

# Models of radiative neutrino mass and lepton-flavour non-universality

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# Abstract

This is a summary of what we did. We did  $x$  and  $y$ .



# Publications

Refs. [1–5] below are the journal publications, preprints and other publications authored or co-authored during my PhD candidature. The authors are listed alphabetically in all of the titles.

## Journal papers and preprints

- [1] R. Foot and J. Gargalionis, *Explaining the 750 GeV diphoton excess with a colored scalar charged under a new confining gauge interaction*, *Phys. Rev. D* **94** (2016), no. 1 011703, [[arXiv:1604.06180](#)].
- [2] Y. Cai, J. Gargalionis, M. A. Schmidt, and R. R. Volkas, *Reconsidering the One Leptoquark solution: flavor anomalies and neutrino mass*, *JHEP* **10** (2017) 047, [[arXiv:1704.05849](#)].
- [3] I. Bigaran, J. Gargalionis, and R. R. Volkas, *A near-minimal leptoquark model for reconciling flavour anomalies and generating radiative neutrino masses*, *JHEP* **10** (2019) 106, [[arXiv:1906.01870](#)].
- [4] J. Gargalionis, I. Popa-Mateiu, and R. R. Volkas, *Radiative neutrino mass model from a mass dimension-11  $\Delta L = 2$  effective operator*, *JHEP* **03** (2020) 150, [[arXiv:1912.12386](#)].
- [5] Exploding operators

## Other publications

- [6] M. Balsiger et al., *Solutions to Problems at Les Houches Summer School on EFT*, in *Les Houches summer school: EFT in Particle Physics and Cosmology*, 5, 2020. [arXiv:2005.08573](#).



# Declaration

This is to certify that

1. the thesis comprises only my original work towards the PhD except where indicated clearly,
2. due acknowledgement has been made in the text to all other material used,
3. the thesis is less than 100,000 words in length, exclusive of tables, maps, bibliographies and appendices.

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John Gargalionis, September 2020





# Statement of contribution

I did  $x$  and someone else did  $y$ .



# Preface

Particle physics currently finds itself in a strange or exciting place, depending on who you ask. The discovery of a Higgs-like boson at close to 125 GeV has meant both the completion of the Standard Model (SM), and the end of clear signs of new particles at the electroweak scale. Although the Large Hadron Collider (LHC) will continue to collect data well into the next few decades, the mass reach will not increase significantly. The community waits for a new machine, for which there are many candidates and promises, that will continue to push the energy frontier and test theories addressing the many shortcomings of the SM. Time frames for many of these see data taking beginning at the end of my career. If progress is driven by experiment, where do we go from here?

Thankfully, there are already clear signs of new physics in the neutrino sector. The observation of neutrino oscillations, and therefore neutrino masses, is by far the strongest terrestrial evidence demanding an extension of the SM. It is no surprise that a full understanding of the neutrinos has alluded us so far; they are, with the possible exception of the Higgs boson, the most elusive particles currently under laboratory scrutiny. As we move into an era of precision neutrino measurements, now is the right time to take stock of the phenomenologically viable and economic models that explain the pattern of neutrino masses and mixings observed. Armed with the list of possible mechanisms, we can make progress in probing those that are testable and, given that these models are falsified, build circumstantial evidence in favour of those that are not.

Even on the collider front, it is unclear yet that the LHC has left us with the so-called ‘nightmare scenario’ of a lonely Higgs. Perhaps unexpectedly, the most interesting signs of new physics from CERN have come from the  $LHCb$  experiment. The now famous ‘flavour anomalies’ are a collection of theoretically consistent anomalous measurements indicating a departure from the lepton-flavour universality present in the SM. Are these related to the growing evidence for deviations in leptonic anomalous magnetic moments? Might they be clues to a deeper theory of flavour and mass? The Belle II experiment has only just begun taking data, and we wait eagerly for what it has to say on these matters.  $LHCb$  too will continue to improve its measurements with

more collisions; if the anomalies persist, these will be undeniable evidence of physics beyond the SM accessible to the next generation of hadron colliders.

These measurements are tantalising because of their consistency and breadth, but it would not be the first time that physicists have been lead astray, should they disappear with more statistics. Even so, what is perhaps the central result of my doctoral work will remain unchanged: that deviations from lepton-flavour universality in four-fermion operators may be intimately connected to mass generation in the neutrino sector.

# Acknowledgements

I would like to thank  $x$  and  $y$ .



*For  $x$  and  $y$ .*





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A.1 The SM fields and their transformation properties under the SM gauge group  $G_{\text{SM}}$  and the Lorentz group. The final unbolded number in the 3-tuples of the  $G_{\text{SM}}$  column represents the  $\text{U}(1)_Y$  charge of the field, normalised such that  $Q = I_3 + Y$ . For the fermions a generational index has been suppressed. . . . . 25



## 1

## Introduction

*The following is a general introduction to the background topics referred to and assumed in subsequent chapters. This includes a review of popular theories of neutrino mass, the current status of neutrino-oscillation parameters, a general introduction to Effective Field Theory (EFT), the experimental situation relevant to the flavour anomalies, and topics peripheral to all of these.*

## 1.1 The Standard Model and neutrinos

Laboratory experiments to date have firmly established the predictive power of the Standard Model (SM) of particle physics, a combined theory of the electroweak and strong interactions described by the gauge group  $G_{\text{SM}} = \text{SU}(3)_c \otimes \text{SU}(2)_L \otimes \text{U}(1)_Y$ . It is a model whose probes and predictions span at least 33 orders of magnitude<sup>1</sup> with varying degrees of precision, and these are consistent with almost all known experiments. Although it displays a number of arbitrary features, the dynamics of the theory are mostly fixed by the fundamental principles of gauge theory and Lorentz invariance. Most of this arbitrariness resides in the matter sector of the theory, whose properties

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<sup>1</sup>The interval given is from the distance scales probed at the LHC (roughly  $10^{-17}$  cm) to the size of the solar system (roughly  $10^{16}$  cm).

Field	$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$	$SU(2)_+ \otimes SU(2)_-$
$Q^{\alpha ai}$	$(3, 2, \frac{1}{6})$	$(2, 1)$
$L^{\alpha i}$	$(1, 2, -\frac{1}{2})$	$(2, 1)$
$\bar{u}_a^\alpha$	$(\bar{3}, 1, -\frac{2}{3})$	$(2, 1)$
$\bar{d}_a^\alpha$	$(\bar{3}, 1, \frac{1}{3})$	$(2, 1)$
$\bar{e}^\alpha$	$(1, 1, 1)$	$(2, 1)$
$(G_{\alpha\beta})^a_b$	$(8, 1, 0)$	$(3, 1)$
$(W_{\alpha\beta})^i_j$	$(1, 3, 0)$	$(3, 1)$
$B_{\alpha\beta}$	$(1, 1, 0)$	$(3, 1)$
$H^i$	$(1, 2, \frac{1}{2})$	$(1, 1)$

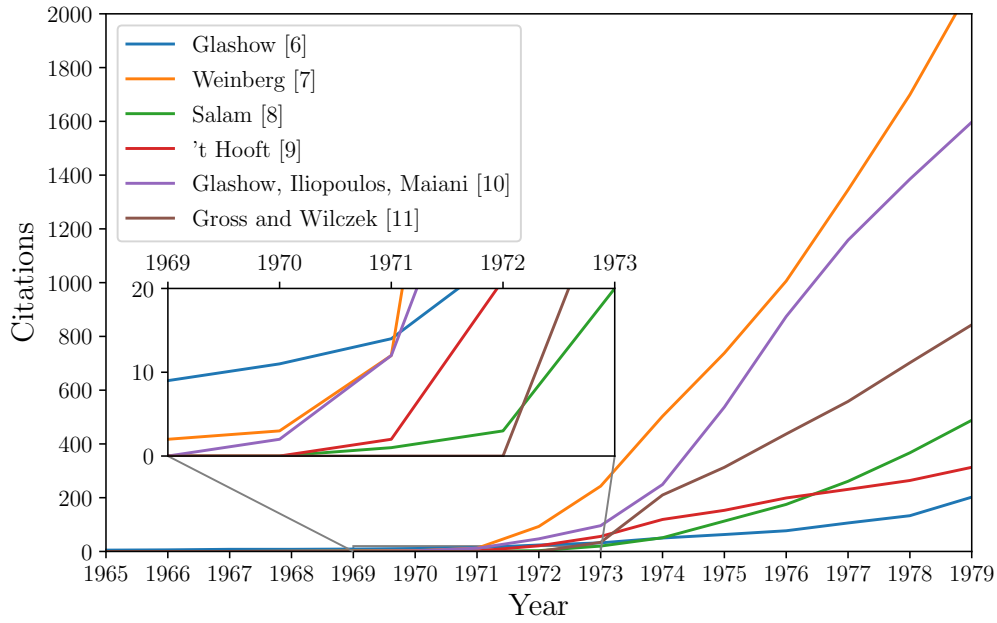
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(masses, coupling constants, quantum numbers, *etc.*) are not predicted, but are instead motivated on phenomenological grounds. We show the fields of the SM and their defining properties in Table 1.1, according to the mathematical conventions of Appendix A.

The SM inherits the experimental success of the  $SU(2) \otimes U(1)$  theory of the weak interactions, first proposed by Glashow [10] in 1961 as a possible underlying structure for Fermi’s theory of beta decay. Before the end of the same decade, Weinberg [11] and Salam [12] had constructed the modern theory of leptons based on the spontaneous breaking of  $SU(2)_L \otimes U(1)_Y$  to the electromagnetic symmetry. Interestingly, it seems that these seminal papers went mostly unnoticed (see Fig. 1.1) until the early 1970s, when ’t Hooft proved the renormalisability of spontaneously broken gauge theories [13] as a graduate student working under the supervision of Veltman. By the mid 1970s the framework had been extended to include the quarks [14] and the unbroken chromodynamic group, which was successfully shown to reproduce the Bjorken scaling seen in deep-inelastic-scattering experiments through asymptotic freedom [15].

