

# Domain Adaptation



John Blitzer and Hal Daumé III



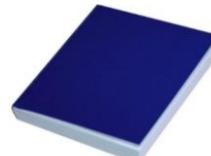
# Classical “Single-domain” Learning



Predict:  $x \rightarrow y$

$$(x, y) \sim \text{Pr}[x, y]$$

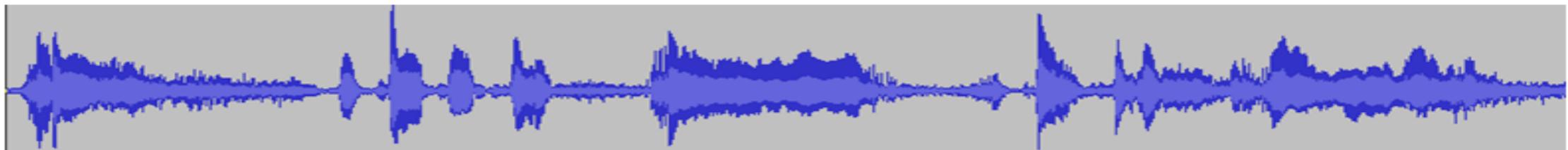
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**Running with Scissors**

**Title:** Horrible book, horrible.

This book was horrible. I read half, suffering from a headache the entire time, and eventually i lit it on fire. 1 less copy in the world. Don't waste your money. I wish i had the time spent reading this book back. It wasted my life



So the topic of ah the talk today is online learning



# Domain Adaptation



$$(x, y) \sim \Pr_S[x, y]$$

Training



Source



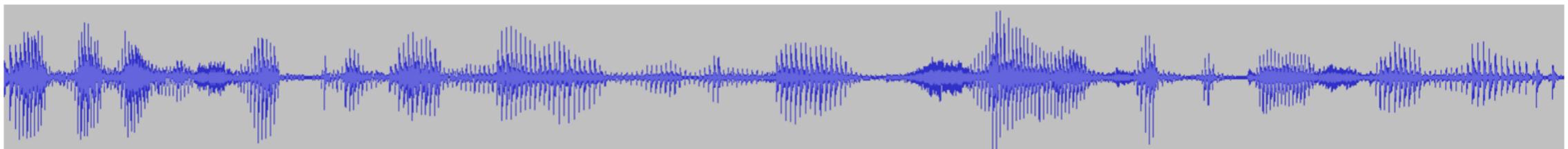
So                   the topic of                   ah                   the talk today is online learning

$$(x, y) \sim \Pr_T[x, y]$$

Testing



Target



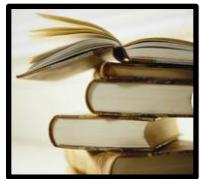
Everything is happening online. Even the slides are produced on-line



# Domain Adaptation



## Natural Language Processing



Packed with fascinating info



A breeze to clean up



## Visual Object Recognition

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# Domain Adaptation



## Natural Language Processing



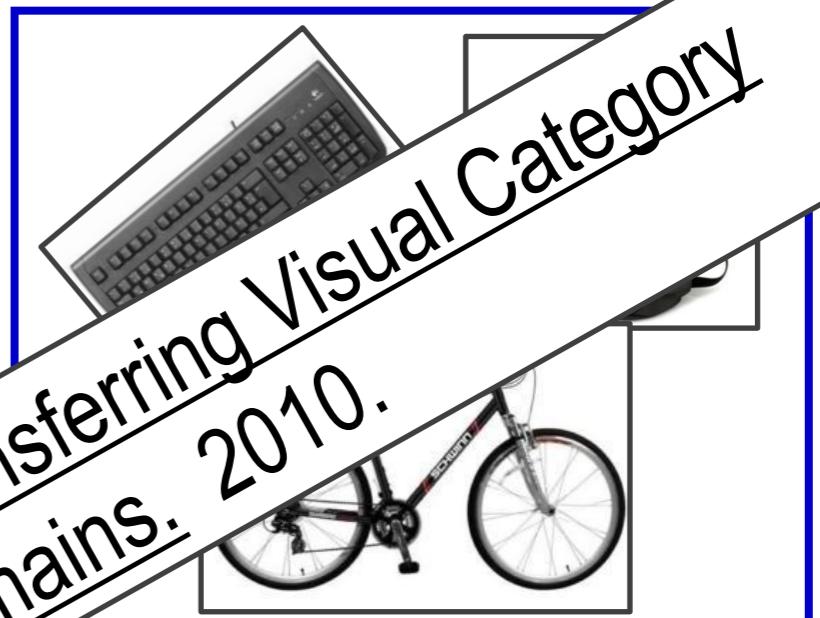
Packed with fascinating info



A breeze to clean up



## Visual Object Recognition





# Tutorial Outline

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1. Domain Adaptation: Common Concepts
2. Semi-supervised Adaptation
  - Learning with Shared Support
  - Learning Shared Representations
3. Supervised Adaptation
  - Feature-Based Approaches
  - Parameter-Based Approaches
4. Open Questions and Uncovered Algorithms



# Classical vs Adaptation Error



## Classical Test Error:

$$\epsilon_{\text{test}} \leq \hat{\epsilon}_{\text{train}} + \sqrt{\frac{\text{complexity}}{n}}$$

Measured on the  
same distribution!

## Adaptation Target Error:

$$\epsilon_{\text{test}} \leq ??$$

Measured on a  
**new** distribution!



# Common Concepts in Adaptation



## Covariate Shift

$$\Pr_S[y|x] = \Pr_T[y|x]$$



understands both



&



## Single Good Hypothesis

$\exists h^*, \epsilon_S(h^*), \epsilon_T(h^*)$  small



understands both

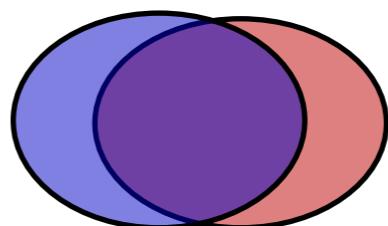


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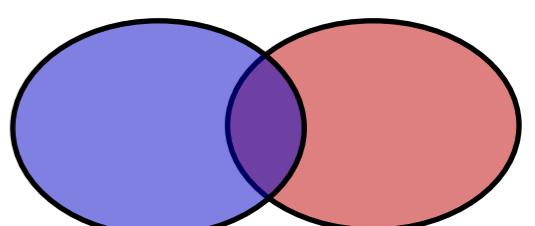


## Domain Discrepancy and Error

Easy



Hard





# Tutorial Outline

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2. Semi-supervised Adaptation
  - Covariate shift with Shared Support
  - Learning Shared Representations
3. Supervised Adaptation
  - Feature-Based Approaches
  - Parameter-Based Approaches
4. Open Questions and Uncovered Algorithms



# A bound on the adaptation error



Let  $h$  be a binary hypothesis. If  $\Pr_S(y|x) = \Pr_T(y|x)$ , then

$$\epsilon_T(h) \leq \epsilon_S(h) + \int_{\mathcal{X}} |\Pr_T(x) - \Pr_S(x)| dx$$

Minimize the total variation



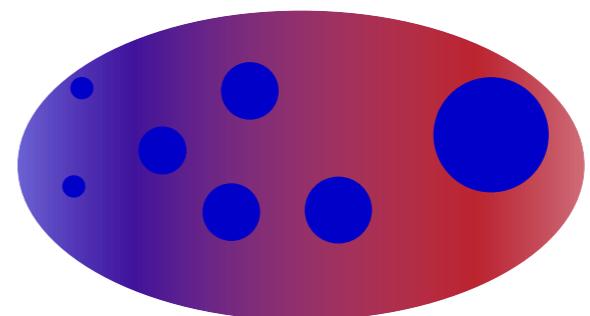
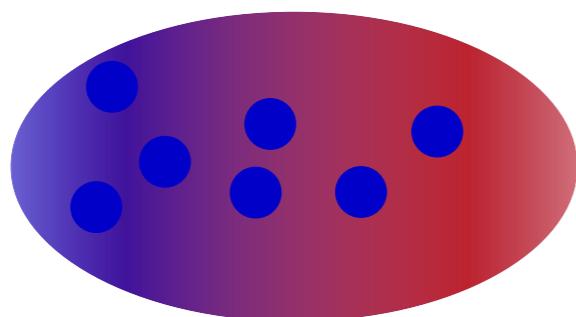
# Covariate Shift with Shared Support



Assumption: Target & Source Share Support

$$\forall x, \Pr_S[x] \neq 0 \text{ iff } \Pr_T[x] \neq 0$$

Reweighting source instances to minimize discrepancy





# Source Instance Reweighting



## Defining Error

$$\epsilon_T(h) = \mathbb{E}_{\Pr_T[x]} \mathbb{E}_{\Pr[y|x]} [h(x) \neq y]$$

## Using Definition of Expectation

$$= \sum_x \Pr_T[x] \mathbb{E}_{\Pr[y|x]} [h(x) \neq y]$$

## Multiplying by 1

$$= \sum_x \frac{\Pr_S[x]}{\Pr_T[x]} \Pr_T[x] \mathbb{E}_{\Pr[y|x]} [h(x) \neq y]$$

per-instance  
weights  $w$

## Rearranging

$$\epsilon_T(h) = \epsilon_S(h, w) = \mathbb{E}_{\Pr_S[x]} \frac{\Pr_T[x]}{\Pr_S[x]} \mathbb{E}_{\Pr[y|x]} [h(x) \neq y]$$

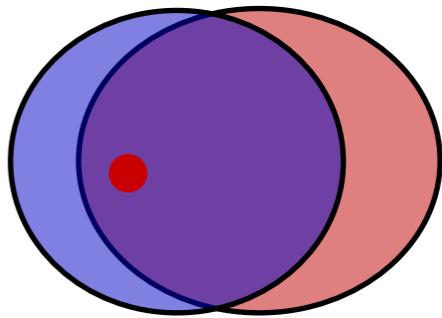


# Sample Selection Bias



## Another Way to View

- 1) Draw from the target  $\Pr_T[x]$



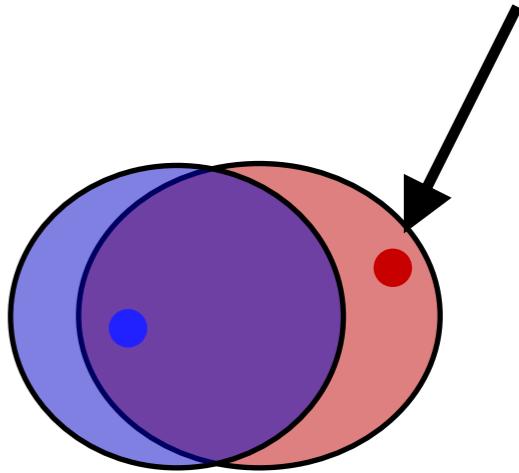


# Sample Selection Bias



Redefine the source distribution

- 1) Draw from the target  $\Pr_T[x]$
- 2) Select into the source with  $\Pr[\sigma = 1|x]$



$$\Pr_S[x] = \frac{\Pr_T[x]\Pr[\sigma = 1|x]}{\Pr[\sigma = 1]}$$



# Rewriting Source Risk



$$\Pr_S[x] = \frac{\Pr_T[x]\Pr[\sigma = 1|x]}{\Pr[\sigma = 1]}$$

## Rearranging

$$\frac{\Pr_T[x]}{\Pr_S[x]} = \frac{\Pr[\sigma = 1]}{\Pr[\sigma = 1|x]}$$

per-instance  
weights  $w$

$\Pr[\sigma = 1]$  not dependent on  $x$

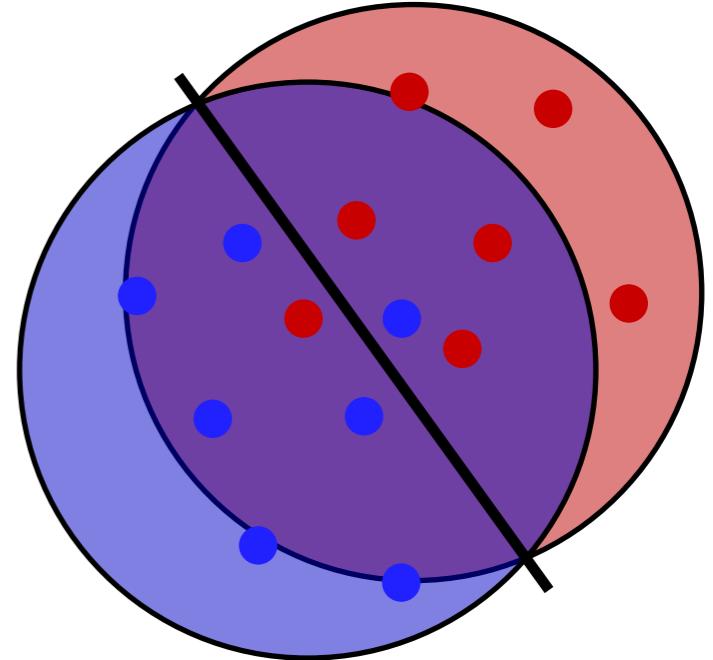
$$\epsilon_S(h, w) \propto \mathbb{E}_{\Pr_S[x]} \frac{1}{\Pr[\sigma = 1|x]} \mathbb{E}_{\Pr[y|x]} [h(x) \neq y]$$



# Logistic Model of Source Selection



$$\Pr[\sigma = 1 | x] = \frac{1}{1 + \exp(\theta^\top x + b)}$$



## Training Data

Source instances,  $\sigma = 1$

Target unlabeled instances,  $\sigma = 0$

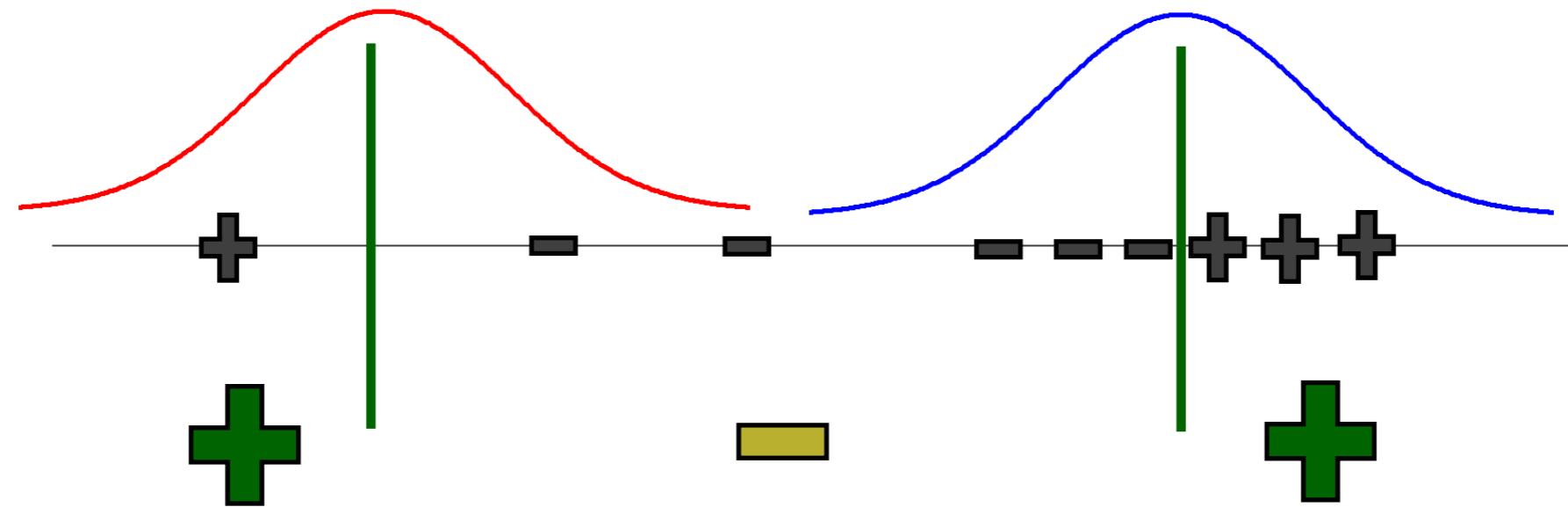


# Selection Bias Correction Algorithm



Input:

Labeled **source** data





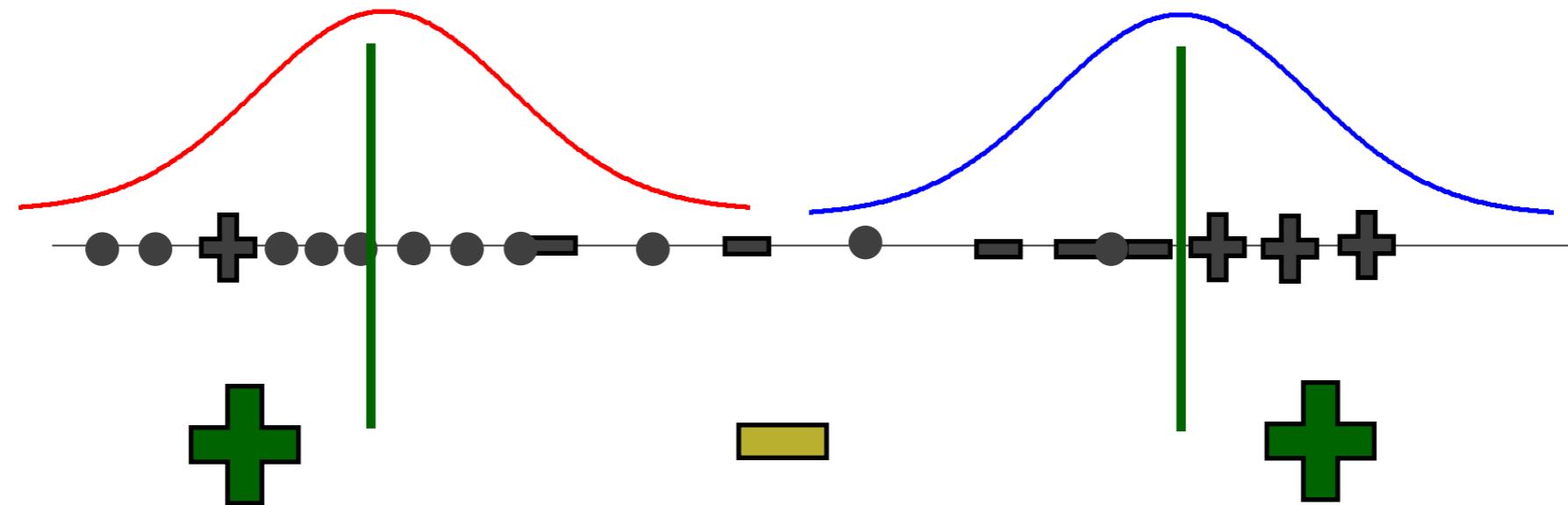
# Selection Bias Correction Algorithm



Input:

Labeled **source** data

Unlabeled **target** data



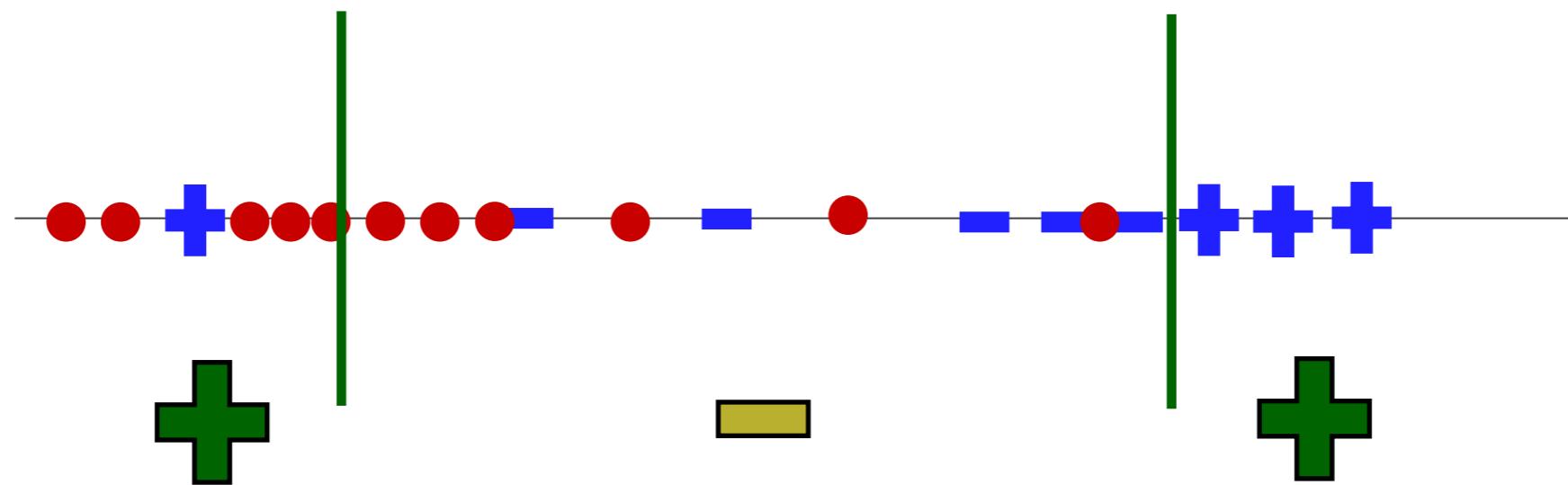


# Selection Bias Correction Algorithm



Input: Labeled **source** and unlabeled **target** data

- 1) Label source instances as  $\sigma = 1$ , target as  $\sigma = 0$



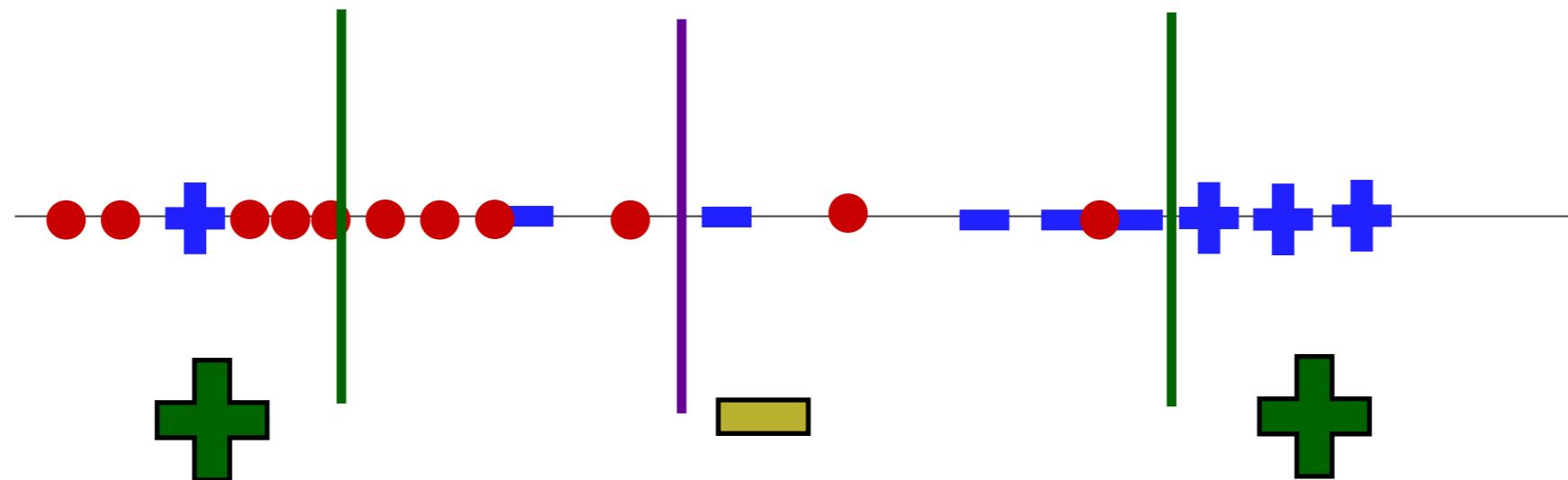


# Selection Bias Correction Algorithm



Input: Labeled **source** and unlabeled **target** data

- 1) Label source instances as  $\sigma = 1$ , target as  $\sigma = 0$
- 2) Train predictor  $\Pr[\sigma = 1|x] = \frac{1}{1+\exp(\theta^\top x+b)}$



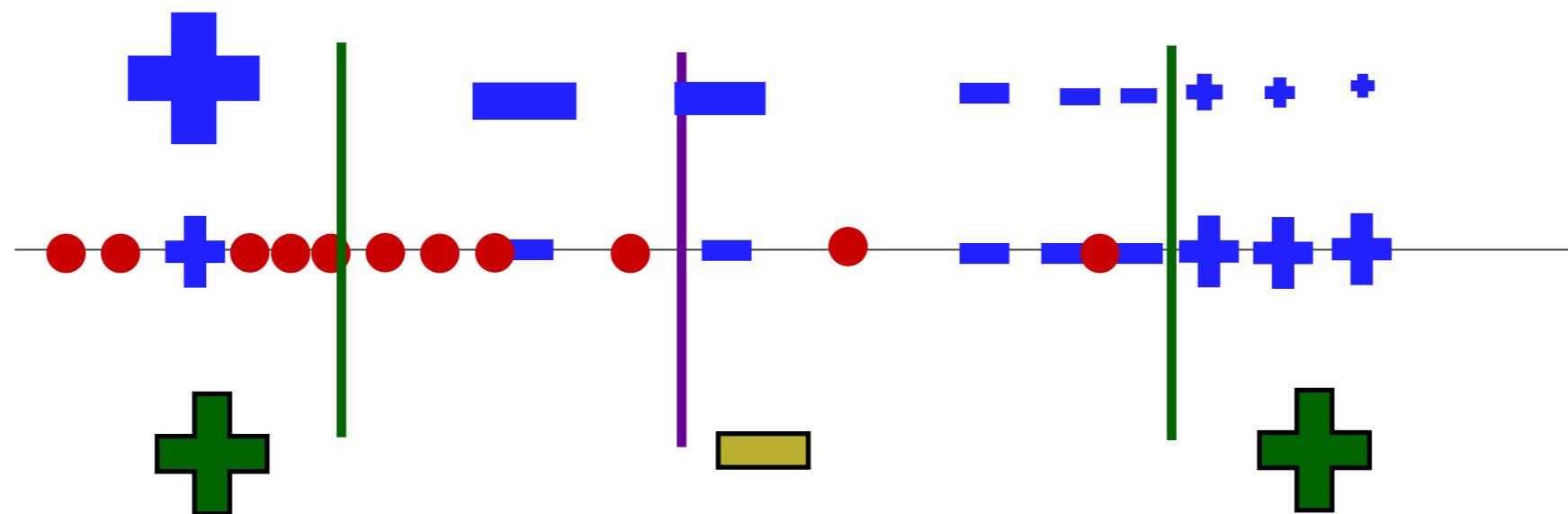


# Selection Bias Correction Algorithm



Input: Labeled **source** and unlabeled **target** data

- 1) Label source instances as  $\sigma = 1$ , target as  $\sigma = 0$
- 2) Train predictor  $\Pr[\sigma = 1|x] = \frac{1}{1+\exp(\theta^\top x+b)}$
- 3) Reweight source instances



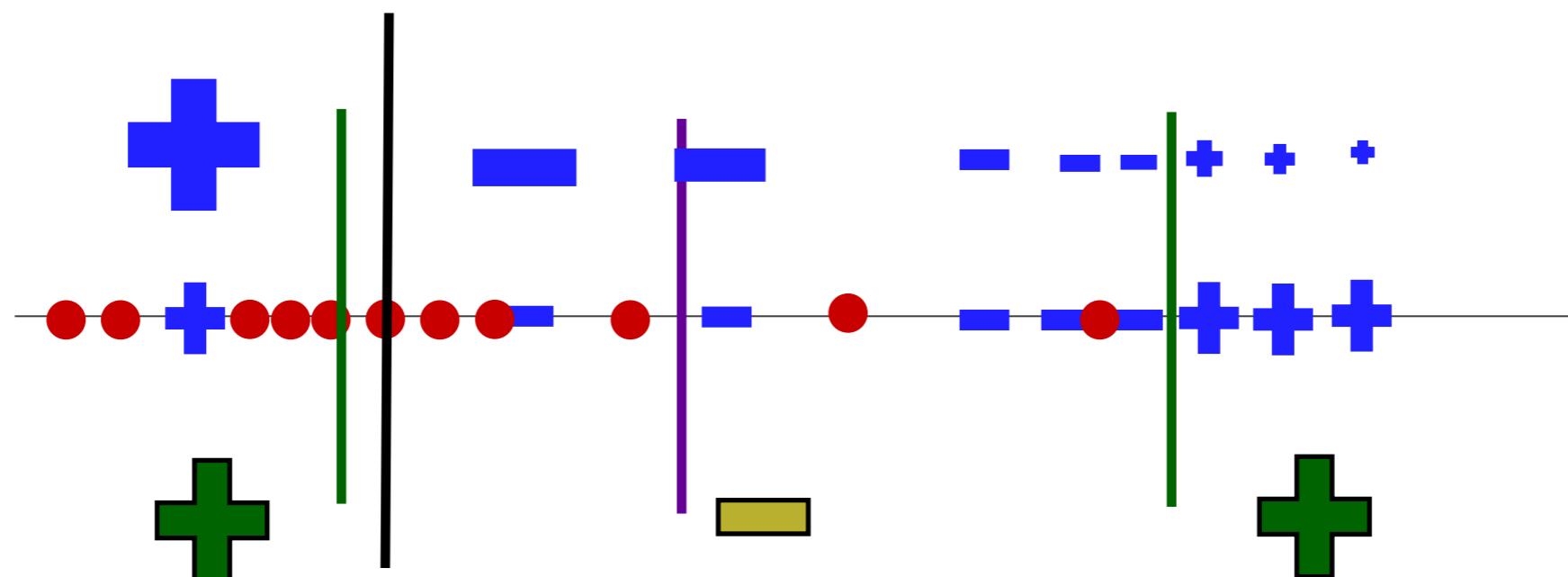


# Selection Bias Correction Algorithm



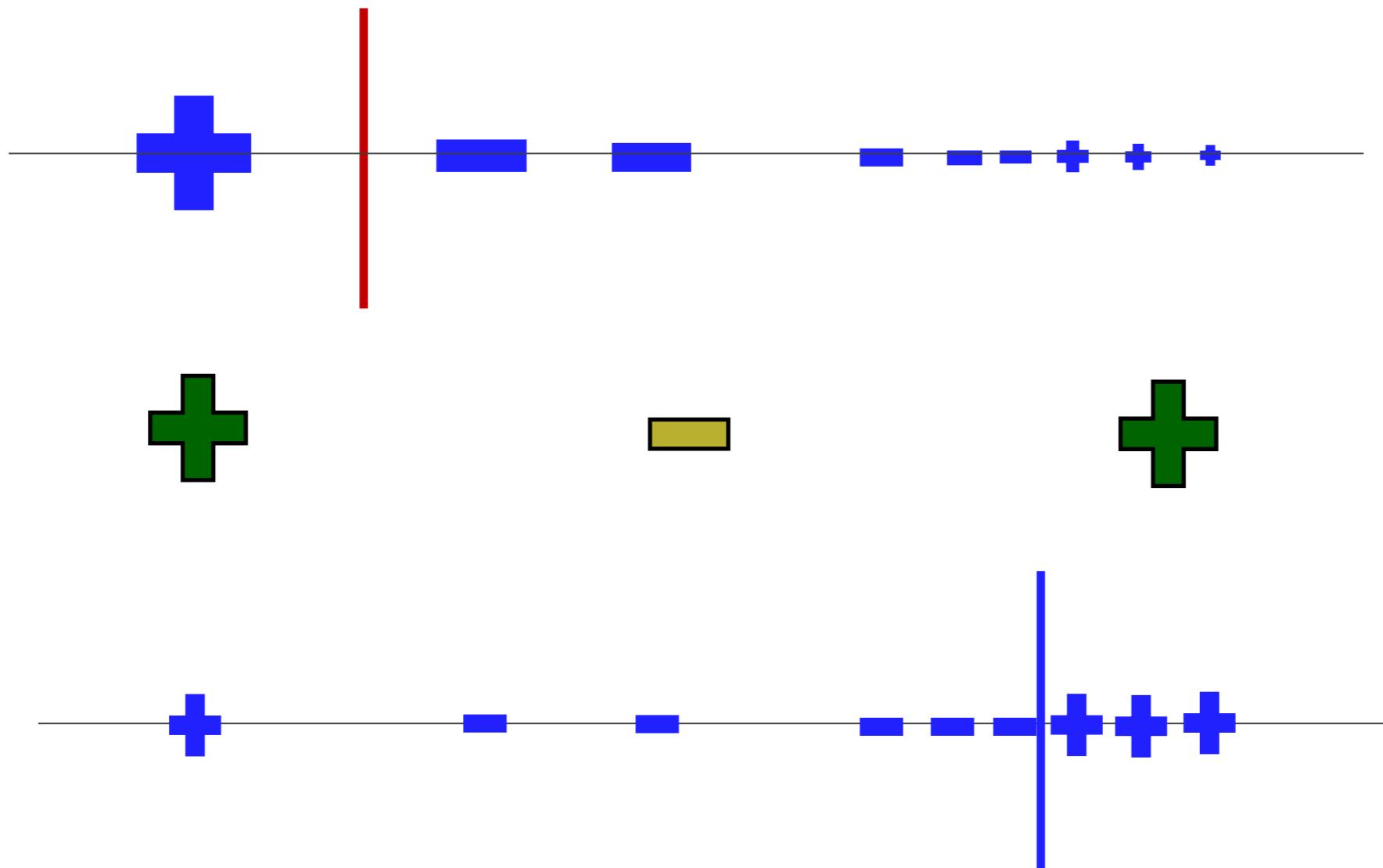
Input: Labeled **source** and unlabeled **target** data

- 1) Label source instances as  $\sigma = 1$ , target as  $\sigma = 0$
- 2) Train predictor  $\Pr[\sigma = 1|x] = \frac{1}{1+\exp(\theta^\top x+b)}$
- 3) Reweight source instances
- 4) Train target predictor





# How Bias gets Corrected





# Rates for Re-weighted Learning



$\hat{\epsilon}_s^n(h, w)$ : weighted source test error on sample of size n

With probability  $1 - \delta$ , for every  $h$

$$|\hat{\epsilon}_S^n(h, w) - \epsilon_T(h)| \leq \sqrt{\frac{O\left(\frac{1}{\delta}\right) + O\left(\max_{x \in \mathcal{X}} w(x)^2\right)}{n}}$$

Adapted from Gretton et al.



