

Thesis

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Chapter 1

Opening Comments

I would like to thank David Kane and Michael Parzen for their contribution and help on my thesis. This would not have been possible without their assistance.

Chapter 2

Introduction

I would like to start by introducing the main index this thesis will be focusing on, USMV. The MSCI Minimum Volatility Index (USMV) is intended to have a lower beta, lower volatility, lower cap bias, and contain more stocks with less risk than its parent index. It is rebalanced twice a year, on the last trading days of May and November. The index typically has around 180 constituents, with an average of 20 new additions and 14 deletions every 6 months when rebalancing occurs. Over the last five years, the number of additions has ranged from 12 to 25, while the deletions have been between 10 and 19. Changes to the index are usually announced nine trading days before they are set to take place.

Using the Barra Open Optimizer, USMV creates a minimum variance portfolio of low risk stocks, as a subset from its parent index, EUSA. Using this estimated security covariance matrix, the MSCI Minimum Volatility Index is the product of the lowest absolute volatility, considering the constraints. Moreover, these additions are simply a relabeling of existing stocks in the parent index, and do not include new additions to the parent index. The low-risk stocks chosen to be in USMV are determined by a set of constraints, like maintaining a certain sector or country weight relative to the parent index.

There are many specific constraints to this index. The first is that an individual stock cannot exceed 1.5% or 20 times the weight of the stock in the parent index. The minimum weight of a security in the index is also capped at 0.05%. USMV also aims to keep the weight of specific countries within a 5% range of the weight in the parent index, or 3 times the weight of the country in the parent index. Sector weights of USMV also cannot deviate more than 5% from the sector weights in the parent index. One way turnover of the index is also maxed at 10%. Thus, taking into account these constraints, the Barra Open Optimizer creates the lowest absolute volatility portfolio possible.

Chapter 3

Literature Review

3.1 High Returns from Low Risk By Pim van Vliet and Jan De Koning

One of the most widely believed tenants of finance is the concept that with more risk comes more reward. However, looking at historical market returns, this does not appear to be the case. Over an 86-year period from 1929, low volatility stocks outperformed high volatility stocks by a factor of 18. If both portfolios started off with the same \$100, the low volatility portfolio end value would be \$395,000, while the high volatility portfolio would be worth just \$21,000. Low risk stocks returned 10.2% annually whereas the high risk stocks returned just 6.4% annually. This difference of 3.8% is striking, and presents an anomaly in the field of finance.

This begs the question of how a portfolio of lower volatility stocks can outperform higher volatility stocks over a long period of time. The primary way this occurs is that the low volatility portfolio loses less during times of financial stress. For example, in 1932 following the Great Depression, it was observed that the high volatility portfolio shrunk from \$100 in value to \$5 in value, while the low volatility portfolio shrunk from \$100 to \$30. Since the low volatility portfolio is able to lose less money, it is able to grow capital more effectively than the high volatility portfolio. In this example, the annualized volatility of the low risk portfolio was 13%, and the annualized volatility of the high risk portfolio was around 2.5 times that, at 36%. In addition to being more risky, the high volatility portfolio was outperformed by 18 times.

Thus, it seems very counterintuitive that fund managers and investors would not only invest in low risk stocks. Part of understanding this comes from interpreting what risk is defined as in the financial community. Risk is not necessarily defined as losing money, as it may be for an individual, but instead underperforming a benchmark. Volatility is also an important concept to understand. Volatility is an important measure of financial risk, as it comes from the price fluctuations of a stock or investment. Volatility is also one of the best indicators of bankruptcy. Taking some risk does pay off, as the relationship between risk and return starts off slightly positive before leveling off and becoming negative. Many researchers focus on short-term periods when analyzing stock returns instead of longer term for a couple of reasons. The first reason many focus on “single period returns”, which in most academic studies is just a one month period, is because this takes away the significance of compounding. The longer the investment period, the more risk one takes in hurting long term returns through compounding. By not fully including the magic “return upon return” effect of compounding, a high-risk portfolio in this book performs more than 6% better per year. For example, if in month a portfolio worth \$100 drops 50% to \$50, then the next month increases 50% to \$75, the investment return is dependent on how one divides the time period. Looking at it on a monthly basis, even though the portfolio lost \$25, the net return would be $-50\% + 50\%$, or 0%. Looking at it on a long term basis, the net return was -25% .

David Blitz, the head of quantitative equity research at Robeco, discusses this different perspective as

somewhat due to the need to benchmark the performance of an investment manager. This is a concept known as “relative” risk. In the examples above, everything has been in respect to absolute risk - that is how much money is being gained or lost due to overall stock movements, with regard to the starting amount of money invested. Volatility, in itself, captures these changes in the price of a stock, and is an absolute risk measurement. Many institutional investors do not look at risk on an absolute level, as a retiree or mom and pop investor may, but instead look at the risk of a portfolio with respect to market or some other widely accepted benchmark. For these investors, the risk is not as much about losing money, rather is more about lagging the market or their peers. Investing is very much a relative game. If a portfolio drops 20% while the market drops 40%, this is seen as a much better outcome than if a portfolio goes up 20% while the market goes up 40%. Thus, a portfolio that moves closely with the market has a very low relative risk. This risk can be calculated as volatility by looking at the relative price movements, instead of the absolute price movements.

Investment professionals focus on relative risk for a number of reasons, one of which is the fact that they are not managing their own money. They need to prove to their bosses and clients that they are above average in their job. If a particular benchmark cannot be beaten by these investors, clients may ask why pay for them to manage their money when they could put it in a low-fee or no-fee mutual fund. This is one of the reasons that institutional investors need to compare their performance to some benchmark. Thus, the focus for investors is return and relative risk. Adding low risk stocks to the portfolio causes relative risk to increase a lot, making it an unappealing investment because low absolute risk inherently causes high relative risk. A low risk portfolio only makes sense if absolute risk is what one cares about. Thus, for those investors who don’t care about relative risk and just absolute risk, low risk stocks are a great investing opportunity.

In addition to the reasons mentioned, there are several additional reasons why some investors are not attracted to low-risk stocks. Eric Falkenstein, a renowned author in the low volatility investing realm, wrote that “envy is at the root of the investment paradox.” Some investors don’t recognize the significance of compounding returns. Others do, but are unable to utilize the paradox due to relative risk and career pressures. Analysts who choose big winners are more likely to get recognized than those who pick safer stocks with lower upside potential, and funds that pick the right high risk stocks also see more reward in an increase in AUM. Moreover, some people do not invest in low risk stocks because they have less appeal of high risk stocks, where they think they can make money easily and quickly. These high risk stocks are more “sexy” and have a “lottery ticket” element that attracts investors with the appeal of a big payday.

3.2 Betting Against Correlation: Testing Theories of the Low-Risk Effect

A recurring phenomena in finance, is the observation of the “low-risk effect.” This is the idea that lower risk or lower volatility stocks, tend to have higher alpha than higher risk or higher volatility stocks. In trying to understand the reason this anomaly occurs, are two possible explanations. The first looks at whether this is caused by leverage constraints, meaning measurement using systematic risk. The second focuses on the behavioral effects, or idiosyncratic risks. One of the main issues with prior research, is that a lot of the low-risk factors are correlated and interrelated, making it hard to isolate certain factors or effects. In this paper, the global data was used, with a couple new factors meant to control for existing factors.

Previous studies, like one by Adrian, Etula, and Muir in 2014, showed a link between return to the BAB (Betting Against Beta) factor and financial intermediary leverage. Many of these factors, though, including BAB, generally exhibit the “low-risk effect” and are thus very hard to differentiate between. Thus, this paper decided to do just that, by breaking down BAB into two other factors: betting against correlation (BAC) and betting against volatility (BAV). BAC is accomplished through longing stocks with low correlation to the market, and shorting those with high correlation to the market, while trying to match the volatilities of both the long and short portfolios. BAV is achieved in a similar manner, except instead of longing and shorting correlation, volatility is used, and correlation is kept constant.

To address the behavioral explanation, the paper looks at some prior factors from studies done by Ang,

Hodrick, Xing, and Zhang in 2006 and 2009. The first study found stocks with low idiosyncratic volatility (IVOL) have a greater risk-adjusted return, while the second found that a low maximum return (LMAX), a measure of idiosyncratic skewness, is associated with greater risk-adjusted returns. This paper kept the focus on LMAX and IVOL, but added another factor, scaled MAX (SMAX), which longs stocks with a low MAX return divided by ex ante volatility, and then shorts stocks with a high MAX return divided by ex ante volatility. This focuses on the lottery demand, holding volatility relatively constant and only focusing on the distribution of the returns. Margin debt held by investors, and investor sentiment were also noted.

In the paper, 58,415 stocks from the MSCI World Index, from 24 countries between January 1926 and December 2015 were covered. BAB and BAC ended up being very successful in controlling for the other factors that could influence the “low-risk effect.” For all stocks, the BAC factor produced a significant six-factor alpha that was nearly independent of the other low-risk factors studied. In terms of explaining the behavioral side with factors, SMAX was the only truly great, resilient measure used. The rest generally had higher turnover, and were consequently very susceptible to microstructure noise. SMAX attained positive risk-adjusted returns in the U.S. but negative risk-adjusted returns globally, which was seen with some other idiosyncratic risk factors. The paper showed that systematic low-risk factor generally tended to outperform behavioral risk factors, especially when considering turnover and time period length. All in all, the low-risk effect was believed to be driven by multiple factor effects, meaning both leverage constraints and the demand for lottery could play a role in effecting this. However, leverage constraint effects were a bit stronger, especially internationally.

