Thesis

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4 CONTENTS

Opening Comments

Introduction

Literature Review

Data Collection and Summary Statistics

Data was downloaded from www.ishares.com for EUSA (iShares MSCI USA Equal Weighted ETF) and USMV (iShares Edge MSCI Min Vol USA ETF), from Oct 31, 2011 to December 31, 2016. iShares are a type of ETF managed by BlackRock, and www.ishares.com contains the month end data for the two ETFs of interest in this dissertation. The data sets included information for the constituents of each ETF of the time, and some other characteristics of them, including: ticker, company name, asset class, weight of the stock relative to the entire index, price per share, number of shares, market value of the position, notional value of the position, sector, sedol number, isin number, exchange that the stock is listed on, and the month end date for the data. An R function was created for both ETFs that would combine each month end data set into one aggregated one. Thus, each month end data set was individually downloaded, then aggregated to create the data sets "usa" and "minvol". These were stored in the data-raw folder, for safekeeping.

However, after having a quick overview of the data, there were many issues with it that needed to be fixed before the analysis could begin. First, looking at unique exchanges of the data on R, it was seen that there were many foreign exchanges like the Swiss Exchange and the Mexican Exchange, which did not make sense, given the ETF constituents are supposed to be listed on US-based exchanges. One clear discrepancy between the company name and ticker was "AAPL*" (yes, the ticker had an asterisk) which was listed on the Mexican Exchange, instead of being listed as AAPL on the NYSE. This would cause issues for reading the data later on, because AAPL with the asterisk was not read in as "AAPL" due to the asterisk. Other tickers were very easy to notice as incorrect because they included numbers. Seeing as this is a US index with US stocks, this was a clear issue. One example was the company Aflac, Inc. which was recorded by the ticker 8686. This corresponded to Aflac, Inc. on the Tokyo exchange, but when checking the recorded price of the stock for corresponding dates, it matched up with the Aflac, Inc. stock in the US, with ticker AFL. Other tickers were read in correctly, but corresponded to non-US exchanges. One example was BAC, Bank of America, which is listed on the NYSE. Though the price for each date corresponded to the price of BAC in the NYSE, it was listed on the Swiss Exchange. BAC did not correspond to Bank of America on the Swiss Exchange either, which made me question how these companies were being read in.

Instead of looking through 800+ tickers at once, I created a subset of the usa data that looked at all of the companies not listed on the NYSE or NASDAQ exchanges. This included stocks listed on the Boerse Berlin, Bolsa Mexicana De Valores, and London Stock Exchange. There were 16 exchanges that were not the NYSE or NASDAQ, which seemed problematic. There were 74 tickers within these, that I went through and looked at by hand. These included many tickers with numbers and asterisks. In the end, I was able to figure out 67 of these tickers pretty definitively. Some of these tickers were recorded properly, just with the wrong exchange listed (i.e. F, Ford, listed on the Swiss Exchange). Thus, these tickers were kept as is. Some other tickers were harder to find because of M&A activity causing the company to no longer be traded. One example was LinkedIn, which was incorrectly listed as LKI. Before it was acquired by Microsoft, the ticker

was LNKD. Thus, the ticker was changed to show this, as we will need to get old data for companies based off their tickers at the time. Other tickers were for US companies, and included their tickers for overseas exchanges. One example was Intel Corp, which was listed as INCO. INCO is the correct ticker for Intel on the Amsterdam exchange, but not on the NYSE, which lists it as INTC. The general methodology to make sure a change in ticker was appropriate was to check the price of the stock at a specific date, in the usa data set, and then comparing it to the new ticker I was going to assign it. If the price matched, the change was made. If the price did not match up and was very different, then I looked to see if a stock-split might be the cause of this. If there was no evidence of a stock-split, then the stock was highlighted and left alone for further analysis. An entire list of what was changed and what was not is shown in the appendix. In the end, the ticker named "1015736" and Orchard Supply Hardware Stores were removed from the data set. This accounted for less than 0.2% of the data from one month-end date. I also removed cash assets as well by removing values if the sector was cash, since this is not important for our purposes.