Despite its successes, the SM cannot be the complete theory of fundamental particles and their interactions. It does not explain phenomena such as the baryon asym-





**Figure 1.1:** The cumulative citation graph for a selection of papers presenting foundational results relevant to the SM. Weinberg’s seminal paper ‘A model of leptons’ (1967) saw an explosion of citations following ’t Hooft’s work on the renormalisability of gauge theories (1971).

metry present in the Universe or its accelerating expansion. Additionally, the particle spectrum contains no viable candidate for dark matter, whose existence is strongly suggested by astrophysical and cosmological data. The SM cannot explain why the electric dipole moment of the neutron is so small, why there are three generations of matter or, notably in our case, the origin of neutrino oscillations and the implied small but non-zero neutrino masses.

## 1.2 Massive neutrinos in experiment and theory

In the SM the neutrino fields appear only within the lepton doublet  $L$ , and one cannot write down—in analogy to the up-type Yukawa—a renormalisable operator that leads to neutrino masses because of the absence of the right-handed fields. The wealth of experimental evidence for massive neutrinos then constitutes clear evidence for physics beyond the SM.

This evidence could in principle have come from many kinds of experiments, but

currently only neutrino oscillations provide strong signs that the masses are non-zero. Below we discuss the phenomenon of neutrino oscillations in the context of the outstandingly successful three-flavour mixing paradigm. We then move on to other probes of neutrino masses, which currently only provide limits on the mass scale. On the theory side, we summarise some popular and motivated extensions of the SM that accommodate massive neutrinos, placing particular emphasis on the direction we have followed in the novel work presented in this thesis. This includes an overview of tree- and loop-level models of Majorana neutrino mass.

### 1.2.1 Neutrino oscillations

The neutrino flavour eigenstates  $\check{\nu}_i = (\nu_e, \nu_\mu, \nu_\tau)$  are defined as the states that couple at charged-current interaction vertices with the corresponding charged lepton. These are the states in which the neutrinos are almost always produced in experiments, and certainly always measured. If neutrinos are massive there is no reason to expect these to coincide with the mass eigenstates  $\nu_i = (\nu_1, \nu_2, \nu_3)$ . In general, the flavour eigenstates will be an admixture of the propagating fields

$$\check{\nu}_i = U_i^{*j} \nu_j, \quad (1.1)$$

where the  $U_i^j$  are elements of the unitary Pontecorvo–Maki–Nakagawa–Sakata (PMNS) neutrino mixing matrix [16, 17]. The PMNS matrix is defined such that it diagonalises the neutrino mass matrix:

$$\mathbf{U}^\dagger \mathbf{m}_\nu \mathbf{U}^* = \text{diag}(m_1, m_2, m_3), \quad (1.2)$$

where the  $m_i$  are the neutrino masses. Being a  $3 \times 3$  unitary matrix,  $\mathbf{U}$  is in general parametrised by three mixing angles and six phases. Not all of the phases are physical, since the neutrino and charged-lepton fields can be redefined in such a way that five of the phases are removed in the case of Dirac neutrinos. In the presence of a Majorana mass term, only the charged leptons can be rephased. This leaves three physical phases with the two additional ones termed *Majorana phases*. In general

$$\mathbf{U} = \begin{bmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{\text{CP}}} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta_{\text{CP}}} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta_{\text{CP}}} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta_{\text{CP}}} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta_{\text{CP}}} & c_{23}c_{13} \end{bmatrix} \mathbf{P}, \quad (1.3)$$

where  $c_{ij} = \cos \theta_{ij}$ ,  $s_{ij} = \sin \theta_{ij}$  and

$$\mathbf{P} = \begin{cases} \text{diag}(e^{i\alpha_1}, e^{i\alpha_2}, 1) & \text{for Majorana neutrinos} \\ \mathbf{1}_{3 \times 3} & \text{for Dirac neutrinos} \end{cases}. \quad (1.4)$$

The phase  $\delta_{\text{CP}}$  is often called the *Dirac phase*, while  $\alpha_{1,2}$  are the Majorana phases discussed above.

Neutrino oscillation experiments typically involve the production of neutrino flavour states from charged-current processes, *e.g.* leptonic pion decays. Each mass eigenstate evolves in time independently according to the Schrödinger equation: *i.e.*  $|\nu_i(t)\rangle = \exp(-iE_i t)|\nu_i(0)\rangle$ , for evolution *in vacuo*. This alters the initial superposition away from being a pure flavour eigenstate:

$$|\check{\nu}_i(t)\rangle = \sum_j U_i^{*j} e^{-iE_j t} |\nu_j\rangle \quad (1.5)$$

$$= \sum_{j,k} U_i^{*j} e^{-iE_j t} U_j^k |\check{\nu}_k\rangle. \quad (1.6)$$

The probability of measuring a specific flavour through the charged-current interaction then oscillates with time:

$$P(\check{\nu}_m \rightarrow \check{\nu}_n) = |\langle \check{\nu}_n | \check{\nu}_m(t) \rangle|^2 = \left| \sum_i U_m^{*i} U_i^n e^{-iE_i t} \right|^2. \quad (1.7)$$

The expression can be expanded and the kinematic factors simplified from the fact that the neutrinos are ultra-relativistic. We follow the usual convention and take  $E_i = \sqrt{\mathbf{p}^2 + m_i^2} \approx |\mathbf{p}| + m_i^2/(2E)$  with  $E = |\mathbf{p}|$ . This gives

$$\begin{aligned} P(\check{\nu}_m \rightarrow \check{\nu}_n) = & \delta_{mn} - 4 \sum_{i < j} \text{Re} \left( U_m^i U_m^{*j} U_n^{*i} U_n^j \right) \sin^2 \frac{\Delta m_{ij}^2 L}{4E} \\ & + 2 \sum_{i < j} \text{Im} \left( U_m^i U_m^{*j} U_n^{*i} U_n^j \right) \sin \frac{\Delta m_{ji}^2 L}{2E}, \end{aligned} \quad (1.8)$$

where  $\Delta m_{ij}^2 \equiv m_j^2 - m_i^2$  are the squared neutrino mass differences and  $L = ct$ , sometimes called the baseline, is the approximate distance travelled by the particles. To interpret the results of many experiments, it is often sufficient to consider an effective two-flavour oscillation paradigm. In this case, the neutrino-oscillation probabilities are governed

by a single squared mass difference  $\Delta m^2$  and a single angle  $\theta$ . Interestingly, the CP-violating phase is completely absent from the two flavour formula:

$$P(\check{\nu}_m \rightarrow \check{\nu}_n)_{n_f=2} = \sin^2(2\theta) \sin^2 \frac{\Delta m^2 L}{4E}. \quad (1.9)$$

From the expressions in Eqs. (1.8) and (1.9) a number of properties of the vacuum neutrino oscillations become clear.

1. The neutrino oscillation probabilities depend on the neutrino mass differences, and not on the absolute mass scale. For three flavours, there are only two independent squared mass differences. Typically chosen to be  $\Delta m_{21}^2$  and  $\Delta m_{31}^2$ , although often they are referred to with the historical names  $\Delta m_{\text{sol}}^2$  and  $\Delta m_{\text{atm}}^2$ , discussed in detail below.
2. From Eq. (1.8) it is clear that the oscillations only occur if the neutrinos are non-degenerate and the neutrino mixing is non-trivial, *i.e.* if  $\Delta m_{ij} \neq 0$  and  $\mathbf{U} \neq \mathbf{1}$ .
3. The PMNS matrix elements only appear in the combination  $U_m^i U_m^{*i}$ , to which the Majorana phases contained within the matrix  $\mathbf{P}$  do not contribute. This implies that oscillation experiments cannot comment on the Dirac or Majorana nature<sup>2</sup> of the neutrinos. Oscillations can however probe  $\delta_{\text{CP}}$ .
4. In the effective two-flavour mixing paradigm, both  $\theta$  and  $\Delta m^2$  appear in such a way that neither the sign of  $\Delta m^2$  nor the octant of  $\theta$  can be uniquely determined.

Thus, neutrino oscillations imply that the neutrino masses of at least two of the mass eigenstates are non-degenerate, and therefore only one neutrino could potentially be massless. The largest squared mass difference can therefore be translated into an upper bound on the mass of the heaviest neutrino, which we present later with modern data.

Historically, the effective two-flavour mixing paradigm has provided a good framework for interpreting early indications of neutrino oscillations. Specifically, the solar and atmospheric neutrino puzzles have approximate descriptions in terms of a two-flavour picture in which  $\nu_e \rightarrow \nu_\mu$  oscillation in both matter and vacuum accounts for the deficit of electron neutrinos measured from the sun, and  $\nu_\mu \rightarrow \nu_\tau$  oscillations *in vacuo* explain the shortage of muon neutrinos from cosmic-ray-induced production in the upper atmosphere.

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<sup>2</sup>Of course, this is already clear from the fact that neutrino oscillations conserve total lepton number, despite breaking the individual familial lepton-number symmetries  $L_{e,\mu,\tau}$ .

The measurement and resolution of these puzzles is an interesting and exciting chapter in the recent history of physics. Experiments as early as the 1960s had noticed a shortage of electron neutrinos coming from the sun relative to the predictions of solar models [18–21], which themselves were subject to much uncertainty [22]. For detection there were three main approaches: Raymond Davis and collaborators [23] pioneered experiments that measured the solar electron-neutrino flux using Chlorine, the Kamiokande and later Super-Kamiokande collaborations [24, 25] used water Cherenkov detectors, and the experiments GALLEX [26] and SAGE [27] had Gallium as the detecting material. All of these experiments showed a deficit of solar electron neutrinos, although they were sensitive to neutrinos of different energies. The Sudbury Neutrino Observatory gave the final word on the oscillation solution to the solar neutrino puzzle with accurate confirmation of the electron-neutrino deficit, along with a measurement of the *total* neutrino flux which was found to be in agreement with the solar models [28, 29].

Atmospheric neutrinos were known to come about from helicity-suppressed kaon and pion decays to muons and muon neutrinos. A suppression by about 50% of the expected flux of atmospheric muon neutrinos was measured by the Kamiokande [30] and Irvine–Michigan–Brookhaven [31] experiments in the early 1990s, and after the upgrade to Super-Kamiokande the deficit was confirmed to high precision with results presented at the ‘Neutrino 2002’ conference [32–35].