3.3 Price Response to Factor Index Additions and Deletions

Some of the driving fundamental assumptions of finance is the flat demand curve for stocks, where risk is the main driver and each stock has a perfect substitute. However, this concept has been questioned for the past few years, with literature picking up on stocks with show supply shocks and checking how this affects their price. The literature has shown several instances where large block sales of stock has negatively affected its price. This was often due to information contamination, which is new, significant information about the company in the market. This information often reflects fundamental changes in the company, and if it is negative, will understandably trigger block sales. Thus, the price change is less due to the supply shock, and moreso due to the fundamental change in the company’s value (like a scandal or earnings report).

However, interesting patterns that have not yet been fully explained have been observed regarding S&P 500 company addition and deletions. When companies are added or removed from the index, it is purely mechanical, and usually not due to some drastic fundamental change in the company. Assuming the market is efficient, the demand for stocks should not change due to being added or removed from an index, but several studies have shown that it does. Harris and Gurel (1986), Shleifer (1986), Beneish and Whaley (1996), Chen, Noronha, and Singal (2004) all show how new additions to the S&P come with higher than normal returns for that company. Though they agree on the price movement, the studies tend to have a hard time agreeing on the reason for this price movement. Some possible explanations include compensation for providing liquidity, better monitoring for investors when a company is added to a reputable and large index, and higher analyst coverage leading to more information and analysis available on the company. One primary concern is whether or not index reshuffling is an information-free event - that is, whether a company being added or removed adds information to the market about the company.

In this paper, the authors look at factor index rebalancing for an information-free event. Factor indices are part of a parent index of many other stocks, and are constructed in a mechanical way that is publically available and usually based on ranking stocks off a particular ratio of characteristic. Looking at the MSCI Minimum Volatility index, stocks returns were recorded for the stocks that had been added/dropped. It was found that the cumulative return from announcement to the effective day was 1.07% for stocks added with a significant t-statistic of 7.16, with 62% of the stocks exhibiting a positive cumulative abnormal return. Of the 1.07% increase, 0.63% of it was gained the following day, indicating that a large part of the increase is from an increase in demand from index funds. 0.31% of the return is lost five days after the rebalancing, but generally the price tends to stabilize afterwards after ten days. Thus, 68% of the price increase is permanent,

while the other 32% is temporary and lost after a few days. This can be due to a number of reasons including a liquidity premium charged by the stock's owner or arbitrage activity. Average trading volume was also significantly more for stocks that were recently added to the index. Between the announcement and actual day of adding the stock, the average trading volume was 30% higher than normal, with a significant t-statistic of 3.81. Moreover, there is a 74% increase in volume for the day prior to the actual adding of the security. A very similar phenomena occurs with stocks set to be dropped from the MSCI Minimum Volatility Index. From the announcement of a stock being dropped to the day before it is actually deleted from the index, the total cumulative abnormal return is -0.91%, and -0.57% of this comes the day right before. After the stocks are deleted, 64% of them have a negative return the following day, and only 0.49% of the -0.91% is regained after three weeks. Trading volume also spikes 46% on the day prior to removal from the index. After three weeks, it returns back to within 1% of the normal trading volume.

These findings imply that once a security is added to a factor index, the demand curve shifts to the right, moving the equilibrium. The trading volume change is likely due to index funds buying or selling massive amounts of the stocks that will be added or removed. Moreover, it was found that the amount of the return is also directly related to the weighting of the volume of stocks entering or leaving the factor index. All in all, these findings suggest an index arbitrage opportunity if the index additions or deletions can be predicted.

3.4 Benchmarks as Limits to Arbitrage: Understanding the Low-Volatility Anomaly

Low-beta and low-volatility stocks have outperformed high-beta, high-volatility stocks from 1968-2008, combining great returns with low downturns. This can be explained by behavioral models of security prices. First is the idea that investors have a preference for "lotteries" and a bias of overconfidence creates a higher demand for higher-volatility securities. Second is the idea that this arbitrage opportunity is very limited, as the need to benchmark creates a greater demand for higher risk stocks, while discouraging investments in low-beta, low-volatility stocks. Several other papers have tried to explain this seemingly misunderstood phenomena, including Karceski in 2002, where it was noted that an extrapolation bias could cause mutual fund managers to care more about overperforming in a bull market, than underperforming in a bear market. This understandably, increases the market's appetite for risky stocks with high reward potential. This paper focuses on the distortions caused specifically by benchmarking.

In the paper, the authors used 41 years of CRSP data, ranging from January 1968 – December 2008. Using the top 1,000 stocks by market cap, the five year trailing volatilities were calculated and returns were tracked. A dollar investment from 1968 made its way to \$59.55, or \$10.12 in real terms when accounting for inflation. On the other hand, the highest volatility portfolio went from a dollar in value to 58 cents during the period, with a real value of just around 10 cents when considering inflation. When using beta as a measure for risk, the finding was very similar. In the lowest-beta portfolio, a dollar grew to \$60.46 in nominal value, or \$10.28 in real value after inflation. The highest-beta portfolio grew from a dollar to \$3.77 in nominal terms, or \$0.64 in real terms after inflation. This held true for large cap companies, but the discrepancy was even higher for smaller cap companies. Generally, the low-risk portfolios also grew much more steadily and constant, without many drawdowns. To add on to this as well, the portfolio values did not include transaction costs. The high-risk portfolios cost more to rebalance on a monthly level, as was done in the paper, than the low-risk portfolios, indicating this anomaly is more pronounced than initially reported. These findings are not novel, but this paper attempts to explain them in a new way. Many theories add evidence for disproving the Capital Asset Pricing Model (CAPM), and even suggest that beta may not be the correct measure of risk. Other models relating risk and return, however, have had difficulty gaining acceptance and widespread usage in the finance industry.

One theory explored in detail is an investor's irrational preference for high-volatility stocks. First, many investors have a natural preference for lotteries, even though there is a general aversion towards loss. If a stock has a positive skew, that is a larger probability of a large positive payoff than probability of a small payoff, investors typically are very interested. Though skew is not the same as volatility, in their paper in

2010, Boyer, Mitton, and Vorkink make a strong case for how expected skewness is a proxy for volatility. Another idea is representativeness, or that Bayes' rule and probability theory are often not natural to people. One example of this is, selectively looking at a few speculative investments that have turned out to be massive successes, without considering the numerous failures. Overconfidence has also been tied to a preference for volatile stocks; optimists are generally more aggressive than pessimists.

The need for benchmarking, especially among institutional investors, is also believed to heavily play into the anomaly. In fact, from the period when institutional investors managed 30% of all money to 60%, the anomaly intensified. This still begs the question as to why institutional investors do not buy more low-volatility stocks, and the answer has to do with benchmarking. The typical fund manager is judged for his/her "information ratio" (IR) which is the expected return difference between the manager and the expected return of the S&P 500, divided by the volatility of this return difference (tracking error). The goal of the investment manager is to maximize this information ratio, best as possible, through picking stocks. In 2009, Sensoy showed that over 61% of U.S. mutual fund managers are benchmarked against the S&P 500, while over 94% are benchmarked to some U.S. index benchmark. Moreover, SEC rules require mutual funds to compare their performance to some benchmark. This intuitively makes sense, as it allows investors to assess the skill and ability of managers in an unbiased way, and also allows fund managers a chance to differentiate themselves.

Investment managers without leverage will try to find mispriced stocks with a beta very close to market risk (beta of 1), overweighting positive-alpha stocks while underweighting negative-alpha stocks. When comparing the Sharpe ratio of large cap stocks for a low-volatility portfolio, it was quite high at 0.38. However, IR was a very low 0.08, showing this would be very tough for a fund manager to invest in. While Beta and volatility are undoubtedly very correlated, the study showed that beta is more related to the anomaly than volatility, especially with large cap stocks, which is what most fund managers disproportionately focus their invests in. Both volatility and beta play a significant role in this anomaly in smaller cap stocks. Looking at the period from 1968-2008, the top value strategy portfolios had an IR of 0.51, and top momentum strategy portfolios had an IR of 0.64. This is extremely high compared to the IR of low-volatility stocks in this period, which ranged from 0.08 to 0.17.

Overall, irrational investor preference for lotteries and high volatility stocks, as well as investment managers' focus on benchmarks and IR flatten or even invert the relationship between risk and return as we know it. This has been shown by the study, and prior observations that the anomaly intensified with the increase in AUM of fund managers in the U.S. These reasons appear perennial, so the anomaly will likely not be going away anytime soon. One other factor to this is compounding of the low-volatility portfolio. Since it suffers fewer drawdowns, this means the portfolio is able to experience more stable and upward growth.

3.5 Betting Against Beta

In this paper, a real-world resembling model is created with leverage and margin constraints in 55,600 stocks from 20 global stock, bond, credit, and futures markets. Some agents in this model cannot use any leverage, and some have limited margin constraints, much like many investors and fund managers.

Many mutual funds, pension funds, and individual investors are constrained by the amount of leverage they can take on, such that instead of investing in a portfolio yielding the highest Sharpe Ratio, they are forced to overweight portfolios with higher risk stocks. This suggests fund managers hold high-beta stocks to a lower risk adjusted return standard than low-beta stocks, which would require leverage. Thus, if one cannot leverage or has significant leverage constraints, then this agent will overweight riskier securities. The model was able to empirically show this in the equities, bonds, and futures markets. This was done by sorting portfolios by betas, and realizing alphas and sharpe ratios declining with increases in portfolio beta.

