$$\nabla f(\boldsymbol{\alpha}^1) \underset{\searrow}{\overset{\rightrightarrows}{\searrow}} \begin{array}{l} (i_1, j_1) \\ (i_2, j_2) \\ \vdots \\ (i_r, j_r) \end{array}$$