Thus, after removing a couple tickers and cash, I wanted to check how accurate the data set was. This was accomplished by comparing the weighted returns of the constructed index we have (looking at each constituent's monthly return, multiplied by its weight), and comparing it to the ETF return. Because the iShares price data did not reflect stock splits, it was very problematic in some returns. For example, when AAPL split its stock in 2014, from 4-30-2014 to 5-30-2014, the price went from \$633.00 to \$92.93 per share. This would have been improperly recorded as an 85% decrease in the price of the stock, when in reality this was due to a stock split. Since WRDS generally gives price information adjusted for stock splits and dividends, those prices were used instead. However, this was not always the case, and for some instances, these issues were changed manually. This was done by sorting the highest deltas in the data set, with delta corresponding to the monthly change in stock price. I investigated stocks with deltas greater than 0.3 in magnitude for the given month to see if it needed to be adjusted. This same procedure was used for the minvol data set, as it is a subset of the usa data.

Shown below are some of the summary statistics of the usa and min vol data

```
devtools::install_github("johngil/gilheany.thesis")

## Skipping install of 'gilheany.thesis' from a github remote, the SHA1 (060f4bb9) has not changed sinc

## Use `force = TRUE` to force installation

library(mscidata)
library(ggplot2)
data(usa)
data(minvol)
```

Summary statistics of EUSA Data
head(usa)