The pairs of mixing parameters associated with these two classes of measurements are usually dubbed  $\theta_{\text{sol}}, \Delta m_{\text{sol}}^2$  and  $\theta_{\text{atm}}, \Delta m_{\text{atm}}^2$ . Experimental results find  $\Delta m_{\text{sol}}^2 \ll \Delta m_{\text{atm}}^2$  and that both  $\theta_{\text{sol}}$  and  $\theta_{\text{atm}}$  are large compared to any angles found in the CKM matrix. Interpreted in terms of three-flavour mixing, common convention identifies  $\Delta m_{\text{sol}}^2$  with the squared mass difference between  $\nu_2$  and  $\nu_1$ , which is known to be positive<sup>3</sup> (i.e.  $\Delta m_{21}^2 > 0$ ). The solar mixing angle  $\theta_{\text{sol}}$  is then associated with  $\theta_{12}$ . The atmospheric mixing parameters are identified with  $|\Delta m_{31}^2|$  or  $|\Delta m_{32}^2|$  and  $\theta_{23}$ . Of course, three-flavour effects alter the simplistic picture presented here and must be included to interpret measurements of  $\theta_{13}$  and  $\delta_{\text{CP}}$ , see e.g. Ref. [36] and references therein for a more detailed discussion. The picture that emerges from these experiments is then

$$\Delta m_{\text{sol}}^2 \approx \Delta m_{21}^2 \ll |\Delta m_{31}^2| \approx |\Delta m_{32}^2| \approx |\Delta m_{\text{atm}}^2|, \quad (1.10)$$

with which both the *normal mass ordering*  $m_1 < m_2 < m_3$  and the *inverted mass ordering*  $m_3 < m_1 < m_2$  are consistent.

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<sup>3</sup>We note that the sign of  $\Delta m_{21}^2$  can be known since oscillations in matter are also relevant for the solar squared mass difference, which depart from the simple formula of Eq. (1.9).

Neutrino oscillation experiments have continued to probe the squared mass differences and mixing parameters with impressively high precision, see *e.g.* Refs. [6, 37]. Reactor neutrino experiments like KamLAND [38] and long-baseline accelerators, *e.g.* T2K [39] and NOvA [40], are sensitive to all of these parameters, although  $\Delta m_{\text{atm}}^2$  and  $\theta_{13}$  are best measured at short-baseline reactors like Double Chooz [41], RENO [42] and Daya Bay [43]. Today the octant of  $\theta_{12}$  is certainly known, while  $\theta_{13}$  is constrained to be close to 0.15. The sign of the atmospheric squared mass difference is still unknown, and therefore so is the mass ordering for the neutrinos. The value of the CP-violating Dirac phase  $\delta_{\text{CP}}$  is less clear, although there is a preference for a value somewhere between  $\pi$  and  $3\pi/2$ . The extent of CP-violation in the neutrino sector can be represented in a rephasing-invariant way with the leptonic Jarlskog invariant

$$J_{\text{CP}} = \frac{1}{8} \cos \theta_{13} \sin 2\theta_{12} \sin 2\theta_{13} \sin 2\theta_{23} \sin \delta_{\text{CP}} , \quad (1.11)$$

so a value of  $\pi$  would imply no CP-violating effects, while  $\delta_{\text{CP}} = 3\pi/2$  would make these maximal. For this work we take the results of the most recent fit to neutrino oscillation data by the NuFit collaboration [6, 7] in the context of the three-flavour paradigm. These results are summarised in Fig. 1.2 separately for the cases of normal and inverted mass ordering. Results including atmospheric neutrino oscillation data from Super-Kamiokande and those not are also distinguished. Two-dimensional projections of the  $\chi^2$  fit for the same parameters are shown in Fig. 1.3. These data suggest a leptonic mixing matrix that has a very different form to the CKM matrix, which we call  $\mathbf{V}$ . We represent this qualitatively by using boxes whose side lengths are scaled to the magnitude of the best-fit values of the parameters in the matrices, the textures are

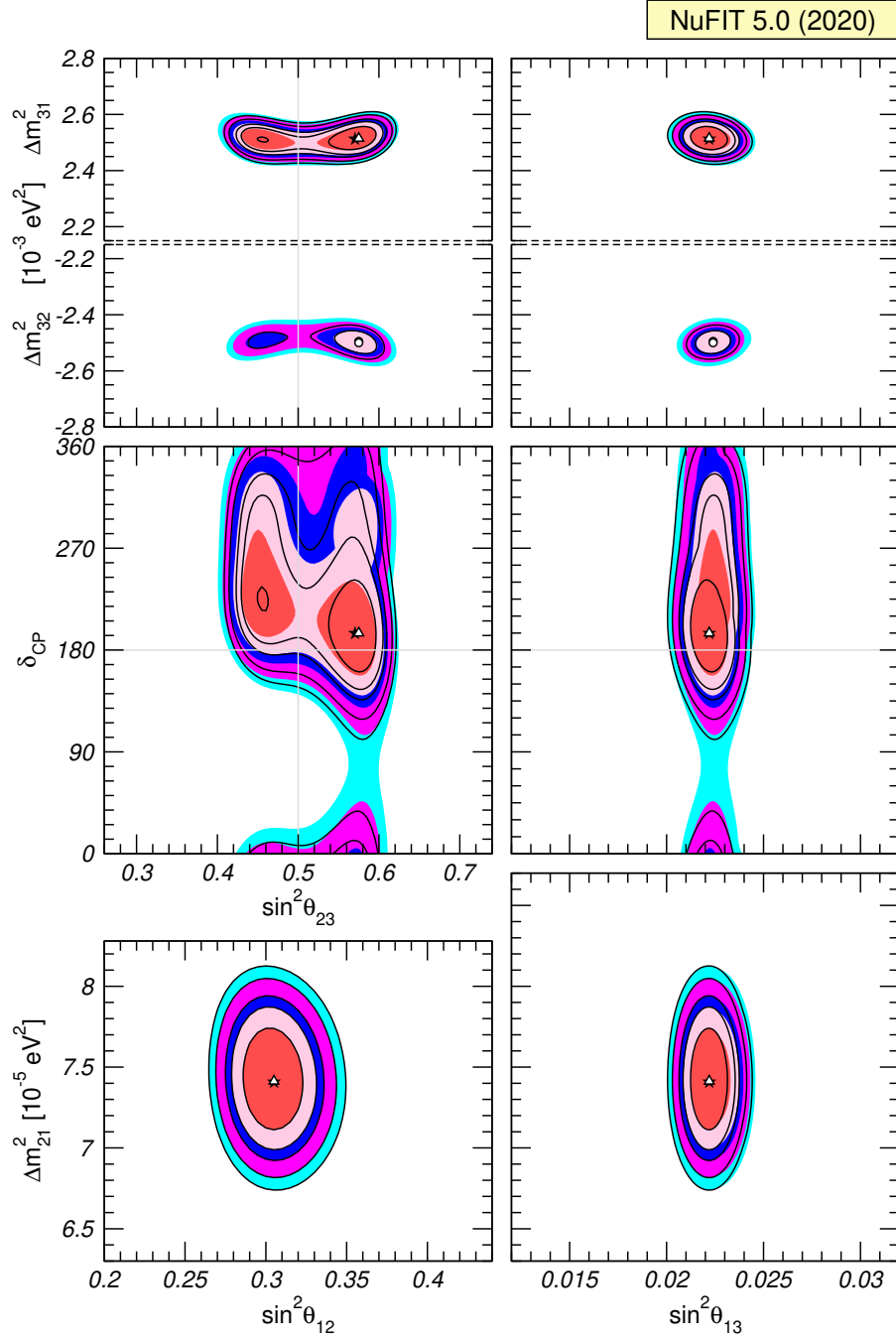
$$\mathbf{U} \sim \begin{pmatrix} \blacksquare & \blacksquare & \cdot \\ \cdot & \blacksquare & \blacksquare \\ \blacksquare & \blacksquare & \blacksquare \end{pmatrix}, \quad \mathbf{V} \sim \begin{pmatrix} \blacksquare & \cdot & \\ \cdot & \blacksquare & \\ & & \blacksquare \end{pmatrix}. \quad (1.12)$$

For the PMNS matrix we take the best fit values for the normal mass ordering including the Super-Kamiokande results, *i.e.* the numbers in the top-left quadrant of Fig. 1.2. The same numbers also imply an upper bound on the mass of the heaviest neutrino at

$$m_{\text{heaviest}} \leq \sqrt{|\Delta m_{\text{atm}}^2|} \approx 0.05 \text{ eV} . \quad (1.13)$$

