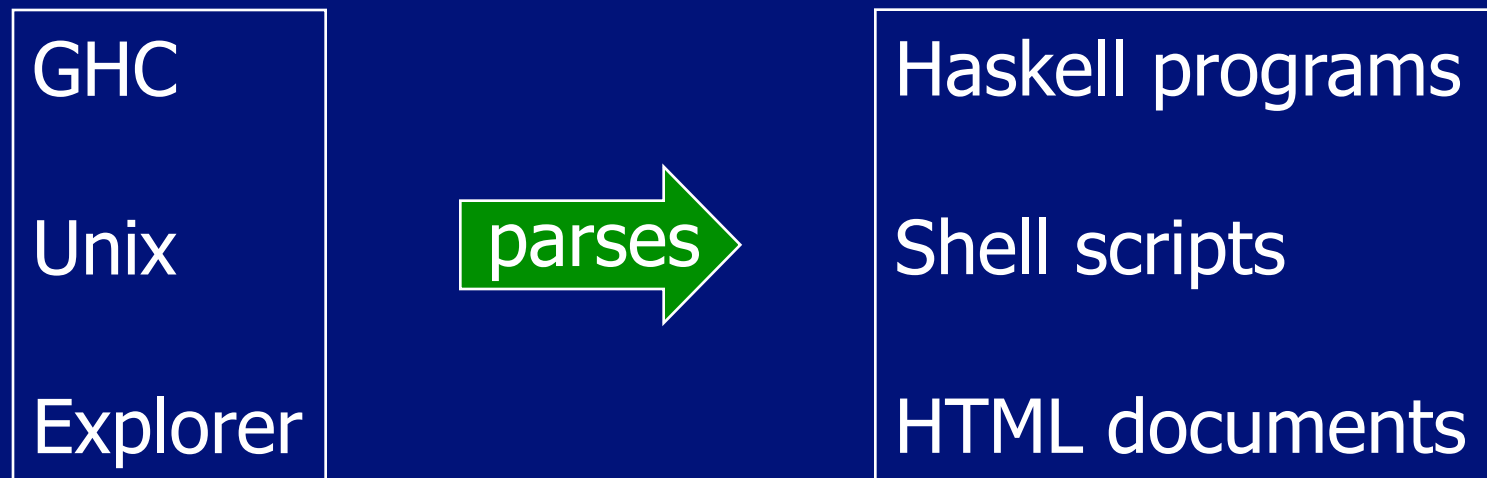
# What is a Parser?

A parser is a program that analyses a piece of text to determine its syntactic structure.



# Where Are They Used?

Almost every real life program uses some form of parser to pre-process its input.



# The Parser Type

In a functional language such as Haskell, parsers can naturally be viewed as functions.

```
type Parser = String → Tree
```

A parser is a function that takes a string and returns some form of tree.

However, a parser might not require all of its input string, so we also return any unused input:

```
type Parser = String → (Tree,String)
```

A string might be parsable in many ways, including none, so we generalize to a list of results:

```
type Parser = String → [(Tree,String)]
```

Finally, a parser might not always produce a tree, so we generalize to a value of any type:

```
type Parser a = String → [(a,String)]
```

Note:

- For simplicity, we will only consider parsers that either fail and return the empty list of results, or succeed and return a singleton list.

# Basic Parsers

- The parser item fails if the input is empty, and consumes the first character otherwise:

```
item :: Parser Char
```

```
item = λinp → case inp of
```

```
    []      → []
```

```
    (x:xs) → [(x,xs)]
```

- The parser failure always fails:

```
failure :: Parser a  
failure = λinp → []
```

- The parser return v always succeeds, returning the value  $v$  without consuming any input:

```
return :: a → Parser a  
return v = λinp → [(v, inp)]
```

- The parser  $p \text{ +++ } q$  behaves as the parser  $p$  if it succeeds, and as the parser  $q$  otherwise:

```
(+++)  :: Parser a → Parser a → Parser a
p +++ q = λinp → case p inp of
                []           → parse q inp
                [(v,out)]    → [(v,out)]
```

- The function parse applies a parser to a string:

```
parse :: Parser a → String → [(a,String)]
parse p inp = p inp
```



# Examples

The behavior of the five parsing primitives can be illustrated with some simple examples:

```
% ghci Parsing  
  
> parse item ""  
[]  
  
> parse item "abc"  
[('a', "bc")]
```

```
> parse failure "abc"  
[]
```

```
> parse (return 1) "abc"  
[(1,"abc")]
```

```
> parse (item +++ return 'd') "abc"  
[('a',"bc")]
```

```
> parse (failure +++ return 'd') "abc"  
[('d',"abc")]
```

## Note:

- The library file Parsing is available on the web from the Programming in Haskell home page.
- For technical reasons, the first failure example actually gives an error concerning types, but this does not occur in non-trivial examples.
- The Parser type is a monad, a mathematical structure that has proved useful for modeling many different kinds of computations.