Load Packages and View the Data

```
##
                  Name Asset.Class Weight.... Price Shares Market.Value
     X Ticker
## 1 1
         <NA> 1015736
                               <NA>
                                        0.1950 26.63
                                                       10991
                                                                 292690000
## 2 2
                 3M CO
                                        0.4706 79.02
                                                         160
                                                                  12643000
          MMM
                            Equity
## 3 3
                 3M CO
          MMM
                            Equity
                                        0.4659 81.04
                                                         154
                                                                  12480000
                 3M CO
## 4 4
                                        0.4626 81.73
                                                        6872
          MMM
                            Equity
                                                                 561649000
## 5 5
          MMM
                 3M CO
                            Equity
                                        0.4709 86.71
                                                        7211
                                                                 625266000
                                        0.4556 87.60
## 6 6
          MMM
                 3M CO
                            Equity
                                                        6672
                                                                 584467000
##
     Notional.Value
                          Sector
                                    SEDOL
                                                   ISIN
## 1
                  NA Industrials
                                                   <NA>
                                     <NA>
## 2
                  NA Industrials 2595708 US88579Y1010
## 3
                  NA Industrials 2595708 US88579Y1010
                  NA Industrials 2595708 US88579Y1010
## 4
## 5
                  NA Industrials 2595708 US88579Y1010
                  NA Industrials 2595708 US88579Y1010
## 6
##
                          Exchange
                                          Date
```

```
## 1
                              <NA> 2012-12-31
## 2 New York Stock Exchange Inc. 2011-10-31
## 3 New York Stock Exchange Inc. 2011-11-30
## 4 New York Stock Exchange Inc. 2011-12-30
## 5 New York Stock Exchange Inc. 2012-01-31
## 6 New York Stock Exchange Inc. 2012-02-29
tail(usa)
##
             X Ticker
                                     Name Asset.Class Weight.... Price Shares
## 39325 39325
                  ZTS ZOETIS INC CLASS A
                                               Equity
                                                          0.1649 51.10
                                                                          2377
## 39326 39326
                  ZTS ZOETIS INC CLASS A
                                               Equity
                                                           0.1695 52.01
                                                                          2397
## 39327 39327
                  ZTS ZOETIS INC CLASS A
                                               Equity
                                                           0.1600 47.80
                                                                          2472
  39328 39328
                  ZTS ZOETIS INC CLASS A
                                               Equity
                                                           0.1608 50.38
                                                                          2847
                  ZTS ZOETIS INC CLASS A
## 39329 39329
                                               Equity
                                                           0.1706 53.53
                                                                          3015
                  ZTS ZOETIS INC CLASS A
  39330 39330
                                               Equity
                                                           0.1690 53.93
                                                                          3015
##
         Market. Value Notional. Value
                                                                   ISIN
                                           Sector
                                                    SEDOL
## 39325
            121465000
                             121464.7 Health Care B95WG16 US98978V1035
## 39326
            124668000
                             124668.0 Health Care B95WG16 US98978V1035
## 39327
            118162000
                             118161.6 Health Care B95WG16 US98978V1035
## 39328
                             143431.9 Health Care B95WG16 US98978V1035
            143432000
## 39329
            161393000
                             161393.0 Health Care B95WG16 US98978V1035
## 39330
                             162599.0 Health Care B95WG16 US98978V1035
            162599000
                             Exchange
                                             Date
## 39325 New York Stock Exchange Inc. 2016-08-31
## 39326 New York Stock Exchange Inc. 2016-09-30
## 39327 New York Stock Exchange Inc. 2016-10-31
## 39328 New York Stock Exchange Inc. 2016-11-30
## 39329 New York Stock Exchange Inc. 2016-12-30
## 39330 New York Stock Exchange Inc. 2017-01-05
summary(usa)
##
          X
                        Ticker
                                                           Name
                    CB
                               102
                                     3M CO
    1st Qu.: 9833
                    NLSN
                                65
                                     ABBOTT LABORATORIES
                                                                 64
    Median :19666
                    Α
                            :
                                64
                                     ACCENTURE PLC
                                                                 64
```

```
##
    Mean
                                64
                                     ACTIVISION BLIZZARD INC:
           :19666
                    AAP
                                     ADOBE SYSTEM INC
    3rd Qu.:29498
                    ABC
                                64
           :39330
                     (Other):38939
                                     ADVANCE AUTO PARTS INC :
                                                                  64
##
    Max.
##
                    NA's
                                32
                                      (Other)
                                                              :38946
##
          Asset.Class
                            Weight....
                                                 Price
                                                                   Shares
                :
                     66
                                 :-0.3905
                                             Min.
                                                   : 0.56
                                                               Min.
                                                                      :-174670
    Cash
                          Min.
                          1st Qu.: 0.0542
                                             1st Qu.: 35.08
##
    Equity
                :39240
                                                               1st Qu.:
                                                                           805
##
    Money Market:
                     23
                          Median : 0.1236
                                             Median : 55.21
                                                               Median:
                                                                          1563
##
    NA's
                      1
                          Mean
                                : 0.1626
                                             Mean
                                                    : 72.05
                                                               Mean
                                                                          3566
##
                          3rd Qu.: 0.1638
                                             3rd Qu.: 83.77
                                                                          3199
                                                               3rd Qu.:
##
                          Max.
                                : 4.6773
                                             Max.
                                                    :953.00
                                                               Max.
                                                                      : 873628
##
                                             NA's
                                                    :47
##
     Market.Value
                         Notional. Value
                                                                Sector
                                :-174670
##
   Min.
           :0.000e+00
                         Min.
                                            Financials
                                                                   :6909
    1st Qu.:5.321e+07
                         1st Qu.: 55505
                                            Consumer Discretionary:6703
##
    Median :8.418e+07
                         Median : 75582
                                            Information Technology:5590
           :1.607e+08
                         Mean : 91931
    Mean
                                            Industrials
                                                                   :4765
    3rd Qu.:1.435e+08
                         3rd Qu.: 118997
                                            Health Care
                                                                   :4138
```

```
:6.804e+09
                       Max.