# Sample Selection Bias Summary



## Two Key Assumptions

- 1) Covariate shift:  $\Pr_S[y|x] = \Pr_T[y|x]$
- 2) Shared support:  $\forall x, \Pr_S[x] \neq 0$  iff  $\Pr_T[x] \neq 0$

Advantage

$$\hat{\epsilon}_S^n(h, w) \xrightarrow[n]{\infty} \epsilon_T(h)$$

Optimal target predictor  
without labeled target data



# Sample Selection Bias Summary



## Two Key Assumptions

- 1) Covariate shift:  $\Pr_S[y|x] = \Pr_T[y|x]$
- 2) Shared support:  $\forall x, \Pr_S[x] \neq 0$  iff  $\Pr_T[x] \neq 0$

**Advantage**  $\hat{\epsilon}_S^n(h, w) \xrightarrow[n]{\infty} \epsilon_T(h)$

## Disadvantage

Convergence to  $\epsilon_T(h)$  depends on  $\max_x \frac{\Pr_T(x)}{\Pr_S(x)}$



# Sample Selection Bias References

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<http://adaptationtutorial.blitzer.com/references/>

- [1] J. Heckman. Sample Selection Bias as a Specification Error. 1979.
- [2] A. Gretton et al. Covariate Shift by Kernel Mean Matching. 2008.
- [3] C. Cortes et al. Sample Selection Bias Correction Theory. 2008
- [4] S. Bickel et al. Discriminative Learning Under Covariate Shift. 2009.



# Tutorial Outline

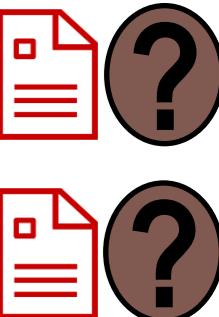
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# Unshared Support in the Real World



# Running with Scissors

## **Title:** Horrible book, horrible.

This book was horrible. I read half, suffering from a headache the entire time, and eventually i lit it on fire. 1 less copy in the world. Don't waste your money. I wish i had the time spent reading this book back. It wasted my life



## **Avante Deep Fryer; Black**

## Title: lid does not work well...

I love the way the Tefal deep fryer cooks, however, I am returning my second one due to a defective lid closure. The lid may close initially, but after a few uses it no longer stays closed. I won't be buying this one again.





# Unshared Support in the Real World



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## Running with Scissors

Title: Horrible book, horrible.

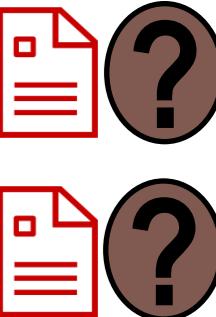
This book was horrible I read half



## Avante Deep Fryer; Black

Title: lid **does not work** well...

I love the way the Tefal deep fryer



Error increase: 13% → 26%

: time, and eventually i lit it on fire. 1 less copy in the world. Don't waste your money. I wish i had the time spent reading this book back. It wasted my life

: second one due to a **defective** lid closure. The lid may close initially, but after a few uses it no longer stays closed. I won't be buying this one again.



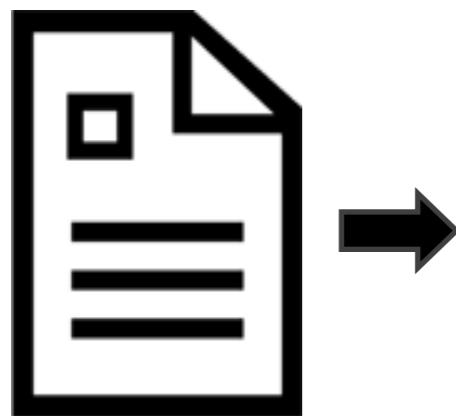


# Linear Regression for Rating Prediction



$$h(x) = \text{sgn}(\theta^\top x)$$

$$h(x) \in \{\begin{array}{c} \text{green thumbs up} \\ \text{red thumbs up} \end{array}\}$$



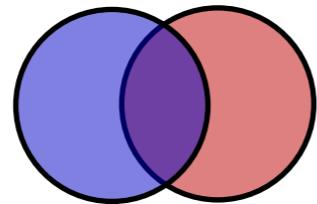
	<i>excellent</i>	<i>great</i>	<i>fascinating</i>						
$x$	3	0	...	0	1	0	...	0	1
$\theta$	0.5	1	...	-1.1	2	-0.3	...	0.1	1.5



# Coupled Subspaces

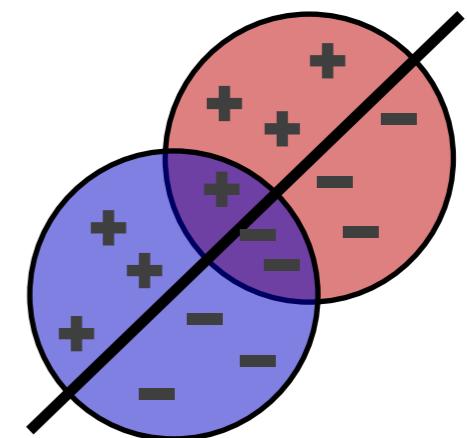


No Shared Support



Single Good Linear Hypothesis

$\exists \theta^*, \quad \epsilon_S(\theta^*) + \epsilon_T(\theta^*) \quad \text{small}$



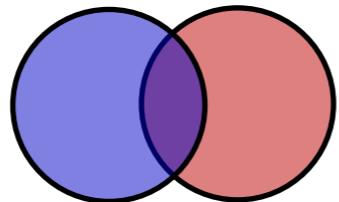
Stronger than  $\Pr_{\mathcal{S}}[y|x] = \Pr_{\mathcal{T}}[y|x]$



# Coupled Subspaces

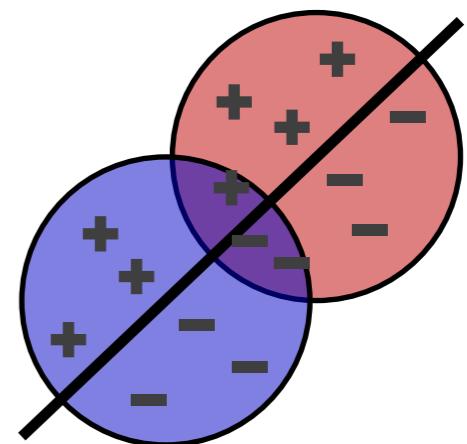


No Shared Support



Single Good Linear Hypothesis

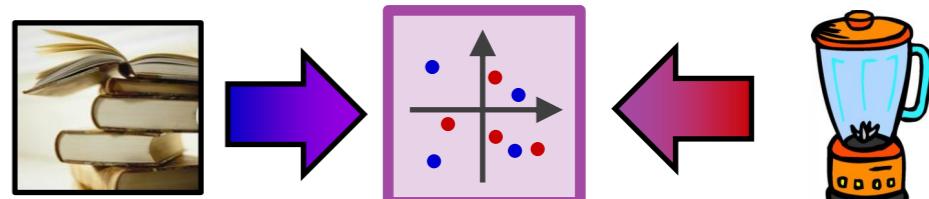
$$\exists \theta^*, \quad \epsilon_S(\theta^*) + \epsilon_T(\theta^*) \quad \text{small}$$



Coupled Representation Learning

$P_x$  couples domains

Bound target error  $\epsilon_{P,T}(\theta)$





# Single Good Linear Hypothesis?



$\exists \theta^*, \quad \epsilon_S(\theta^*) + \epsilon_T(\theta^*) \quad \text{small}$

Adaptation Squared Error

Source\Target	Books	Kitchen
Books	1.35	
Kitchen		1.19
Both		



# Single Good Linear Hypothesis?



$\exists \theta^*, \quad \epsilon_S(\theta^*) + \epsilon_T(\theta^*) \quad \text{small}$

## Adaptation Squared Error

Source \ Target	Books	Kitchen
Books	1.35	
Kitchen		1.19
Both	1.38	1.23



# Single Good Linear Hypothesis?



$\exists \theta^*, \quad \epsilon_S(\theta^*) + \epsilon_T(\theta^*) \quad \text{small}$

## Adaptation Squared Error

Source \ Target	Books	Kitchen
Books	1.35	1.68
Kitchen	1.80	1.19
Both	1.38	1.23



# A bound on the adaptation error



Let  $h$  be a binary hypothesis. If  $\Pr_S(Y|x) = \Pr_T(Y|x)$ , then

$$\epsilon_T(h) \leq \epsilon_S(h) + \int_{\mathcal{X}} |\Pr_T(x) - \Pr_S(x)| dx$$

What if a single good hypothesis exists?

A better discrepancy than total variation?



# A generalized discrepancy distance



Measure how hypotheses make mistakes





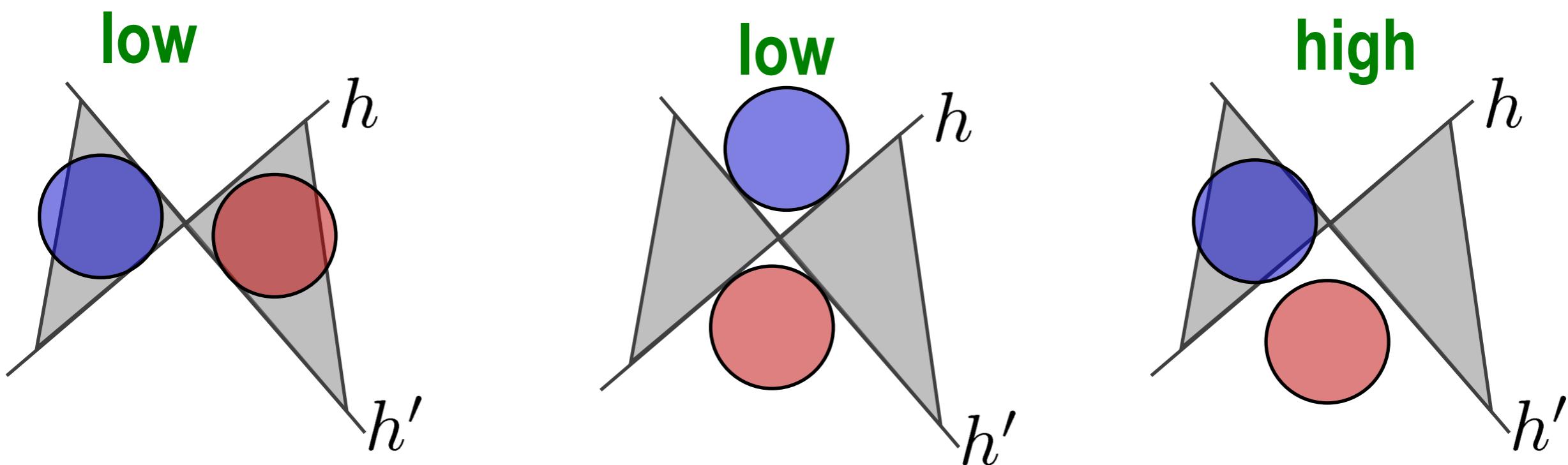
# A generalized discrepancy distance



Measure how hypotheses make mistakes

$$\text{disc}_H(Q, P) =$$

$$\max_{h, h' \in H} |E_Q[h(x) \neq h'(x)] - E_P[h(x) \neq h'(x)]|$$



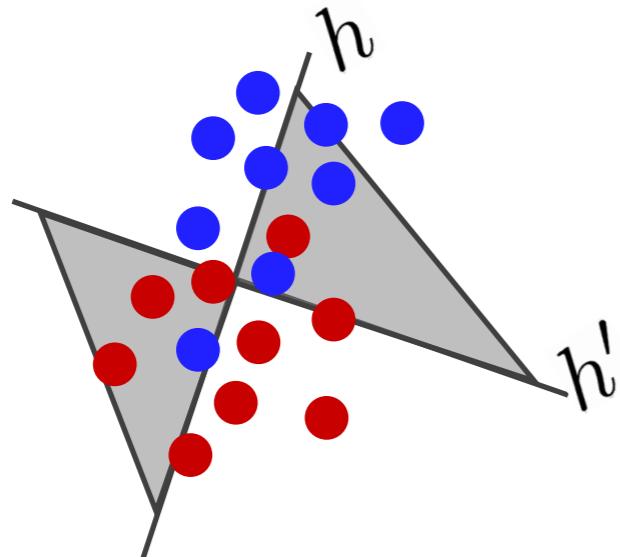


# Discrepancy vs. Total Variation



## Discrepancy

Computable from finite samples.



## Total Variation

Not computable in general

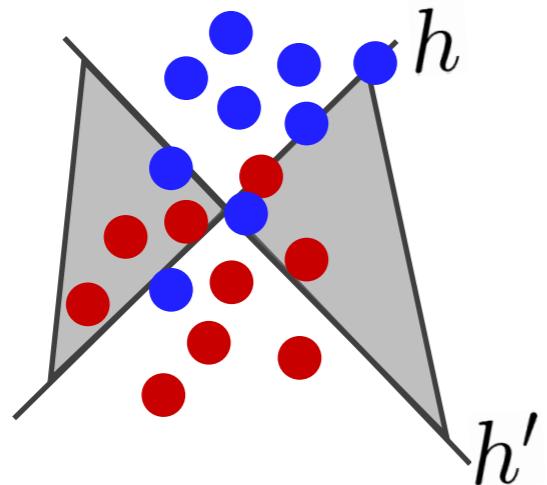


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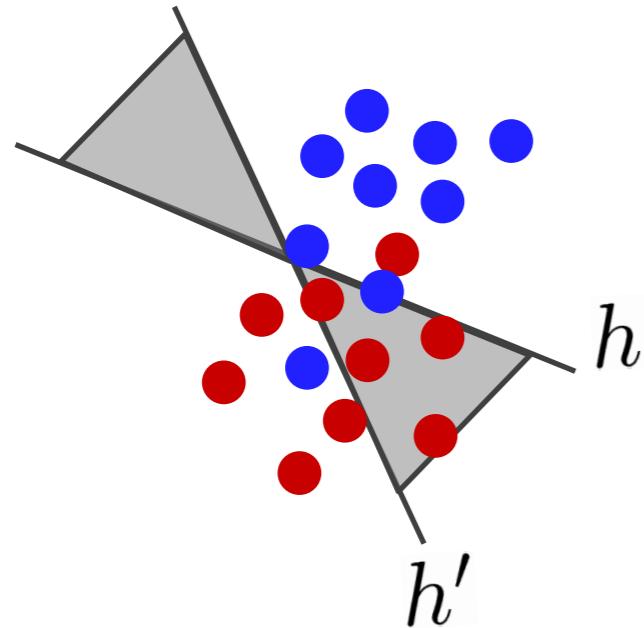


# Discrepancy vs. Total Variation



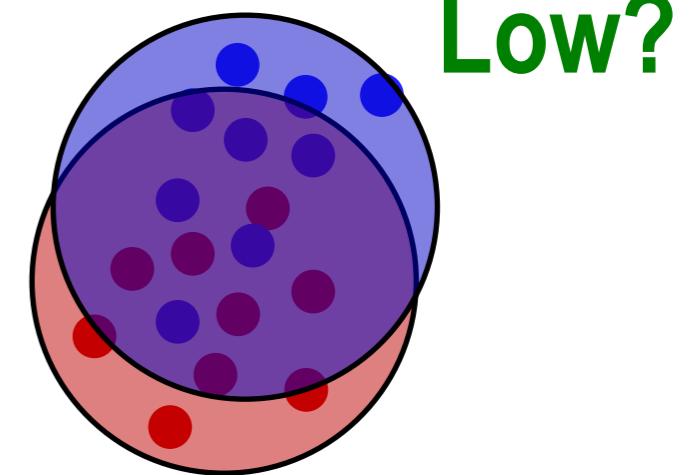
## Discrepancy

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Not computable in general



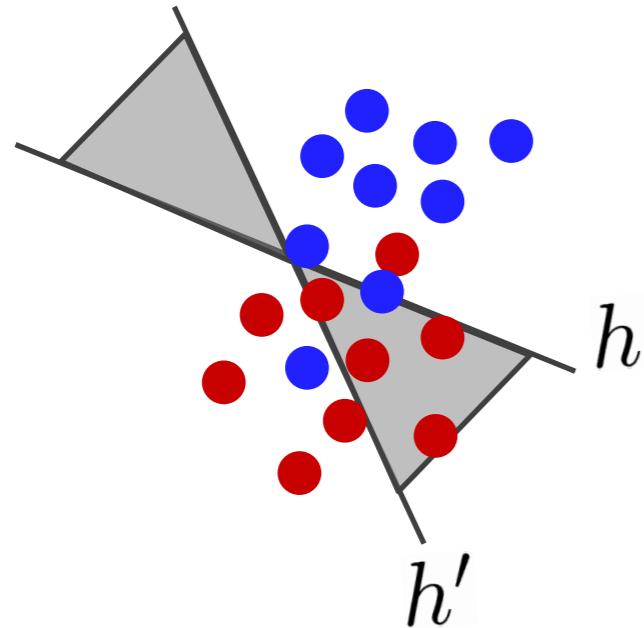


# Discrepancy vs. Total Variation



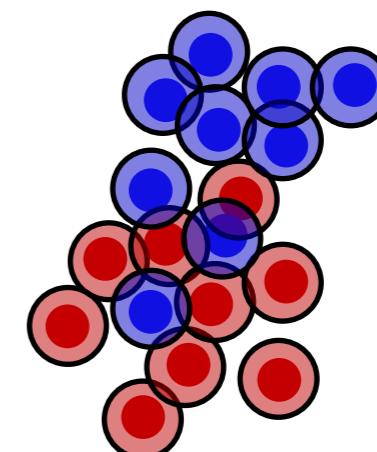
## Discrepancy

Computable from finite samples.



## Total Variation

Not computable in general



High?

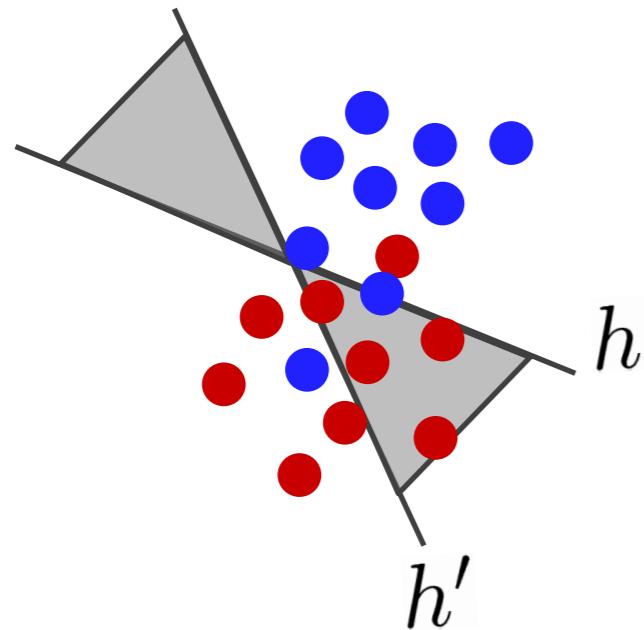


# Discrepancy vs. Total Variation



## Discrepancy

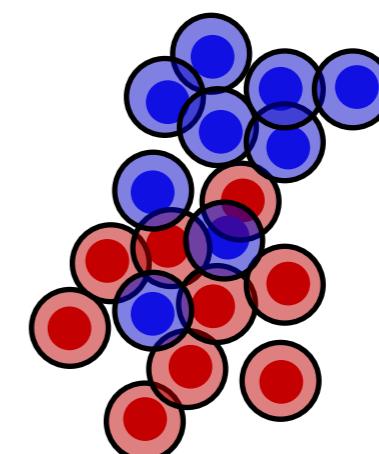
Computable from finite samples.



Related to hypothesis class

## Total Variation

Not computable in general



High?

Unrelated to hypothesis class

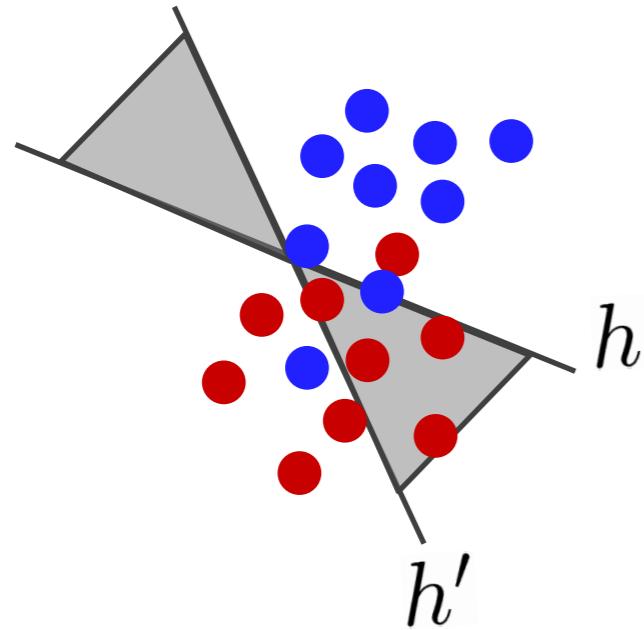


# Discrepancy vs. Total Variation



## Discrepancy

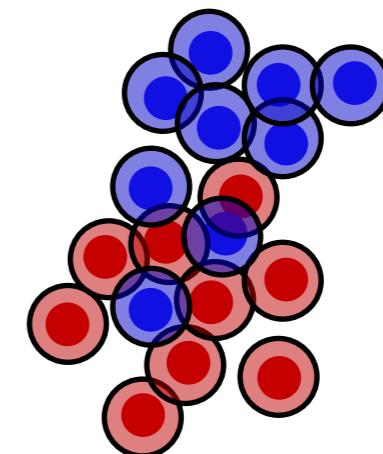
Computable from finite samples.



Related to hypothesis class

## Total Variation

Not computable in general



High?

Unrelated to hypothesis class

Bickel covariate shift algorithm heuristically minimizes both measures



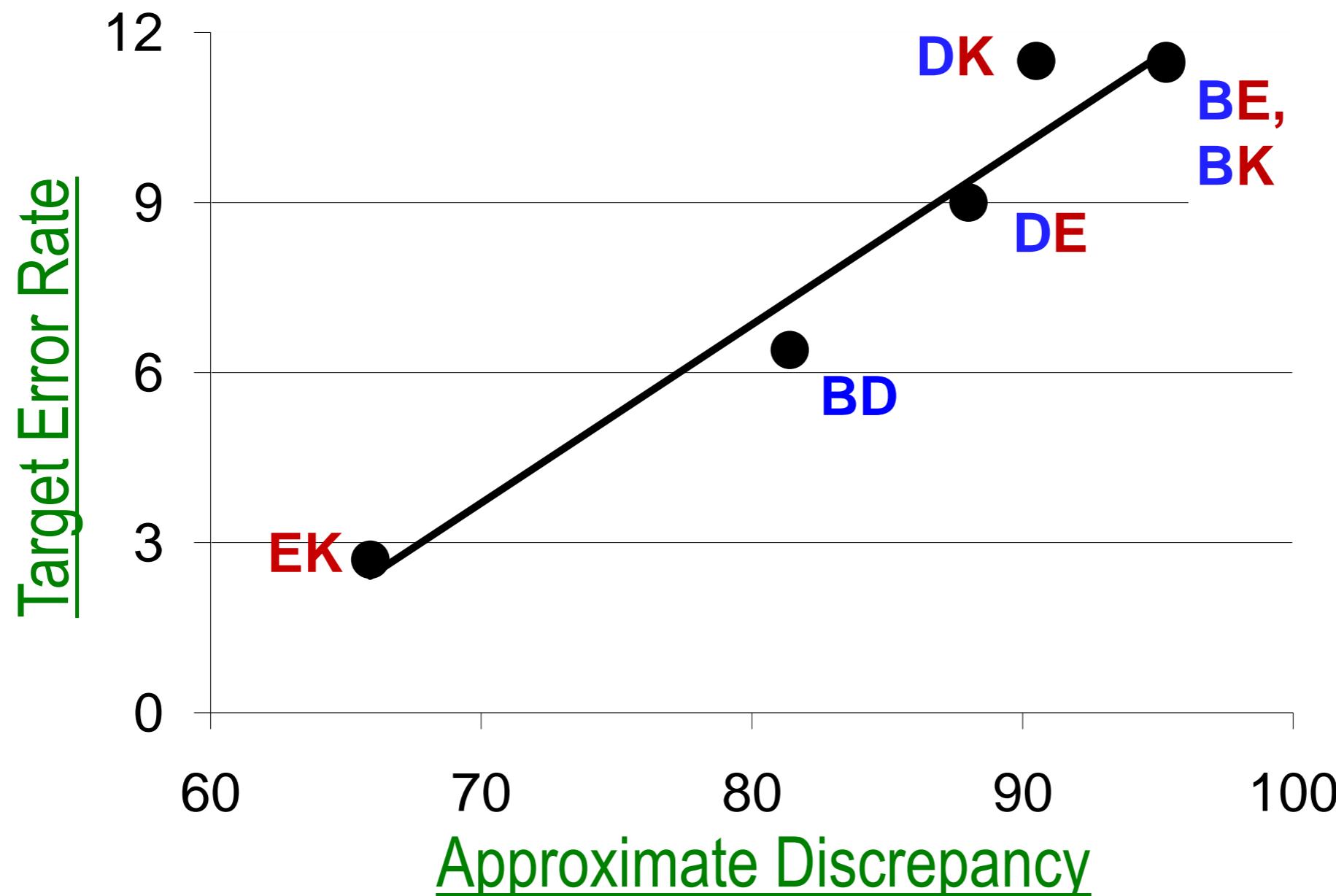
# Is Discrepancy Intuitively Correct?