Moreover, if one can leverage without constraint, then they would underweight high-beta assets and overweight low-beta assets. Betting against beta (BAB) factors help explain this better. A BAB factor is a portfolio longing low-beta securities (leveraged to a beta of 1), shorting high-beta assets (deleveraged to a beta of 1). Hence, a BAB factor is market neutral. The model in the paper predicts that this portfolio will have a positive return, that increases with the spread in the betas and tightness of leverage constraints. Thus,

longing low-beta and shorting high-beta yields significant, and positive risk-adjusted returns. This was observed in the model by looking at U.S., developing, and international equity markets and observing that the BAB factor yielded a Sharpe ratio that was double its value effect, and 40% greater than momentum. The BAB factor had very high risk adjusted returns, and during four twenty-year periods between 1926 and 2012, produced significant positive returns. This generally held across other asset classes, including credit and treasury bond markets.

When a leverage constraint is met or surpassed, and the agent needs to deleverage, the BAB factor portfolio experiences negative returns, but its expected future returns increase. This was once again shown with a time series with spreads of various funding constraints.

Another central idea of the model was that increased funding liquidity risk compresses betas toward one. This was proven by looking at the volatility of funding constraints as funding liquidity risk, and the end result was that the dispersion of betas when funding liquidity risk is high, was much lower than when funding liquidity risk is low.

Finally, the model showed that investors that are more constrained are forced to overweight riskier securities, while investors without such constraints can overweight lower-risk securities. Studying a number of stock portfolios from constrained investors, most fund managers and individual investors' portfolios have a beta greater than one. On the flip side, many PE firms that perform an LBO get firms with a beta below one, and apply leverage. Great investor Warren Buffett even bets against beta, as many of his investments are leveraged, low-beta stocks.

3.6 The Low-Risk Anomaly: A Decomposition into Micro and Macro Effects

The low beta anomaly can be broken up into micro and macro effects. The micro effects include picking low beta stocks, while the macro effects are picking low beta countries or industries. In this paper, the micro effects were recorded by creating long-short portfolios of stocks, holding constant country and industry risk. The macro effects were observed through long-short portfolios of various countries and industries, holding stock level risk constant. Studying a number of stocks within 29 industries and 31 different developed countries, the macro and micro effects were observed, and both together were shown to play an important role in the low risk anomaly.

Micro selection of stocks, that is constructing a low risk portfolio of stocks, holding country and industry constant, showed that risk could be significantly decreased without a significant decrease in return. Macro selection, especially with regards to the country chosen, causes greater returns with small differences in risk. These findings have pretty significant implications, as this indicates that people seeking arbitrage opportunities through mispricing of industry or sector ETFs may not be as feasible or profitable as one may think. There is more of an opportunity exploiting the micro effects of individual stock selection.

It was found that using industry beta to predict future stock betas was possible, but not as effective as just using historical stock betas. However, industry beta information without stock information does improve risk-adjusted returns, just not as to the same level as with stock information. The paper also goes into detail trying to isolate pure industry effects and pure stock effects. Pure industry effects are the average differences between high and low beta industries, while holding constant stock risk. Pure stock risk is the opposite of that, calculating the average difference between high bet and low beta stocks, keeping industry risk constant. In the end, finding low-risk portfolios using selection of low risk stocks keeping industry constant was around four times more effective than using industries and keeping stock risk constant. Using the historical betas of both together, however, has more predictive power than either one alone.

Next, looking at 31 developed countries including Canada, France, Germany, Japan, and Singapore, the paper worked to decompose the low risk anomaly into country and stock specific effects. Similar to the industry findings, country beta was able to predict stock betas to a certain extent, but not as well as historical stock betas were. Looking only at country betas yielded around half the risk reduction and two-thirds the

risk adjusted return improvement, as compared to stock betas. This study implies that predicting risk of individual stocks is in itself very hard when only given data on country or industry risk, but when given all the data can have much more predictive power.

Chapter 4

Data Collection and Summary Statistics

Data was collected from ishares.com, and compiled from 10/31/2011 to 1/5/2017, for EUSA and USMV.

```
# Load Packages and View the Data
```

```
devtools::install_github("johngil/mscidata")
```

```
## Skipping install of 'mscidata' from a github remote, the SHA1 (0f33dcee) has not changed since last
```

```
## Use `force = TRUE` to force installation
```

```
library(mscidata)
```

```
library(ggplot2)
```

```
data(usa)
```

```
data(minvol)
```

```
## Summary statistics of EUSA Data
```

```
head(usa)
```

```
##   X Ticker   Name Asset.Class Weight.... Price Shares Market.Value
## 1 1 <NA> 1015736      <NA>    0.1950 26.63  10991   292690000
## 2 2   MMM   3M CO      Equity    0.4706 79.02   160    12643000
## 3 3   MMM   3M CO      Equity    0.4659 81.04   154    12480000
## 4 4   MMM   3M CO      Equity    0.4626 81.73   6872   561649000
## 5 5   MMM   3M CO      Equity    0.4709 86.71   7211   625266000
## 6 6   MMM   3M CO      Equity    0.4556 87.60   6672   584467000
##   Notional.Value      Sector  SEDOL      ISIN
## 1              NA Industrials  <NA>      <NA>
## 2              NA Industrials 2595708 US88579Y1010
## 3              NA Industrials 2595708 US88579Y1010
## 4              NA Industrials 2595708 US88579Y1010
## 5              NA Industrials 2595708 US88579Y1010
## 6              NA Industrials 2595708 US88579Y1010
##              Exchange      Date
## 1              <NA> 2012-12-31
## 2 New York Stock Exchange Inc. 2011-10-31
## 3 New York Stock Exchange Inc. 2011-11-30
## 4 New York Stock Exchange Inc. 2011-12-30
## 5 New York Stock Exchange Inc. 2012-01-31
## 6 New York Stock Exchange Inc. 2012-02-29
```

```
tail(usa)
```

```
##           X Ticker           Name Asset.Class Weight.... Price Shares
## 39325 39325   ZTS ZOETIS INC CLASS A      Equity      0.1649 51.10   2377
## 39326 39326   ZTS ZOETIS INC CLASS A      Equity      0.1695 52.01   2397
## 39327 39327   ZTS ZOETIS INC CLASS A      Equity      0.1600 47.80   2472
## 39328 39328   ZTS ZOETIS INC CLASS A      Equity      0.1608 50.38   2847
## 39329 39329   ZTS ZOETIS INC CLASS A      Equity      0.1706 53.53   3015
## 39330 39330   ZTS ZOETIS INC CLASS A      Equity      0.1690 53.93   3015
##           Market.Value Notional.Value      Sector  SEDOL      ISIN
## 39325      121465000      121464.7 Health Care B95WG16 US98978V1035
## 39326      124668000      124668.0 Health Care B95WG16 US98978V1035
## 39327      118162000      118161.6 Health Care B95WG16 US98978V1035
## 39328      143432000      143431.9 Health Care B95WG16 US98978V1035
## 39329      161393000      161393.0 Health Care B95WG16 US98978V1035
## 39330      162599000      162599.0 Health Care B95WG16 US98978V1035
##           Exchange      Date
## 39325 New York Stock Exchange Inc. 2016-08-31
## 39326 New York Stock Exchange Inc. 2016-09-30
## 39327 New York Stock Exchange Inc. 2016-10-31
## 39328 New York Stock Exchange Inc. 2016-11-30
## 39329 New York Stock Exchange Inc. 2016-12-30
## 39330 New York Stock Exchange Inc. 2017-01-05
```

```
summary(usa)
```

```
##           X           Ticker           Name
## Min.      :    1   CB       : 102   3M CO           : 64
## 1st Qu.: 9833   NLSN      : 65   ABBOTT LABORATORIES : 64
## Median :19666   A        : 64   ACCENTURE PLC       : 64
## Mean   :19666   AAP       : 64   ACTIVISION BLIZZARD INC: 64
## 3rd Qu.:29498   ABC       : 64   ADOBE SYSTEM INC     : 64
## Max.    :39330   (Other):38939 ADVANCE AUTO PARTS INC : 64
##           NA's      : 32   (Other)           :38946
##           Asset.Class Weight....      Price      Shares
## Cash      : 66   Min.    :-0.3905   Min.    : 0.56   Min.    :-174670
## Equity    :39240 1st Qu.: 0.0542   1st Qu.: 35.08   1st Qu.: 805
## Money Market: 23 Median : 0.1236   Median : 55.21   Median : 1563
## NA's      : 1   Mean   : 0.1626   Mean   : 72.05   Mean   : 3566
##           3rd Qu.: 0.1638   3rd Qu.: 83.77   3rd Qu.: 3199
##           Max.    : 4.6773   Max.    :953.00   Max.    : 873628
##           NA's      :47
##           Market.Value Notional.Value      Sector
## Min.      :0.000e+00   Min.      :-174670   Financials      :6909
## 1st Qu.:5.321e+07     1st Qu.: 55505     Consumer Discretionary:6703
## Median :8.418e+07     Median : 75582     Information Technology:5590
## Mean   :1.607e+08     Mean   : 91931     Industrials     :4765
## 3rd Qu.:1.435e+08     3rd Qu.: 118997     Health Care     :4138
## Max.    :6.804e+09     Max.    :2106050     Energy          :3253
## NA's     :7           NA's     :22930     (Other)         :7972
##           SEDOL      ISIN
## 2000019: 64   AN8068571086: 64
## 2002305: 64   BMG0450A1053: 64
## 2005973: 64   BMG0692U1099: 64
```

```
## 2008154: 64 BMG169621056: 64
## 2011602: 64 BMG3223R1088: 64
## (Other):38920 (Other) :38952
## NA's : 90 NA's : 58
##
## Exchange
## New York Stock Exchange Inc. :27970
## NASDAQ : 9405
## Boerse Berlin : 427
## Deutsche Boerse Ag : 395
## Bolsa Mexicana De Valores (Mexican Stock Exchange): 266
## (Other) : 661
## NA's : 206
## Date
## 2015-06-30: 641
## 2015-08-31: 641
## 2015-05-29: 639
## 2015-09-30: 639
## 2015-10-30: 639
## 2015-11-30: 638
## (Other) :35493
```

```
## Summary statistics of USMV Data
head(minvol)
```

```
## X Ticker Name Asset.Class Weight.... Price Shares Market.Value
## 1 1 MMM 3M CO Equity 0.7488 79.02 244 19281
## 2 2 MMM 3M CO Equity 0.7592 81.04 244 19774
## 3 3 MMM 3M CO Equity 0.2892 109.35 94494 10332919
## 4 4 MMM 3M CO Equity 0.3000 117.43 59406 6976047
## 5 5 MMM 3M CO Equity 0.2999 113.58 57686 6551976
## 6 6 MMM 3M CO Equity 0.3095 119.41 52611 6282280
## Notional.Value Sector SEDOL ISIN
## 1 NA Industrials 2595708 US88579Y1010
## 2 NA Industrials 2595708 US88579Y1010
## 3 NA Industrials 2595708 US88579Y1010
## 4 NA Industrials 2595708 US88579Y1010
## 5 NA Industrials 2595708 US88579Y1010
## 6 NA Industrials 2595708 US88579Y1010
## Exchange Date
## 1 New York Stock Exchange Inc. 2011-10-31
## 2 New York Stock Exchange Inc. 2011-11-30
## 3 New York Stock Exchange Inc. 2013-06-28
## 4 New York Stock Exchange Inc. 2013-07-31
## 5 New York Stock Exchange Inc. 2013-08-30
## 6 New York Stock Exchange Inc. 2013-09-30
```

```
tail(minvol)
```

```
## X Ticker Name Asset.Class Weight.... Price
## 9498 9498 ZBH ZIMMER BIOMET HOLDINGS INC Equity 0.1391 104.95
## 9499 9499 ZTS ZOETIS INC CLASS A Equity 0.1002 30.89
## 9500 9500 ZTS ZOETIS INC CLASS A Equity 0.0962 29.81
## 9501 9501 ZTS ZOETIS INC CLASS A Equity 0.0972 29.15
## 9502 9502 ZTS ZOETIS INC CLASS A Equity 0.1021 31.12
## 9503 9503 ZTS ZOETIS INC CLASS A Equity 0.0992 31.66
## Shares Market.Value Notional.Value Sector SEDOL ISIN
```

```

## 9498 163220      17129939      17129939 Health Care 2783815 US98956P1021
## 9499 115890      3579836          NA Health Care B95WG16 US98978V1035
## 9500 75069       2237807          NA Health Care B95WG16 US98978V1035
## 9501 72889       2124714          NA Health Care B95WG16 US98978V1035
## 9502 66567       2071565          NA Health Care B95WG16 US98978V1035
## 9503 66458       2104060          NA Health Care B95WG16 US98978V1035
##
##                      Exchange      Date
## 9498 New York Stock Exchange Inc. 2017-01-05
## 9499 New York Stock Exchange Inc. 2013-06-28
## 9500 New York Stock Exchange Inc. 2013-07-31
## 9501 New York Stock Exchange Inc. 2013-08-30
## 9502 New York Stock Exchange Inc. 2013-09-30
## 9503 New York Stock Exchange Inc. 2013-10-31