                              :2106050
                                         Energy
                                                              :3253
   NA's :7
##
                       NA's
                              :22930
                                         (Other)
                                                              :7972
##
       SEDOL
                             ISIN
   2000019: 64 AN8068571086:
##
                                   64
   2002305: 64 BMG0450A1053:
##
##
   2005973: 64 BMG0692U1099:
   2008154:
              64 BMG169621056:
              64 BMG3223R1088:
   2011602:
##
                                   64
   (Other):38920 (Other)
##
                              :38952
##
   NA's : 90 NA's
                                   58
##
                                                Exchange
##
  New York Stock Exchange Inc.
                                                    :27970
                                                    : 9405
  NASDAQ
## Boerse Berlin
                                                       427
## Deutsche Boerse Ag
                                                       395
   Bolsa Mexicana De Valores (Mexican Stock Exchange):
                                                       266
##
                                                       661
   (Other)
##
  NA's
                                                       206
##
           Date
##
   2015-06-30: 641
## 2015-08-31: 641
## 2015-05-29: 639
## 2015-09-30: 639
   2015-10-30: 639
## 2015-11-30: 638
## (Other)
             :35493
## Summary statistics of USMV Data
head(minvol)
    X Ticker Name Asset.Class Weight.... Price Shares Market.Value
## 1 1
                        Equity
                                   0.7488 79.02
         MMM 3M CO
                                                   244
                                                              19281
## 2 2
         MMM 3M CO
                        Equity
                                   0.7592 81.04
                                                    244
                                                              19774
## 3 3
         MMM 3M CO
                        Equity
                                   0.2892 109.35 94494
                                                           10332919
                        Equity
## 4 4
         MMM 3M CO
                                   0.3000 117.43 59406
                                                           6976047
## 5 5
         MMM 3M CO
                        Equity
                                   0.2999 113.58 57686
                                                           6551976
         MMM 3M CO
                                   0.3095 119.41 52611
## 6 6
                        Equity
                                                            6282280
                        Sector
    Notional.Value
                                 SEDOL
                                               TSTN
## 1
                NA Industrials 2595708 US88579Y1010
## 2
                NA Industrials 2595708 US88579Y1010
                NA Industrials 2595708 US88579Y1010
                NA Industrials 2595708 US88579Y1010
## 4
## 5
                NA Industrials 2595708 US88579Y1010
## 6
                NA Industrials 2595708 US88579Y1010
                        Exchange
                                      Date
## 1 New York Stock Exchange Inc. 2011-10-31
## 2 New York Stock Exchange Inc. 2011-11-30
## 3 New York Stock Exchange Inc. 2013-06-28
## 4 New York Stock Exchange Inc. 2013-07-31
## 5 New York Stock Exchange Inc. 2013-08-30
## 6 New York Stock Exchange Inc. 2013-09-30
tail(minvol)
                                         Name Asset.Class Weight.... Price
          X Ticker
## 9498 9498 ZBH ZIMMER BIOMET HOLDINGS INC
                                                  Equity 0.1391 104.95
```

```
## 9499 9499
                ZTS
                             ZOETIS INC CLASS A
                                                      Equity
                                                                 0.1002
                                                                          30.89
## 9500 9500
                ZTS
                             ZOETIS INC CLASS A
                                                      Equity
                                                                          29.81
                                                                 0.0962
## 9501 9501
                ZTS
                             ZOETIS INC CLASS A
                                                      Equity
                                                                 0.0972
                                                                          29.15
## 9502 9502
                                                                 0.1021
                ZTS
                             ZOETIS INC CLASS A
                                                      Equity
                                                                          31.12
  9503 9503
                ZTS
                             ZOETIS INC CLASS A
                                                      Equity
                                                                  0.0992
                                                                          31.66
        Shares Market. Value Notional. Value
                                                  Sector
                                                                          ISIN
##
                                                           SEDOL
## 9498 163220
                                   17129939 Health Care 2783815 US98956P1021
                   17129939
## 9499 115890
                                         NA Health Care B95WG16 US98978V1035
                    3579836
## 9500 75069
                    2237807
                                         NA Health Care B95WG16 US98978V1035
## 9501
                                         NA Health Care B95WG16 US98978V1035
        72889
                    2124714
## 9502
         66567
                    2071565
                                         NA Health Care B95WG16 US98978V1035
                                         NA Health Care B95WG16 US98978V1035
## 9503
         66458
                    2104060
                                            Date
                             Exchange
## 9498 New York Stock Exchange Inc. 2017-01-05
## 9499 New York Stock Exchange Inc. 2013-06-28
## 9500 New York Stock Exchange Inc. 2013-07-31
## 9501 New York Stock Exchange Inc. 2013-08-30
## 9502 New York Stock Exchange Inc. 2013-09-30
## 9503 New York Stock Exchange Inc. 2013-10-31
summary(minvol)
##
          X
                        Ticker
                                                               Name
##
                   CB
                           :
                              82
                                   ABBOTT LABORATORIES
                                                                 :
                                                                    64
    Min.
               1
                                   ALTRIA GROUP INC
##
    1st Qu.:2376
                   ABT
                              64
                                                                    64
    Median: 4752
                   ACGL
                              64
                                   ARCH CAPITAL GROUP LTD
                                                                    64
##
                   ADP
                              64
                                   AT&T INC
    Mean
           :4752
                                                                    64
##
    3rd Qu.:7128
                   AMT
                           •
                              64
                                   AUTOMATIC DATA PROCESSING INC:
                                                                    64
                                   AUTOZONE INC
##
    Max.
           :9503
                    (Other):9134
                                                                    64
##
                                   (Other)
                                                                  :9119
                   NA's
                           : 31
##
          Asset.Class
                           Weight....
                                               Price
##
                   66
                                :-0.3451
    Cash
                :
                         Min.
                                           Min. : 0.56
    Equity
                :9413
                         1st Qu.: 0.2697
                                           1st Qu.: 48.35
##
##
    Money Market:
                   24
                         Median: 0.5922
                                           Median: 71.56
##
                         Mean
                                : 0.6730
                                           Mean
                                                   : 92.93
##
                         3rd Qu.: 1.0116
                                           3rd Qu.:100.98
##
                         Max.
                                : 2.8287
                                           Max.
                                                   :953.00
                                           NA's
                                                   :6
##
        Shares
                         Market.Value
                                             Notional. Value
                                             Min.
                                                     :-20891956
##
    Min.
          :-20891956
                        Min.
                               :
                                      1138
                         1st Qu.: 5184586
##
    1st Qu.:
                62755
                                             1st Qu.: 18801242
##
    Median :
               240777
                         Median: 18738857
                                             Median: 39482427
```