4 domains: Books, DVDs, Electronics, Kitchen      B&D, E&K      Shared Vocabulary

B&D: *fascinating, boring*

E&K: *super easy, bad quality*





# A new adaptation bound



$S, T$ : Source and target     $\mathcal{H}$ : Hypothesis class     $n$ : Sample size

$\hat{S}$ : Labeled  $S$  sample     $\hat{T}$ : Unlabeled  $T$  sample

$\mathcal{R}_{\hat{S}}(\mathcal{H}), \mathcal{R}_{\hat{T}}(\mathcal{H})$ : Rademacher complexities

With probability  $1 - \delta$ , for  $h$  the ERM of  $\hat{S}$ :

$$\epsilon_T(h) - \epsilon_T(h^*) \leq \epsilon_{\hat{S}}(h, h^*) + O(\mathcal{R}_{\hat{S}}(\mathcal{H}) + \mathcal{R}_{\hat{T}}(\mathcal{H}))$$
$$+ O\left(\sqrt{\frac{\log \frac{1}{\delta}}{n}}\right) + \text{disc}_{\mathcal{H}}(\hat{S}, \hat{T})$$



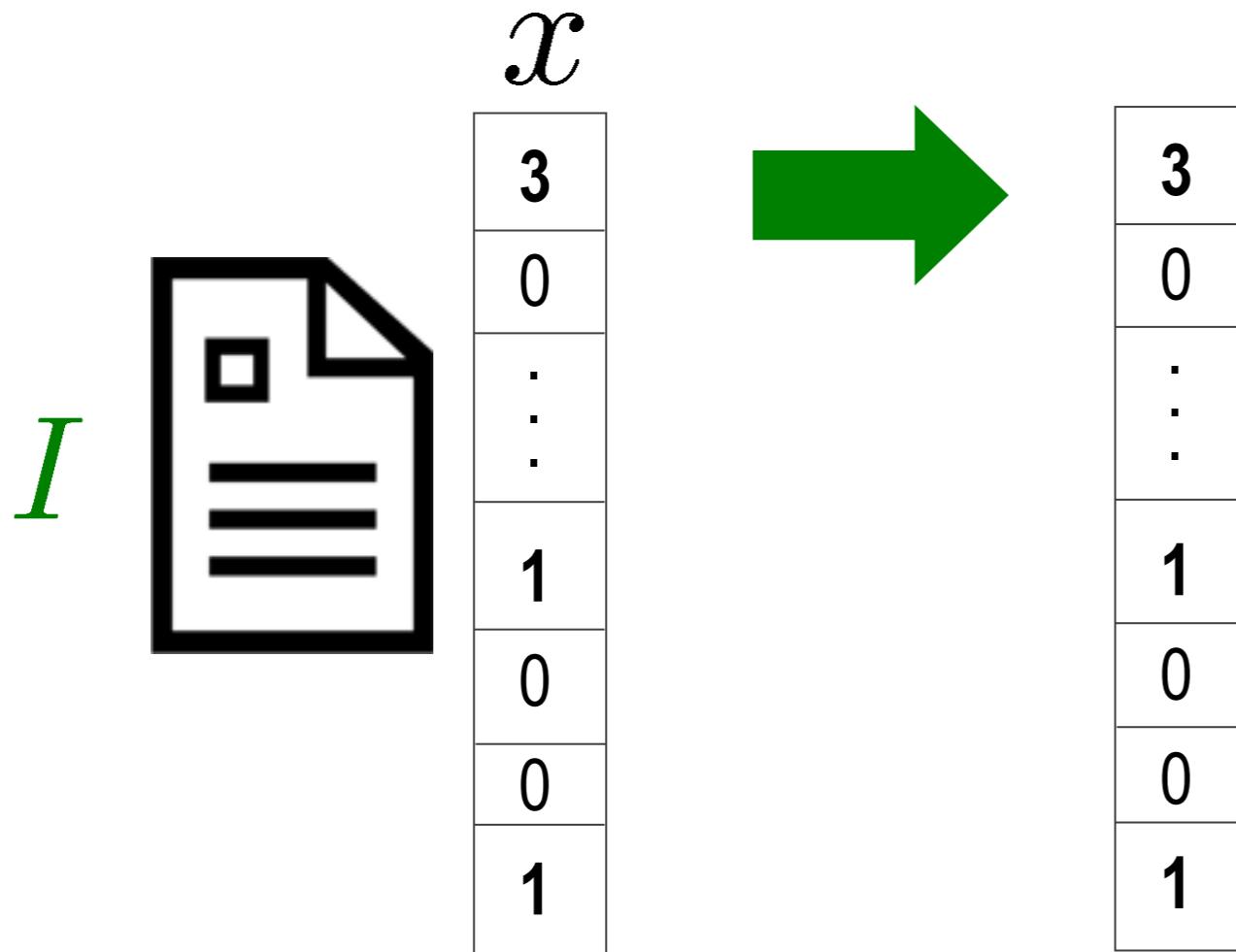
# Representations and the Bound



Linear Hypothesis Class:  $h(x) = \text{sgn}(\theta^\top x)$

$$P = I$$

Hypothesis classes from projections  $P$ :  $\theta^\top P x$





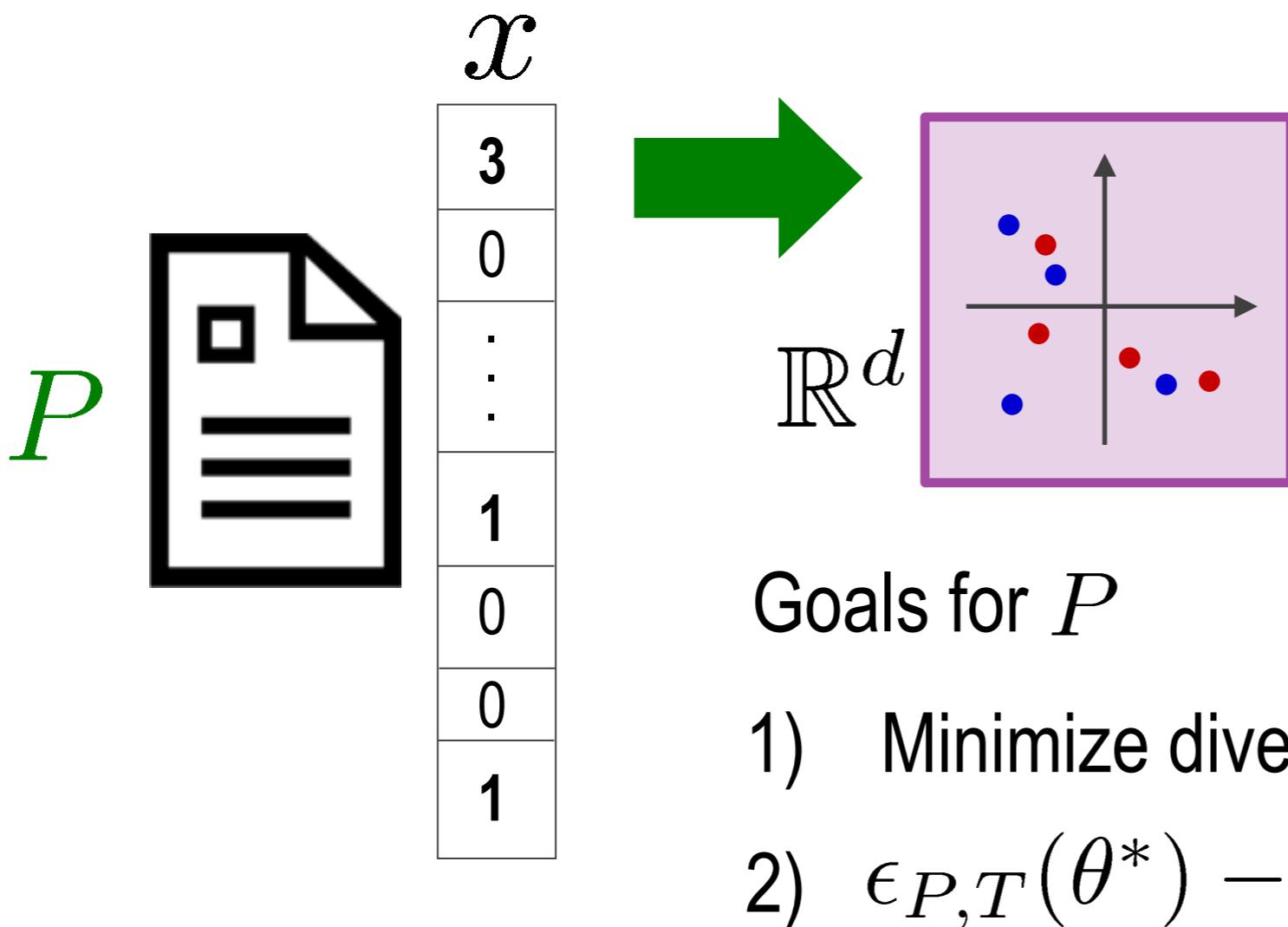
# Representations and the Bound



Linear Hypothesis Class:  $h(x) = \text{sgn}(\theta^\top x)$

$P$

Hypothesis classes from projections  $P$ :  $\theta^\top P x$





# Learning Representations: Pivots



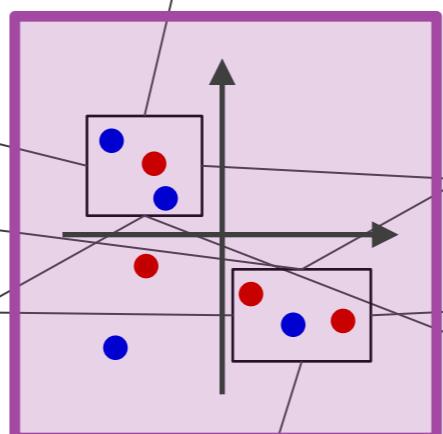
Source



*fascinating*  
*boring*  
*read half*  
*couldn't put it down*

Pivot words  
*fantastic*  
*highly recommended*

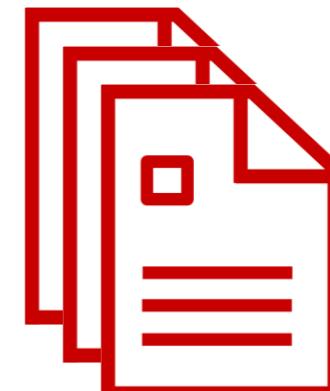
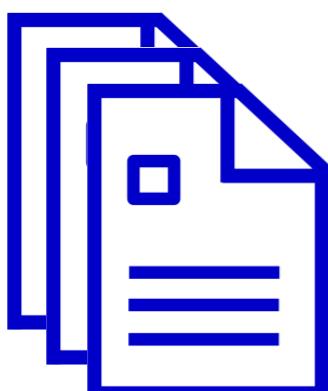
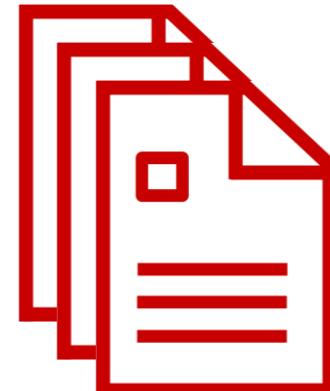
$$\mathbb{R}^d$$



*defective*  
*sturdy*  
*leaking*  
*like a charm*

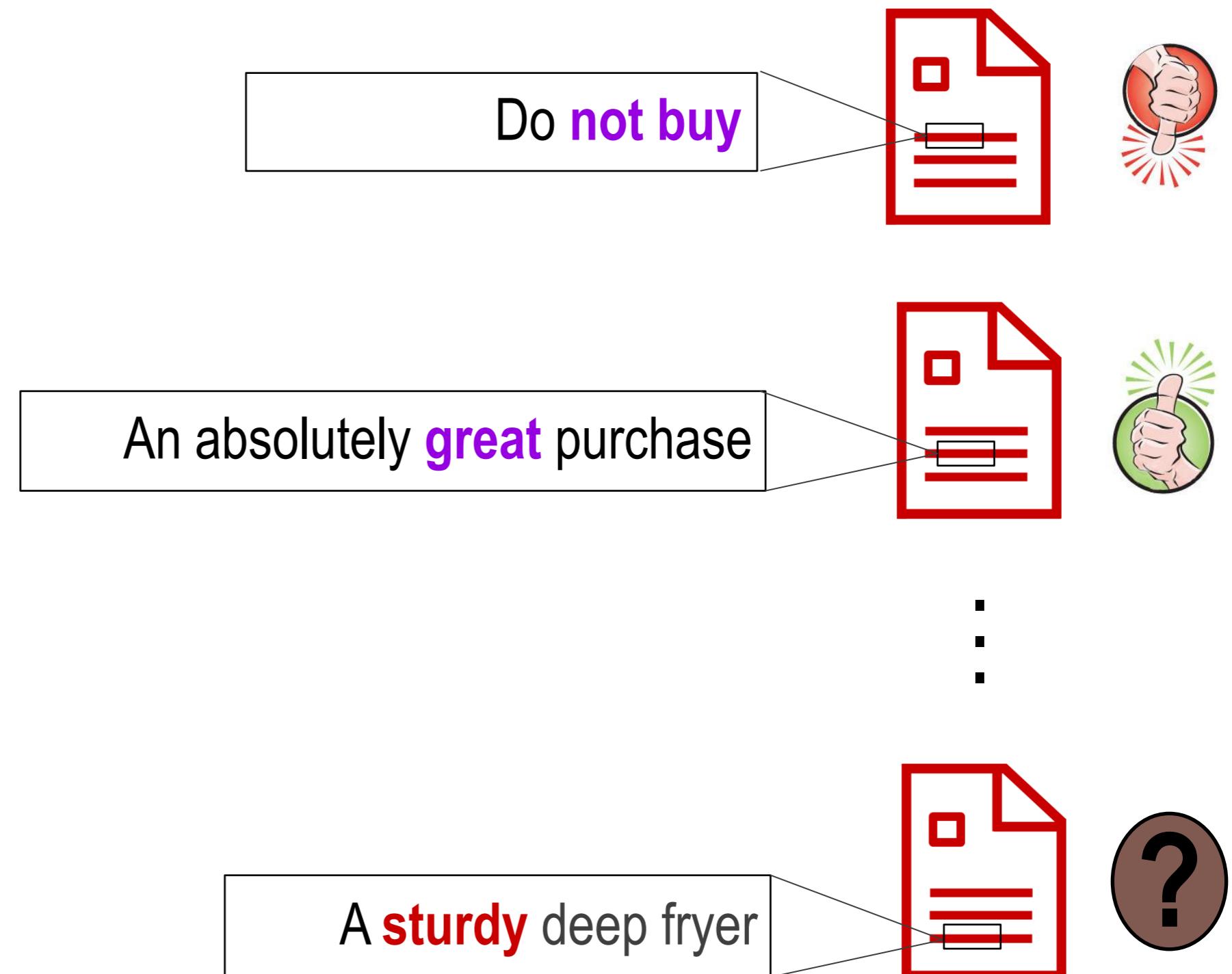
*waste of money*  
*horrible*

Target





# Predicting pivot word presence

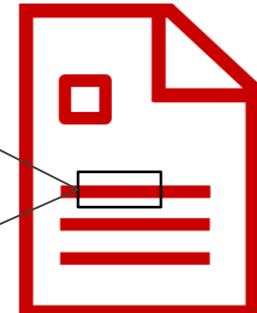




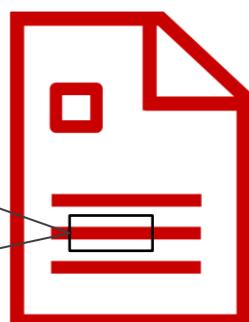
# Predicting pivot word presence



Do **not buy** the Shark portable steamer.  
The trigger mechanism is **defective**.

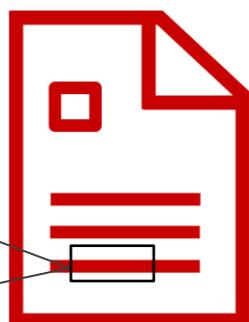


An absolutely **great** purchase



⋮

A **sturdy** deep fryer

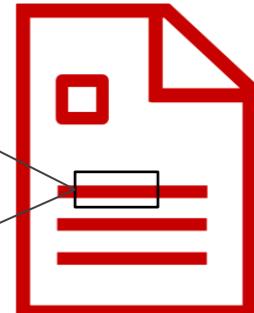




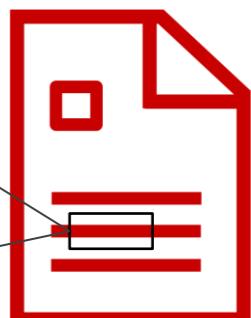
# Predicting pivot word presence



Do **not buy** the Shark portable steamer.  
The trigger mechanism is **defective**.



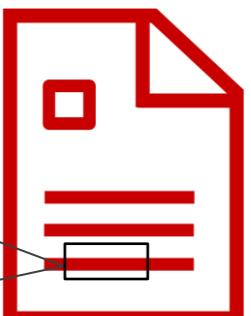
An absolutely **great** purchase. . . . This  
blender is incredibly **sturdy**.



## Predict presence of pivot words

$$p_{w(\text{great})}(\text{great} | x) \propto \exp \{ \langle x, w(\text{great}) \rangle \}$$

A **sturdy** deep fryer



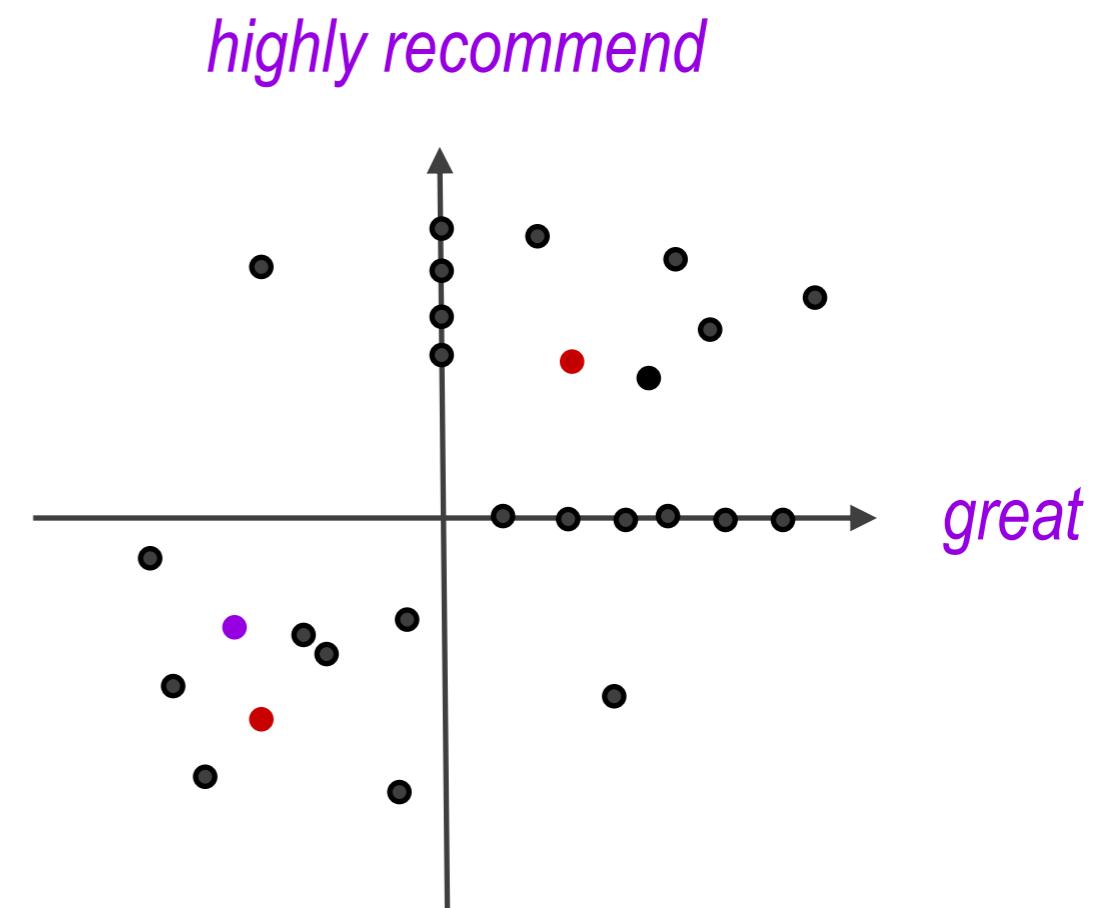


# Finding a shared sentiment subspace



$$W = \begin{bmatrix} | & & | & & | \\ w_1 & \dots & w(\text{highly recommend}) & \dots & w_N \\ | & & | & & | \end{bmatrix}$$

- $p_W(\text{pivots}|x)$  generates N new features
- $p_{w(\text{highly recommend})}(\text{highly recommend}|x)$  : “Did *highly recommend* appear?”
- Sometimes predictors capture non-sentiment information



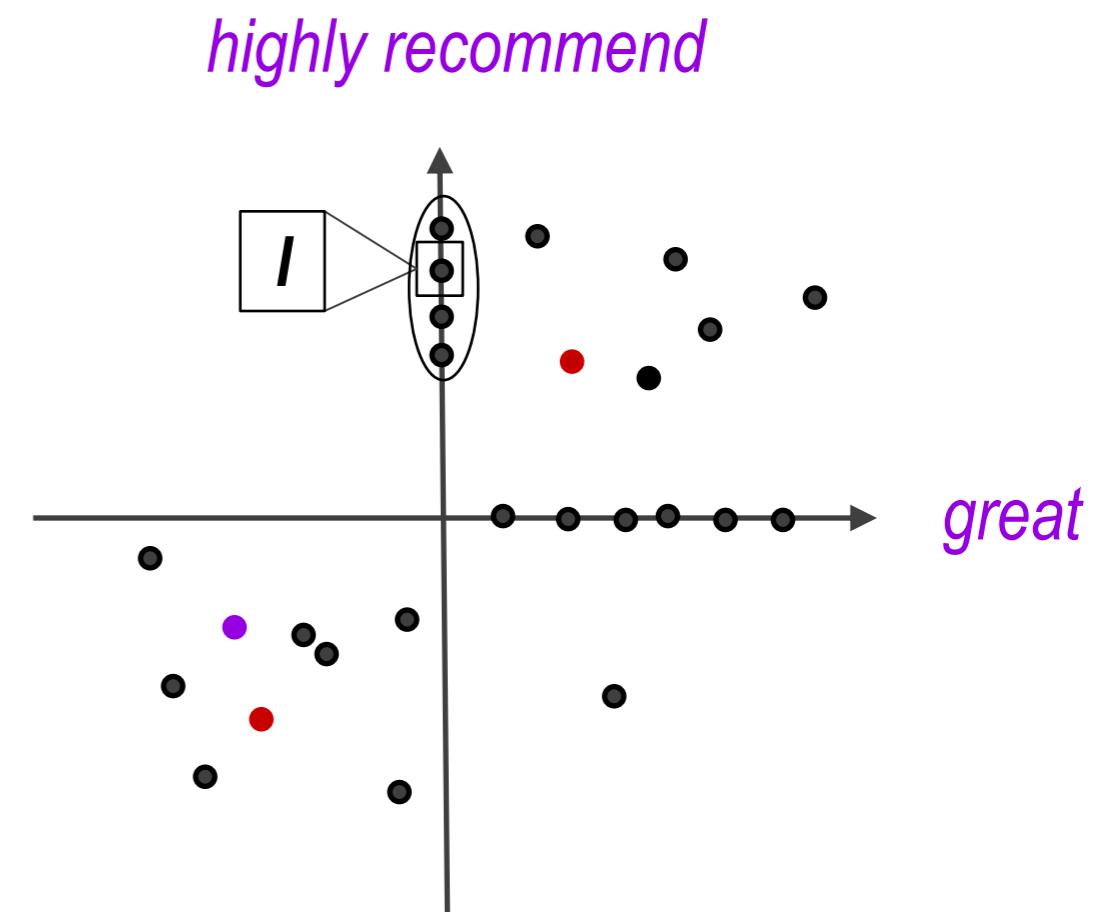


# Finding a shared sentiment subspace



$$W = \begin{bmatrix} | & & | & & | \\ w_1 & \dots & w(\text{highly recommend}) & \dots & w_N \\ | & & | & & | \end{bmatrix}$$

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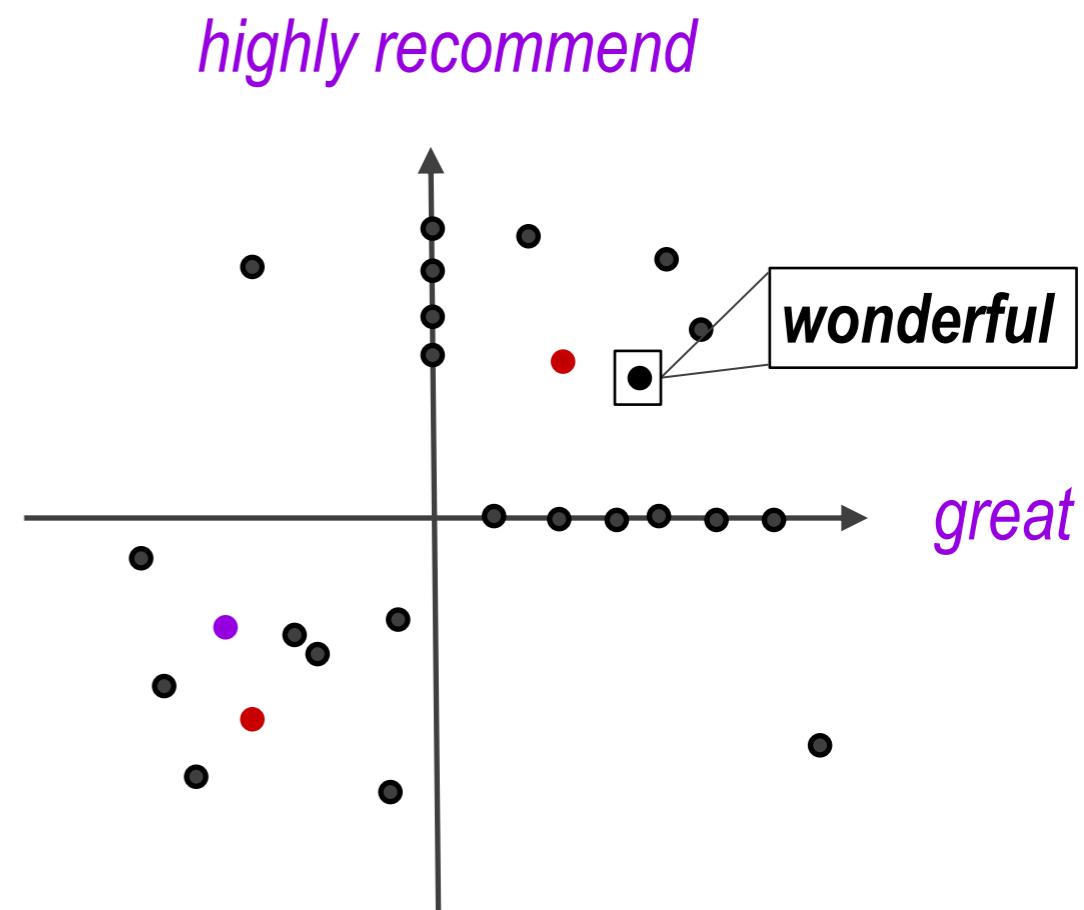


# Finding a shared sentiment subspace



$$W = \begin{bmatrix} | & & | & & | \\ w_1 & \dots & w(\text{highly recommend}) & \dots & w_N \\ | & & | & & | \end{bmatrix}$$

- $p_W(\text{pivots}|x)$  generates N new features
- $p_w(\text{highly recommend})(\text{highly recommend}|x)$  : “Did *highly recommend* appear?”
- Sometimes predictors capture non-sentiment information





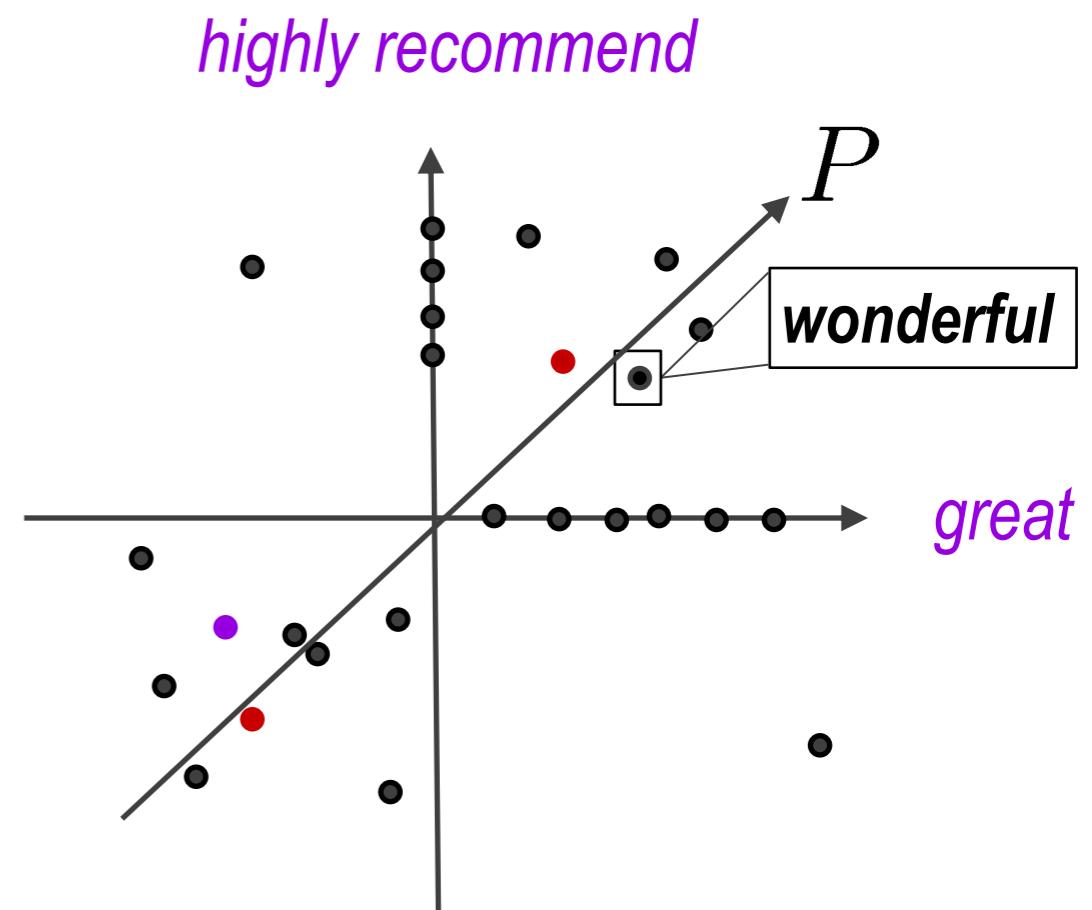
# Finding a shared sentiment subspace



$$W = \begin{bmatrix} | & & | & & | \\ w_1 & \dots & w(\text{highly recommend}) & \dots & w_N \\ | & & | & & | \end{bmatrix}$$

- Let  $P$  be a basis for the subspace of best fit to  $W$

- $p_W(\text{pivots}|x)$  generates N new features
- $p_w(\text{highly recommend})(\text{highly recommend}|x)$  : “Did *highly recommend* appear?”
- Sometimes predictors capture non-sentiment information





# Finding a shared sentiment subspace

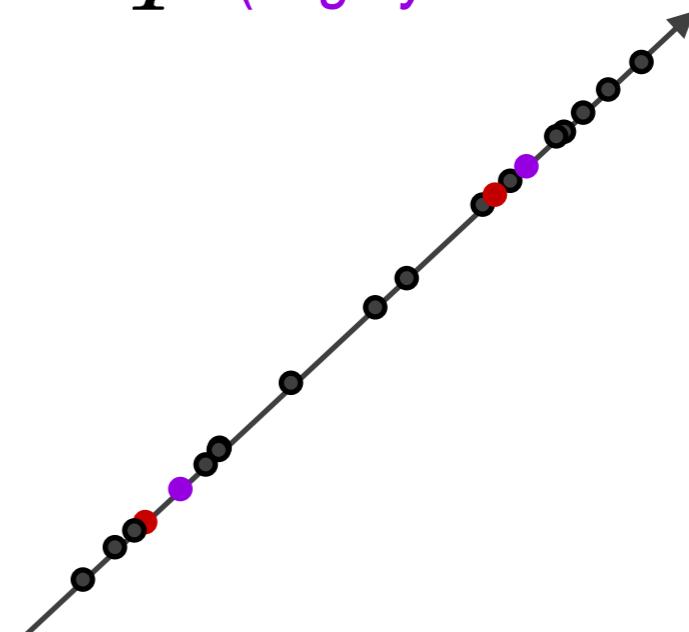


$$W = \begin{bmatrix} | & & | & & | \\ w_1 & \dots & w(\text{highly recommend}) & \dots & w_N \\ | & & | & & | \end{bmatrix}$$

- Let  $P$  be a basis for the subspace of best fit to  $W$
- $P$  captures sentiment variance in  $W$

- $p_W(\text{pivots}|x)$  generates N new features
- $p_{w(\text{highly recommend})}(\text{highly recommend}|x)$  : “Did **highly recommend** appear?”
- Sometimes predictors capture non-sentiment information

$P$  (*highly recommend, great*)

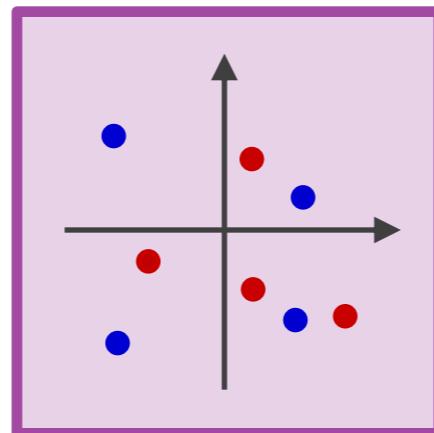
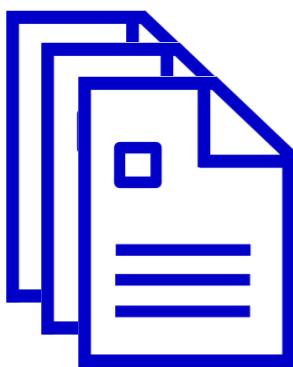