```

```
summary(minvol)
```

```

##           X           Ticker           Name
## Min.      : 1      CB       : 82      ABBOTT LABORATORIES      : 64
## 1st Qu.:2376      ABT       : 64      ALTRIA GROUP INC        : 64
## Median :4752      ACGL      : 64      ARCH CAPITAL GROUP LTD  : 64
## Mean    :4752      ADP       : 64      AT&T INC                 : 64
## 3rd Qu.:7128      AMT       : 64      AUTOMATIC DATA PROCESSING INC: 64
## Max.     :9503      (Other):9134      AUTOZONE INC             : 64
##                      NA's      : 31      (Other)                   :9119
##
##      Asset.Class      Weight....      Price
## Cash      : 66      Min.      : -0.3451      Min.      : 0.56
## Equity     :9413      1st Qu.: 0.2697      1st Qu.: 48.35
## Money Market: 24      Median : 0.5922      Median : 71.56
##                      Mean    : 0.6730      Mean    : 92.93
##                      3rd Qu.: 1.0116      3rd Qu.:100.98
##                      Max.     : 2.8287      Max.     :953.00
##                      NA's      :6
##
##      Shares      Market.Value      Notional.Value
## Min.      : -20891956      Min.      : 1138      Min.      : -20891956
## 1st Qu.: 62755      1st Qu.: 5184586      1st Qu.: 18801242
## Median : 240777      Median : 18738857      Median : 39482427
## Mean    : 525786      Mean    : 31303694      Mean    : 52633035
## 3rd Qu.: 590304      3rd Qu.: 40420826      3rd Qu.: 71639502
## Max.     : 38506545      Max.     :240885300      Max.     :240885300
##                      NA's      :8      NA's      :5064
##
##           Sector      SEDOL      ISIN
## Health Care      :1664      2002305: 64      BMG0450A1053: 64
## Financials       :1569      2005973: 64      BMG3223R1088: 64
## Information Technology:1510      2065308: 64      BMG7496G1033: 64
## Consumer Staples :1246      2065955: 64      US00206R1023: 64
## Consumer Discretionary:1071      2073390: 64      US0028241000: 64
## Utilities        : 628      (Other):9093      (Other)      :9126
## (Other)          :1815      NA's      : 90      NA's      : 57
##
##                      Exchange      Date
## New York Stock Exchange Inc.:7158      2016-11-30: 187
## NASDAQ              :1926      2016-12-30: 187
## Deutsche Boerse Ag      : 58      2017-01-05: 186
## Spot Regulated Market - Bvb : 58      2016-05-31: 180
## Boerse Berlin          : 32      2016-06-30: 179
## (Other)                : 164      2016-07-29: 179

```

NA's : 107 (Other) :8405

Chapter 5

Data Analysis

5.1 Sector Weights

First, sector weights were calculated over time for both EUSA and USMV. Plots were made by sector and displayed to compare the relative weights of EUSA and USMV.

Sector Weight Summary Statistics:

```
data(usa_percent)
data(minvol_percent)

## Summary statistics of EUSA sector weights
head(usa_percent)

##           sector_name sector_count total    percent    date
## 1 Cash and/or Derivatives          2   631 0.003169572 2017-01-05
## 2 Consumer Discretionary        106   631 0.167987322 2017-01-05
## 3 Consumer Staples              43   631 0.068145800 2017-01-05
## 4 Energy                        44   631 0.069730586 2017-01-05
## 5 Financials                    84   631 0.133122029 2017-01-05
## 6 Health Care                   71   631 0.112519810 2017-01-05

tail(usa_percent)

##           sector_name sector_count total    percent    date
## 827 Information Technology          79   585 0.135042735 2011-10-31
## 828 Materials                    33   585 0.056410256 2011-10-31
## 829 Real Estate                   0   585 0.000000000 2011-10-31
## 830 S-T Securities                 1   585 0.001709402 2011-10-31
## 831 Telecommunications            12   585 0.020512821 2011-10-31
## 832 Utilities                    35   585 0.059829060 2011-10-31

summary(usa_percent)

##           sector_name sector_count    total
## Cash and/or Derivatives: 64 Length:832 Length:832
## Consumer Discretionary : 64 Class :character Class :character
## Consumer Staples      : 64 Mode  :character Mode  :character
## Energy                 : 64
## Financials             : 64
## Health Care            : 64
```

```
## (Other) :448
## percent date
## Min. :0.00000 Min. :2011-10-31
## 1st Qu.:0.01426 1st Qu.:2013-02-21
## Median :0.06820 Median :2014-06-14
## Mean :0.07692 Mean :2014-06-14
## 3rd Qu.:0.12236 3rd Qu.:2015-10-07
## Max. :0.19293 Max. :2017-01-05
##
```

```
## Summary statistics of USMV sector weights
head(minvol_percent)
```

```
##          sector_name sector_count total    percent    date
## 1 Cash and/or Derivatives          2   186 0.01075269 2017-01-05
## 2 Consumer Discretionary         18   186 0.09677419 2017-01-05
## 3      Consumer Staples          24   186 0.12903226 2017-01-05
## 4              Energy            4   186 0.02150538 2017-01-05
## 5      Financials                21   186 0.11290323 2017-01-05
## 6      Health Care              33   186 0.17741935 2017-01-05
```

```
tail(minvol_percent)
```