590304 3rd Qu.: 40420826 3rd Qu.: 71639502 ## 3rd Qu.: :240885300 ## Max. : 38506545 Max. Max. :240885300 ## NA's NA's :5064 ## Sector SEDOL ISIN ## Health Care :1664 2002305: 64 BMG0450A1053: ## Financials :1569 2005973: 64 BMG3223R1088: 64 Information Technology:1510 2065308: BMG7496G1033: US00206R1023: 64 ## Consumer Staples :1246 2065955: 64 ## Consumer Discretionary: 1071 2073390: US0028241000: 64 64 ## Utilities : 628 (Other):9093 (Other) :9126 ## (Other) :1815 NA's NA's ## Date Exchange

: 31303694

Mean

: 52633035

##

Mean

:

525786

Mean

##

date

```
New York Stock Exchange Inc.:7158
                                         2016-11-30: 187
##
  NASDAQ
                                         2016-12-30: 187
##
                                 :1926
  Deutsche Boerse Ag
                                         2017-01-05: 186
##
                                   58
## Spot Regulated Market - Bvb :
                                         2016-05-31: 180
                                   58
##
   Boerse Berlin
                                   32
                                         2016-06-30: 179
   (Other)
                                         2016-07-29: 179
##
                                 : 164
##
   NA's
                                 : 107
                                         (Other)
                                                   :8405
```

weighted return

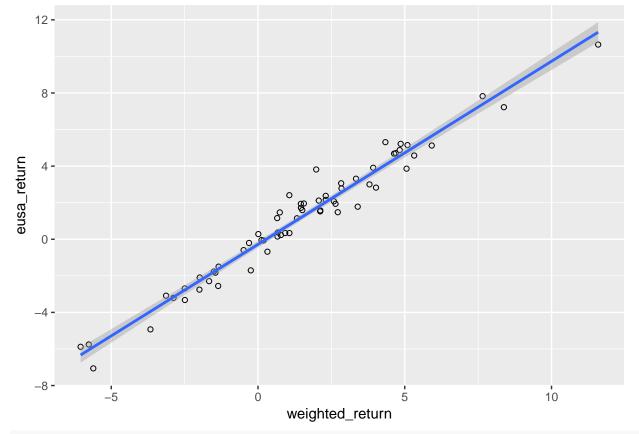
Before taking the data as given, some checks were done to ensure the data was accruate. First, we wanted to check how our weighted returns compared to the ETF returns. Though we did not expect it to be perfectly correlated, we wanted to aim for a 98% or higher correlation between the weighted returns we calculated, and the ETF returns, on a monthly basis. The results for the usa data are shown below.

```
# USA data
data(returns1)
summary(returns1)
```

```
##
   Min.
           :2011-10-31
                                                  :-7.061848
                         Min.
                               :-6.0439
                                           Min.
##
   1st Qu.:2013-02-14
                         1st Qu.:-0.3983
                                           1st Qu.:-1.088819
##
  Median :2014-05-30
                         Median : 1.4592
                                           Median : 1.524721
  Mean
           :2014-05-30
                         Mean
                               : 1.3886
                                                  : 1.111701
                                           Mean
##
   3rd Qu.:2015-09-15
                         3rd Qu.: 3.3678
                                           3rd Qu.: 3.031121
           :2016-12-30
                                :11.5892
                                                  :10.647011
  Max.
                         Max.
                                           Max.
```

ggplot(returns1, aes(x=weighted_return, y=eusa_return)) + geom_point(shape=1) + geom_smooth(method=lm)

eusa return.Delt.1.arithmetic



cor(returns1\$eusa_return, returns1\$weighted_return)