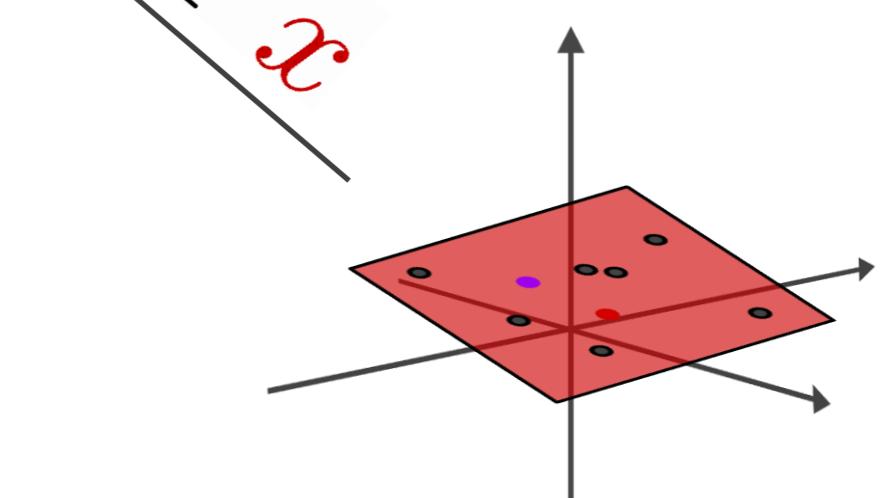
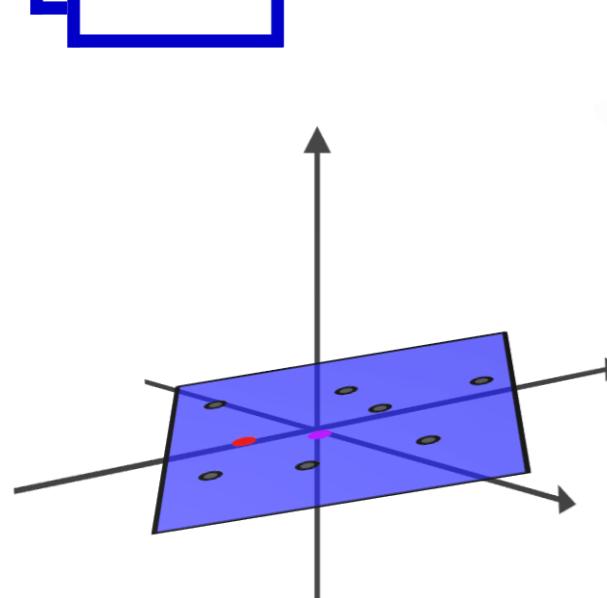
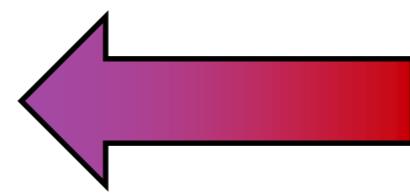
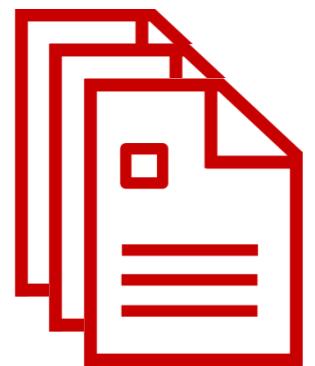
# P projects onto shared subspace



Source



Target



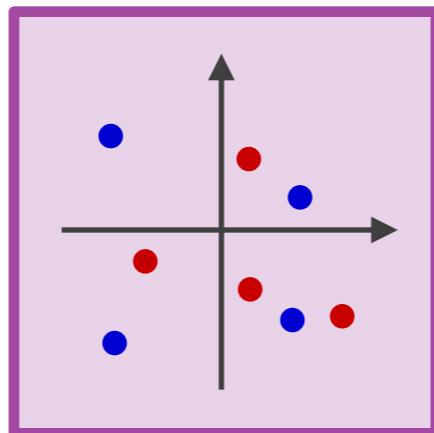
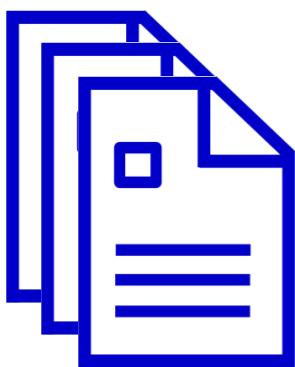
$$p_{\tilde{\theta}}(\text{👍} | x) \propto \exp \left\{ \langle \phi(\text{👍}, P x), \tilde{\theta} \rangle \right\}$$



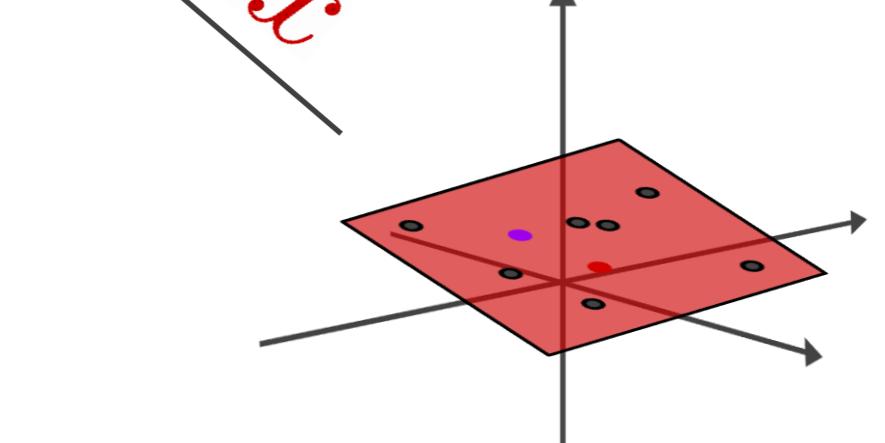
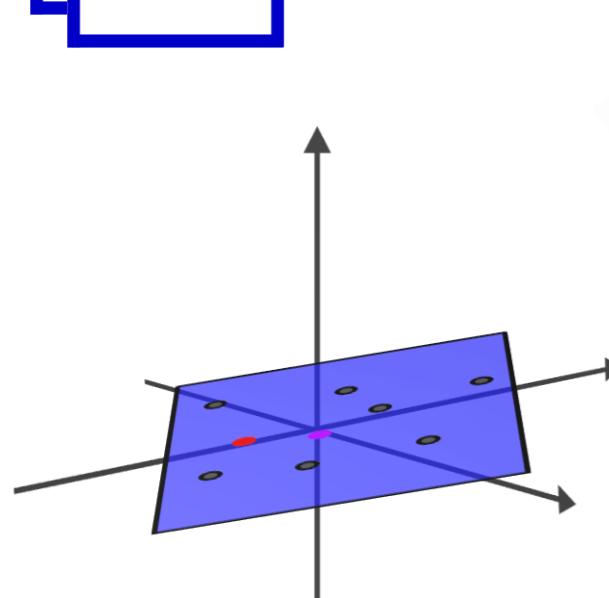
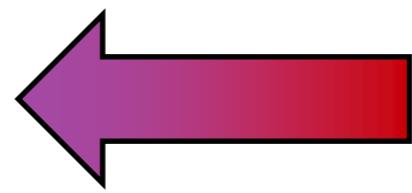
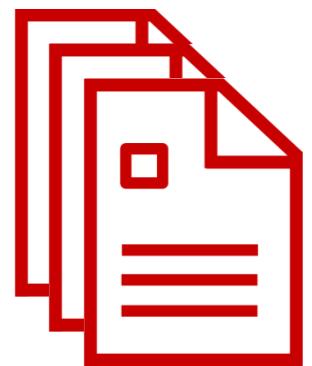
# P projects onto shared subspace



Source



Target



$$h(x) = \text{sgn} (\theta^\top P x)$$



# Correlating Pieces of the Bound



$$\begin{aligned}\epsilon_T(h) - \epsilon_T(h^*) &\leq \epsilon_{\hat{S}}(h, h^*) + O(\mathcal{R}_{\hat{S}}(\mathcal{H}) + \mathcal{R}_{\hat{T}}(\mathcal{H})) \\ &+ O\left(\sqrt{\frac{\log \frac{1}{\delta}}{n}}\right) + \text{disc}_{\mathcal{H}}(\hat{S}, \hat{T})\end{aligned}$$

Component Projection	Discrepancy	Source	Target Error
Identity	1.796	0.003	0.253



# Correlating Pieces of the Bound



$$\begin{aligned}\epsilon_T(h) - \epsilon_T(h^*) &\leq \epsilon_{\hat{S}}(h, h^*) + O(\mathcal{R}_{\hat{S}}(\mathcal{H}) + \mathcal{R}_{\hat{T}}(\mathcal{H})) \\ &+ O\left(\sqrt{\frac{\log \frac{1}{\delta}}{n}}\right) + \text{disc}_{\mathcal{H}}(\hat{S}, \hat{T})\end{aligned}$$

Component Projection	Discrepancy	Source	Target Error
Identity	1.796	0.003	0.253
Random	0.223	0.254	0.561



# Correlating Pieces of the Bound

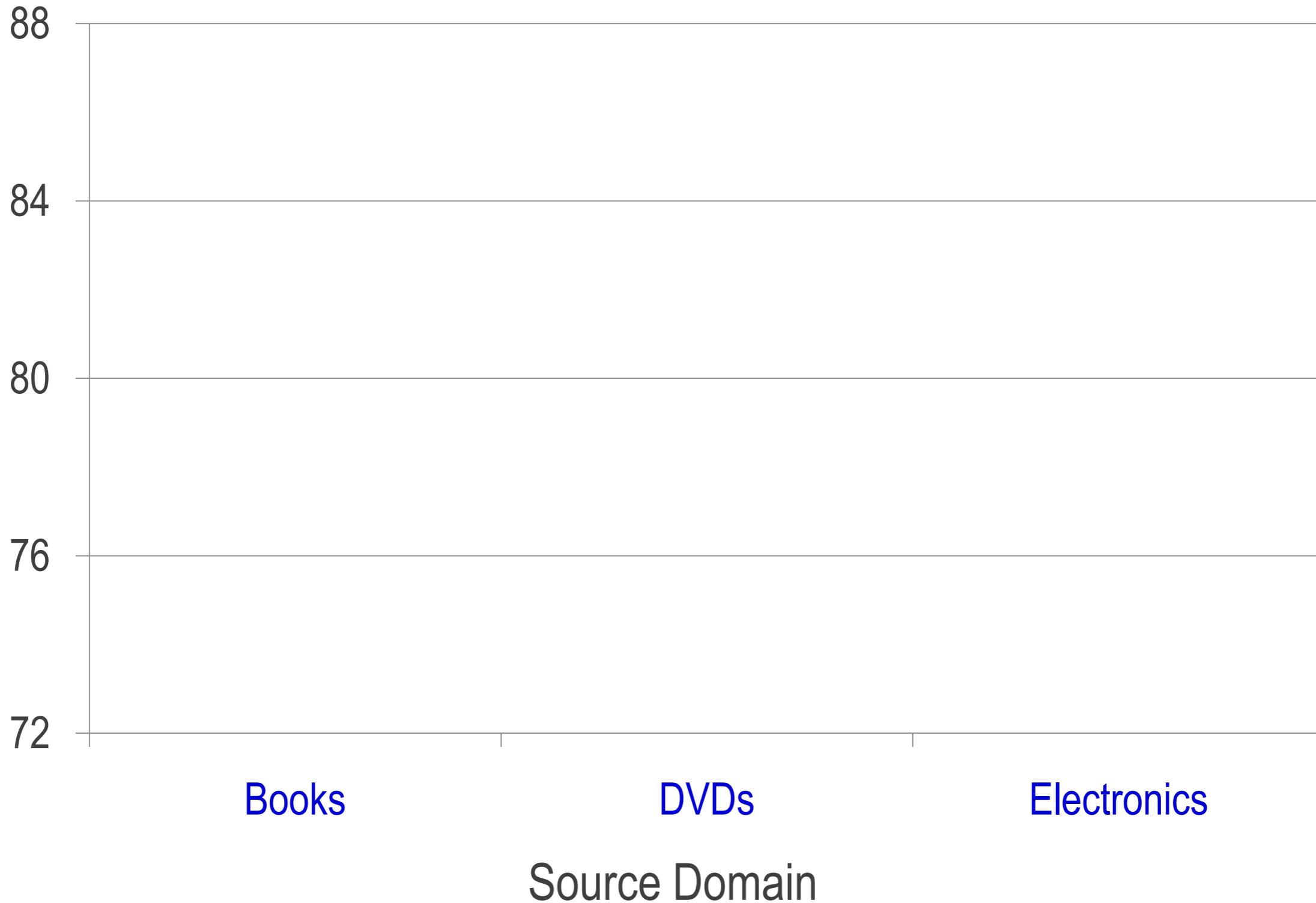


$$\begin{aligned}\epsilon_T(h) - \epsilon_T(h^*) &\leq \epsilon_{\hat{S}}(h, h^*) + O(\mathcal{R}_{\hat{S}}(\mathcal{H}) + \mathcal{R}_{\hat{T}}(\mathcal{H})) \\ &+ O\left(\sqrt{\frac{\log \frac{1}{\delta}}{n}}\right) + \text{disc}_{\mathcal{H}}(\hat{S}, \hat{T})\end{aligned}$$

Component Projection	Discrepancy	Source Huber Loss	Target Error
Identity	1.796	0.003	0.253
Random	0.223	0.254	0.561
Coupled Projection	0.211	0.07	0.216

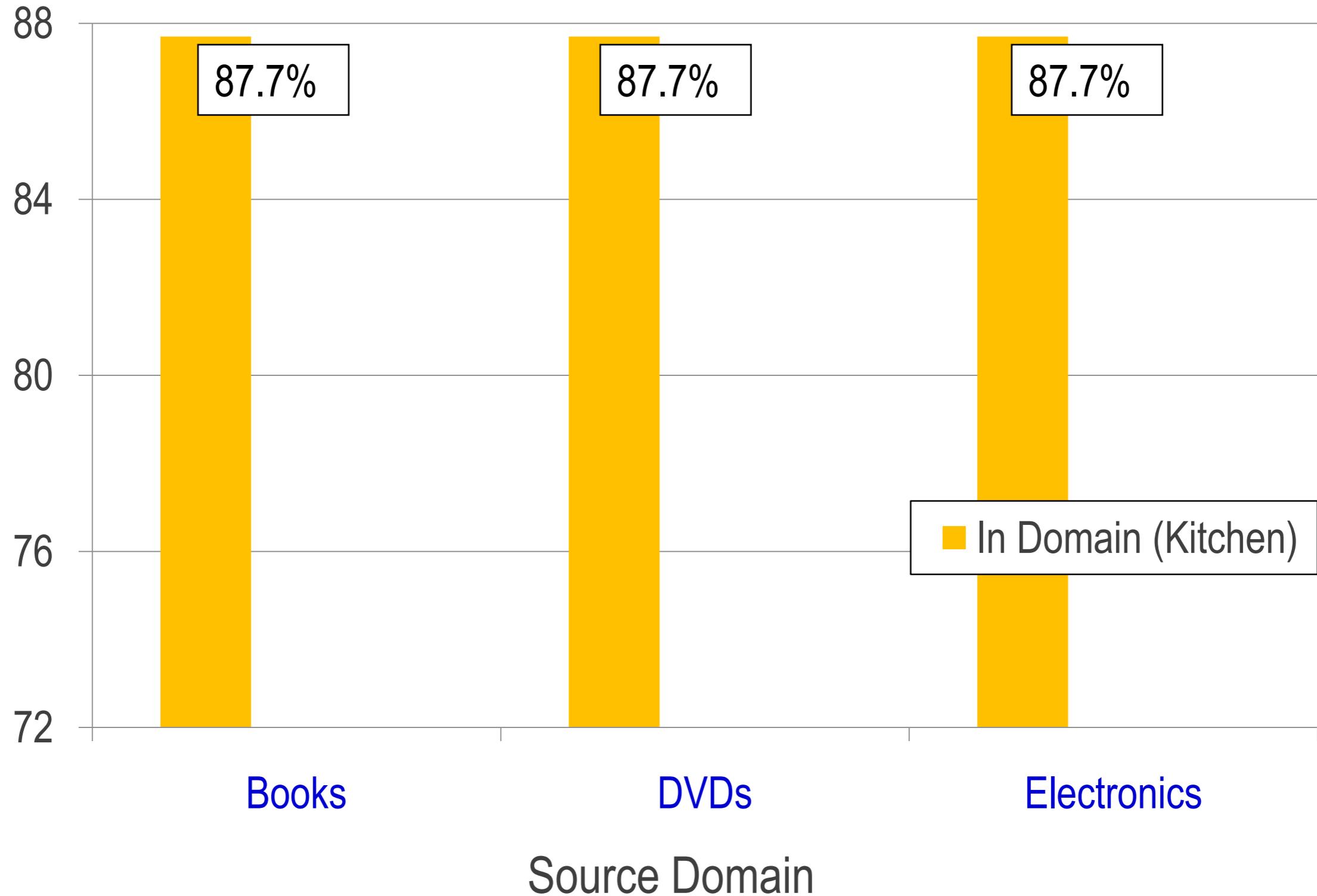


# Target Accuracy: Kitchen Appliances



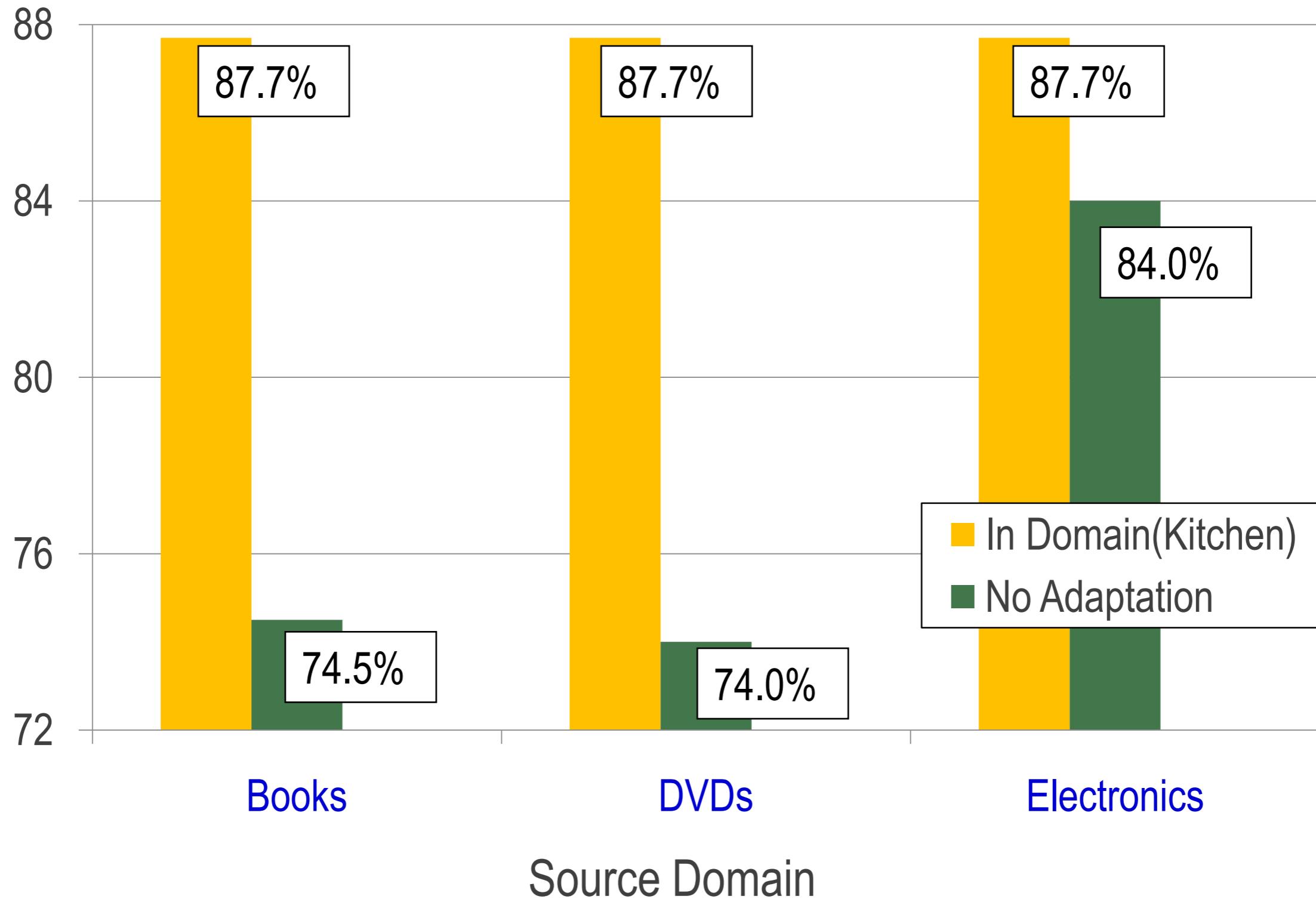


# Target Accuracy: Kitchen Appliances



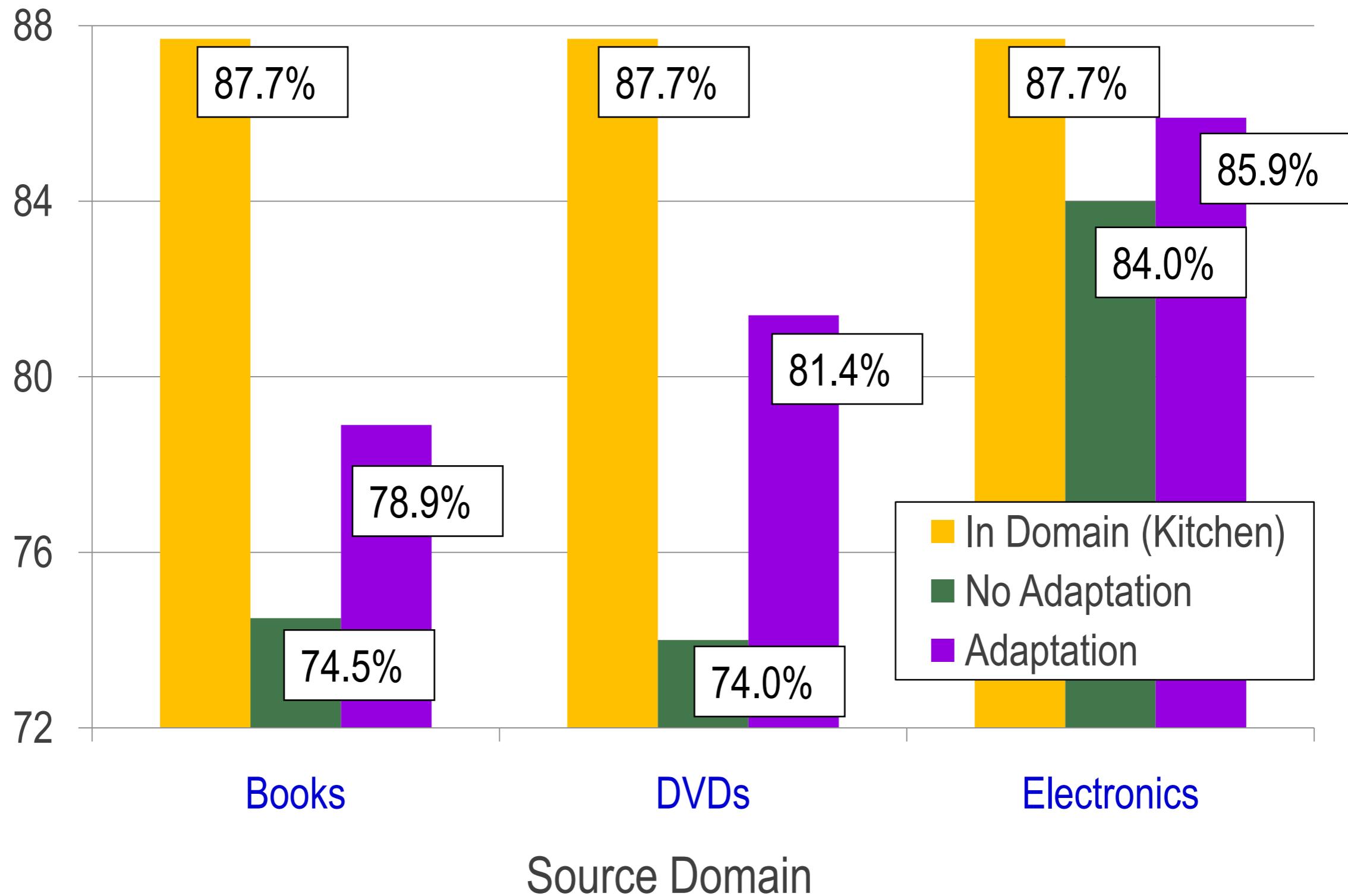


# Target Accuracy: Kitchen Appliances



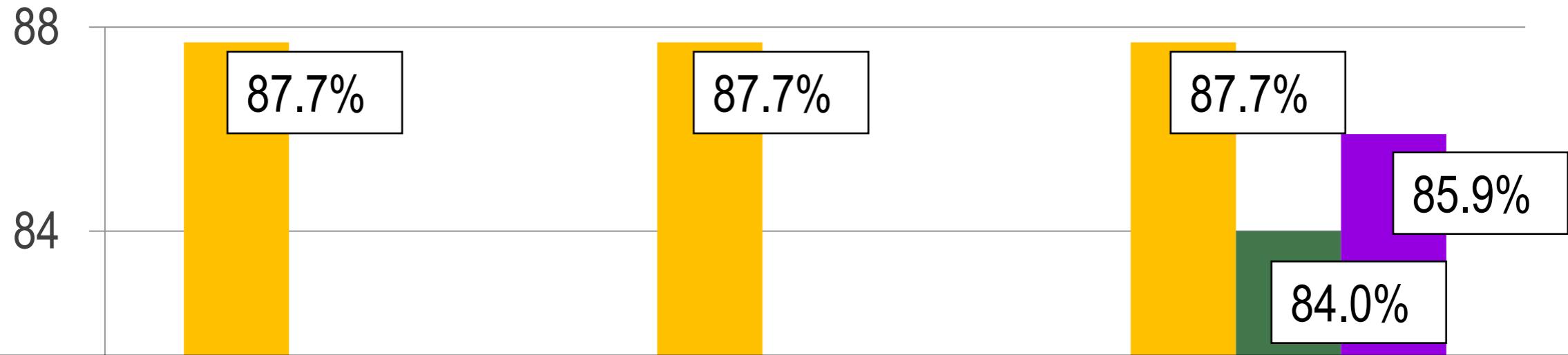


# Target Accuracy: Kitchen Appliances





# Adaptation Error Reduction



**36% reduction in error due to adaptation**



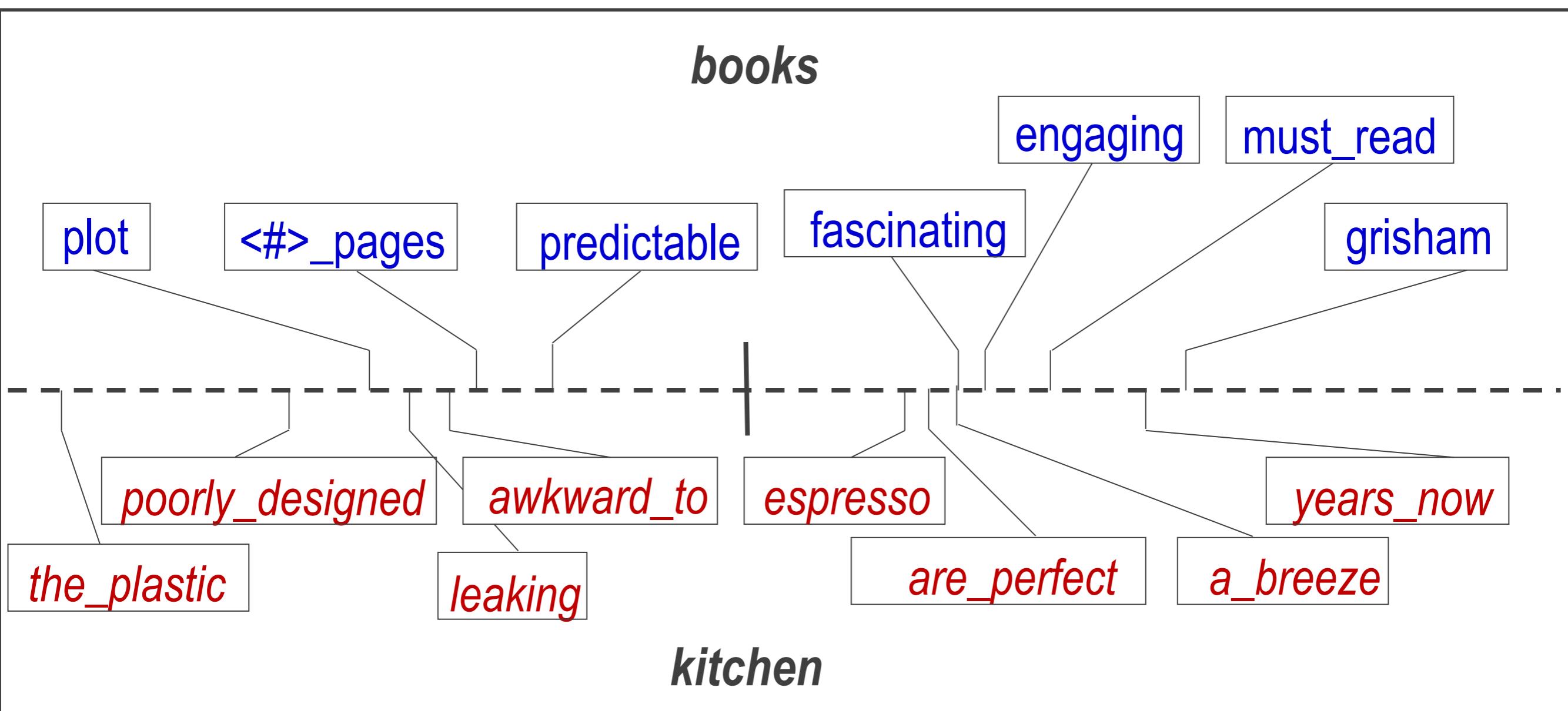
# Visualizing $P$ (books & kitchen)



negative

vs.

positive





# Representation References

---



<http://adaptationtutorial.blitzer.com/references/>

- [1] Blitzer et al. Domain Adaptation with Structural Correspondence Learning. 2006.
- [2] S. Ben-David et al. Analysis of Representations for Domain Adaptation. 2007.
- [3] J. Blitzer et al. Domain Adaptation for Sentiment Classification. 2008.
- [4] Y. Mansour et al. Domain Adaptation: Learning Bounds and Algorithms. 2009.