NuFIT 5.0 (2020)					
without SK atmospheric data		Normal Ordering (best fit)		Inverted Ordering ( $\Delta\chi^2 = 2.7$ )	
		bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
	$\sin^2 \theta_{12}$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.44^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.86$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.570^{+0.018}_{-0.024}$	$0.407 \rightarrow 0.618$	$0.575^{+0.017}_{-0.021}$	$0.411 \rightarrow 0.621$
	$\theta_{23}/^\circ$	$49.0^{+1.1}_{-1.4}$	$39.6 \rightarrow 51.8$	$49.3^{+1.0}_{-1.2}$	$39.9 \rightarrow 52.0$
	$\sin^2 \theta_{13}$	$0.02221^{+0.00068}_{-0.00062}$	$0.02034 \rightarrow 0.02430$	$0.02240^{+0.00062}_{-0.00062}$	$0.02053 \rightarrow 0.02436$
	$\theta_{13}/^\circ$	$8.57^{+0.13}_{-0.12}$	$8.20 \rightarrow 8.97$	$8.61^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.98$
	$\delta_{\text{CP}}/^\circ$	$195^{+51}_{-25}$	$107 \rightarrow 403$	$286^{+27}_{-32}$	$192 \rightarrow 360$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.514^{+0.028}_{-0.027}$	$+2.431 \rightarrow +2.598$	$-2.497^{+0.028}_{-0.028}$	$-2.583 \rightarrow -2.412$
with SK atmospheric data		Normal Ordering (best fit)		Inverted Ordering ( $\Delta\chi^2 = 7.1$ )	
		bfp $\pm 1\sigma$	$3\sigma$ range	bfp $\pm 1\sigma$	$3\sigma$ range
	$\sin^2 \theta_{12}$	$0.304^{+0.012}_{-0.012}$	$0.269 \rightarrow 0.343$	$0.304^{+0.013}_{-0.012}$	$0.269 \rightarrow 0.343$
	$\theta_{12}/^\circ$	$33.44^{+0.77}_{-0.74}$	$31.27 \rightarrow 35.86$	$33.45^{+0.78}_{-0.75}$	$31.27 \rightarrow 35.87$
	$\sin^2 \theta_{23}$	$0.573^{+0.016}_{-0.020}$	$0.415 \rightarrow 0.616$	$0.575^{+0.016}_{-0.019}$	$0.419 \rightarrow 0.617$
	$\theta_{23}/^\circ$	$49.2^{+0.9}_{-1.2}$	$40.1 \rightarrow 51.7$	$49.3^{+0.9}_{-1.1}$	$40.3 \rightarrow 51.8$
	$\sin^2 \theta_{13}$	$0.02219^{+0.00062}_{-0.00063}$	$0.02032 \rightarrow 0.02410$	$0.02238^{+0.00063}_{-0.00062}$	$0.02052 \rightarrow 0.02428$
	$\theta_{13}/^\circ$	$8.57^{+0.12}_{-0.12}$	$8.20 \rightarrow 8.93$	$8.60^{+0.12}_{-0.12}$	$8.24 \rightarrow 8.96$
	$\delta_{\text{CP}}/^\circ$	$197^{+27}_{-24}$	$120 \rightarrow 369$	$282^{+26}_{-30}$	$193 \rightarrow 352$
	$\frac{\Delta m_{21}^2}{10^{-5} \text{ eV}^2}$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$	$7.42^{+0.21}_{-0.20}$	$6.82 \rightarrow 8.04$
	$\frac{\Delta m_{3\ell}^2}{10^{-3} \text{ eV}^2}$	$+2.517^{+0.026}_{-0.028}$	$+2.435 \rightarrow +2.598$	$-2.498^{+0.028}_{-0.028}$	$-2.581 \rightarrow -2.414$

**Figure 1.2:** The figure shows a table taken from the latest global fit to neutrino mass and mixing parameters by the NuFit collaboration [6, 7] in the three-flavour picture. The results presented in the upper (lower) panel are obtained by excluding (including) the  $\chi^2$  data on atmospheric neutrinos provided by the Super-Kamiokande collaboration (SK). The numbers in the 1st (2nd) column are obtained assuming normal (inverted) neutrino mass ordering. See Ref. [7] for more information.



**Figure 1.3:** The figure shows the two-dimensional allowed regions obtained by the latest fit to the neutrino mass and mixing parameters by the NuFit collaboration [6, 7]. Each plot shows the two-dimensional projection of the allowed region after marginalising with respect to the other parameters. The coloured regions (black contour curves) are obtained by excluding (including) the Super-Kamiokande  $\chi^2$  data. The different contours correspond to the two-dimensional allowed regions at  $1\sigma$ , 90%,  $2\sigma$ , 99%,  $3\sigma$  confidence. See Ref. [7] for more information.



### 1.2.2 Other experimental probes

Although neutrino oscillations provide a wealth of evidence for non-zero masses for at least two of the neutrino fields, they do not probe the absolute mass scale. There are however kinematic and cosmological probes which bound the neutrino masses, and some of these are mentioned here.

#### Beta decay

A study of the kinematics of beta-decay experiments shows that differences in the energy distribution of the emitted electron are expected for different values of the neutrino mass. Currently these experiments only provide upper bounds on the effective neutrino mass [44]

$$m_\beta \equiv \sqrt{\sum_i |U_1^i|^2 m_i^2}. \quad (1.14)$$

The best results come from tritium experiments which probe  ${}^3\text{H} \rightarrow {}^3\text{He} + e + \bar{\nu}_e$ . The KATRIN experiment recently presented the most stringent upper bound [45, 46]

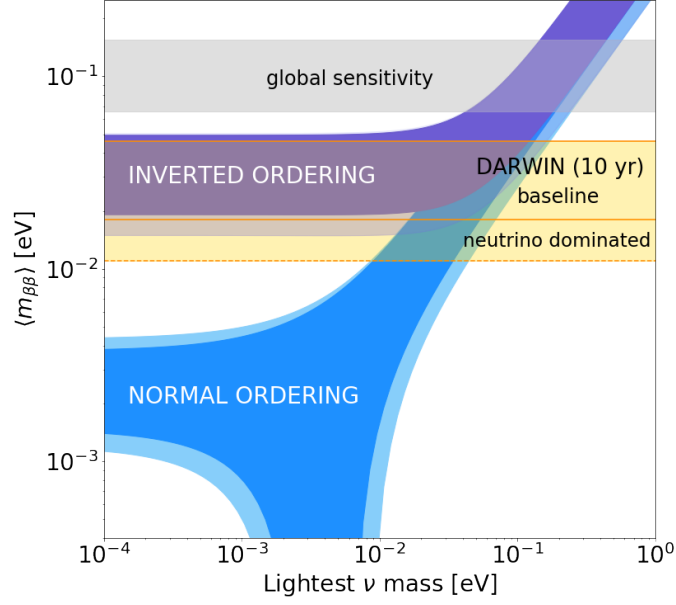
$$m_\beta < 1.1 \text{ eV}, \quad (1.15)$$

at 90% confidence, with a projected limit of  $m_\beta < 0.2 \text{ eV}$  with the full dataset.

Another process with the potential to probe the absolute scale of the neutrino masses, as well as the Majorana phases, is neutrinoless double beta decay ( $0\nu\beta\beta$ ). The process requires the violation of lepton-number by two units, and is therefore intimately tied to the neutrinos' possible Majorana nature. If double-beta decay is seen, the *black box theorem* [47–49] guarantees that the neutrinos pick up a radiative Majorana mass, even if the neutrino masses vanish at tree level. Graphically this is easy to understand: a  $0\nu\beta\beta$  operator can always be turned into a neutrino self-energy graph with four loops. The amplitude for the process is proportional to

$$\langle m_\nu \rangle_{\beta\beta} = \sum_i (U_1^i)^2 m_i, \quad (1.16)$$

which features both the neutrino masses and the Majorana phases. (Of course it may be that the four-loop contribution to the neutrino mass implied by the double-beta-decay operator represents only a small correction to the neutrino masses, which could arise at lower order.) Current limits on  $\langle m_\nu \rangle_{\beta\beta}$  are around 0.2 eV, see e.g. Ref. [50]



**Figure 1.4:** The figure shows limits on the effective neutrino mass for different values of  $m_{\text{lightest}}$  for both normal and inverted mass ordering. The grey region represents the combined sensitivity from a number of leading experiments [8]. The yellow regions are projections for the DARWIN experiment under different background hypotheses. The figure is taken from Ref. [9], and we point the reader there for more information.

for a recent review of the experimental status and prospects. Constraints on  $\langle m_{\nu} \rangle_{\beta\beta}$  are usually presented against the mass of the lightest neutrino mass eigenstate. The behaviour of  $\langle m_{\nu} \rangle_{\beta\beta}$  is very sensitive to the neutrino mass ordering, in such a way that the inverted scenario implies a minimum allowed value of  $\langle m_{\nu} \rangle_{\beta\beta}$ , which will begin to be probed by the next generation of experiments. A combined global limit and the projected sensitivity of the DARWIN experiment [9] are shown in Fig. 1.4, which also illustrates the different behaviour of the inverted and normal neutrino mass orderings in the  $\langle m_{\nu} \rangle_{\beta\beta}$  vs.  $m_{\text{lightest}}$  plane.

### Cosmological limits

The most stringent limits on the sum of the neutrino masses come from cosmology, although they are model-dependent. In the minimal  $\Lambda$ CDM model adjusted for massive

neutrinos, the limit implied by the most recent Planck data release [51] is

$$\sum_i m_i < 0.12 \text{ eV} , \quad (1.17)$$

at 95% confidence. This is impressively small, and puts pressure on the inverted-ordering scenario, for which  $\sum_i m_i \gtrsim 0.1 \text{ eV}$ . Excitingly, future cosmological probes will likely make a measurement of the sum of the neutrino masses.

### 1.2.3 Models of neutrino masses

There are also sensible theoretical arguments for massive neutrinos.

## 1.3 Effective field theories of the SM

Nam dui ligula, fringilla a, euismod sodales, sollicitudin vel, wisi. Morbi auctor lorem non justo. Nam lacus libero, pretium at, lobortis vitae, ultricies et, tellus. Donec aliquet, tortor sed accumsan bibendum, erat ligula aliquet magna, vitae ornare odio metus a mi. Morbi ac orci et nisl hendrerit mollis. Suspendisse ut massa. Cras nec ante. Pellentesque a nulla. Cum sociis natoque penatibus et magnis dis parturient montes, nascetur ridiculus mus. Aliquam tincidunt urna. Nulla ullamcorper vestibulum turpis. Pellentesque cursus luctus mauris.

## 1.4 The flavour anomalies and their explanation

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## 2

## Model building from effective operators

## 2.1 Introduction

This is a test of *something with an apple* that I would like [\[11\]](#). The following is  $4a + 5 = 13$  some inline math and this and we did in in Python.

$$\int_{-\infty}^{\infty} \frac{1}{(2\pi\hbar)^3} \phi(p) dp. \quad (2.1)$$

We need some sans serif **words** here too. Then we need to check **what** the bold looks like.



## 3

## Models of radiative neutrino mass

## 3.1 Introduction

This is a test of *something with an apple* that I would like [\[11\]](#). The following is  $4a + 5 = 13$  some inline math and this and we did in in Python.

$$\int_{-\infty}^{\infty} \frac{1}{(2\pi\hbar)^3} \phi(p) dp. \quad (3.1)$$

We need some sans serif **words** here too. Then we need to check **what** the bold looks like.