Table 4.1: USA Returns

date	weighted_return	eusa return
2011-10-31	11.5892350	10.64701065
2011-11-30	-0.2456645	-1.70244264
2011-12-30	1.0671034	2.40963855
2012-01-31	5.0610248	3.86029412
2012-02-29	4.3400696	5.30973451
2012-03-30	3.3970199	1.78151261
2012-04-30	-0.4906636	-0.59445178
2012-05-31	-6.0439231	-5.88039867
2012-06-29	4.0198762	2.82386163
2012-07-31	1.5618633	1.95674562
2012-08-31	2.3092650	2.15488215
2012-09-28	2.5853910	2.07646671
2012-10-31	-1.6654955	-2.29254117
2012-11-30	0.6531763	1.15664243
2012-12-31	0.7794097	0.22868344
2013-01-31	5.0931233	5.14993481
2013-02-28	1.3265195	1.14693118
2013-03-28	3.7977193	3.00030647
2013-04-30	2.0699705	2.11550478
2013-05-31	1.9830989	3.81701632
2013-06-28	-1.3567937	-2.55402750
2013-07-31	5.3210605	4.57949309
2013-08-30	-2.8771461	-3.20572845
2013-09-30	3.3385738	3.31189894
2013-10-31	4.6359683	4.68190581
2013-11-29	2.8436501	2.77821626
2013-12-31	2.7175078	1.47826755
2014-01-31	-3.1322783	-3.08625626
2014-02-28	4.6903592	4.71108798
2014-03-31	0.6637837	0.14914243
2014-04-30	0.6756760	0.37230082
2014-05-30	2.3076650	2.37363996
2014-06-30	1.5081588	1.59444830
2014-07-31	-1.3446626	-1.49738469
2014-08-29	3.9244135	3.90970838
2014-09-30	-1.5046634	-1.76538908
2014-10-31	2.6410836	1.93899267
2014-11-28	2.8336728	3.06193459
2014-12-31	-0.3058795	-0.20256583
2015-01-30	-2.4954545	-2.68831755
2015-02-27	5.9196423	5.12654121
2015-03-31	-1.4516707	-1.83002646
2015-04-30	0.9272040	0.34066998
2015-05-29	1.4618722	1.71972356
2015-06-30	-1.9847732	-2.09240924
2015-07-31	2.1216832	1.57801299
2015-08-31	-5.7662469	-5.75471448
2015-09-30	-3.6642971	-4.92957746
2015-10-30	7.6518942	7.82716049
2015-11-30	0.1175917	-0.04579803
2015-12-31	-2.4910425	-3.32187858
2016-01-29	-5.6115203	-7.06184834
2016-02-29	0.7419356	1.46813225
2016-03-31	8.3766775	7.22289092
2016-04-29	2.1189998	1.52472106

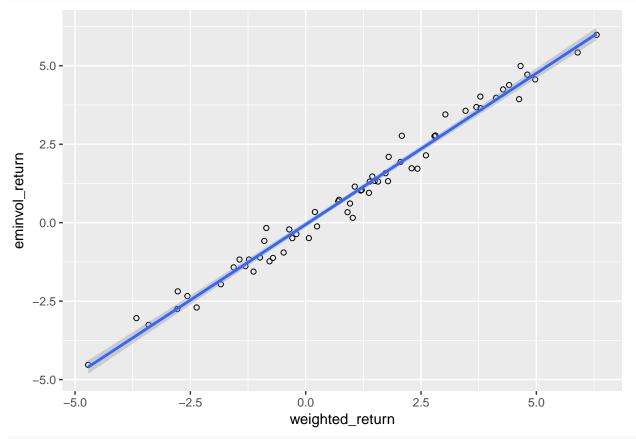
```
## [,1]
## Delt.1.arithmetic 0.9805503
```

As we can see, the returns seem pretty consistent and have a correlation greater than 0.98.