# Tutorial Outline

---



1. Notation and Common Concepts
2. Semi-supervised Adaptation
  - Covariate shift
  - Learning Shared Representations
3. Supervised Adaptation
  - Feature-Based Approaches
  - Parameter-Based Approaches
4. Open Questions and Uncovered Algorithms



# Feature-based approaches



## Cell-phone domain:

“horrible” is **bad**  
“small” is **good**

## Hotel domain:

“horrible” is **bad**  
“small” is **bad**

### **Key Idea:**

Share some features (“horrible”)  
Don't share others (“small”)

(and let an arbitrary *learning algorithm* decide which are which)



F

In feature-vector lingo:

$x \rightarrow \langle x, x, 0 \rangle$  (for source domain)

$x \rightarrow \langle x, 0, x \rangle$  (for target domain)

The phone is small

The hotel is small

Original  
Features

W:the  
W:phone  
W:is  
W:small

W:the  
W:hotel  
W:is  
W:small

Augmented  
Features

S:the  
S:phone  
S:is  
S:small

T:the  
T:hotel  
T:is  
T:small



# A Kernel Perspective



In feature-vector lingo:

$x \rightarrow \langle x, x, 0 \rangle$  (for source domain)

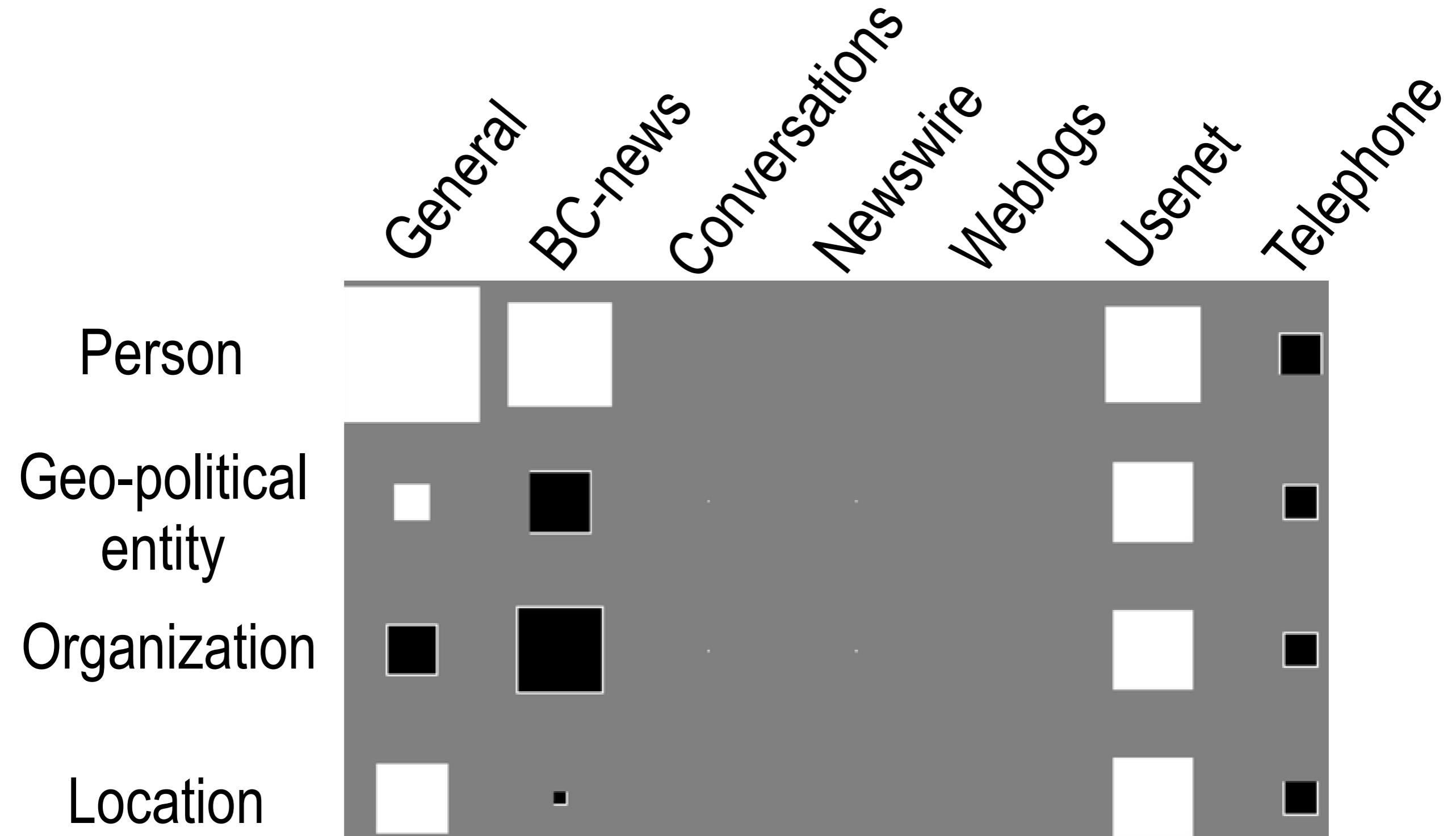
$x \rightarrow \langle x, 0, x \rangle$  (for target domain)

$$K^{\text{aug}}(x, z) = \begin{cases} 2K(x, z) & \text{if } x, z \text{ from same domain} \\ K(x, z) & \text{otherwise} \end{cases}$$

We have *ensured*  
SGH & *destroyed*  
shared support

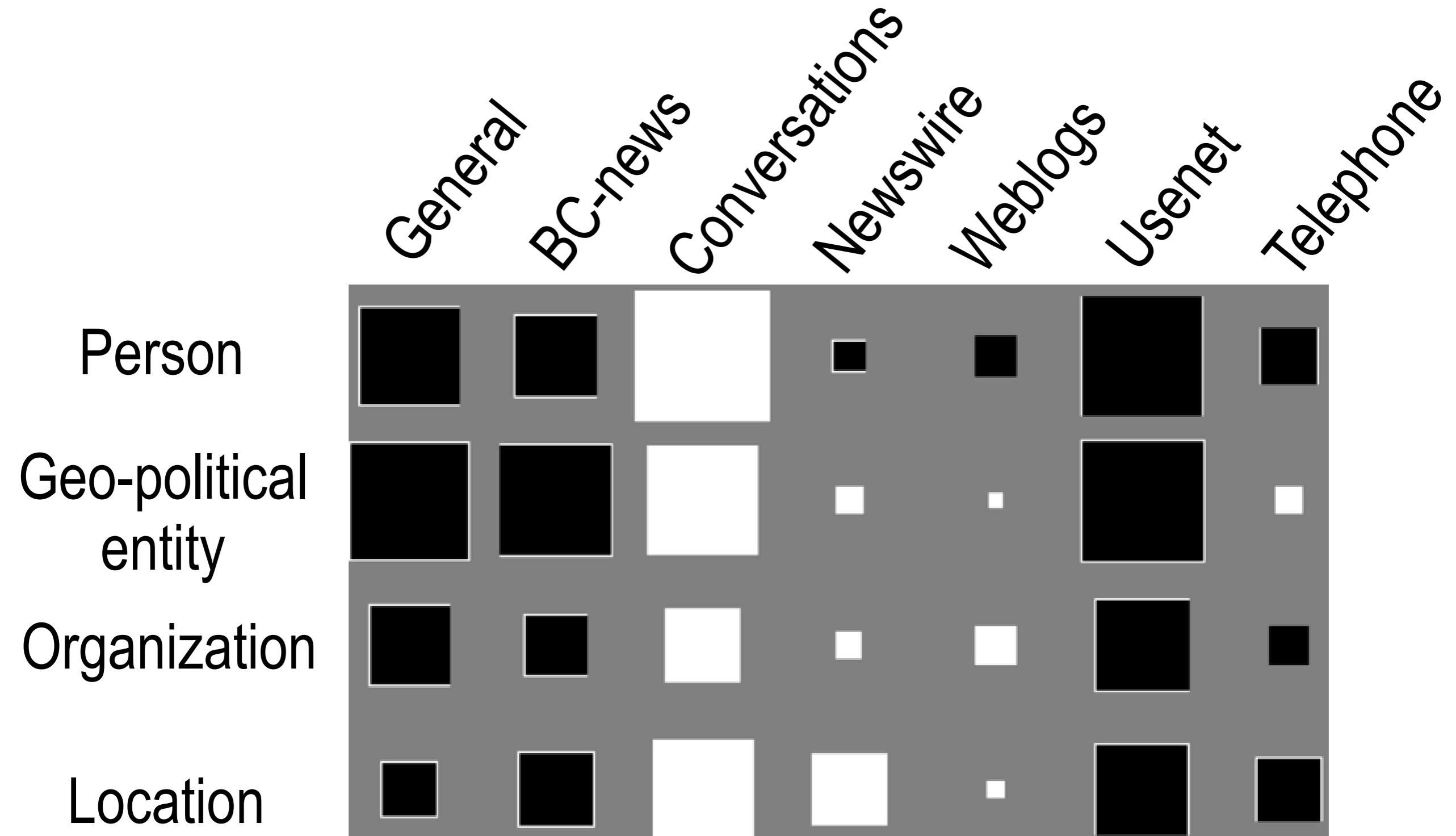


# Named Entity Rec.: /bush/





# Named Entity Rec.: p=/the/





# Some experimental results



Task	Dom	SrcOnly	TgtOnly	Baseline	Prior	Augment
ACE-NER	bn	4.98	2.37	2.11 (pred)	2.06	<b>1.98</b>
	bc	4.54	4.07	3.53 (weight)	<b>3.47</b>	<b>3.47</b>
	nw	4.78	3.71	3.56 (pred)	3.68	<b>3.39</b>
	wl	2.45	2.45	<b>2.12</b> (all)	2.41	<b>2.12</b>
	un	3.67	2.46	2.10 (linint)	2.03	<b>1.91</b>
	cts	2.08	0.46	0.40 (all)	<b>0.34</b>	<b>0.32</b>
CoNLL	tgt	2.49	2.95	<b>1.75</b> (wgt/li)	1.89	<b>1.76</b>
PubMed	tgt	12.02	4.15	3.95 (linint)	3.99	<b>3.61</b>
CNN	tgt	10.29	3.82	3.44 (linint)	<b>3.35</b>	<b>3.37</b>
Treebank-Chunk	wsj	6.63	4.35	4.30 (weight)	4.27	<b>4.11</b>
	swbd3	15.90	4.15	4.09 (linint)	3.60	<b>3.51</b>
	br-cf	5.16	6.27	<b>4.72</b> (linint)	5.22	5.15
	br-cg	4.32	5.36	<b>4.15</b> (all)	4.25	4.90
	br-ck	5.05	6.32	<b>5.01</b> (prd/li)	5.27	5.41
	br-cl	5.66	6.60	<b>5.39</b> (wgt/prd)	5.99	5.73
	br-cm	3.57	6.59	<b>3.11</b> (all)	4.08	4.89
	br-cn	4.60	5.56	<b>4.19</b> (prd/li)	4.48	4.42
	br-cp	4.82	5.62	<b>4.55</b> (wgt/prd/li)	4.87	4.78
	br-cr	5.78	9.13	<b>5.15</b> (linint)	6.71	6.30
Treebank-brown		6.35	5.75	4.72 (linint)	4.72	<b>4.65</b>



# Some Theory



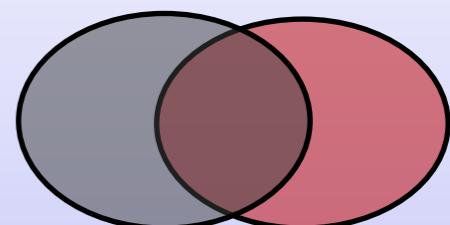
- Can bound expected target error:

Average training error

$$\epsilon_t \leq \frac{1}{2} \left( \hat{\epsilon}_S + \hat{\epsilon}_t \right) + O(\text{complexity}) \\ + \left( \frac{1}{\sqrt{N_S}} + \frac{1}{\sqrt{N_t}} \right) O\left(\frac{1}{\delta}\right) + O(disc_H(S, T))$$

Number of  
source examples

Number of  
target examples

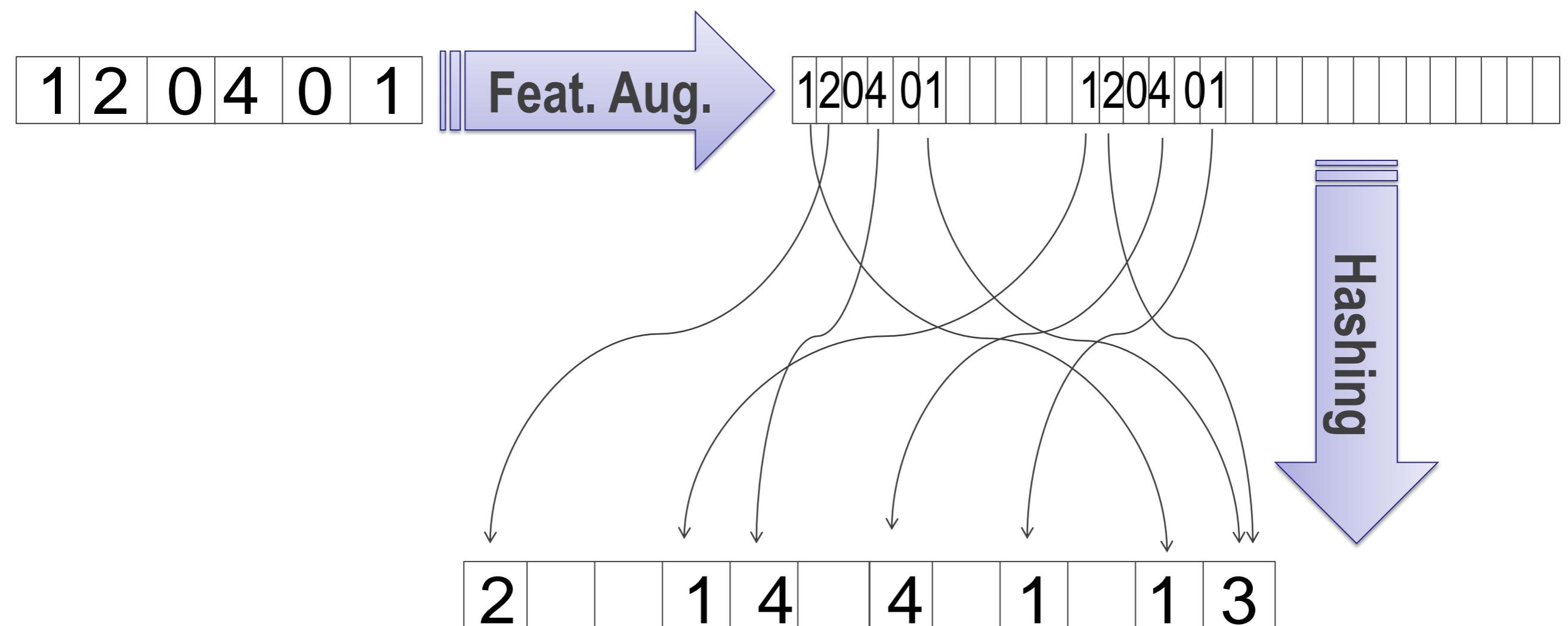




# Feature Hashing

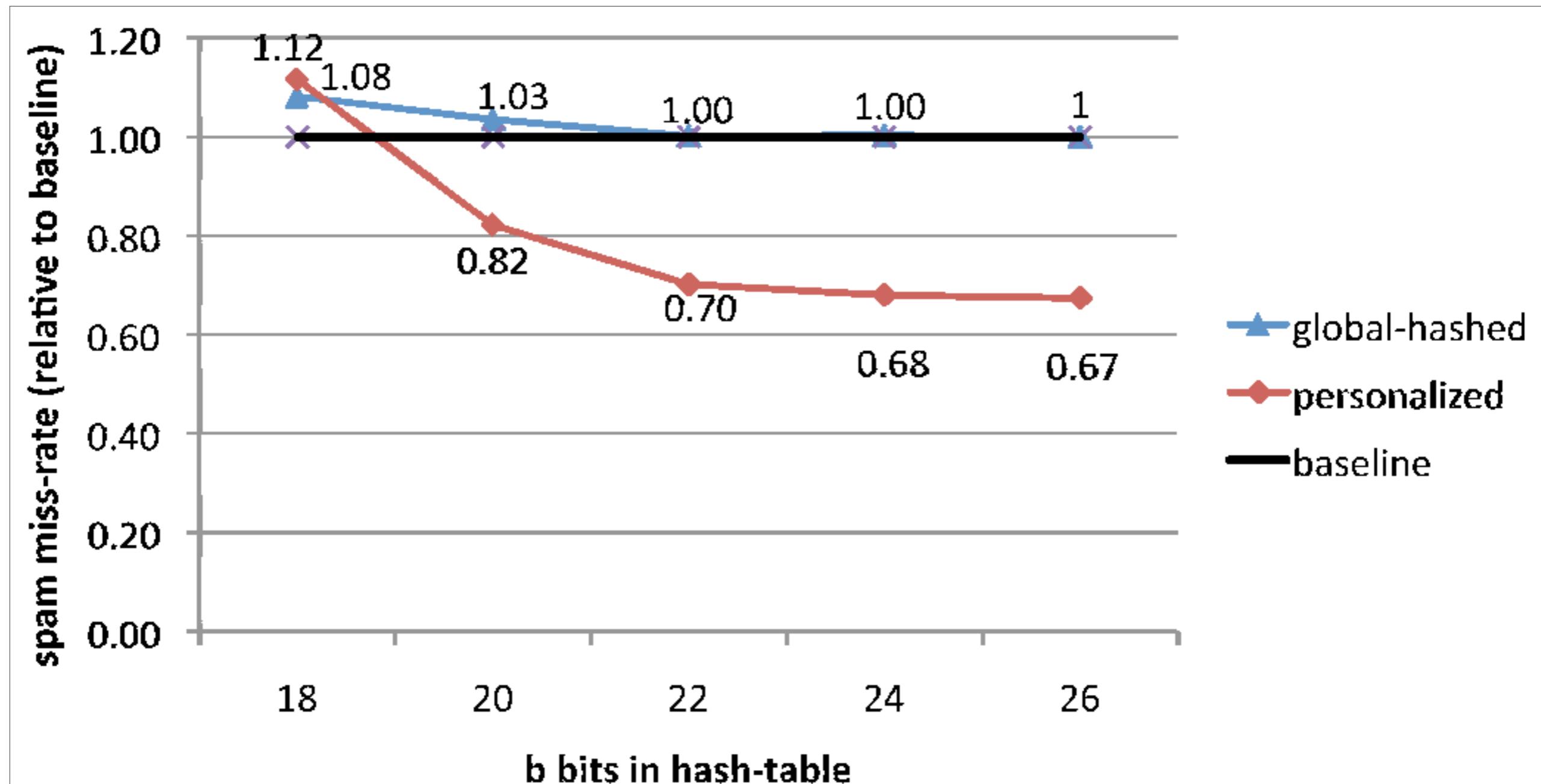


- Feature augmentation creates  $(K+1)D$  parameters
  - Too big if  $K >> 20$ , but *very sparse!*





# Hash Kernels





# Semi-sup Feature Augmentation

---



- For labeled data:
  - $(y, x) \rightarrow (y, \langle x, x, 0 \rangle)$  (for source domain)
  - $(y, x) \rightarrow (y, \langle x, 0, x \rangle)$  (for target domain)
- What about unlabeled data?
- Encourage agreement:

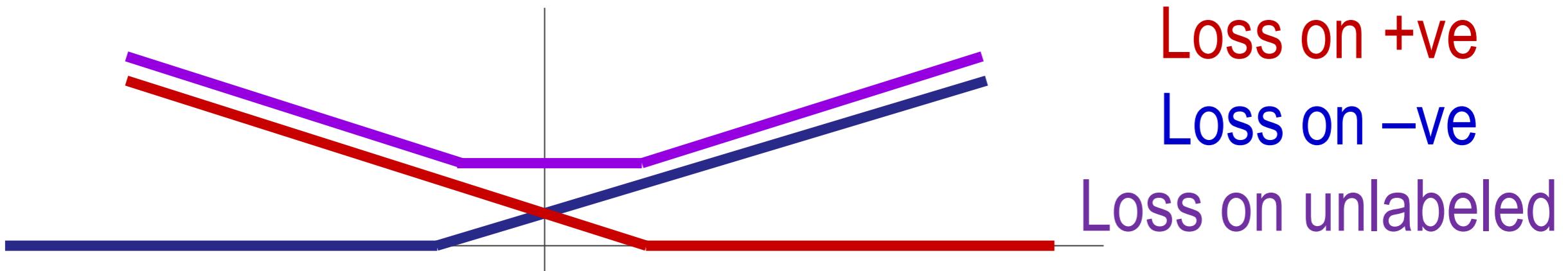
$$[h_t(x) = h_s(x)] \Leftrightarrow [w_t \circ x - w_s \circ x = 0]$$



# Semi-sup Feature Augmentation



- For labeled data:
  - $(y, x) \rightarrow (y, \langle x, x, 0 \rangle)$  (for source domain)
  - $(y, x) \rightarrow (y, \langle x, 0, x \rangle)$  (for target domain)
- What about unlabeled data?
  - $(x) \rightarrow \{ (+1, \langle 0, x, -x \rangle), (-1, \langle 0, x, -x \rangle) \}$



- Encourages *agreement* on unlabeled data
  - Akin to *multiview learning*
  - Reduces generalization bound



# Feature-based References

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- T. Evgeniou and M. Pontil. Regularized Multi-task Learning. (2004).
- H. Daumé III, Frustratingly Easy Domain Adaptation. 2007.
- K. Weinberger, A. Dasgupta, J. Langford, A. Smola, J. Attenberg. Feature Hashing for Large Scale Multitask Learning. 2009.
- A. Kumar, A. Saha and H. Daumé III, Frustratingly Easy Semi-Supervised Domain Adaptation. 2010.



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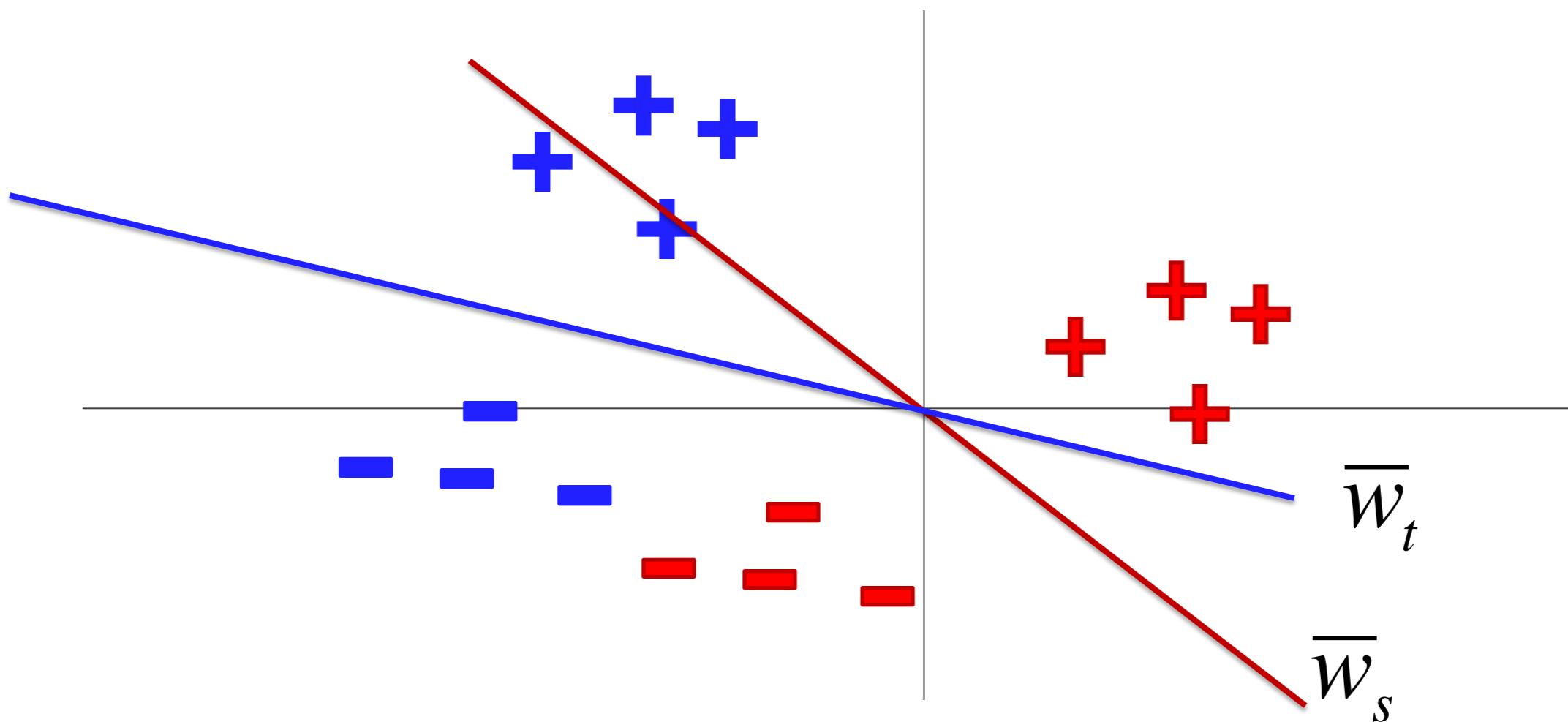
# A Parameter-based Perspective



- Instead of duplicating features, write:

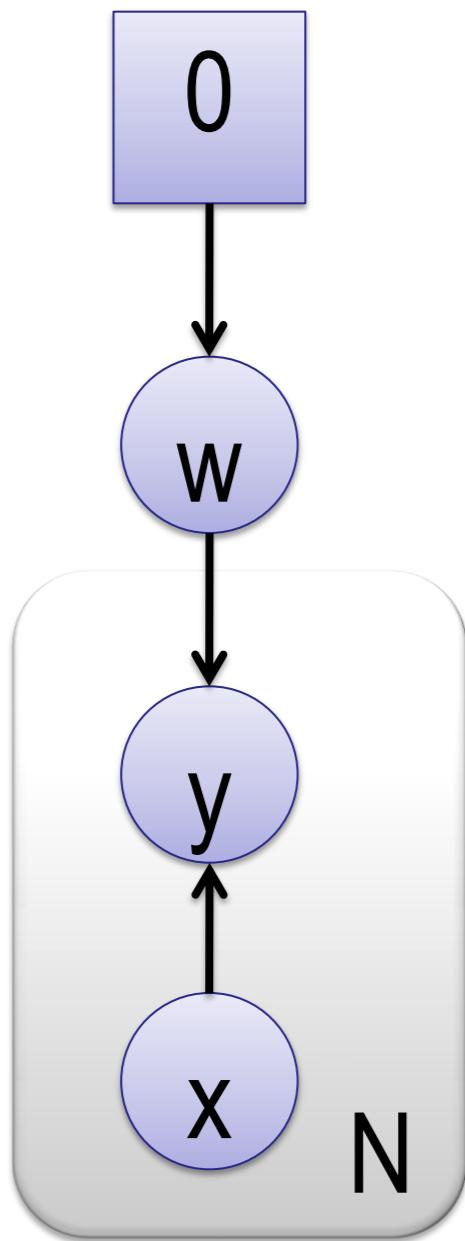
$$\bar{w}_t = \bar{w}_s + \bar{v}$$

- And *regularize*  $\bar{w}_s$  and  $\bar{v}$  toward zero





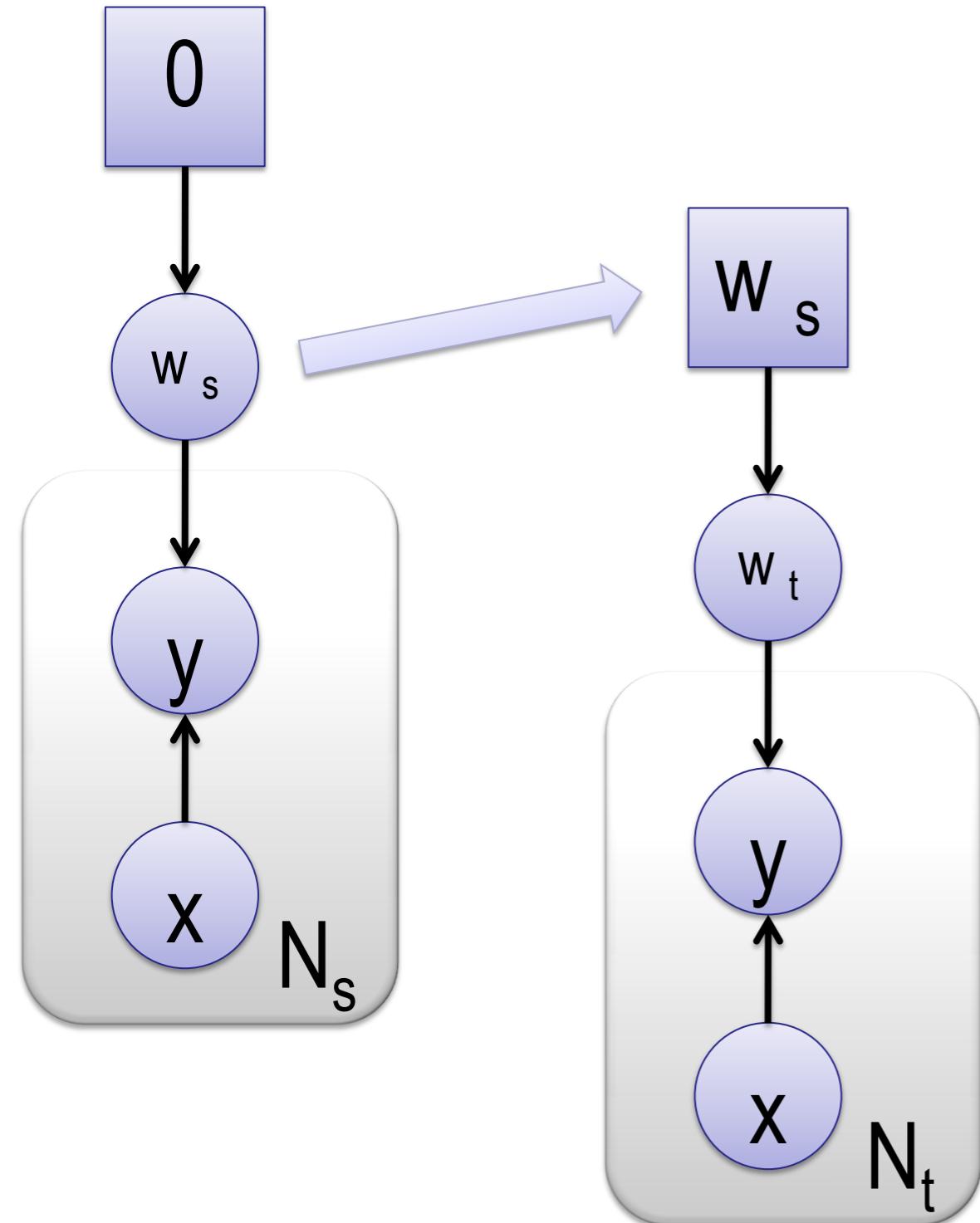
# Sharing Parameters via Bayes



- N data points
- $w$  is regularized to zero
- Given  $x$  and  $w$ , we predict  $y$