## 4

# The $S_1$ leptoquark as an explanation of the flavour anomalies

*This chapter is based on the publication ‘Reconsidering the One Leptoquark scenario: flavour anomalies and neutrino mass,’ written in collaboration with Yi Cai, Michael A. Schmidt, and Raymond R. Volkas [2]. We study the potential of the  $S_1$  leptoquark to explain the flavour anomalies and the anomalous magnetic moment of the muon in a new region of parameter space.*

## 4.1 Introduction

A common origin for  $R_{D^{(*)}}$  and the anomalous  $b \rightarrow s$  data is suggested naturally if the former is explained by the effects of the operator  $(c^\dagger \bar{\sigma}_\mu b)(\tau^\dagger \bar{\sigma}^\mu \nu)$ , related in its general structure by  $SU(2)_L$  invariance to the aforementioned four-fermion effective operator accounting for the  $b \rightarrow s$  anomalies. A number of models exploring this idea have been suggested in the literature [52–66] (along with many others addressing one or the other anomaly, e.g. [67–84]) and among these minimal explanations the Bauer–Neubert (BN) model [53] is one of notable simplicity and explanatory power: a TeV-scale scalar leptoquark protagonist mediating  $\bar{B} \rightarrow D^{(*)} \tau \bar{\nu}$  at tree-level and the  $b \rightarrow s$  decays through

one-loop box diagrams. The leptoquark transforms under the SM gauge group like a right-handed down-type quark and its pattern of couplings to SM fermions can also reconcile the measured and predicted values of the anomalous magnetic moment of the muon, another enduring tension.

Taken together, these measurements paint a picture of new physics interacting more strongly with the second and third generations of SM fermions, introducing lepton flavour non-universality and FCNC interactions at energies not significantly higher than the electroweak scale. Interestingly, many of these phenomenological motifs arise naturally in radiative models of neutrino mass, hinting towards the attractive possibility of a common explanation for both phenomena. Previous work has also considered radiative neutrino mass models whose particle content addresses  $R_K$  [66, 78, 85–87],  $R_{D^{(*)}}$  [60, 66] and  $(g - 2)_\mu$  [66, 85–88]. In Refs. [60, 78] the flavour anomalies are explained through two light scalar or vector leptoquarks whose couplings to the SM Higgs doublet and fermions prohibit a consistent assignment of lepton number to the leptoquarks such that the symmetry is respected. Thus  $U(1)_L$  is explicitly broken by two units and the neutrinos gain mass at the one-loop level [89], apart from the imposition of any additional symmetries<sup>1</sup>. A general feature of such models is that large amounts of fine-tuning are required to suppress the neutrino mass to the required scale with at least one set of leptoquark–fermion couplings sizeable enough to explain the anomalies.

---

<sup>1</sup>Mass generation in Ref. [88] occurs at the two-loop level because the Yukawa couplings of one of the leptoquarks to the left-chiral fermions is turned off.

## 5

## Models of neutrino mass and the flavour anomalies

## 5.1 Introduction

This is a test of *something with an apple* that I would like [\[11\]](#). The following is  $4a + 5 = 13$  some inline math and this and we did in in Python.

$$\int_{-\infty}^{\infty} \frac{1}{(2\pi\hbar)^3} \phi(p) dp . \quad (5.1)$$

We need some sans serif **words** here too. Then we need to check **what** the bold looks like.



# A

## Mathematical notation

Throughout the paper we choose to label representations by their dimension, which we typeset in bold. Fields are labelled by their transformation properties under the Lorentz group and the SM gauge group  $SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$ . All spinors are treated as two-component objects transforming as either  $(2, 1)$  (left-handed) or  $(1, 2)$  (right-handed) under the Lorentz group, written as  $SU(2)_+ \otimes SU(2)_-$ . The left-handed spinors carry undotted spinor indices  $\alpha, \beta, \dots \in \{1, 2\}$ , while the right-handed spinors carry dotted indices  $\dot{\alpha}, \dot{\beta}, \dots \in \{\dot{1}, \dot{2}\}$ . Wherever possible we attempt to conform to the conventions of Ref. [?] when working with spinor fields (see appendix G for the correspondence to four-component notation and appendix J for SM-fermion nomenclature). For objects carrying a single spacetime index  $V_\mu$  we define

$$V_{\alpha\dot{\beta}} = \sigma_{\alpha\dot{\beta}}^\mu V_\mu \quad \text{and} \quad \bar{V}_{\dot{\alpha}\beta} = \bar{\sigma}_{\dot{\alpha}\beta}^\mu V_\mu. \quad (\text{A.1})$$

Note that in this notation

$$\square = \partial_\mu \partial^\mu = \frac{1}{2} \text{Tr}[\partial \bar{\partial}] = \frac{1}{2} \text{Tr}[\bar{\partial} \partial], \quad (\text{A.2})$$

and we will often just use  $\square$  to represent the contraction of two covariant derivatives  $D_\mu D^\mu$  where this is clear from context. For field-strength tensors, generically  $X_{\mu\nu}$ , we

work with the irreducible representations (irreps)  $X_{\alpha\beta}$  and  $\bar{X}_{\dot{\alpha}\dot{\beta}}$ , where

$$X_{\{\alpha\beta\}} = 2i[\sigma^{\mu\nu}]_{\alpha}^{\gamma}\epsilon_{\gamma\beta}X_{\mu\nu} \quad \text{and} \quad \bar{X}_{\{\dot{\alpha}\dot{\beta}\}} = 2i[\bar{\sigma}^{\mu\nu}]_{\dot{\beta}}^{\dot{\gamma}}\epsilon_{\dot{\alpha}\dot{\gamma}}X_{\mu\nu}, \quad (\text{A.3})$$

or the alternate forms with one raised and one lowered index.

Indices for  $\text{SU}(2)_L$  (isospin) are taken from the middle of the Latin alphabet. These are kept lowercase for the fundamental representation for which  $i, j, k, \dots \in \{1, 2\}$  and the indices of the adjoint are capitalised  $I, J, K, \dots \in \{1, 2, 3\}$ . Colour indices are taken from the beginning of the Latin alphabet and the same distinction between lowercase and uppercase letters is made. For both  $\text{SU}(2)$  and  $\text{SU}(3)$ , a distinction between raised and lowered indices is maintained such that, for example,  $(\psi^i)^\dagger = (\psi^\dagger)_i$  for an isodoublet field  $\psi$ . However, we often specialise to the case of only raised, symmetrised indices for  $\text{SU}(2)$ , and use a tilde to denote a conjugate field whose  $\text{SU}(2)_L$  indices have been raised:

$$\tilde{\psi}^i \equiv \epsilon^{ij}\psi_j^\dagger. \quad (\text{A.4})$$

We adopt this notation from the usual definition of  $\tilde{H}$ , and note that throughout the paper we freely interchange between  $\tilde{\psi}^i$  and  $\psi_i^\dagger$ . For the sake of tidiness, we sometimes use parentheses  $(\dots)$  to indicate the contraction of suppressed indices. Curly braces are reserved to indicate symmetrised indices  $\{\dots\}$  and square brackets enclose antisymmetrised indices  $[\dots]$ , but this notation is avoided when the permutation symmetry between indices is clear. We use  $\tau^I$  and  $\lambda^A$  for the Pauli and Gell-Mann matrices, and normalise the non-abelian vector potentials of the SM such that

$$(W_{\alpha\beta})^i_j = \frac{1}{2}(\tau^I)^i_j W_{\alpha\beta}^I \quad \text{and} \quad (G_{\alpha\beta})^a_b = \frac{1}{2}(\lambda^A)^a_b G_{\alpha\beta}^A. \quad (\text{A.5})$$

Flavour (or family) indices of the SM fermions are represented by the lowercase Latin letters  $\{r, s, t, u, v, w\}$ .

For the non-gauge degrees of freedom in the SM we capitalise isospin doublets ( $Q, L, H$ ), while the left-handed isosinglets are written in lowercase with a bar featuring as a part of the name of the field ( $\bar{u}, \bar{d}, \bar{e}$ ). The representations and hypercharges for the SM field content are summarised in Table A.1. Our definition of the SM gauge-covariant derivative is exemplified by

$$\bar{D}_{\dot{\alpha}\beta} Q_r^{\beta ai} = \left[ \delta_b^a \delta_j^i (\bar{\partial}_{\dot{\alpha}\beta} + ig_1 Y_Q \bar{B}_{\dot{\alpha}\beta}) + ig_2 \delta_b^a (\bar{W}_{\dot{\alpha}\beta})^i_j + ig_3 \delta_j^i (\bar{G}_{\dot{\alpha}\beta})^a_b \right] Q_r^{\beta bj}. \quad (\text{A.6})$$

Note that the derivative implicitly carries  $\text{SU}(2)_L$  and  $\text{SU}(3)_c$  indices [explicit on the

Field	$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y$	$SU(2)_+ \otimes SU(2)_-$
$Q^{\alpha ai}$	$(3, 2, \frac{1}{6})$	$(2, 1)$
$L^{\alpha i}$	$(1, 2, -\frac{1}{2})$	$(2, 1)$
$\bar{u}_a^\alpha$	$(\bar{3}, 1, -\frac{2}{3})$	$(2, 1)$
$\bar{d}_a^\alpha$	$(\bar{3}, 1, \frac{1}{3})$	$(2, 1)$
$\bar{e}^\alpha$	$(1, 1, 1)$	$(2, 1)$
$(G_{\alpha\beta})^a_b$	$(8, 1, 0)$	$(3, 1)$
$(W_{\alpha\beta})^i_j$	$(1, 3, 0)$	$(3, 1)$
$B_{\alpha\beta}$	$(1, 1, 0)$	$(3, 1)$
$H^i$	$(1, 2, \frac{1}{2})$	$(1, 1)$

**Table A.1:** The SM fields and their transformation properties under the SM gauge group  $G_{\text{SM}}$  and the Lorentz group. The final unbolded number in the 3-tuples of the  $G_{\text{SM}}$  column represents the  $U(1)_Y$  charge of the field, normalised such that  $Q = I_3 + Y$ . For the fermions a generational index has been suppressed.

right-hand side of Eq. (A.6)] which are suppressed on the left-hand side to reduce clutter. Where appropriate we show these indices explicitly.