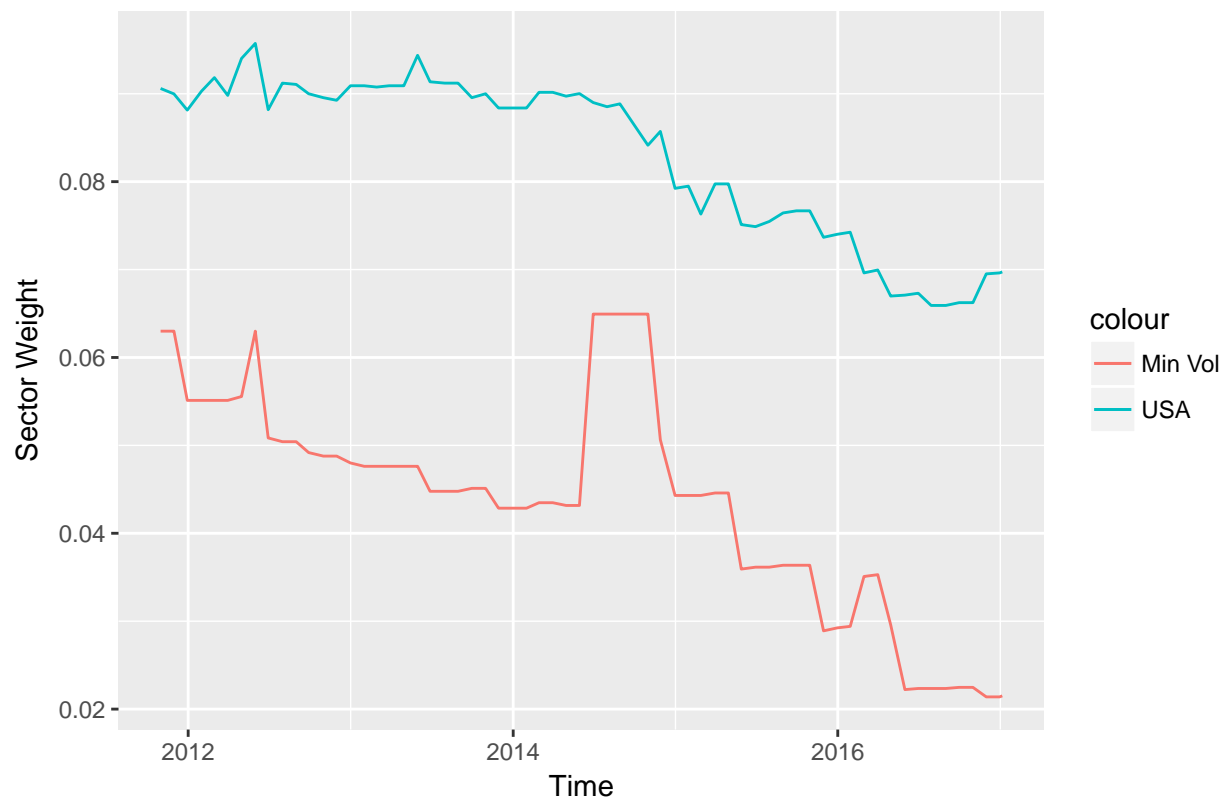
```
##          sector_name sector_count total    percent    date
## 827 Information Technology         19   127 0.149606299 2011-10-31
## 828      Materials                4   127 0.031496063 2011-10-31
## 829      Real Estate              0   127 0.000000000 2011-10-31
## 830      S-T Securities            1   127 0.007874016 2011-10-31
## 831 Telecommunications            7   127 0.055118110 2011-10-31
## 832      Utilities                9   127 0.070866142 2011-10-31
```

```
summary(minvol_percent)
```

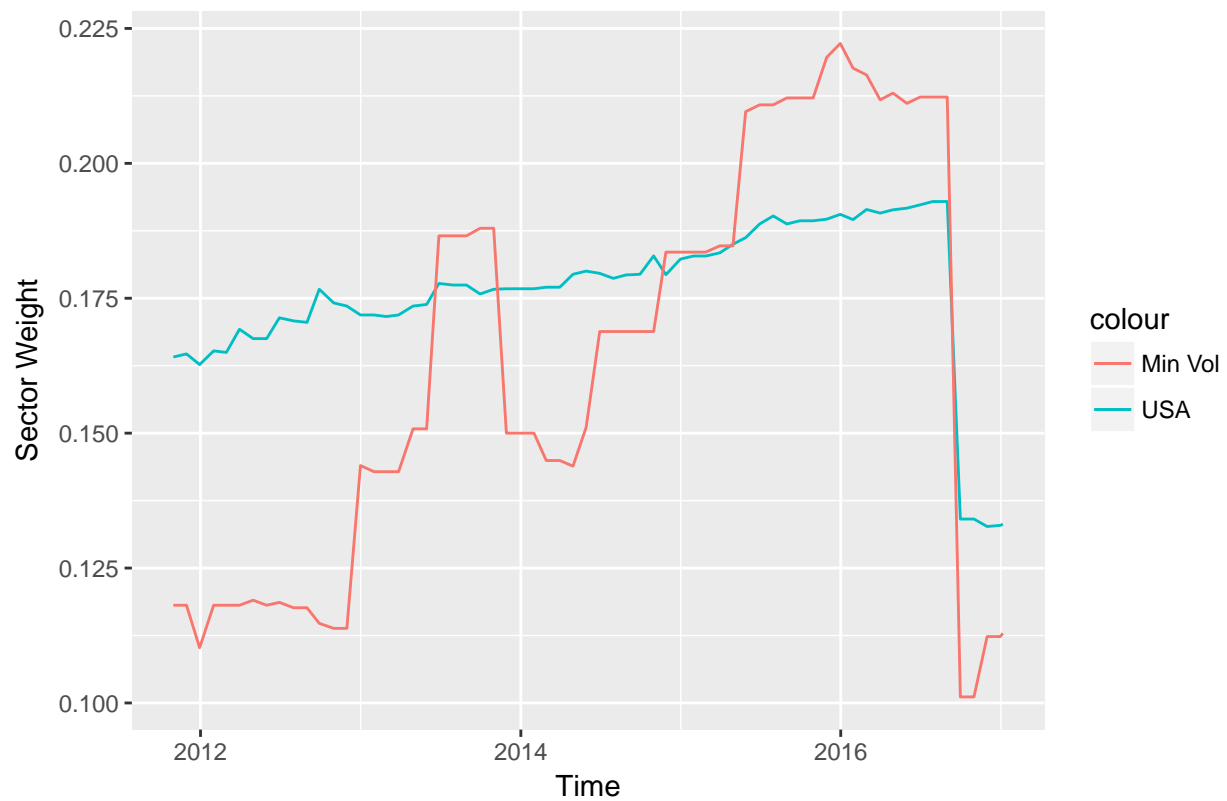
```
##          sector_name sector_count    total
## Cash and/or Derivatives: 64   Length:832   Length:832
## Consumer Discretionary : 64   Class :character   Class :character
## Consumer Staples       : 64   Mode  :character   Mode  :character
## Energy                  : 64
## Financials              : 64
## Health Care             : 64
## (Other)                 :448
##      percent          date
## Min. :0.00000 Min. :2011-10-31
## 1st Qu.:0.02235 1st Qu.:2013-02-21
## Median :0.06349 Median :2014-06-14
## Mean :0.07692 Mean :2014-06-14
## 3rd Qu.:0.13043 3rd Qu.:2015-10-07
## Max. :0.22222 Max. :2017-01-05
##
```