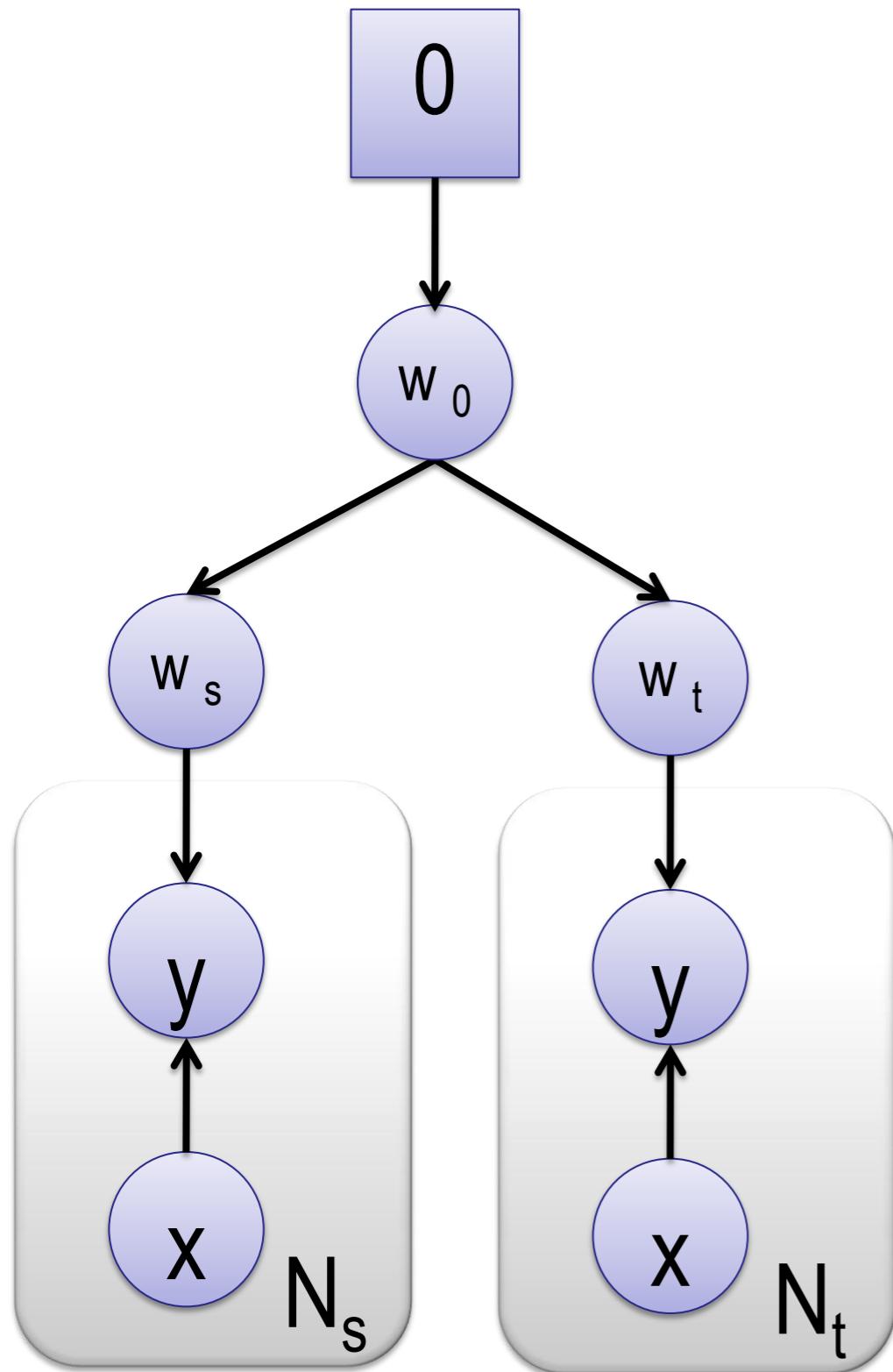
# Sharing Parameters via Bayes



- Train model on source domain, regularized toward zero
- Train model on target domain, regularized toward source domain



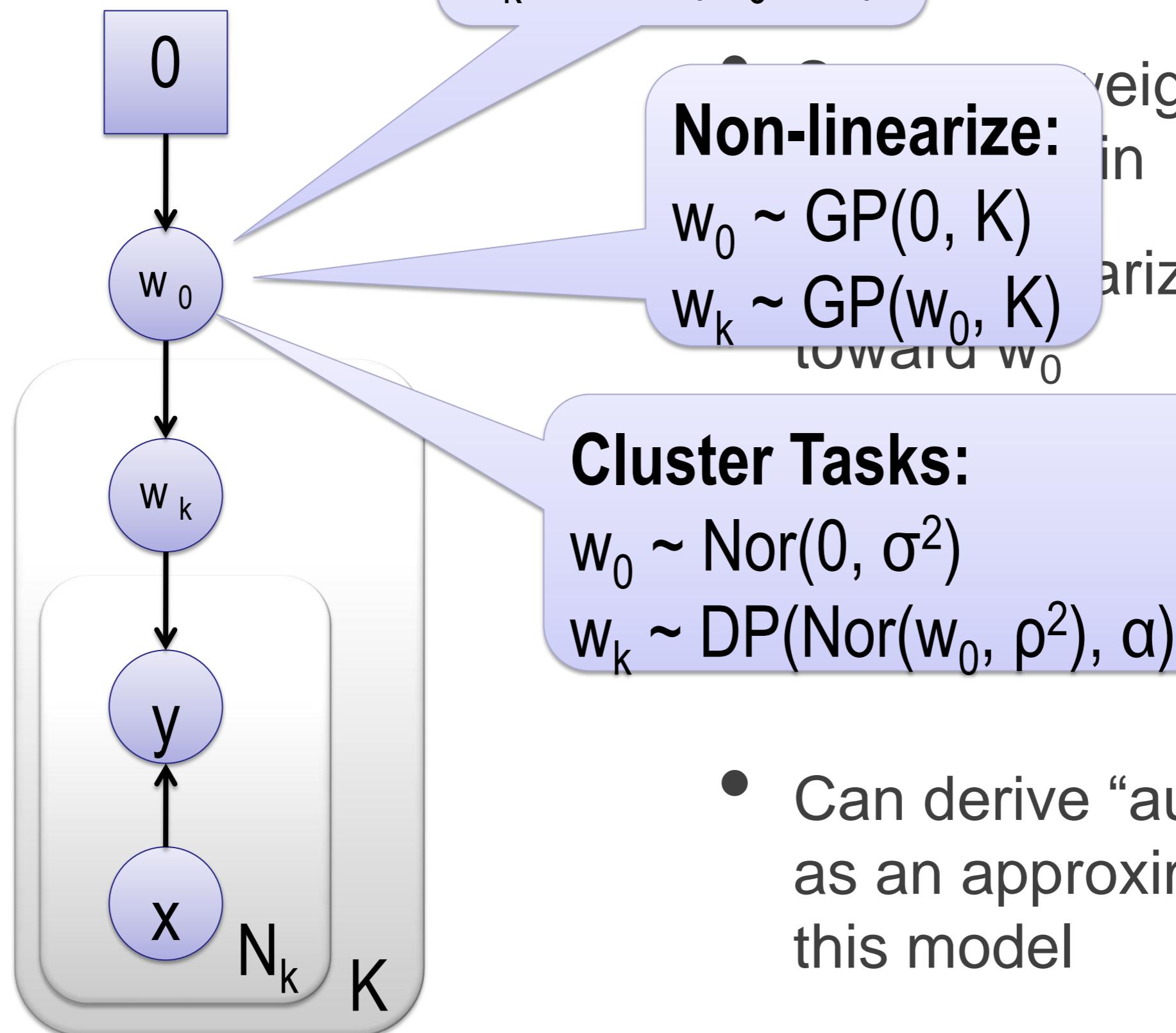
# Sharing Parameters via Bayes



- Separate weights for each domain
- Each regularized toward  $w_0$
- $w_0$  regularized toward zero



# Sharing F

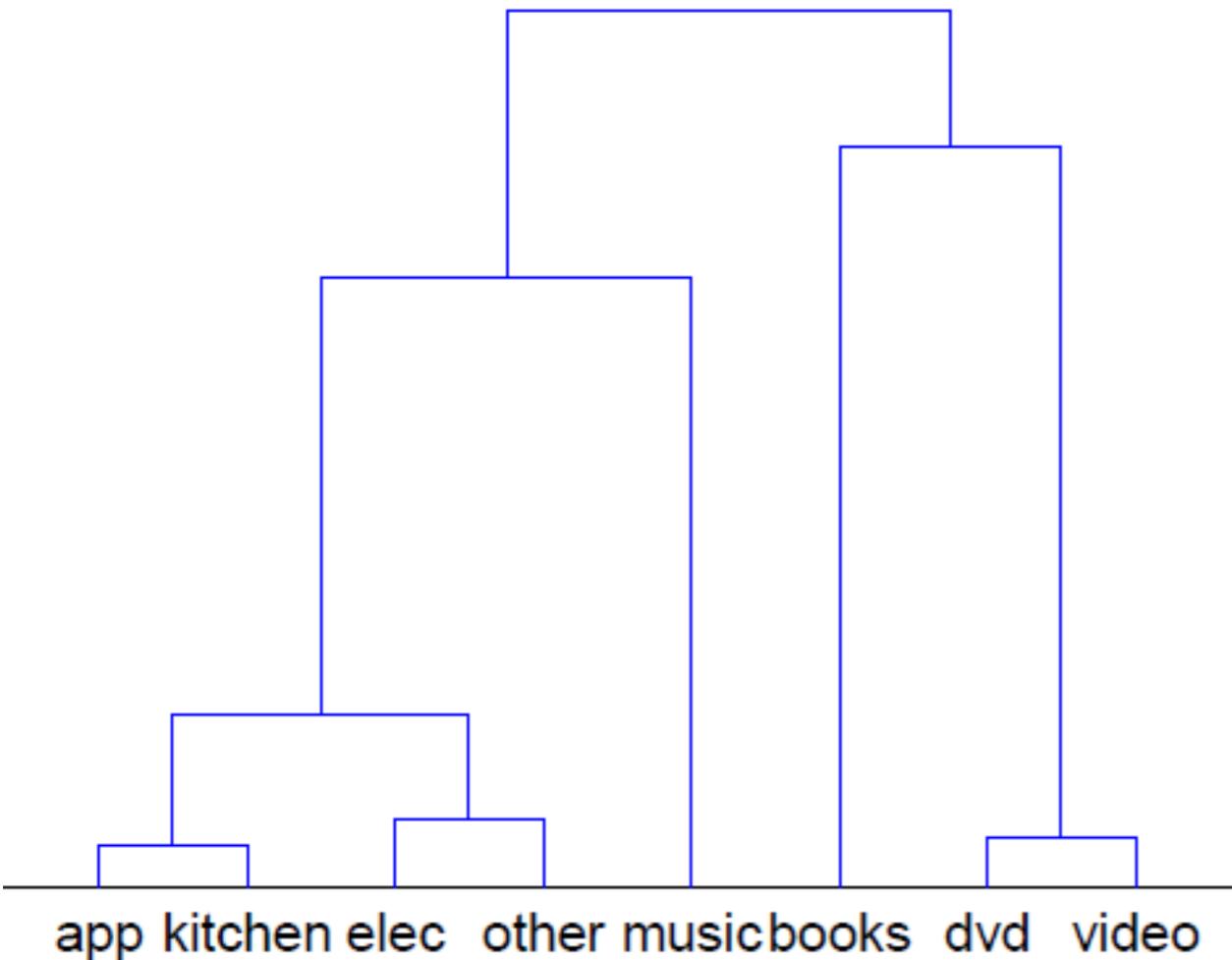




# Not all domains created equal

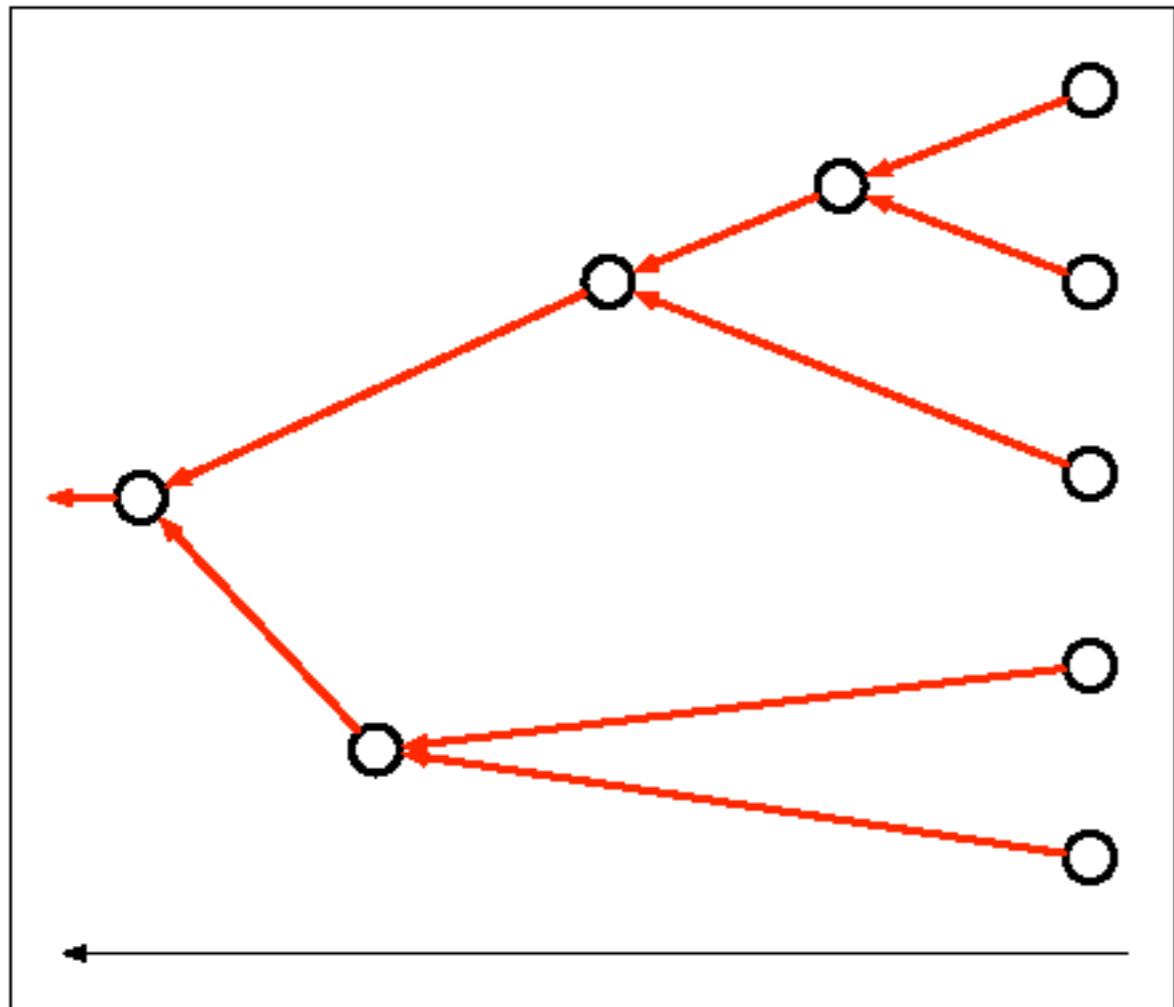


- Would like to infer tree structure automatically
- Tree structure should be good for the *task*
- Want to simultaneously infer tree structure and parameters





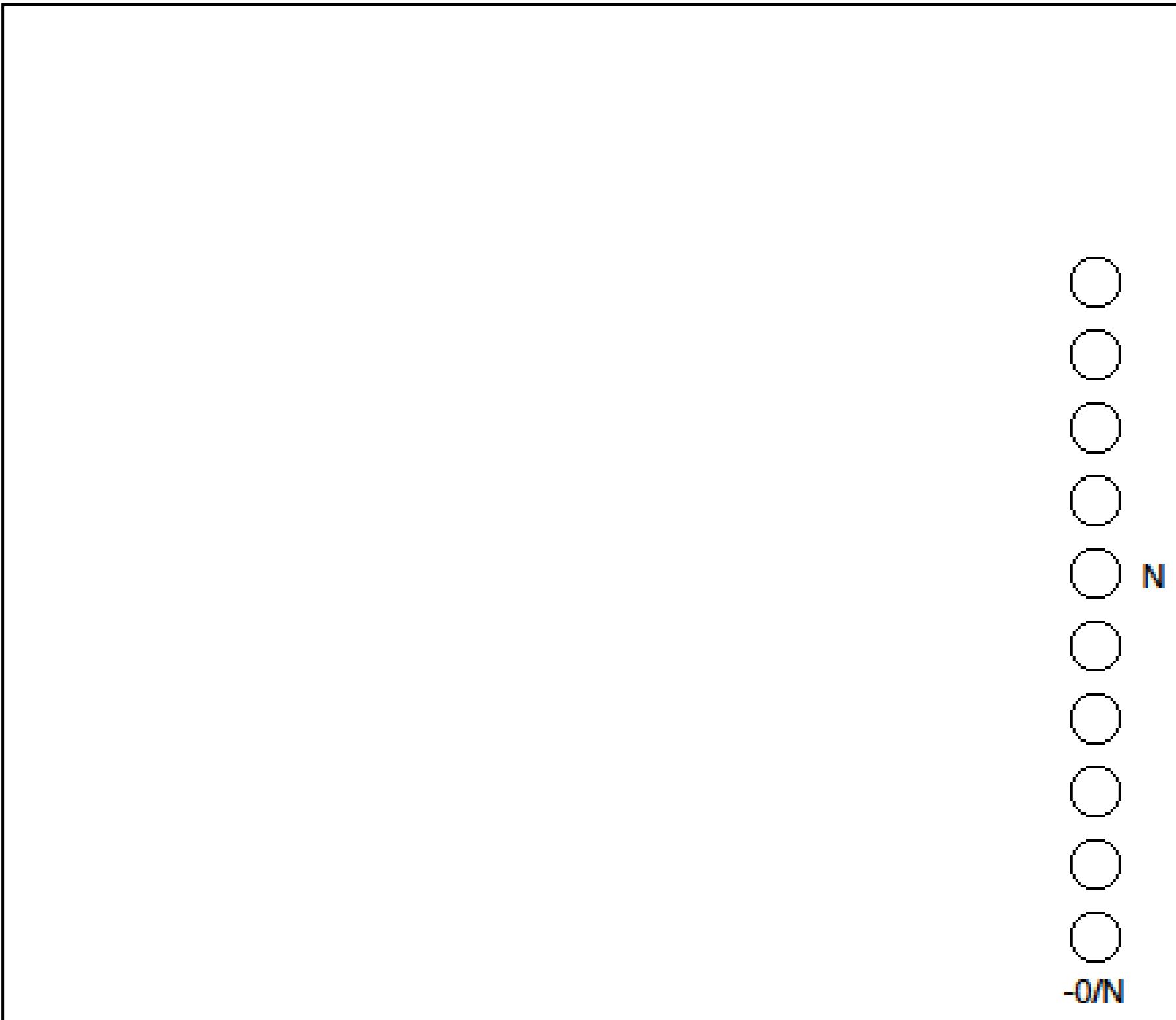
# Kingman's Coalescent



- A standard model for the genealogy of a population
- Each organism has exactly one parent (haploid)
- Thus, the genealogy is a tree