We represent the SM quantum numbers of fields as a 3-tuple  $(C, I, Y)_L$ , with  $C$  and  $I$  the dimension of the colour and isospin representations,  $Y$  the hypercharge of the field, and  $L$  an (often omitted) label of the Lorentz representation:  $S$  (scalar),  $F$  (fermion) or  $V$  (vector), although sometimes we use the irrep, e.g.  $(2, 1)$ . We normalise the hypercharge such that  $Q = I_3 + Y$ . Finally, for exotic fields that contribute to dimension-six operators at tree-level, we try and adopt names consistent with Table 3 of Ref. [? ].





## B

# The two-photon decay of a scalar-quirk bound state

*At the time of writing the original paper, I was too nervous to ask my collaborator what he thought of using  $\mathfrak{f}$  as the name of the hypothetical particle. Unexpectedly, the name ended up becoming very popular. This mistake is corrected in this chapter.*

## B.1 Introduction

An excess of events containing two photons with invariant mass near 750 GeV has been observed in 13 TeV proton–proton collisions by the ATLAS and CMS collaborations [90, 91]. The cross section  $\sigma(pp \rightarrow \gamma\gamma)$  is estimated to be

$$\sigma(pp \rightarrow \gamma\gamma) = \begin{cases} (10 \pm 3) \text{ fb} & \text{ATLAS} \\ (6 \pm 3) \text{ fb} & \text{CMS} \end{cases} \quad (\text{B.1})$$

and there is no evidence of any accompanying excess in the dilepton channel [92]. If we interpret this excess as the two photon decay of a single new particle of mass  $m$  then ATLAS data provide a hint of a large width:  $\Gamma/m \sim 0.06$ , while CMS data prefer

a narrow width. Naturally, further data collected at the LHC should provide a clearer picture as to the nature of this excess.

There has been vast interest in the possibility that the diphoton excess results from physics beyond the SM. Most discussion has focused on models where the excess is due to a new scalar particle which subsequently decays into two photons *e.g.* Ref. [93]. The possibility that the new scalar particle is a bound state of exotic charged fermions has also been considered, *e.g.* Refs. [94–98]. Here we consider the case that the 750 GeV state is a non-relativistic bound state constituted by an exotic *scalar* particle  $\chi$  and its antiparticle, charged under  $SU(3)_c$  as well as a new unbroken non-abelian gauge interaction. Having  $\chi$  be a scalar rather than a fermion is not merely a matter of taste: In such a framework a fermionic  $\chi$  would lead to the formation of bound states which (typically) decay to dileptons more often than to photons; a situation which is not favoured by the data.

The bound state, which we denote  $\Pi$ , can be produced through gluon–gluon fusion directly (*i.e.* at threshold  $\sqrt{s_{gg}} \simeq M_\Pi$ ) or indirectly via  $gg \rightarrow \chi^\dagger \chi \rightarrow \Pi + \text{soft quanta}$  (*i.e.* above  $\Pi$  threshold:  $\sqrt{s_{gg}} > M_\Pi$ ). The indirect production mechanism can dominate the production of the bound state, which is an interesting feature of this kind of theory.

## B.2 The model

We take the new confining unbroken gauge interaction to be  $SU(N)$ , and assume that, like  $SU(3)_c$ , it is asymptotically free and confining at low energies. However, the new  $SU(N)$  dynamics is qualitatively different from QCD as all the matter particles [assumed to be in the fundamental representation of  $SU(N)$ ] are taken to be much heavier than the confinement scale,  $\Lambda_N$ . In fact we here consider only one such matter particle,  $\chi$ , so that  $M_\chi \gg \Lambda_N$  is assumed. In this circumstance a  $\chi^\dagger \chi$  pair produced at the LHC above the threshold  $2M_\chi$  but below  $4M_\chi$  cannot fragment into two jets. The  $SU(N)$  string which connects them cannot break as there are no light  $SU(N)$ -charged states available. This is in contrast to heavy quark production in QCD where light quarks can be produced out of the vacuum enabling the color string to break. The produced  $\chi^\dagger \chi$  pair can be viewed as a highly excited bound state, which de-excites by  $SU(N)$ -ball and soft glueball/pion emission [99].

With the new unbroken gauge interaction assumed to be  $SU(N)$  the gauge symmetry of the SM is extended to

$$SU(3)_c \otimes SU(2)_L \otimes U(1)_Y \otimes SU(N). \quad (\text{B.2})$$

This kind of theory can arise naturally in models which feature large colour groups [100–102] and in models with leptonic colour [103–106] but was also considered earlier by Okun [107]. The notation *quirks* for heavy particles charged under an unbroken gauge symmetry (where  $M_\chi \gg \Lambda_N$ ) was introduced in [99] where the relevant phenomenology was examined in some detail in a particular model<sup>1</sup>. For convenience we borrow their nomenclature and call the new quantum number *hue* and the massless gauge bosons *huons* ( $\mathcal{H}$ ).

The phenomenological signatures of the bound states (quirkonium) formed depend on whether the quirk is a fermion or boson. Here we assume that the quirk  $\chi$  is a Lorentz scalar in light of previous work which indicated that bound states formed from a fermionic  $\chi$  state would be expected to be observed at the LHC via decays of the spin-1 bound state into opposite-sign lepton pairs ( $\ell^+\ell^-$ ) [99, 106]. In fact, this appears to be a serious difficulty in attempts to interpret the 750 GeV state as a bound state of fermionic quirk particles (such as those of Refs. [94–96]). The detailed consideration of a scalar  $\chi$  appears to have been largely overlooked<sup>2</sup>, perhaps due to the paucity of known elementary scalar particles. With the recent discovery of a Higgs-like scalar at 125 GeV [110, 111] it is perhaps worth examining signatures of scalar quirk particles. In fact, we point out here that the two photon decay is the most important experimental signature of bound states formed from electrically charged scalar quirks. Furthermore this explanation is only weakly constrained by current data and thus appears to be a simple and plausible option for the new physics suggested by the observed diphoton excess.

### B.3 Explaining the excess

The scalar  $\chi$  that we introduce transforms under the extended gauge group (Eq. B.2) as

$$\chi \sim (3, 1, Y; \mathbf{N}), \quad (\text{B.3})$$

where we use the normalisation  $Q = Y/2$ . The possibility that  $\chi$  also transforms non-trivially under  $\text{SU}(2)_L$  is interesting, however for the purposes of this letter we focus on the  $\text{SU}(2)_L$  singlet case for definiteness. Since two-photon decays of non-relativistic quirkonium will be assumed to be responsible for the diphoton excess observed at the

<sup>1</sup>Some other aspects of such models have been discussed over the years, including the possibility that the  $\text{SU}(N)$  confining scale is low ( $\sim \text{keV}$ ), a situation which leads to macroscopic strings [108].

<sup>2</sup>The idea has been briefly mentioned in recent literature [97, 109].

LHC, the mass of  $\chi$  will need to be around 375 GeV.

We have assumed that  $\chi$  is charged under  $SU(3)_c$  so that it can be produced at tree-level through QCD-driven pair production. We present the production mechanisms in Fig. B.1. To estimate the production cross section of the bound states, we first consider the indirect production mechanism which we expect to be dominant. Here, a  $\chi^\dagger \chi$  pair is produced above threshold and de-excites emitting soft glueballs/pions and hueballs:  $gg \rightarrow \chi^\dagger \chi \rightarrow \Pi + \text{soft quanta}$ . We first consider the case where the confinement scale of the new  $SU(N)$  interaction is similar to that of QCD. What happens in this case can be adapted from the discussion in [99], where a fermionic quirk charged under an unbroken  $SU(2)$  gauge interaction was considered. As already briefly discussed in the introduction, the  $\chi^\dagger \chi$  pairs initially form a highly excited bound state, which subsequently de-excites in two stages. The first stage is the non-perturbative regime where the hue string is longer than  $\Lambda_N^{-1}$ . The second stage is characterised by a string scale significantly less than  $\Lambda_N^{-1}$ : the perturbative Coulomb region. Here the bound state can be characterised by the quantum numbers  $n$  and  $l$ . De-excitation continues until quirkonium is in a lowly excited state with  $l \leq 1$  and  $n$ . Imagine first that de-excitation continued until the ground state ( $n = 1, l = 0$ ) is reached. Given we are considering  $\chi$  to be a scalar, the quirkonium ground state,  $\Pi$ , will have spin 0, and is thus expected to decay into SM gauge bosons and huons. The cross section  $\sigma(pp \rightarrow \Pi \rightarrow \gamma\gamma)$  in this case is then

$$\sigma(pp \rightarrow \gamma\gamma) \approx \sigma(pp \rightarrow \chi^\dagger \chi) \times \text{Br}(\Pi \rightarrow \gamma\gamma). \quad (\text{B.4})$$