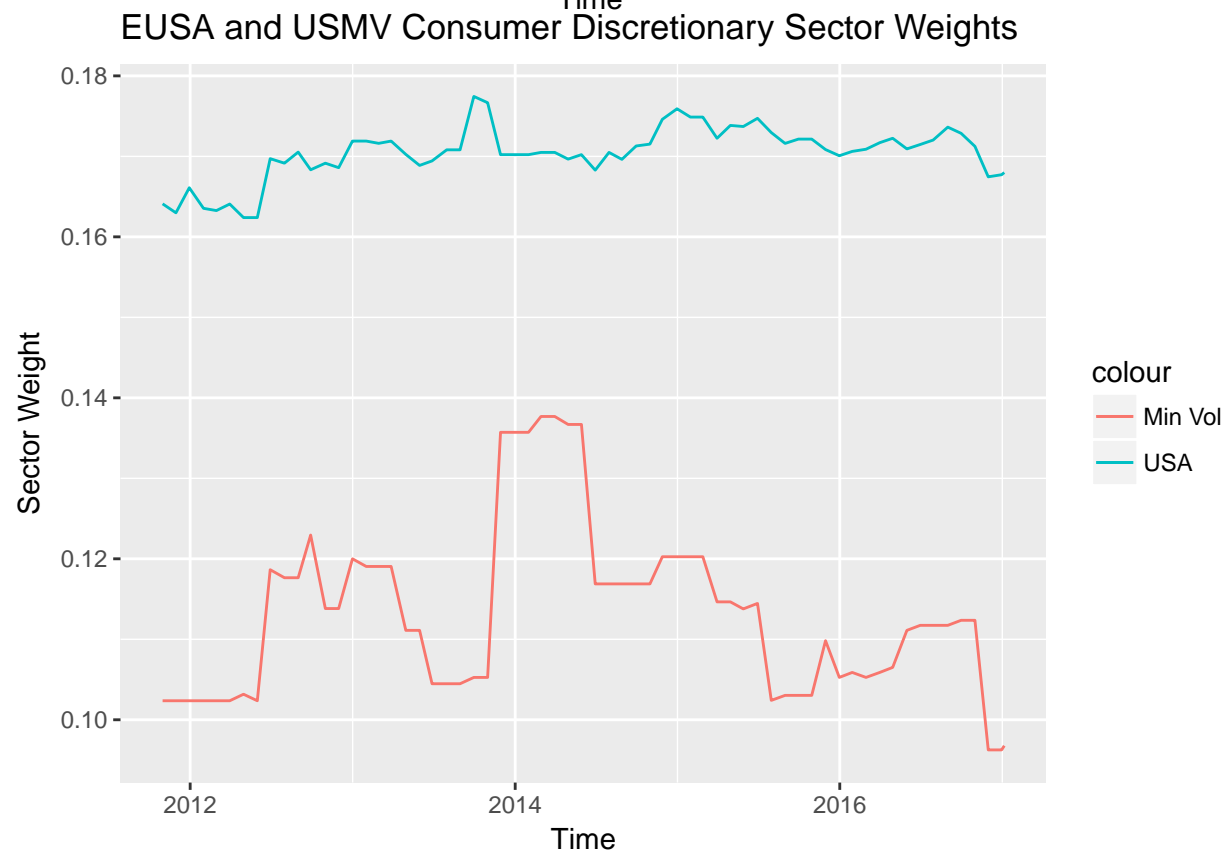
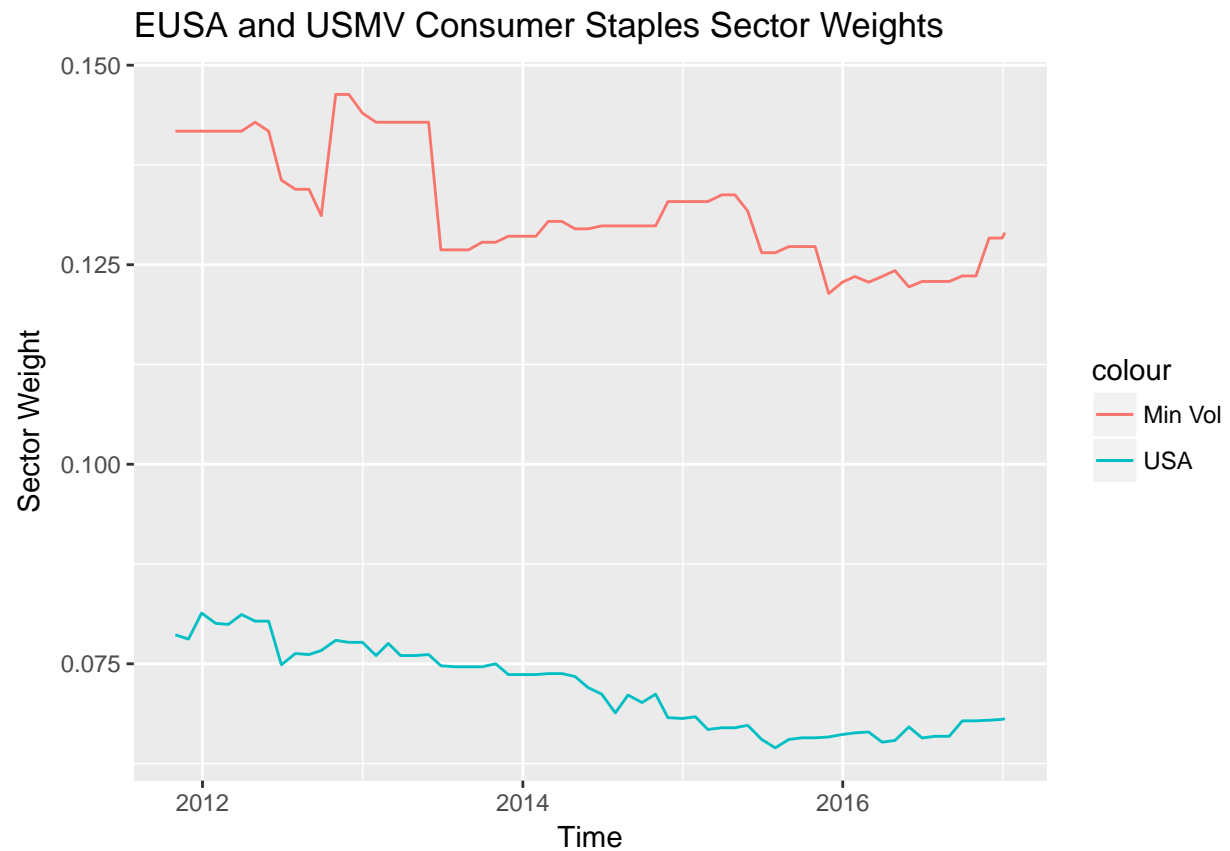
Sector Weights for EUSA and USMV:

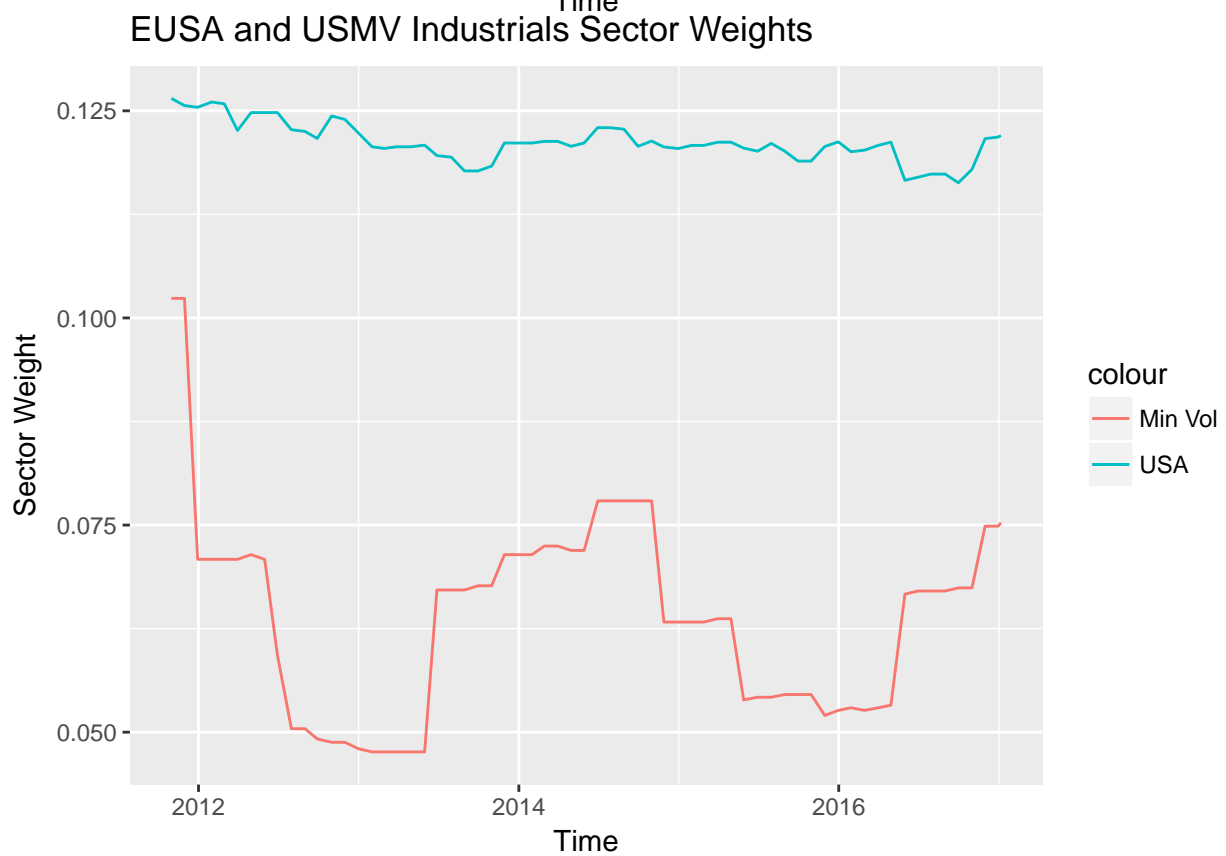
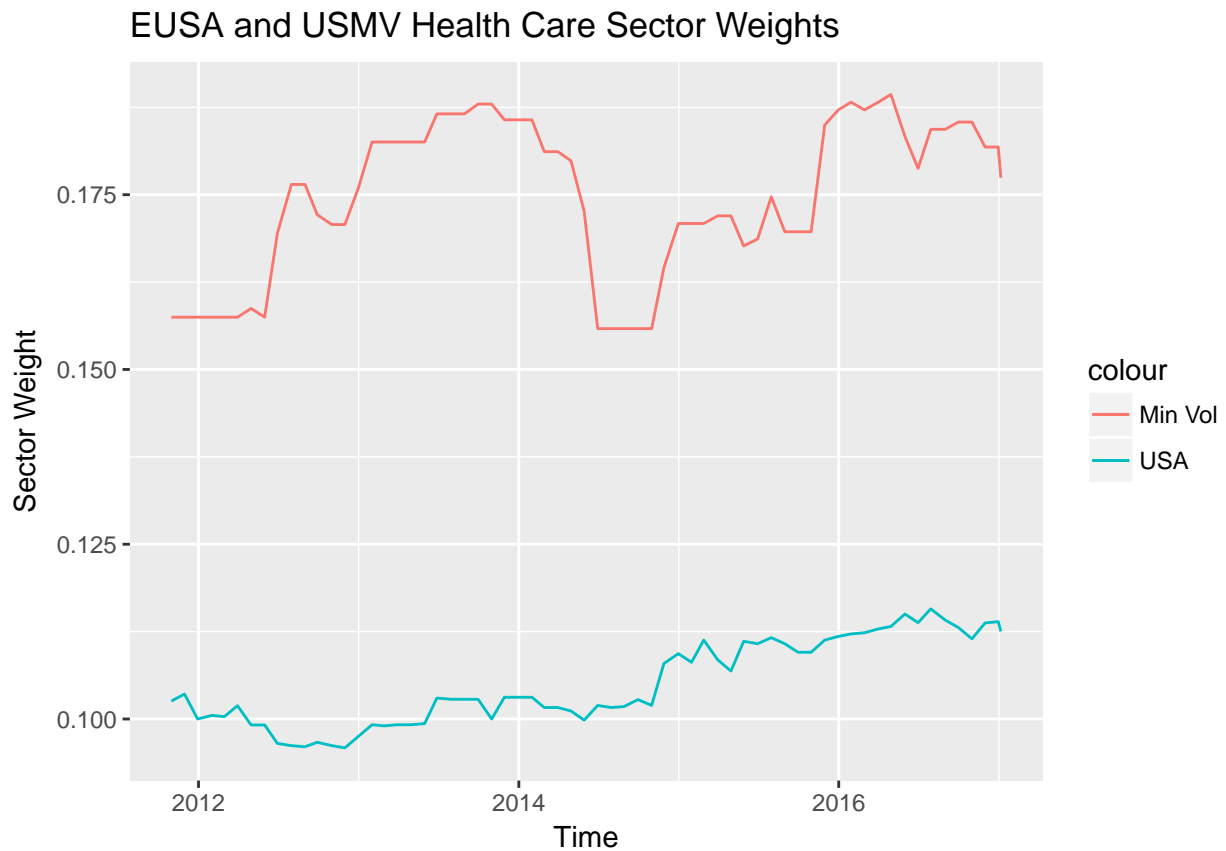
EUSA and USMV Energy Sector Weights