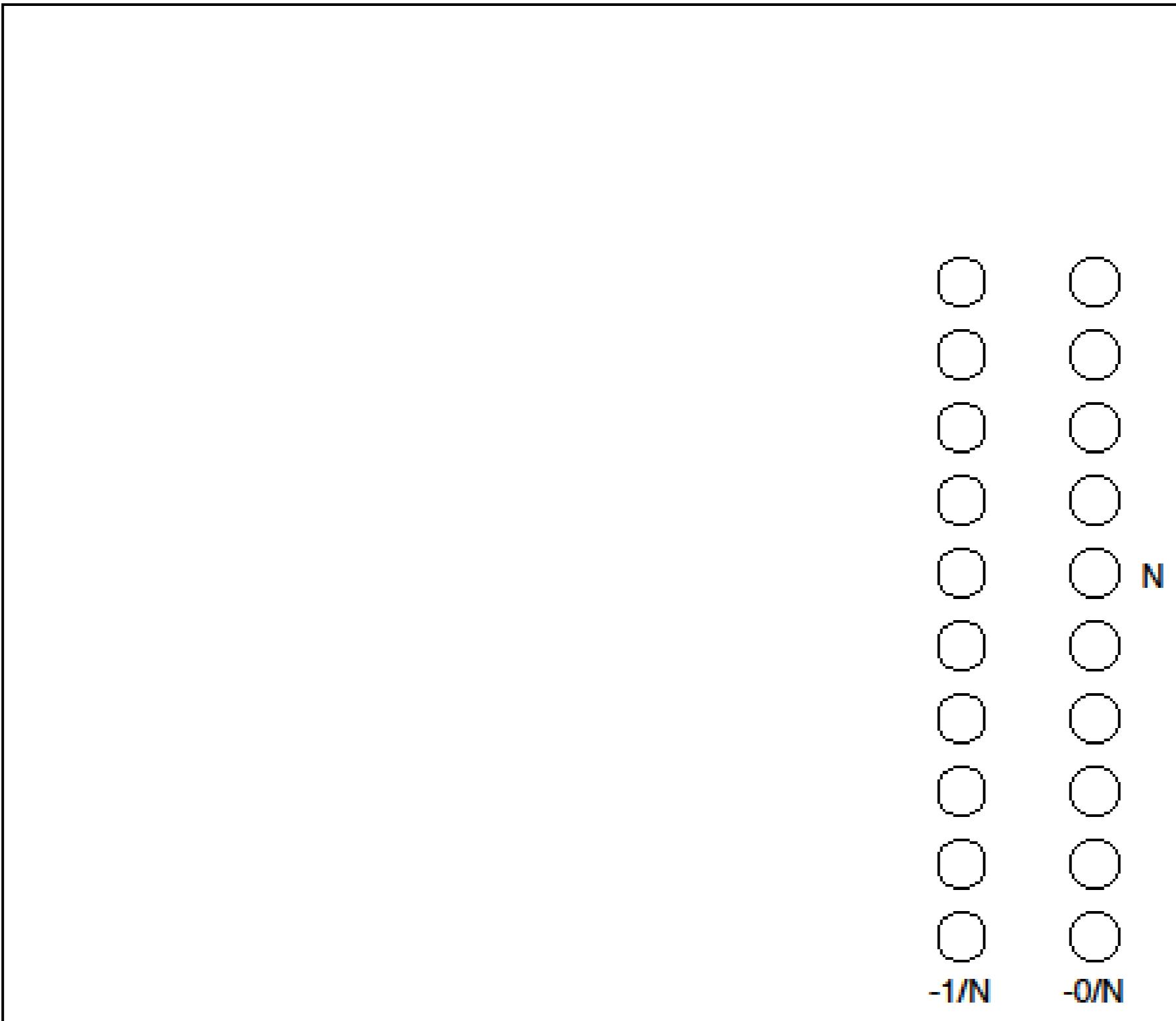


# A distribution over trees



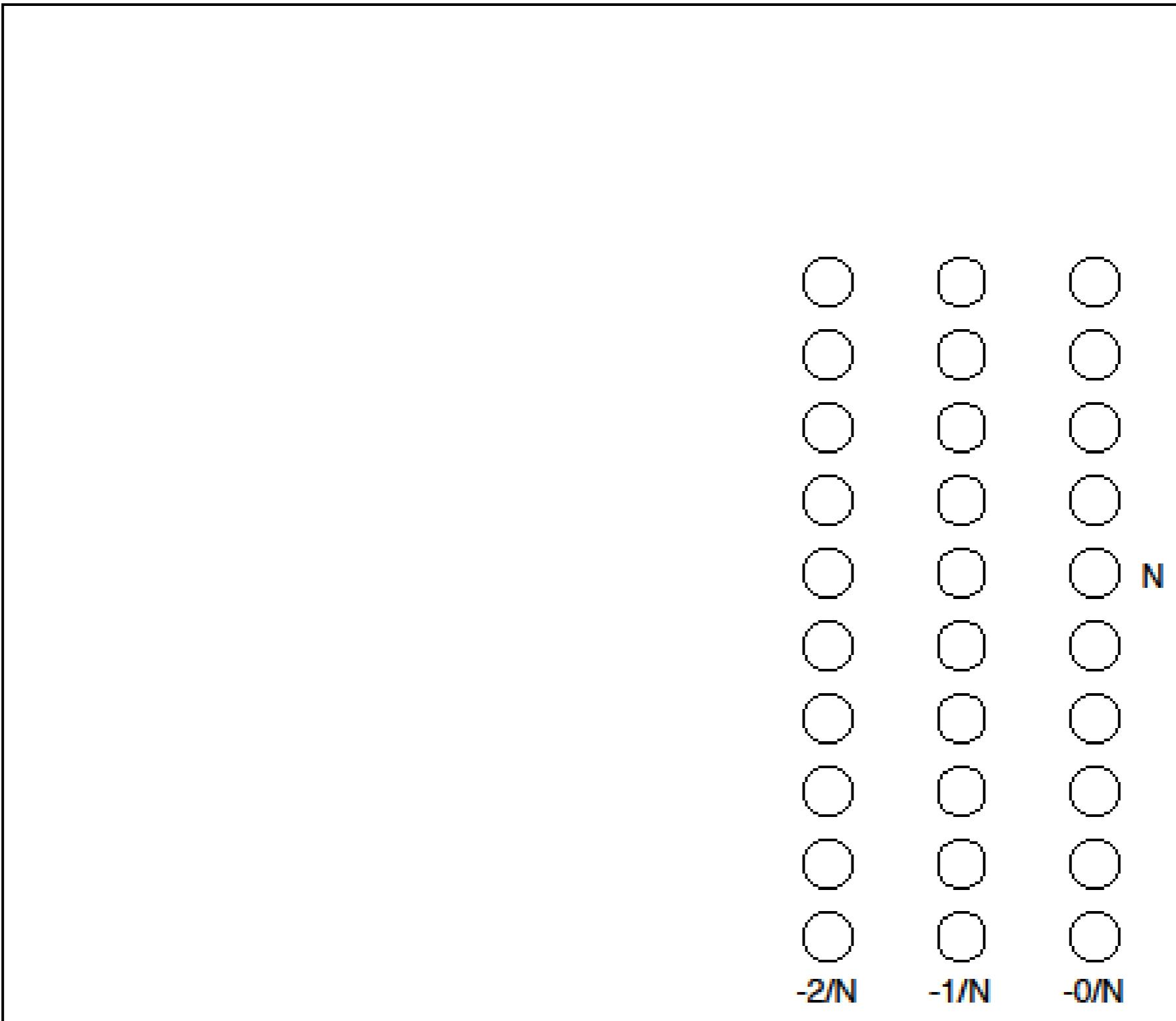


# A distribution over trees



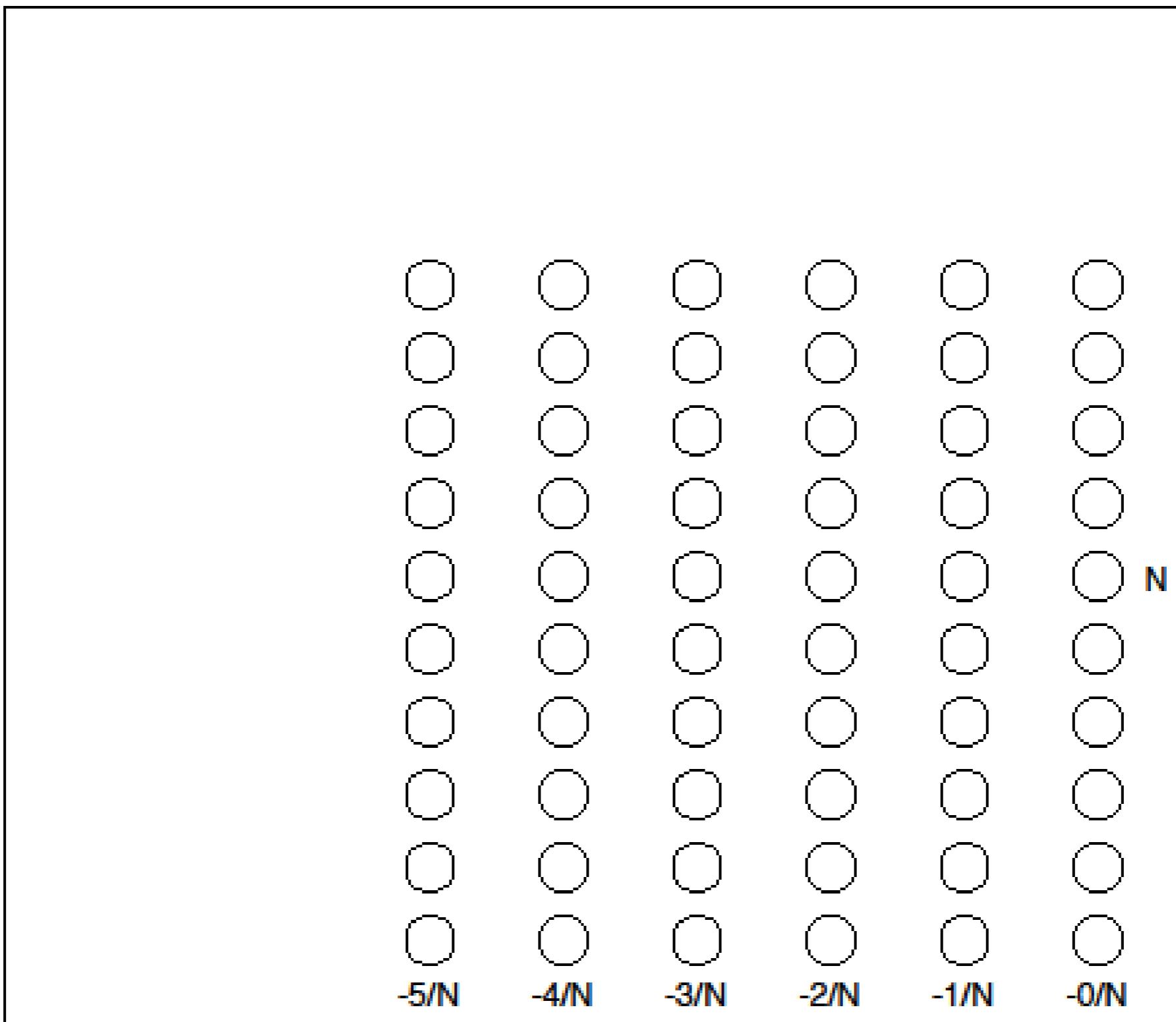


# A distribution over trees



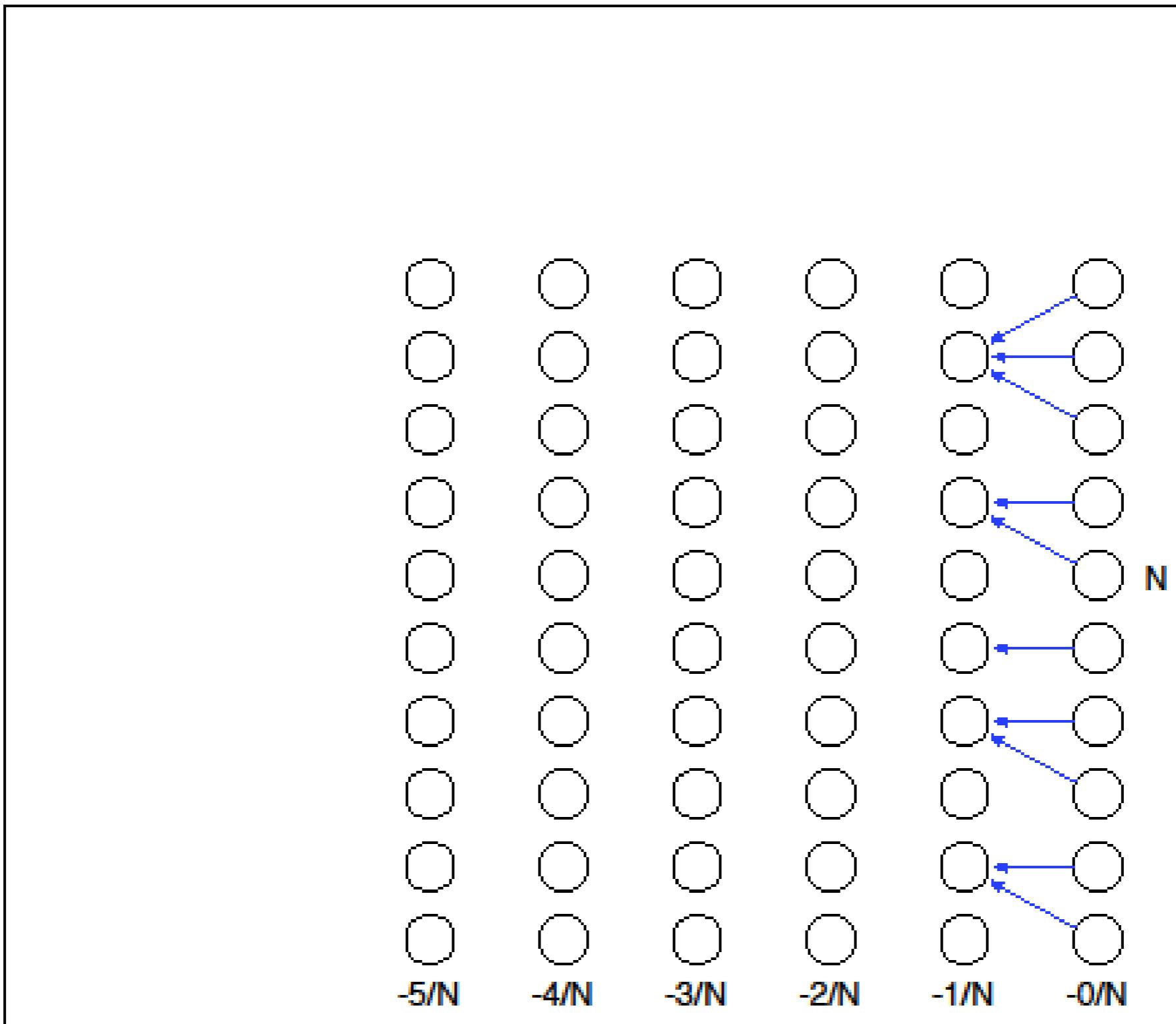


# A distribution over trees



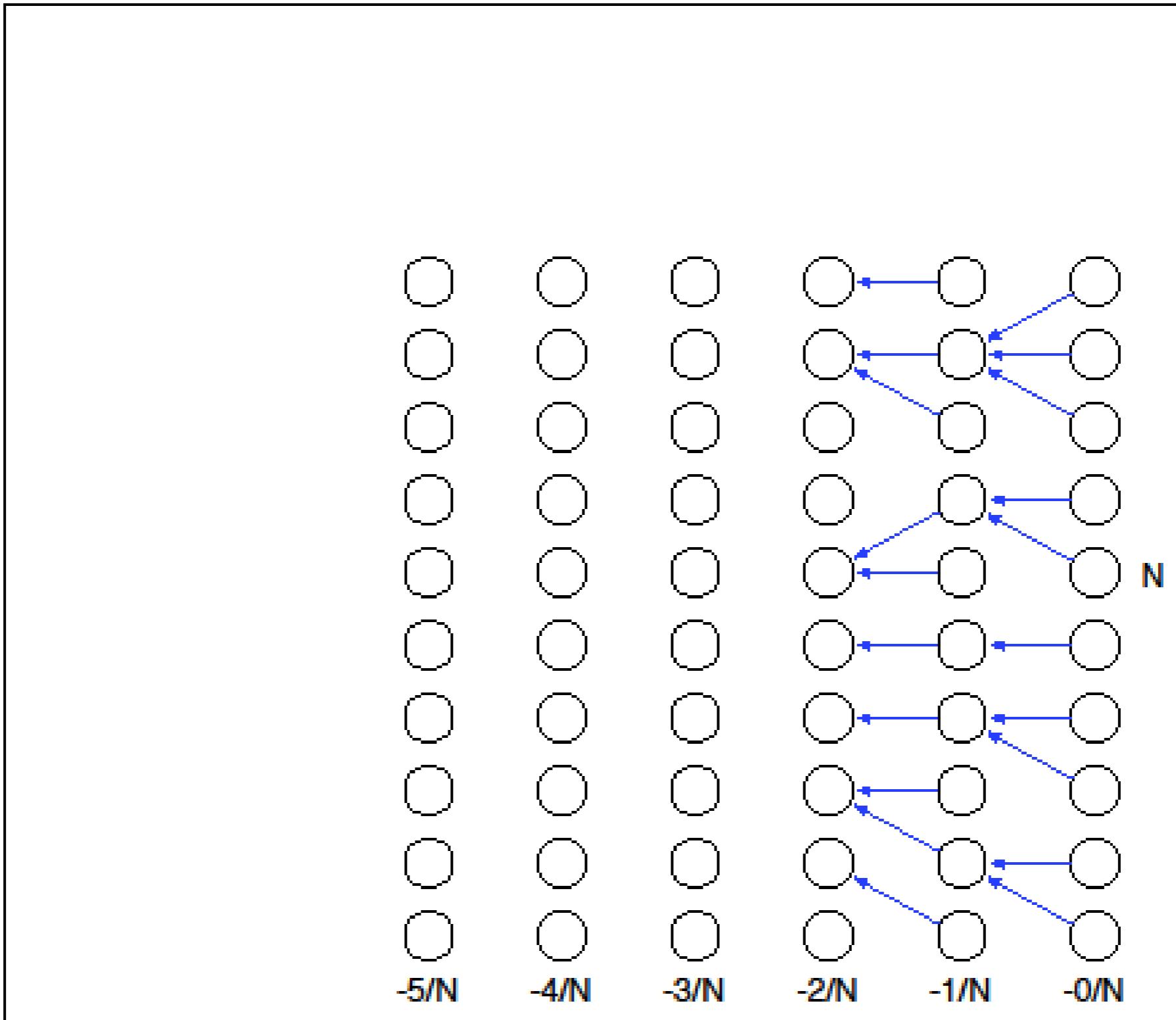


# A distribution over trees



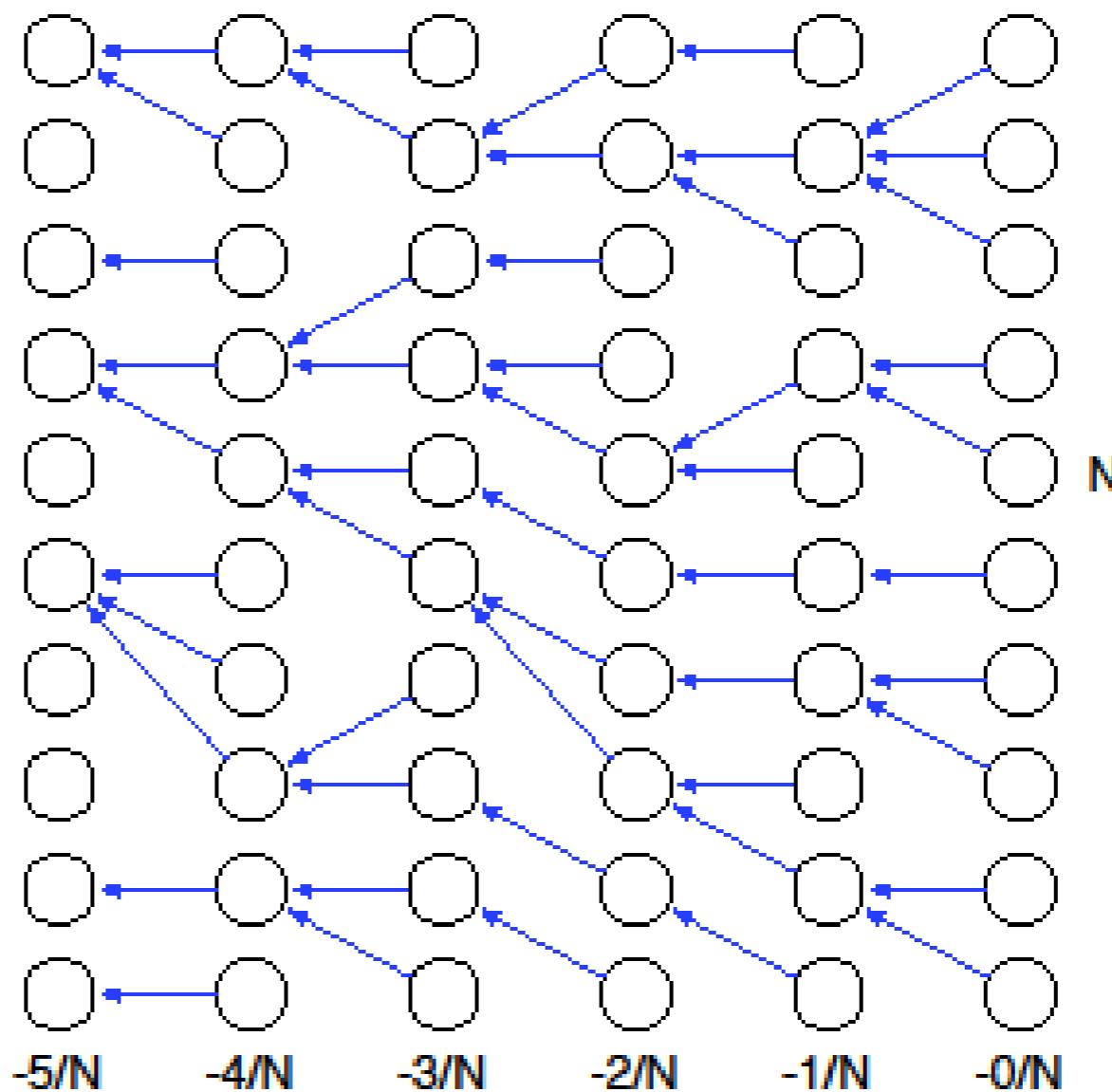


# A distribution over trees



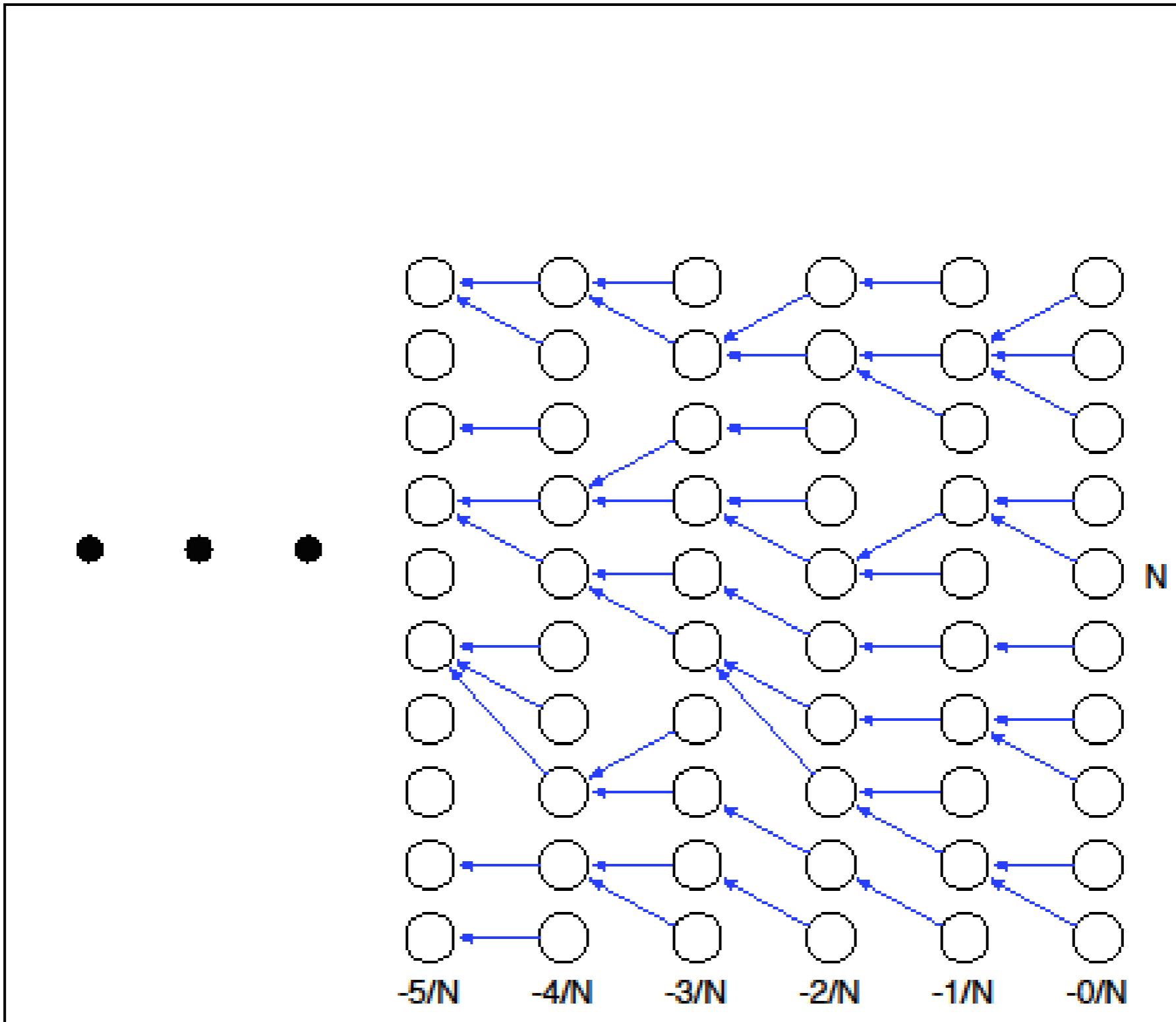


# A distribution over trees



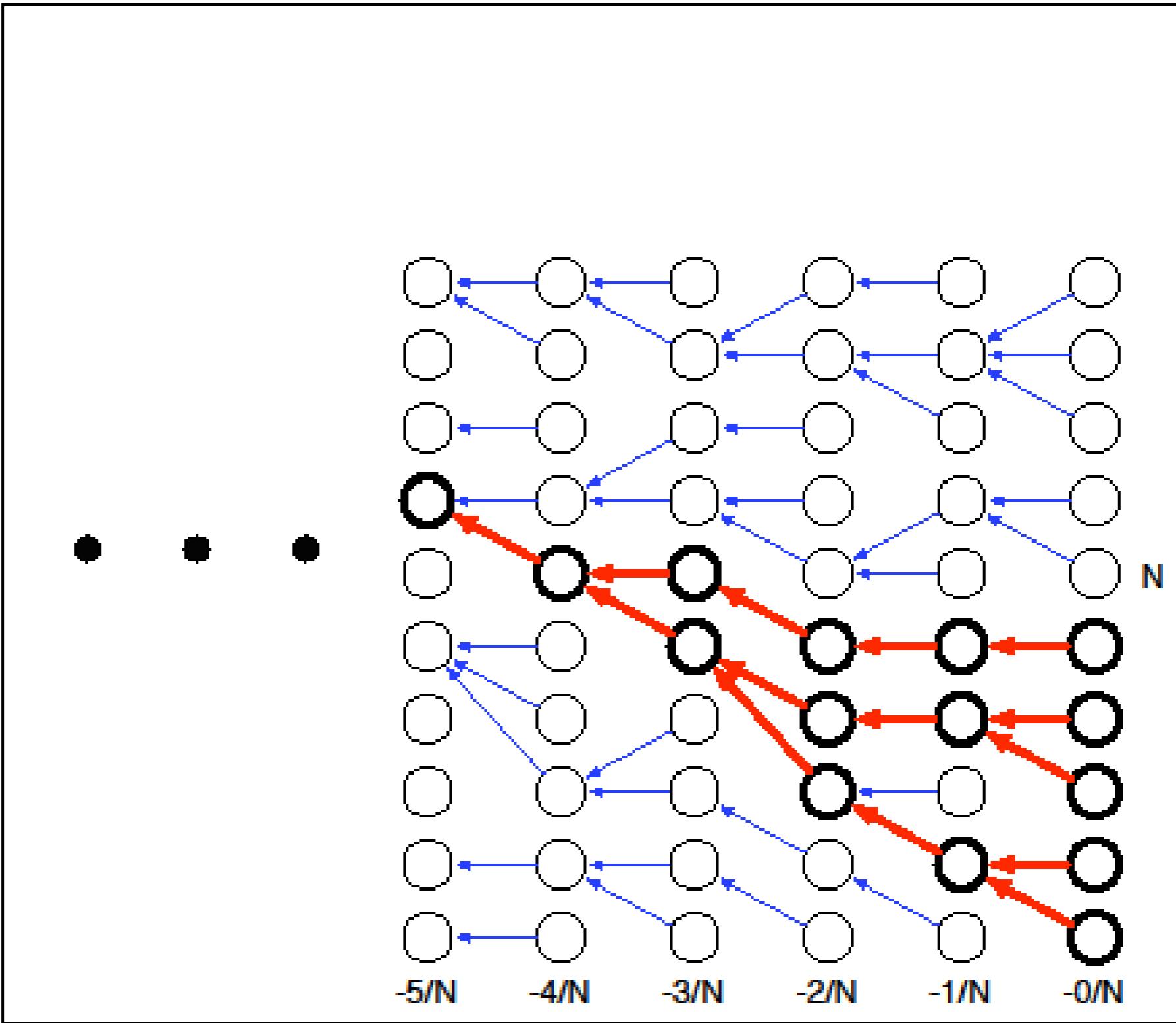


# A distribution over trees



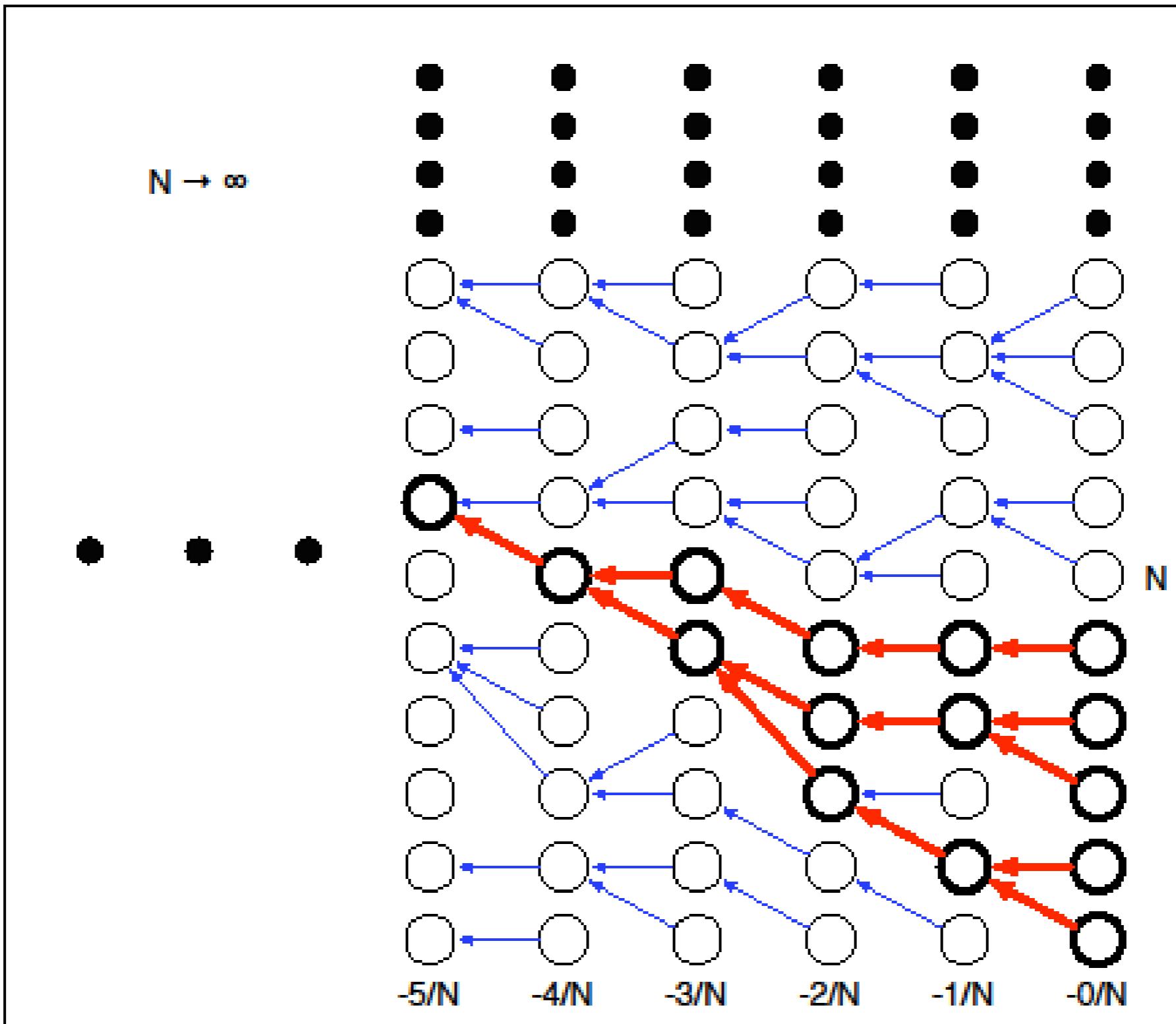


# A distribution over trees



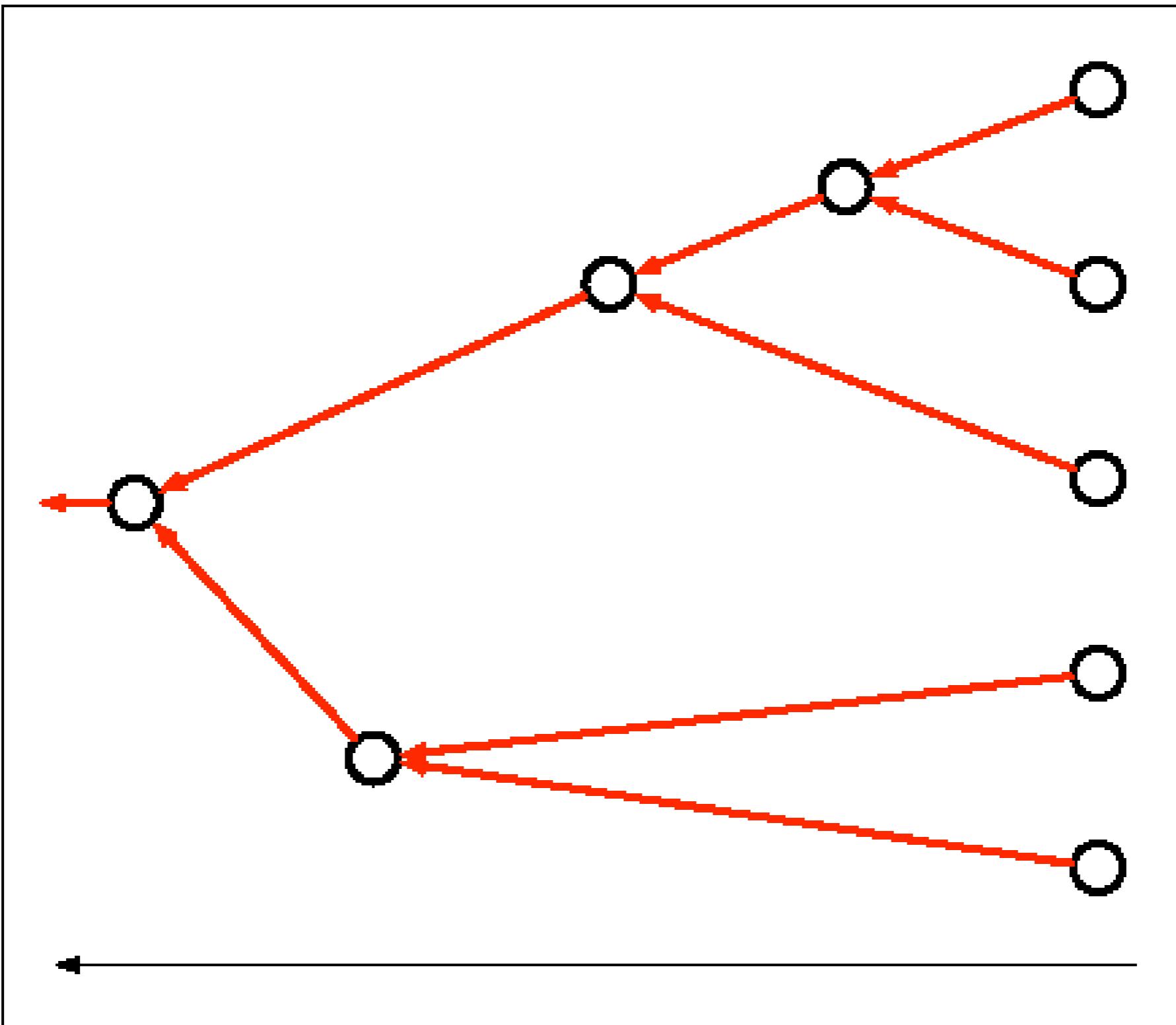


# A distribution over trees



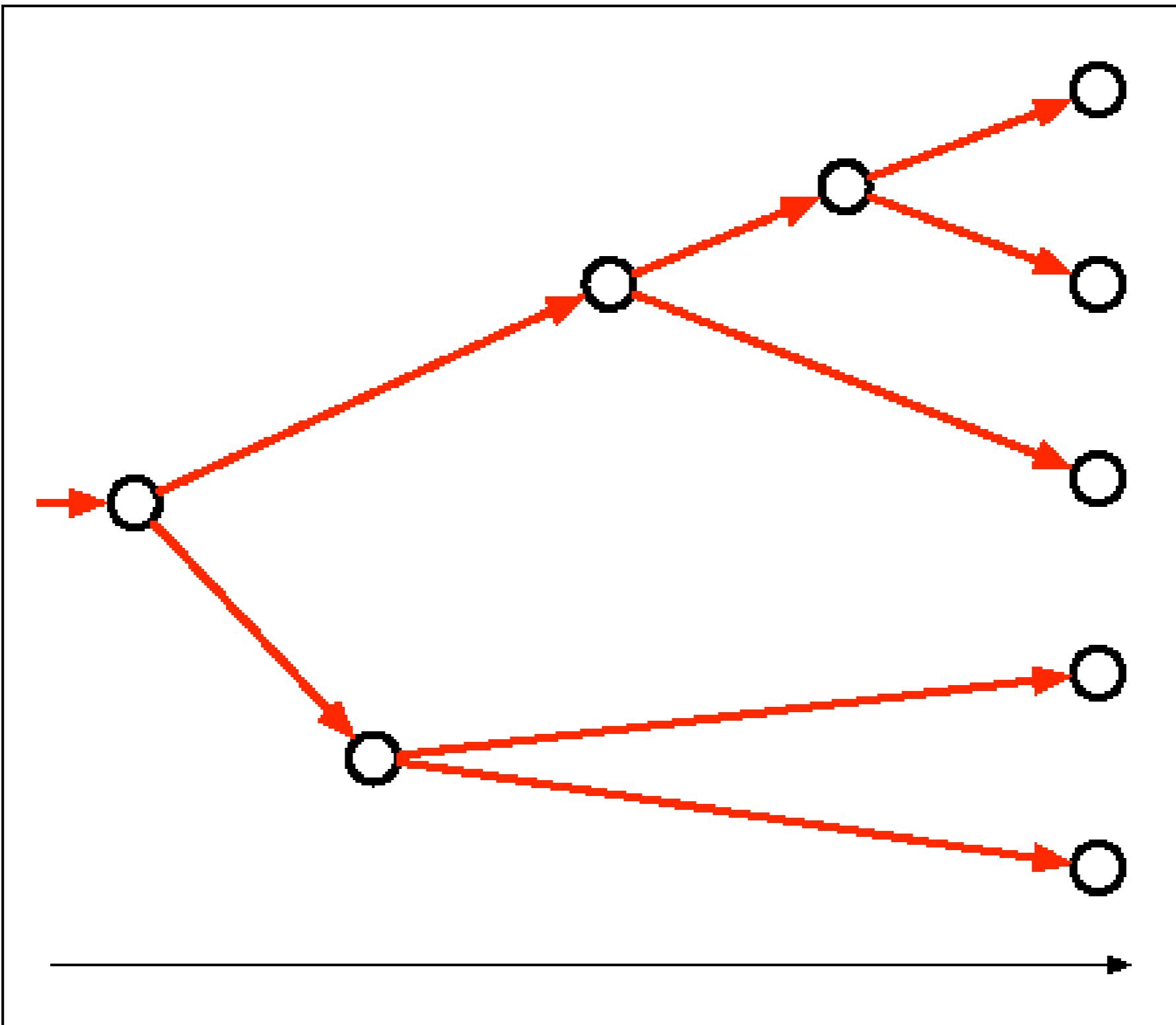


# Coalescent as a graphical model



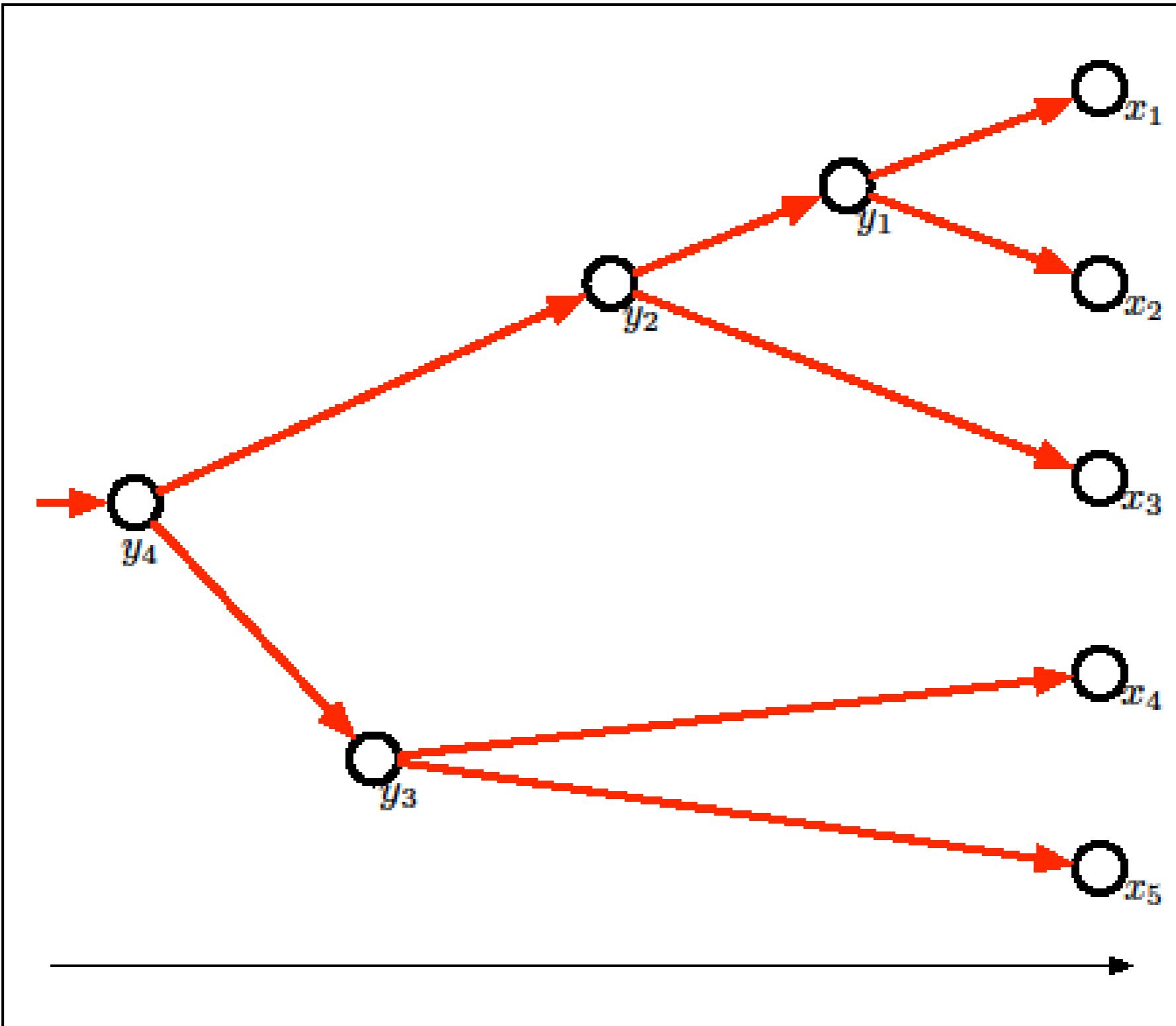


# Coalescent as a graphical model



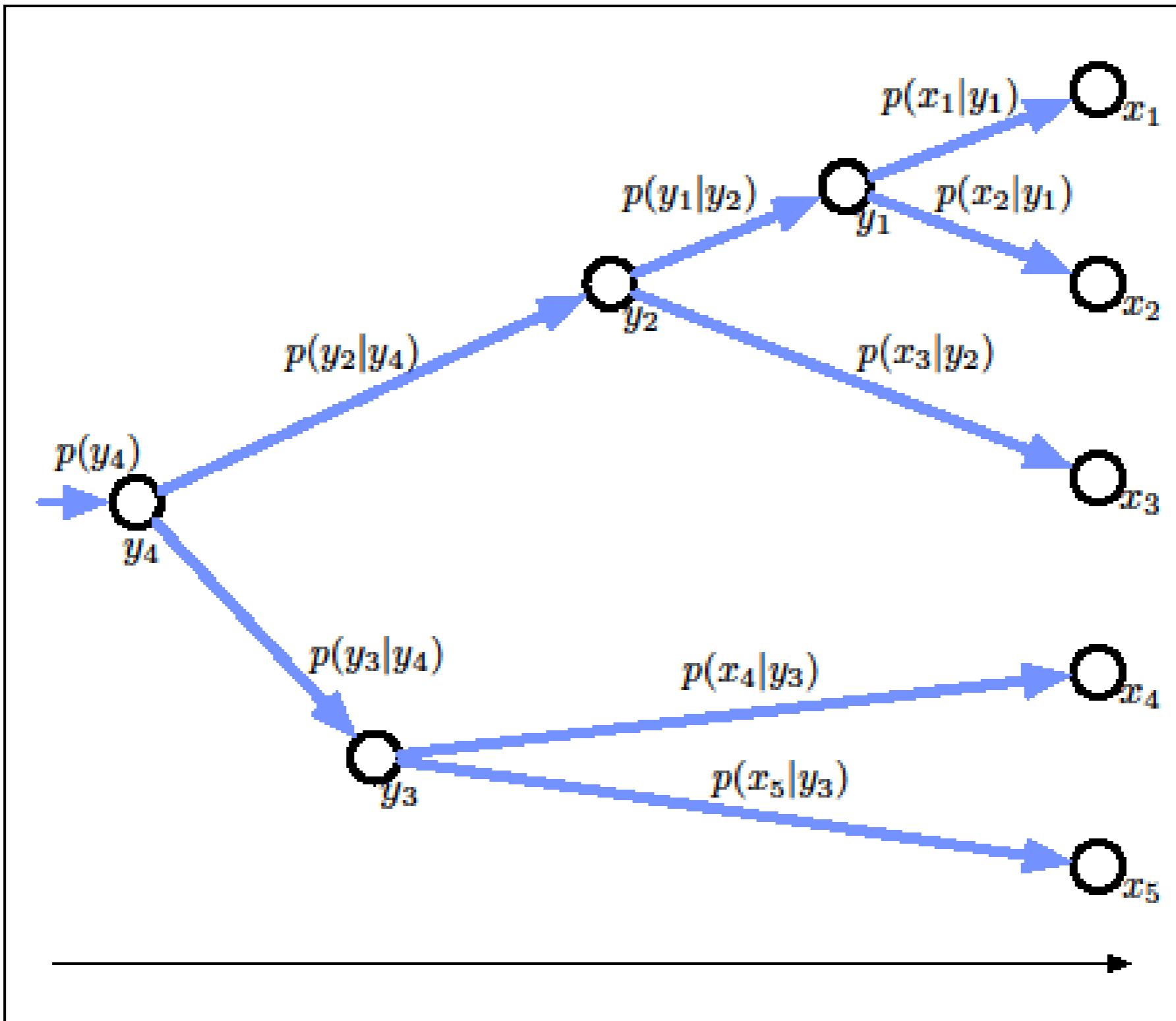


# Coalescent as a graphical model





# Coalescent as a graphical model

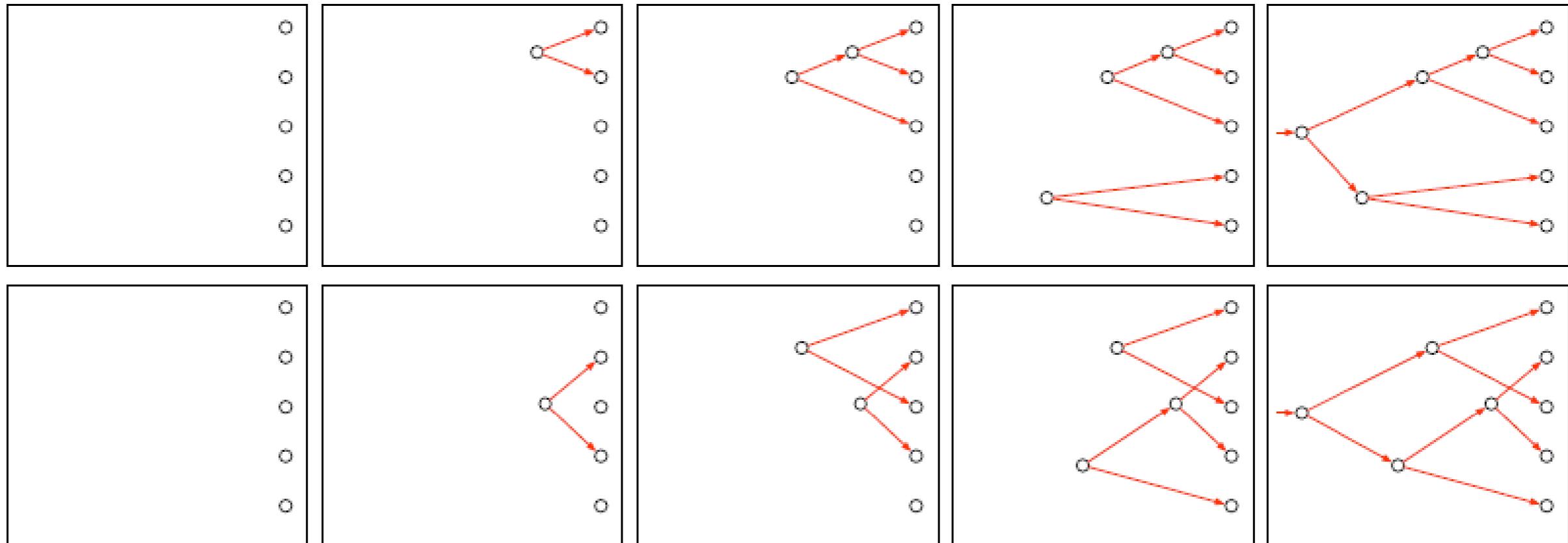




# Efficient Inference



- Construct trees in a bottom-up manner



- Greedy: At each step, pick optimal pair (maximizes joint likelihood) and time to coalesce (branch length)
- Infer values of internal nodes by belief propagation



N

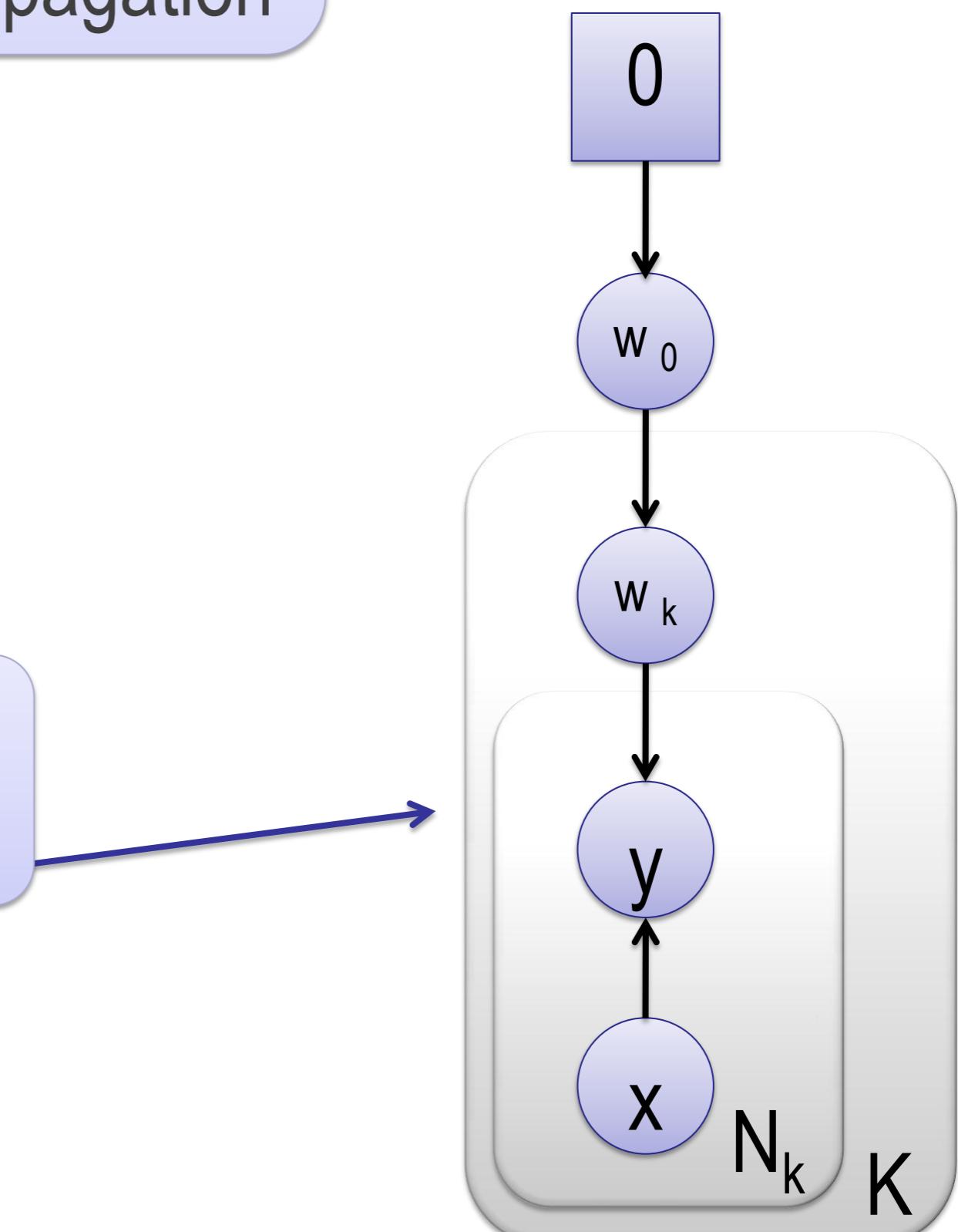
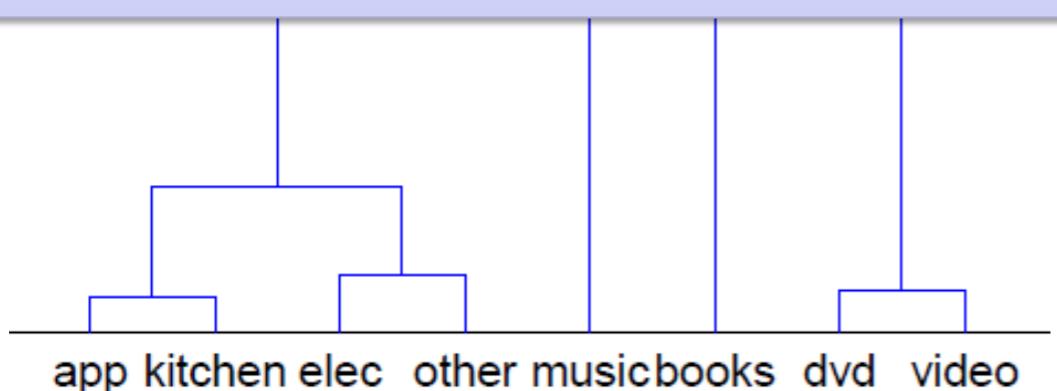
Message passing on  
coalescent tree; efficiently  
done by belief propagation



ated equal

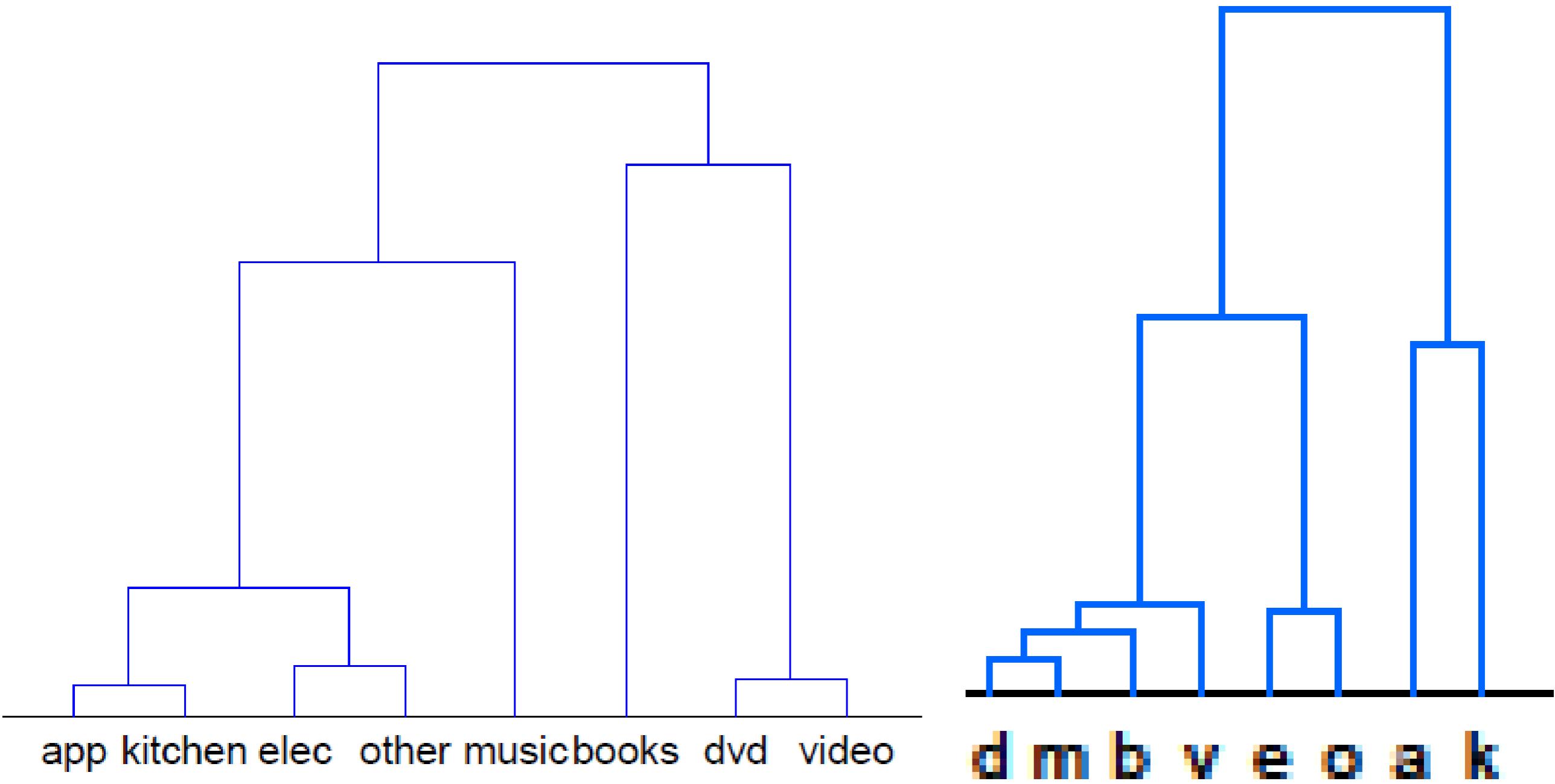
- Inference by EM:
- E: compute expectations over weights
- M: maximize tree structure

Greedy agglomerative  
clustering algorithm



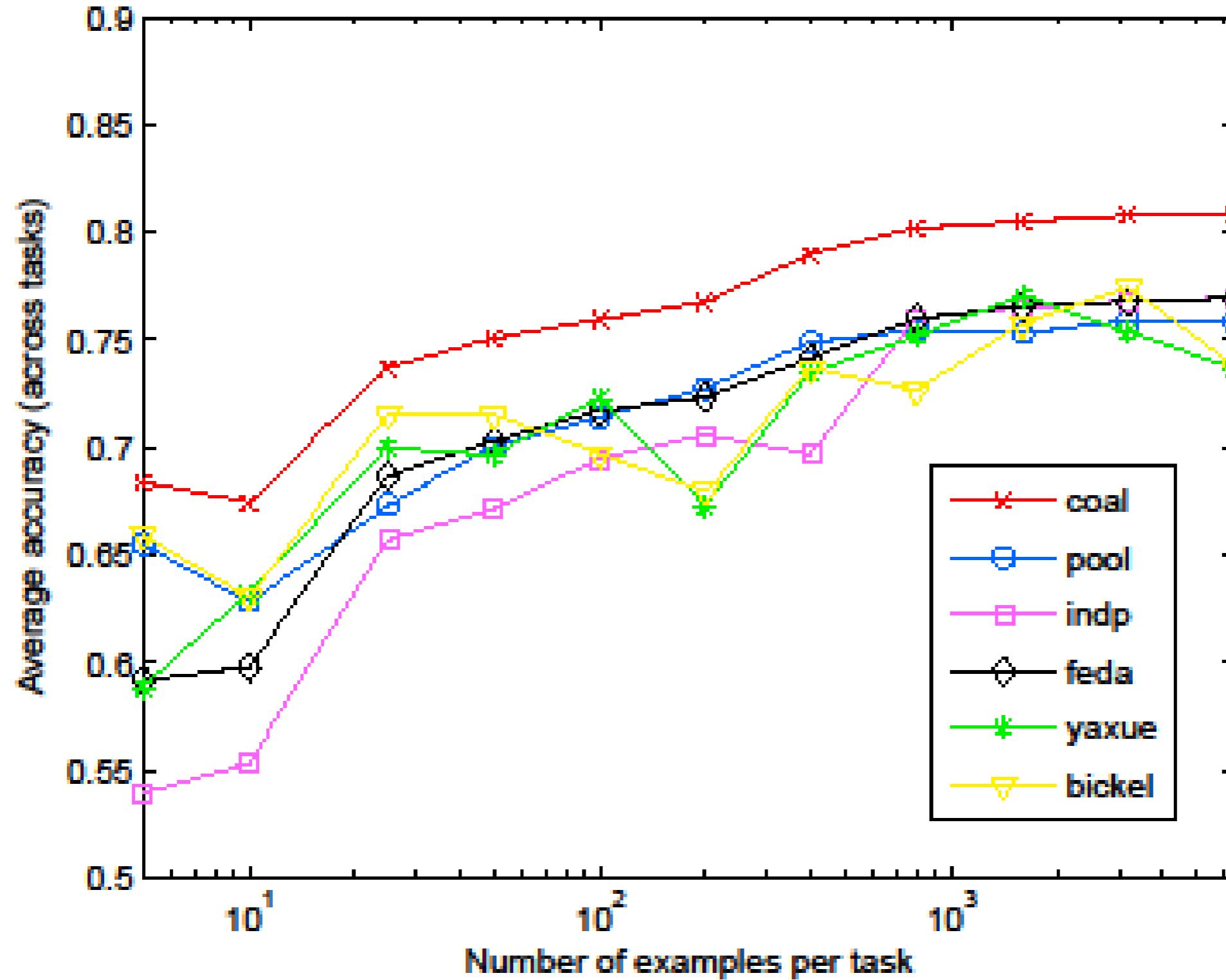


# Data tree versus inferred tree





# Some experimental results





# Parameter-based References

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- O. Chapelle and Z. Harchaoui. A machine learning approach to conjoint analysis. NIPS, 2005.
- K. Yu, V. Tresp, and A. Schwaighofer. Learning Gaussian processes from multiple tasks. ICML, 2005.
- Y. Xue, X. Liao, L. Carin, and B. Krishnapuram. Multi-task learning for classification with Dirichlet process priors. JMLR, 2007.