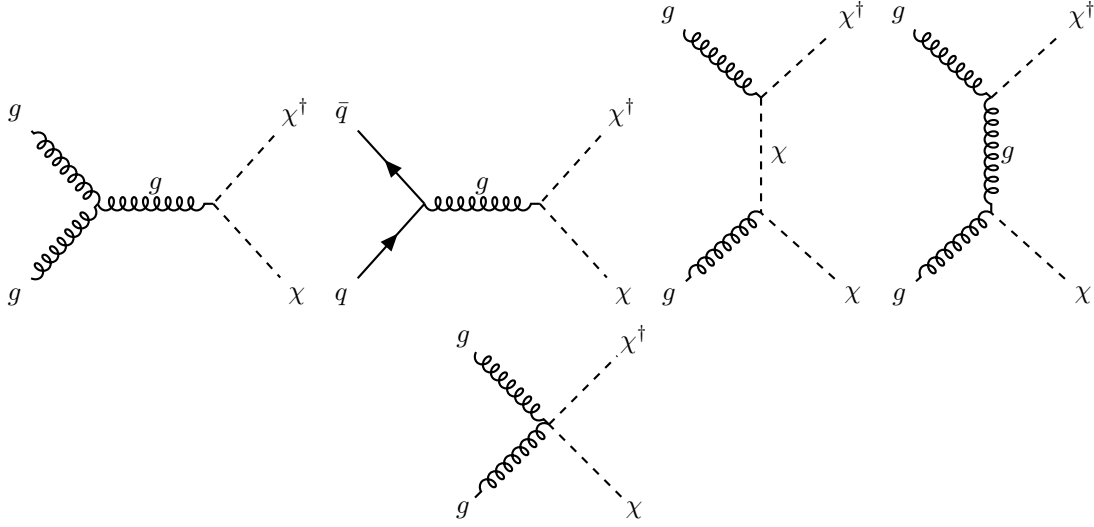
Since production is governed by QCD interactions, we can use the values of the pair production cross sections for stops/sbottoms in the limit of decoupled squarks and gluinos [112]. For a  $\chi$  mass of 375 GeV

$$\sigma(pp \rightarrow \chi^\dagger \chi) \approx \begin{cases} 2.6N \text{ pb} & \text{at 13 TeV} \\ 0.5N \text{ pb} & \text{at 8 TeV} \end{cases}. \quad (\text{B.5})$$

The branching fraction is to leading order

$$\text{Br}(\Pi \rightarrow \gamma\gamma) \simeq \frac{3NQ^4\alpha^2}{\frac{2}{3}N\alpha_s^2 + \frac{3}{2}C_N\alpha_N^2 + 3NQ^4\alpha^2}, \quad (\text{B.6})$$

where  $C_N \equiv (N^2 - 1)/(2N)$ ,  $\alpha_N$  is the new  $SU(N)$  interaction strength and we have neglected the small contribution of  $\Pi \rightarrow Z\gamma/ZZ$  to the total width. Eq. (B.6) also ne-



**Figure B.1:** Tree-level pair production mechanisms for the scalar quirk  $\chi$ .

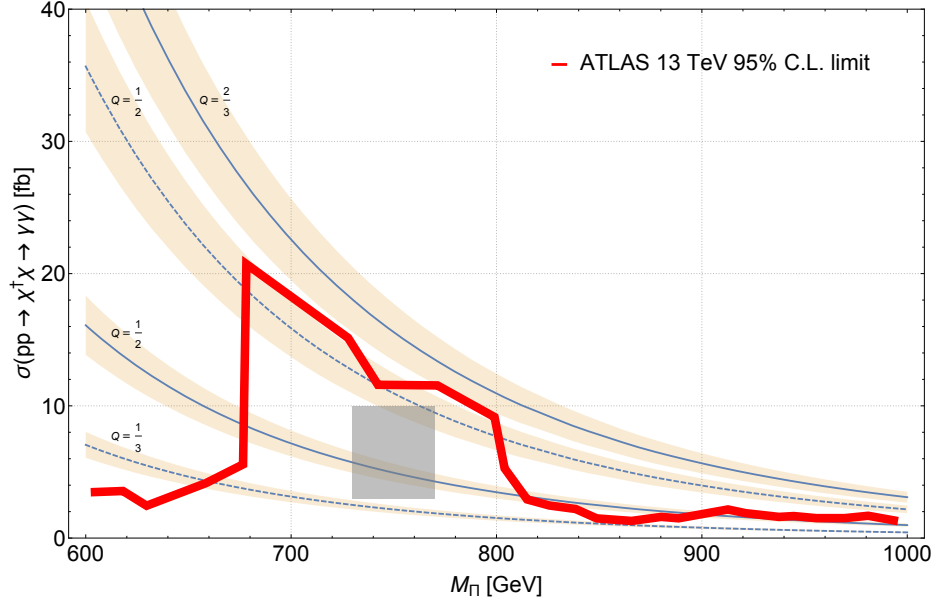
glects the decay to Higgs particles:  $\Pi \rightarrow hh$ , which arises from the Higgs potential portal term  $\lambda_\chi \chi^\dagger \chi \phi^\dagger \phi$ . Theoretically this rate is unconstrained given the dependence on the unknown parameter  $\lambda_\chi$ , but could potentially be important. However, limits from resonant Higgs boson pair production derived from 13 TeV data:  $\sigma(pp \rightarrow X \rightarrow hh \rightarrow bbbb) \lesssim 50 \text{ fb}$  at  $M_X \approx 750 \text{ GeV}$  [113, 114] imply that the Higgs decay channel must indeed be subdominant (*c.f.*  $\Pi \rightarrow gg, \mathcal{H}\mathcal{H}$ ).

The renormalised gauge coupling constants in Eq. (B.6) are evaluated at the renormalisation scale  $\mu \sim M_\Pi/2$ . Taking for instance the specific case of  $N = 2$ ,  $\alpha_N = \alpha_s \simeq 0.10$  (at  $\mu \sim M_\Pi/2$ ) gives

$$\sigma(pp \rightarrow \gamma\gamma) \approx 5 \left( \frac{Q}{1/2} \right)^4 \text{ fb at 13 TeV.} \quad (\text{B.7})$$

At  $\sqrt{s} = 8 \text{ TeV}$  the cross section is around five times smaller. We present the cross section  $\sigma(pp \rightarrow \Pi \rightarrow \gamma\gamma)$  for a range of masses  $M_\Pi$  and different combinations of  $Q$  and  $N$  in Fig. B.2. The parameter choice  $\alpha_N = \alpha_s$  and  $\Lambda_N = \Lambda_{\text{QCD}}$  has been assumed. (The cross section is not highly sensitive to  $\Lambda_N$ ,  $\alpha_N$  so long as we are in the perturbative regime:  $\Lambda_N \lesssim \Lambda_{\text{QCD}}$ .) Evidently, for  $N = 2$ , a  $\chi$  with electric charge  $Q \approx 1/2$  is produced at approximately the right rate to explain the diphoton excess.

In practice de-excitation of the produced quirkonium does not always continue until the ground state is reached. In this case annihilations of excited states can also contribute. However those with  $l = 0$  will decay in the same way as the ground state. The



**Figure B.2:** The cross section  $\sigma(pp \rightarrow \Pi \rightarrow \gamma\gamma)$  at 13 TeV for a range of quirkonium masses  $M_\Pi$  and charge assignments. Solid lines denote choices of  $N = 2$  and dashed lines choices of  $N = 5$ . The rectangle represents the  $\sigma \in [3, 10]$  fb indicative region accommodated by the ATLAS and CMS data. The solid red line is the ATLAS 13 TeV exclusion limit. Uncertainties reflect error associated with the parton distribution functions.

only difference is that the excited states will have a slightly larger mass (which we will estimate in a moment) due to the change in the binding energy. This detail could be important as it can effectively enlarge the observed width. Annihilation of excited states with non-zero orbital angular momentum could in principle also be important, however these are suppressed as the radial wavefunction vanishes at the origin:  $R(0) = 0$  for  $l \geq 1$ . They are expected to de-excite predominately to  $l = 0$  states rather than annihilate [99]. Nevertheless, for sufficiently large  $\alpha_N$  the  $l = 1$  annihilations:  $\Pi \rightarrow \mu^+ \mu^-$  and  $\Pi \rightarrow e^+ e^-$  could potentially be observable.

The  $l = 0$  excited states can be characterized by the quantum number  $n$  with binding energies:

$$\frac{E_n}{M_\Pi} = -\frac{1}{8n^2} \left[ \frac{4}{3} \bar{\alpha}_s + C_N \bar{\alpha}_N + Q^2 \bar{\alpha} \right]^2. \quad (\text{B.8})$$

The above formula was adapted from known results with quarkonium, *e.g.* [94] (and of course also the hydrogen atom). The coupling constants  $\bar{\alpha}_s$ ,  $\bar{\alpha}_N$  and  $\bar{\alpha}$  are evaluated at a

renormalisation scale corresponding to the mean distance between the particles which is of order the Bohr radius:  $a_0 = 4/[(4\bar{\alpha}_s/3 + C_N\bar{\alpha}_N + Q^2\bar{\alpha})M_\Pi]$ . The bound state, described by the radial quantum number  $n$  has mass given by  $M_\Pi(n) = 2M_\chi + E_n$ . Considering as an example  $N = 2$  and  $\bar{\alpha}_N = \bar{\alpha}_s = 0.15$ ,  $\bar{\alpha} = 1/137$  we find the mass difference between the  $n = 1$  and  $n = 2$  states to be  $\Delta M = (E_1 - E_2) \approx 0.01M_\Pi$ . Larger mass splittings will be possible<sup>3</sup> if  $\bar{\alpha}_N > \bar{\alpha}_s$ , although it has been shown in the context of fermionic quirk models that the phenomenology is substantially altered in this regime [95]. In particular, the hueballs can become so heavy that the decays of the bound state into hueballs is kinematically forbidden.