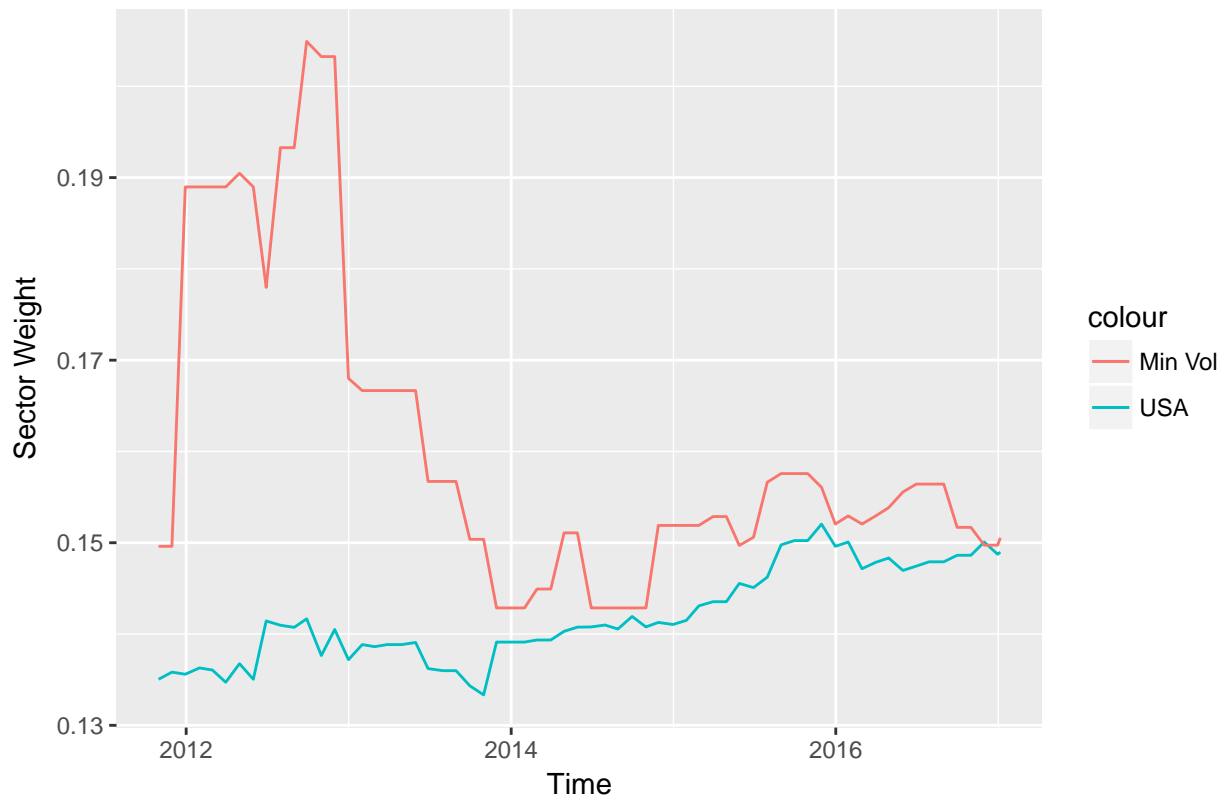
EUSA and USMV Financial Sector Weights



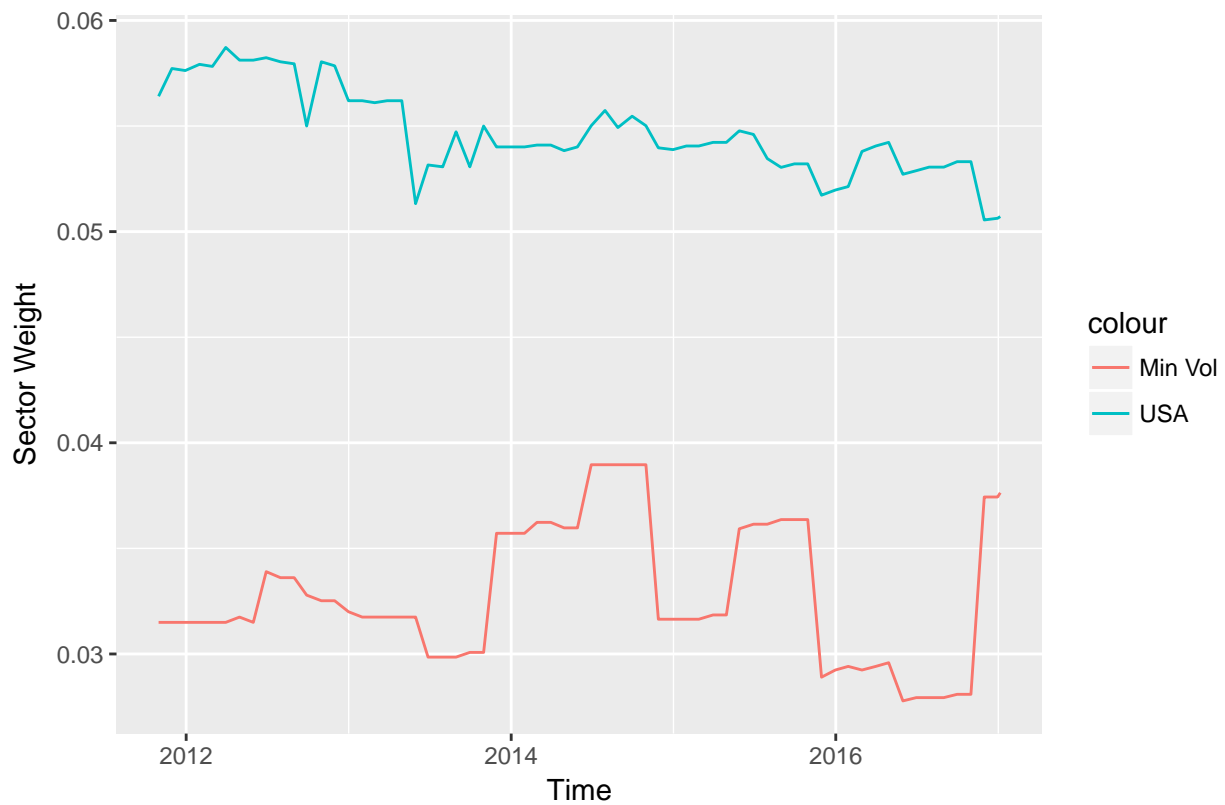




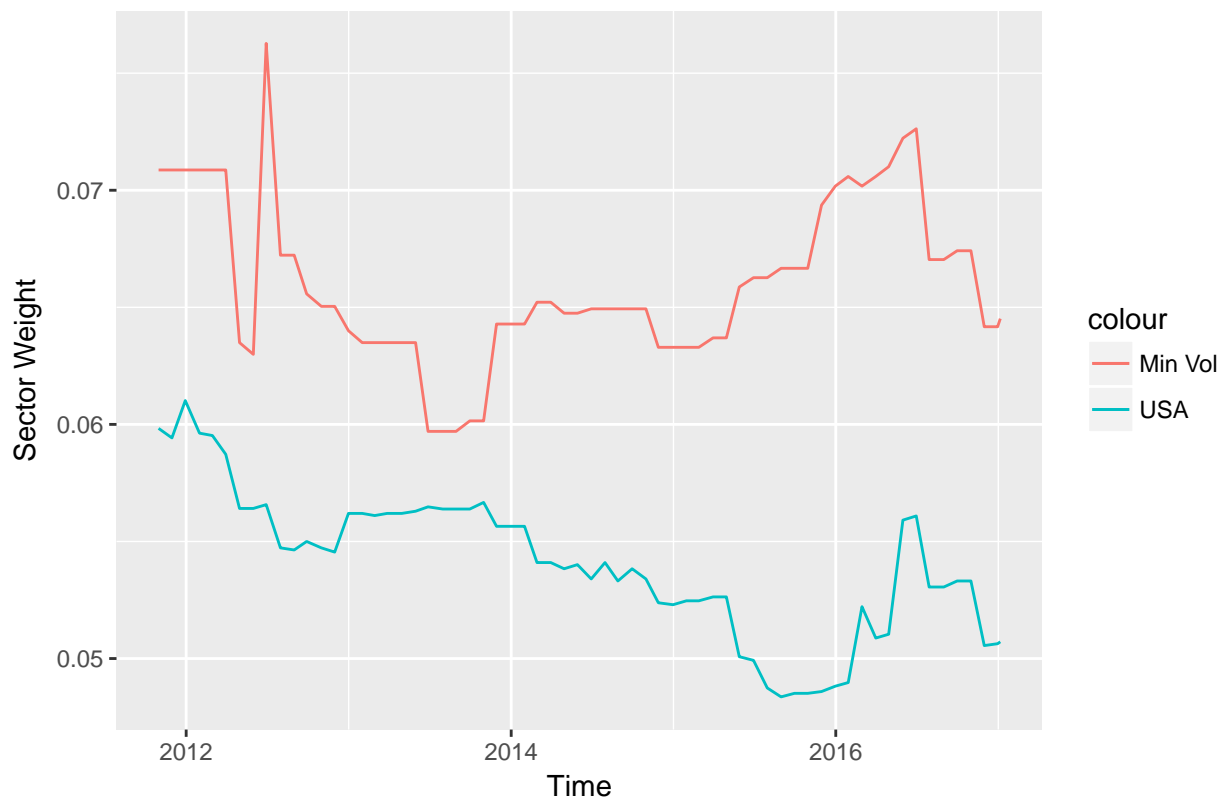
EUSA and USMV Information Technology Sector Weights