- H. Daumé III. Bayesian Multitask Learning with Latent Hierarchies. UAI 2009.



# Tutorial Outline

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1. Notation and Common Concepts
2. Semi-supervised Adaptation
  - Covariate shift
  - Learning Shared Representations
3. Supervised Adaptation
  - Feature-Based Approaches
  - Parameter-Based Approaches
4. Open Questions and Uncovered Algorithms



# Theory and Practice



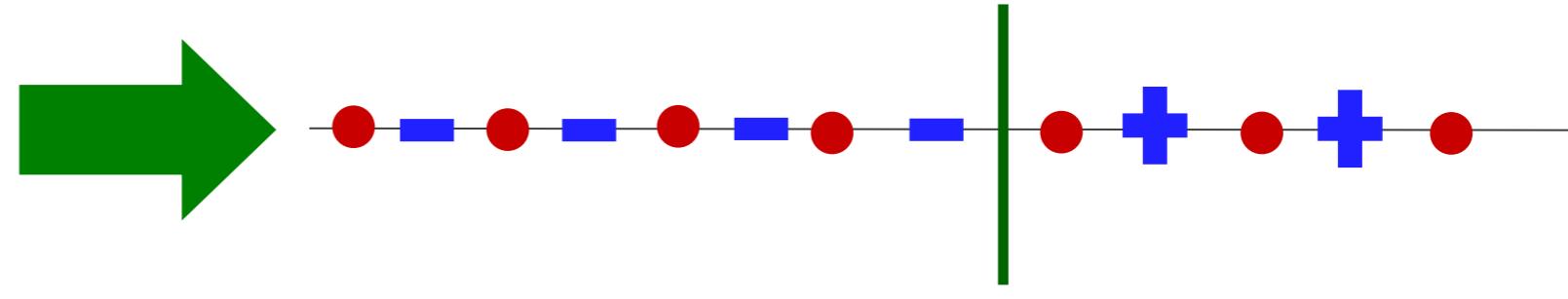
Hypothesis classes from projections  $P : \theta^\top Px$

$P$



$x$
3
0
:
1
0
0
1

$$P = \hat{\theta}\hat{\theta}^\top \quad \hat{\theta} = \text{source ERM}$$



- 1) Minimize divergence
- 2)  $\hat{\epsilon}_S(\theta)$  small

~~$\epsilon_{P,T}(\theta^*) - \epsilon_{T,T}(\theta^*)$  small~~



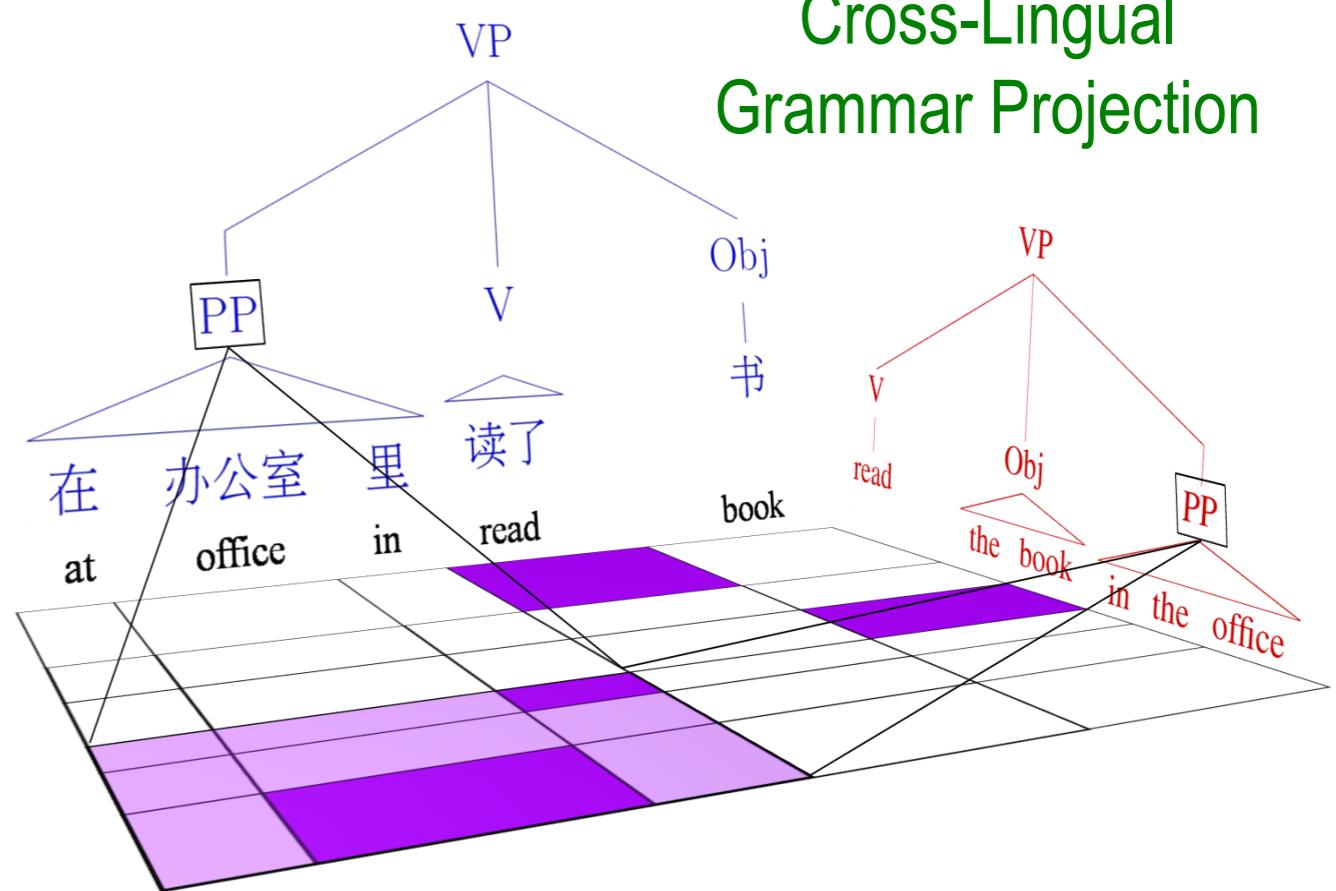
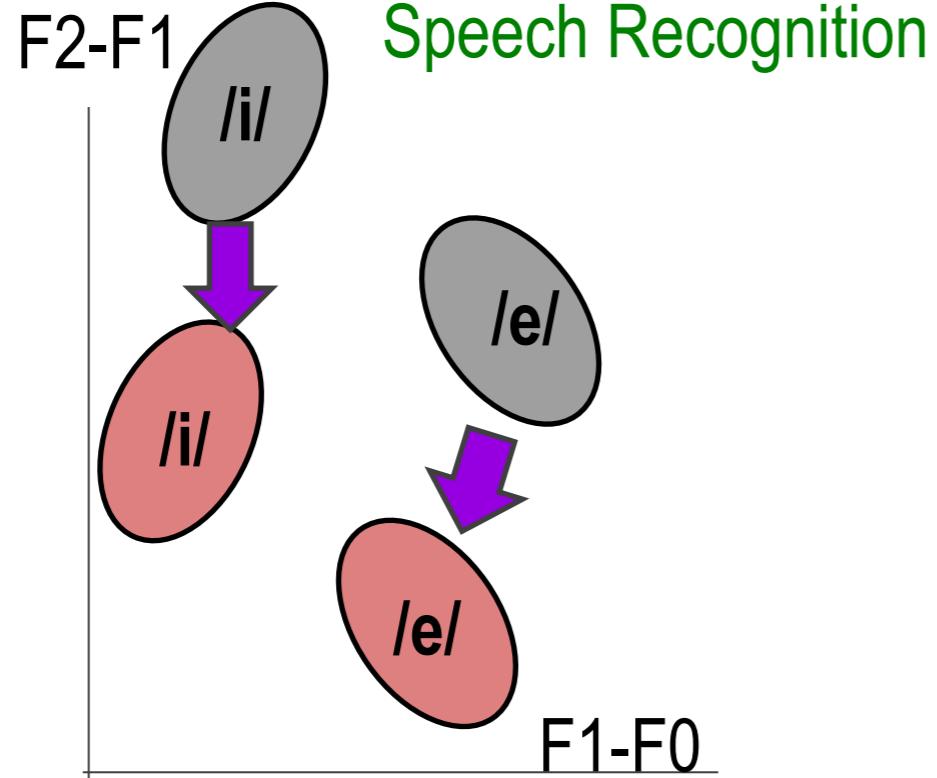
# Open Questions



## Matching Theory and Practice

Theory does not exactly suggest what practitioners do

## Prior Knowledge





# More Semi-supervised Adaptation



<http://adaptationtutorial.blitzer.com/references/>

## Self-training and Co-training

[1] D. McClosky et al. Reranking and Self-Training for Parser Adaptation. 2006.

[2] K. Sagae & J. Tsuji. Dependency Parsing and Domain Adaptation with LR Models and Parser Ensembles. 2007.

## Structured Representation Learning

[3] F. Huang and A. Yates. Distributional Representations for Handling Sparsity in Supervised Sequence Labeling. 2009.



# What is a domain anyway?



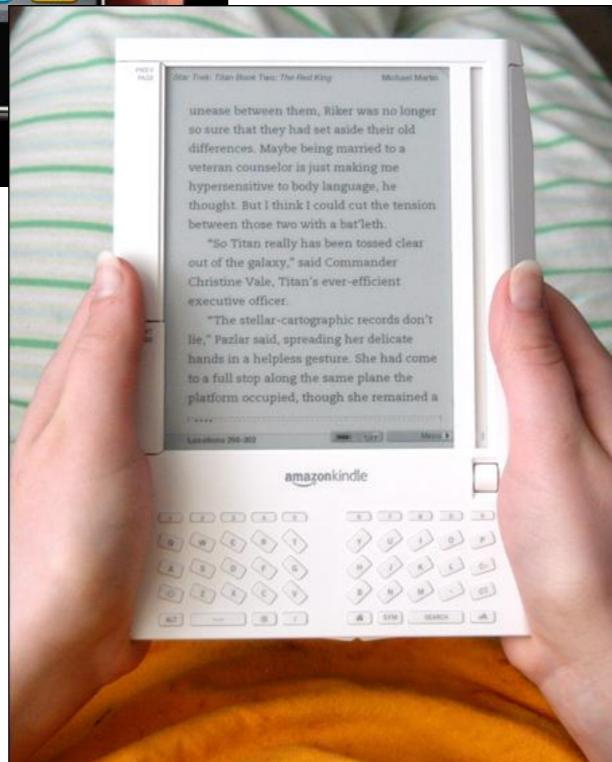
- Time?
  - News the day I was born *vs* news today?
  - News yesterday *vs* news today?
- Space?
  - News back home *vs* news in Haifa?
  - News in Tel Aviv *vs* news in Haifa?
- Do my data even come with a domain specified?

Suggest a continuous structure

Stream of  $\langle x, y, d \rangle$  data  
with  $y$  and  $d$  sometimes  
hidden?



# We're all domains: personalization



- adapt learn across millions of “domains”?
- share enough information to be useful?
- share little enough information to be safe?
- avoid negative transfer?
- avoid DAAM (domain adaptation spam)?



Thanks

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Questions?