Shown below is the data for the min vol index.

```
# USA data
data(returns2)
summary(returns2)
```

```
##
                         weighted_return
                                           eminvol_return.Delt.1.arithmetic
         date
##
   Min.
           :2011-11-30
                               :-4.7156
                                                  :-4.530281
                         Min.
                                           1st Qu.:-1.070307
##
   1st Qu.:2013-03-07
                         1st Qu.:-0.8364
##
  Median :2014-06-14
                         Median : 1.1278
                                           Median: 0.987327
                                                 : 0.927892
##
   Mean
           :2014-06-15
                         Mean
                                : 1.0234
                                           Mean
   3rd Qu.:2015-09-22
                         3rd Qu.: 2.7451
                                           3rd Qu.: 2.765673
##
   Max.
           :2016-12-30
                                : 6.3064
                                           Max.
                                                  : 5.986360
##
                         Max.
ggplot(returns2, aes(x=weighted_return, y=eminvol_return)) +
    geom_point(shape=1) + geom_smooth(method=lm)
```



cor(returns2\$eminvol_return, returns2\$weighted_return)

```
## [,1]
## Delt.1.arithmetic 0.9906848
```

Table 4.2: Min Vol Returns

	date	weighted_return	eminvol return
2	2011-11-30	1.0207211	0.1540832
3	2011-12-30	2.0832643	2.7692308
$\frac{3}{4}$	2012-01-31	1.5682330	1.3098802
5	2012-02-29	1.7985326	2.0982638
$\frac{3}{6}$	2012-02-23	2.6064008	2.1455966
$\frac{0}{7}$	2012-03-30	1.3875986	1.3106160
8	2012-04-30	-2.7737073	-2.1887347
$\frac{\circ}{9}$	2012-05-31	3.0274691	3.4491510
$\frac{9}{10}$	2012-00-29	2.0550335	1.9353902
	2012-07-31	-0.8537533	-0.1694915
$\frac{11}{12}$	2012-08-31	1.3709153	0.9507640
13	2012-10-31	-0.9913378	-1.1099899
14	2012-11-30	0.1997206	0.3401361
15	2012-12-31	-1.1313053	-1.5593220
16	2013-01-31	4.6572484	4.9931129
17	2013-02-28	2.7913166	2.7550016
18	2013-03-28	4.9746988	4.5643154
19	2013-04-30	2.8126037	2.777778
20	2013-05-31	-2.5643787	-2.3379863
21	2013-06-28	-0.4782116	-0.9512572
22	2013-07-31	3.6996474	3.6843721
23	2013-08-30	-3.4070922	-3.2573290
_24	2013-09-30	2.4226946	1.7202326
_25	2013-10-31	4.8035140	4.7183438
_26	2013-11-29	1.7845074	1.3218391
_27	2013-12-31	0.7058349	0.6806580
28	2014-01-31	-3.6699298	-3.0422535
29	2014-02-28	4.4096304	4.3869843
30	2014-03-31	0.9065562	0.3339827
31	2014-04-30	1.4951304	1.3314840
32	2014-05-30	1.0635132	1.1497399
33	2014-06-30	0.7224467	0.7307172
34	2014-07-31	-1.5620464	-1.4239656
35	2014-08-29	4.1272757	3.9792859
36	2014-09-30	-0.7844910	-1.2319790
$\frac{37}{20}$	2014-10-31	4.2794278	4.2462845
38	2014-11-28	3.4656171	3.5641548
39	2014-12-31	0.0684333	-0.4916421
40	2015-01-30	-0.2904233	-0.4940711
41	2015-02-27	3.7922662	3.6494538
42	2015-03-31	-1.4350491	-1.1736527
43	2015-04-30	-0.8969496	-0.5816772
44	2015-05-29	1.1920250	1.0238908
45	2015-06-30	-2.3645382	-2.7027027
46	2015-07-31	3.7854982	4.0178571
47	2015-08-31	-4.7156114	-4.5302814
48	2015-09-30	-0.7096045	-1.1238761
49	2015-10-30	6.3064130	5.9863602
50	2015-11-30	-0.3562819	-0.2144900
51	2015-12-31	0.2454774	-0.1194172
$\frac{52}{52}$	2016-01-29	-1.3065154	-1.3868962
53	2016-02-29	1.2139996	1.0426770
54	2016-03-31	5.8946529	5.4235661
55	2016-04-29	-0.2021128	-0.3642158
56	2016-05-31	1.7304525	1.5764222

Data Analysis

Bibliography