# Sequencing

A sequence of parsers can be combined as a single composite parser using the keyword do.

For example:

```
p :: Parser (Char,Char)
p  = do x ← item
      item
      y ← item
      return (x,y)
```

## Note:

- Each parser must begin in precisely the same column. That is, the layout rule applies.
- The values returned by intermediate parsers are discarded by default, but if required can be named using the  $\leftarrow$  operator.
- The value returned by the last parser is the value returned by the sequence as a whole.

- If any parser in a sequence of parsers fails, then the sequence as a whole fails. For example:

```
> parse p "abcdef"  
[('a', 'c'), "def"]  
  
> parse p "ab"  
[]
```

- The do notation is not specific to the Parser type, but can be used with any monadic type.

# Derived Primitives

- Parsing a character that satisfies a predicate:

```
sat  :: (Char → Bool) → Parser Char
sat p = do x ← item
        if p x then
            return x
        else
            failure
```

## ■ Parsing a digit and specific characters:

```
digit :: Parser Char  
digit = sat isDigit
```

```
char :: Char → Parser Char  
char x = sat (x ==)
```

## ■ Applying a parser zero or more times:

```
many :: Parser a → Parser [a]  
many p = many1 p +++ return []
```



## ■ Applying a parser one or more times:

```
many1  :: Parser a -> Parser [a]
many1 p = do v  <- p
             vs <- many p
             return (v:vs)
```

## ■ Parsing a specific string of characters:

```
string      :: String → Parser String
string []   = return []
string (x:xs) = do char x
                  string xs
                  return (x:xs)
```

# Example

We can now define a parser that consumes a list of one or more digits from a string:

```
p :: Parser String
p = do char '['
      d  ← digit
      ds ← many (do char ','
                    digit)
      char ']'
      return (d:ds)
```

For example:

```
> parse p "[1,2,3,4]"  
[("1234", "")]
```

```
> parse p "[1,2,3,4"  
[]
```

Note:

- More sophisticated parsing libraries can indicate and/or recover from errors in the input string.

# Arithmetic Expressions

Consider a simple form of expressions built up from single digits using the operations of addition  $+$  and multiplication  $*$ , together with parentheses.

We also assume that:

- $*$  and  $+$  associate to the right;
- $*$  has higher priority than  $+$ .

Formally, the syntax of such expressions is defined by the following context free grammar:

$$expr \rightarrow term '+' expr \mid term$$
$$term \rightarrow factor '*' term \mid factor$$
$$factor \rightarrow digit \mid '(' expr ')'$$
$$digit \rightarrow '0' \mid '1' \mid \dots \mid '9'$$

However, for reasons of efficiency, it is important to factorise the rules for *expr* and *term*:

$$expr \rightarrow term \ ('+' \ expr \mid \varepsilon)$$
$$term \rightarrow factor \ ('*' \ term \mid \varepsilon)$$

Note:

- The symbol  $\varepsilon$  denotes the empty string.

It is now easy to translate the grammar into a parser that evaluates expressions, by simply rewriting the grammar rules using the parsing primitives.

That is, we have:

```
expr :: Parser Int
expr  = do t <- term
        do char '+'
        e <- expr
        return (t + e)
+++ return t
```

```
term :: Parser Int
term  = do f ← factor
        do char '*'
        t ← term
        return (f * t)
    +++ return f
```

```
factor :: Parser Int
factor  = do d ← digit
        return (digitToInt d)
    +++ do char '('
        e ← expr
        char ')'
        return e
```



Finally, if we define

```
eval    :: String → Int  
eval xs = fst (head (parse expr xs))
```

then we try out some examples:

```
> eval "2*3+4"  
10  
  
> eval "2*(3+4)"  
14
```

# Exercises

- (1) Why does factorising the expression grammar make the resulting parser more efficient?
- (2) Extend the expression parser to allow the use of subtraction and division, based upon the following extensions to the grammar:

$$expr \rightarrow term \ ('+' \ expr \mid '-' \ expr \mid \varepsilon)$$
$$term \rightarrow factor \ ('*' \ term \mid '/' \ term \mid \varepsilon)$$