In the above calculation of the bound state production cross section, we considered only the *indirect* production following pair production of  $\chi^\dagger\chi$  above threshold. The bound state can also be produced directly:  $gg \rightarrow \Pi$ , where  $\sqrt{s_{gg}} \approx M_\Pi$ . The cross section of the ground state direct resonance production is

$$\sigma(pp \rightarrow \Pi)_{\text{DR}} \approx \frac{C_{gg}K_{gg}\Gamma(\Pi \rightarrow gg)}{sM_\Pi}, \quad (\text{B.9})$$

where  $C_{gg}$  is the appropriate parton luminosity coefficient and  $K_{gg}$  is the gluon NLO QCD K-factor. For  $\sqrt{s} = 13$  TeV we take  $C_{gg} \approx 2137$  [93] and  $K_{gg} = 1.6$  [115]. The partial width  $\Gamma(\Pi \rightarrow gg)$  of the  $n = 1, l = 0$  ground state is given by

$$\Gamma(\Pi \rightarrow gg) = \frac{4}{3}M_\Pi N\alpha_s^2 \frac{|R(0)|^2}{M_\Pi^3}, \quad (\text{B.10})$$

where the radial wavefunction at the origin for the ground state is:

$$\frac{|R(0)|^2}{M_\Pi^3} = \frac{1}{16} \left[ \frac{4}{3}\bar{\alpha}_s + C_N\bar{\alpha}_N + Q^2\bar{\alpha} \right]^3. \quad (\text{B.11})$$

Considering again the example of  $N = 2$  and  $\bar{\alpha}_N = \bar{\alpha}_s = 0.15$ ,  $\bar{\alpha} = 1/137$  we find

$$\sigma(pp \rightarrow \Pi)_{\text{DR}} \approx 0.40 \text{ pb} \quad \text{at } 13 \text{ TeV}. \quad (\text{B.12})$$

Evidently, the direct resonance production cross section is indeed expected to be sub-

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<sup>3</sup>Additional possibilities arise if  $\chi$  transforms non-trivially under  $\text{SU}(2)_L$ , *i.e.* forming a representation  $N_L$ . The mass degeneracy of the multiplet will be broken at tree-level by Higgs potential terms along with electroweak radiative corrections. The net effect is that the predicted width of the  $pp \rightarrow \gamma\gamma$  bump can be effectively larger as there are  $N_L$  distinct bound states,  $\Pi^i$ , (of differing masses) which can each contribute to the decay width. Although each state is expected to have a narrow width, when smeared by the detector resolution the effect can potentially be a broad feature.

dominant, around 8% that of the indirect production cross section (Eq. B.5)<sup>4</sup>.

We now comment on the regime where  $\Lambda_N$  is smaller than  $\Lambda_{\text{QCD}}$ . In fact, if the  $\text{SU}(N)$  confining scale is only a little smaller than  $\Lambda_{\text{QCD}}$  then a light quark pair can form out of the vacuum, leading to a bound state of two QCD color singlet states:  $\chi\bar{q}$  and  $\chi^\dagger q$ . These color singlet states would themselves be bound together by  $\text{SU}(N)$  gauge interactions to form the  $\text{SU}(N)$  singlet bound state. Since only  $\text{SU}(N)$  interactions bind the two composite states ( $\chi\bar{q}$  and  $\chi^\dagger q$ ), it follows that  $\frac{4}{3}\bar{\alpha}_s + C_N\bar{\alpha}_N + Q^2\bar{\alpha} \rightarrow C_N\bar{\alpha}_N + (Q - Q_q)^2\bar{\alpha}$  in eqs. B.8 and B.11. Therefore if the confinement scale of  $\text{SU}(N)$  is smaller than that of QCD then the direct production rate becomes completely negligible relative to the indirect production mechanism. The rate of  $\Pi$  production is the same as that found earlier in Eq. B.5, but the branching ratio to two photons is modified:

$$\text{Br}(\Pi \rightarrow \gamma\gamma) \simeq \frac{3NQ^4\alpha^2}{\frac{7}{3}N\alpha_s^2 + \frac{3}{2}C_N\alpha_N^2 + 3NQ^4\alpha^2}, \quad (\text{B.13})$$

where, as before, we have neglected the small contribution of  $\Pi \rightarrow Z\gamma/ZZ$  to the total width, and also the contribution from  $\Pi \rightarrow hh$ . In this regime somewhat larger values of  $Q$  can be accommodated, such as  $Q = 5/6$  for  $N = 2$ <sup>5</sup>.

Notice that in the  $\Lambda_N < \Lambda_{\text{QCD}}$  regime the size of the mass splittings between the excited states becomes small as  $\frac{4}{3}\bar{\alpha}_s + C_N\bar{\alpha}_N + Q^2\bar{\alpha} \rightarrow C_N\bar{\alpha}_N + (Q - Q_q)^2\bar{\alpha}$  in Eq. B.8. We therefore expect no effective width enhancement due to the excited state decays at the LHC in the small  $\Lambda_N$  regime. Of course a larger effective width is still possible if there are several nearly degenerate scalar quirk states, which, as briefly mentioned earlier, can arise if  $\chi$  transforms nontrivially under  $\text{SU}(2)_L$ .

## Other signatures

While the two photon decay channel of the bound state should be the most important signature, the dominant decay is expected to be via  $\Pi \rightarrow gg$  and  $\Pi \rightarrow \mathcal{H}\mathcal{H}$ . The former process is expected to lead to dijet production while the latter will be an invisible decay.

<sup>4</sup>If  $\bar{\alpha}_N$  is sufficiently large, one can potentially have direct resonance production comparable or even dominating indirect production (such a scenario has been contemplated recently in [96, 97]). Naturally at such large  $\bar{\alpha}_N$  the perturbative calculations become unreliable, and one would have to resort to non-perturbative techniques such as lattice computations.

<sup>5</sup>Although it is perhaps too early to speculate on the possible role of  $\chi$  in a more elaborate framework, we nevertheless remark here that particles fitting its description are required for spontaneous symmetry breaking of extended Pati–Salam type unified theories [116].



The dijet cross section is easily estimated:

$$\sigma(pp \rightarrow jj) \approx \begin{cases} 2.6N \times \text{Br}(\Pi \rightarrow gg) \text{ pb} & \text{at 13 TeV} \\ 0.5N \times \text{Br}(\Pi \rightarrow gg) \text{ pb} & \text{at 8 TeV} \end{cases}. \quad (\text{B.14})$$

The limit from 8 TeV data is  $\sigma(pp \rightarrow jj) \lesssim 2.5 \text{ pb}$  [117, 118]. If gluons dominate the  $\Pi$  decays (i.e.  $\text{Br}(\Pi \rightarrow gg) \approx 1$ ) then this experimental limit is satisfied for  $N \leq 5$ . For sufficiently large  $\alpha_N$  the invisible decay can be enhanced, thereby reducing  $\text{Br}(\Pi \rightarrow gg)$ . In this circumstance the bound on  $N$  from dijet searches would weaken.

The invisible decays  $\Pi \rightarrow \mathcal{H}\mathcal{H}$  are not expected to lead to an observable signal at leading order for much of the parameter space of interest<sup>6</sup>. However, the bremsstrahlung of a hard gluon from the initial state:  $pp \rightarrow \Pi g \rightarrow \mathcal{H}\mathcal{H} g$  can lead to a jet plus missing transverse energy signature. Current data are not expected to give stringent limits from such decay channels, however this signature could become important when a larger data sample is collected. Note though that the rate will become negligible in the limit that  $\alpha_N$  becomes small. Also, in the small  $\Lambda_N$  regime, where the bound state is formed from  $\chi\bar{q}$  and  $\chi^\dagger q$ , the two-body decay  $\Pi \rightarrow g\gamma$  (jet + photon) will also arise as in this case the scalar quirk pair is not necessarily in the color singlet configuration. The decay rate at leading order is substantial:

$$\frac{\Gamma(\Pi \rightarrow j\gamma)}{\Gamma(\Pi \rightarrow \gamma\gamma)} = \frac{8\alpha_s}{3\alpha Q^2}. \quad (\text{B.15})$$

Nevertheless, we estimate that this is still consistent with current data [121], but would be expected to become important when a larger data sample is collected.

Another important signature of the model will be the  $pp \rightarrow \Pi \rightarrow Z\gamma$  and  $pp \rightarrow \Pi \rightarrow ZZ$  processes. The rates of these decays, relative to  $\Pi \rightarrow \gamma\gamma$ , are estimated to be:

$$\begin{aligned} \frac{\Gamma(\Pi \rightarrow Z\gamma)}{\Gamma(\Pi \rightarrow \gamma\gamma)} &= 2 \tan^2 \theta_W, \\ \frac{\Gamma(\Pi \rightarrow ZZ)}{\Gamma(\Pi \rightarrow \gamma\gamma)} &= \tan^4 \theta_W. \end{aligned} \quad (\text{B.16})$$

If  $\chi$  transforms nontrivially under  $SU(2)_L$  then deviations from these predicted rates arise along with the tree-level decay  $\Pi \rightarrow W^+W^-$ .

<sup>6</sup>Scalar quirk loops can mediate hueball decays into gluons and other SM bosons [99, 119, 120]. The decay rate is uncertain, depending on the non-perturbative hueball dynamics. However, if the hueballs are able to decay within the detector then they can lead to observable signatures including displaced vertices. This represents another possible collider signature of the model.

## Conclusions

We have considered a charged scalar particle  $\chi$  of mass around 375 GeV charged under both  $SU(3)_c$  and a new confining gauge interaction (assigned to be  $SU(N)$  for definiteness). These interactions confine  $\chi^\dagger\chi$  into non-relativistic bound states whose decays into photons can explain the 750 GeV diphoton excess observed at the LHC. Taking the new confining group to be  $SU(2)$ , we found that the diphoton excess required  $\chi$  to have electric charge approximately  $Q \sim [\frac{1}{2}, 1]$ . An important feature of our model is that the exotic particle  $\chi$  has a mass much greater than the  $SU(N)$ -confinement scale  $\Lambda_N$ . In the absence of light  $SU(N)$ -charged matter fields this makes the dynamics of this new interaction qualitatively different to that of QCD: pair production of the scalars and the subsequent formation of the bound state dominates over direct bound state resonance production (at least in the perturbative regime where  $\Lambda_N \lesssim \Lambda_{\text{QCD}}$ ). Since  $\chi$  is a Lorentz scalar, decays of  $\chi^\dagger\chi$  bound states to lepton pairs are naturally suppressed, and thus constraints from dilepton searches at the LHC can be ameliorated. This explanation is quite weakly constrained by current searches and data from the forthcoming run at the LHC will be able to probe our scenario more fully. In particular, dijet, mono-jet, di-Higgs and jet + photon searches may be the most promising discovery channels.

## Acknowledgements

This work was supported by the Australian Research Council. Feynman diagrams were generated using the TikZ-Feynman package for L<sup>A</sup>T<sub>E</sub>X [122].





# Definition of Symbols and Acronyms

## D

**DFT** density functional theory

## L

**lipsum** Lorem Ipsum, a special type of fudge

**dolor** No idea why

**ibit** Sounds right, doesn't it?

## P

$\pi$  ( $\pi$ ) Greek letter pi,  $\Pi$  does this work?

## R

**radial distribution function** ( $g(r)$ )

**RDF** radial distribution function

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