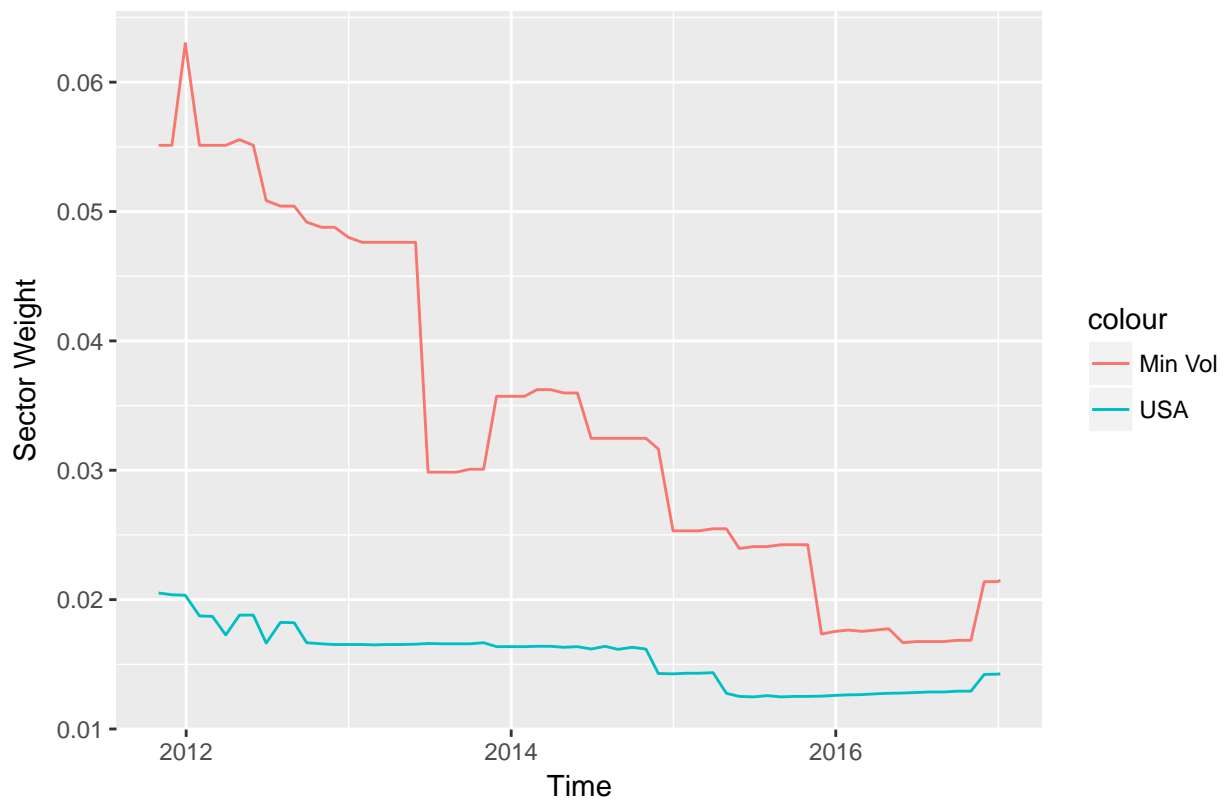
EUSA and USMV Materials Sector Weights



EUSA and USMV Utilities Sector Weights



EUSA and USMV Telecommunications Sector Weights



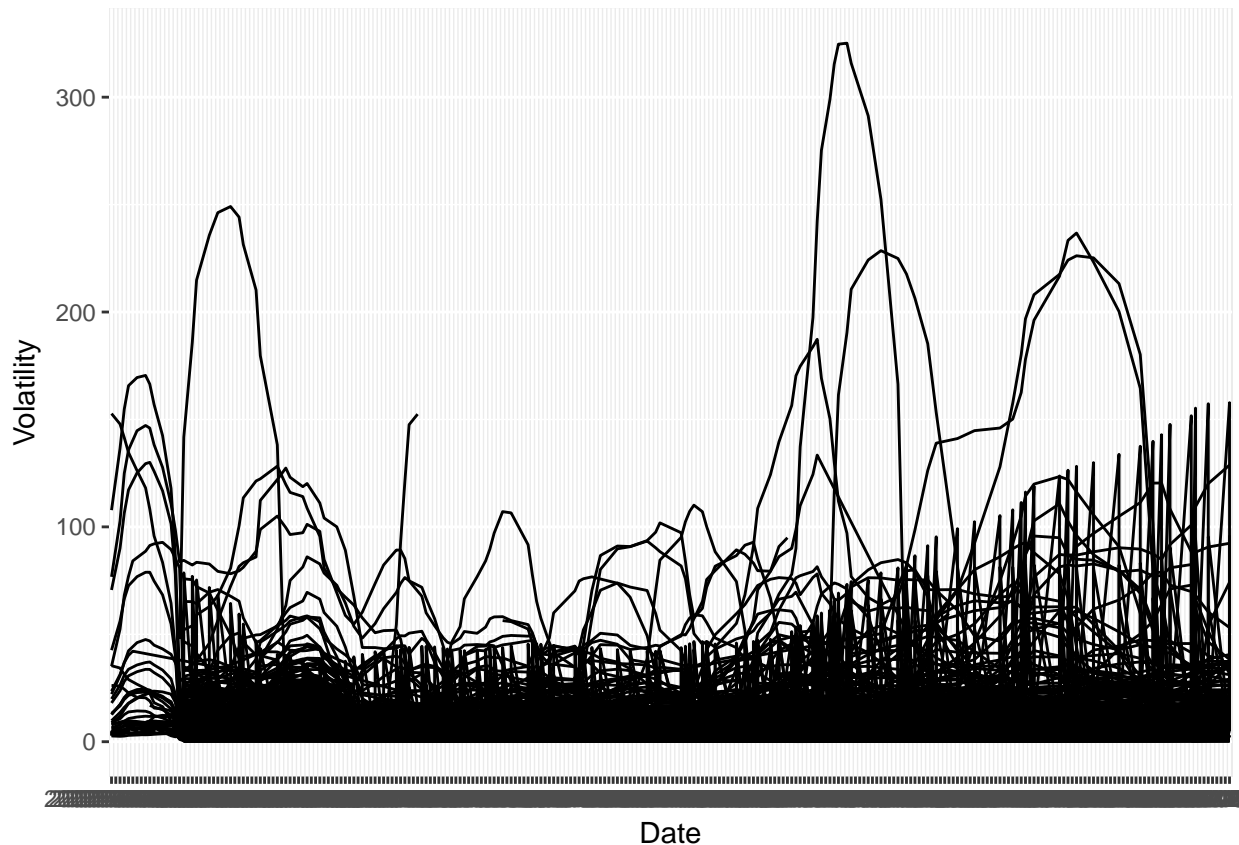
5.2 EUSA Constituent Trailing Volatilities

Data was collected from the past 10 years of the EUSA index. The data was collected from 12/31/2006 to 12/30/2016, was collected from WRDS for the 908 historical constituents of the USA Equal Weight (EUSA) index, of which USMV is derived. Each tickers' 252-day (annual) trailing volatility was calculated and a month end spaghetti plot was produced.

```
##           Date Ticker Volatility
## 1 2008-01-31      A   2.289449
## 2 2008-02-29      A   2.357208
## 3 2008-03-31      A   2.660299
## 4 2008-04-30      A   3.017754
## 5 2008-05-30      A   3.028868
## 6 2008-06-30      A   2.921781
```

```
##           Date Ticker Volatility
## 82257 2016-07-29    ZTS  2.718338
## 82258 2016-08-31    ZTS  3.150629
## 82259 2016-09-30    ZTS  3.363564
## 82260 2016-10-31    ZTS  3.372530
## 82261 2016-11-30    ZTS  3.436391
## 82262 2016-12-30    ZTS  3.664053
```

```
##           Date           Ticker           Volatility
## 2014-09-30: 774    GE      : 432    Min.      : 0.0492
## 2014-10-31: 774    LSI     : 246    1st Qu.: 2.4407
## 2014-11-28: 774    UA      : 234    Median   : 4.3057
## 2014-12-31: 773    CBS     : 228    Mean     : 6.9432
## 2014-06-30: 771    LEN     : 228    3rd Qu.: 7.4648
## 2014-07-31: 771    MKC     : 228    Max.     :325.1242
## (Other)      :77625    (Other):80666
```



5.3 EUSA Constituent Trailing Betas

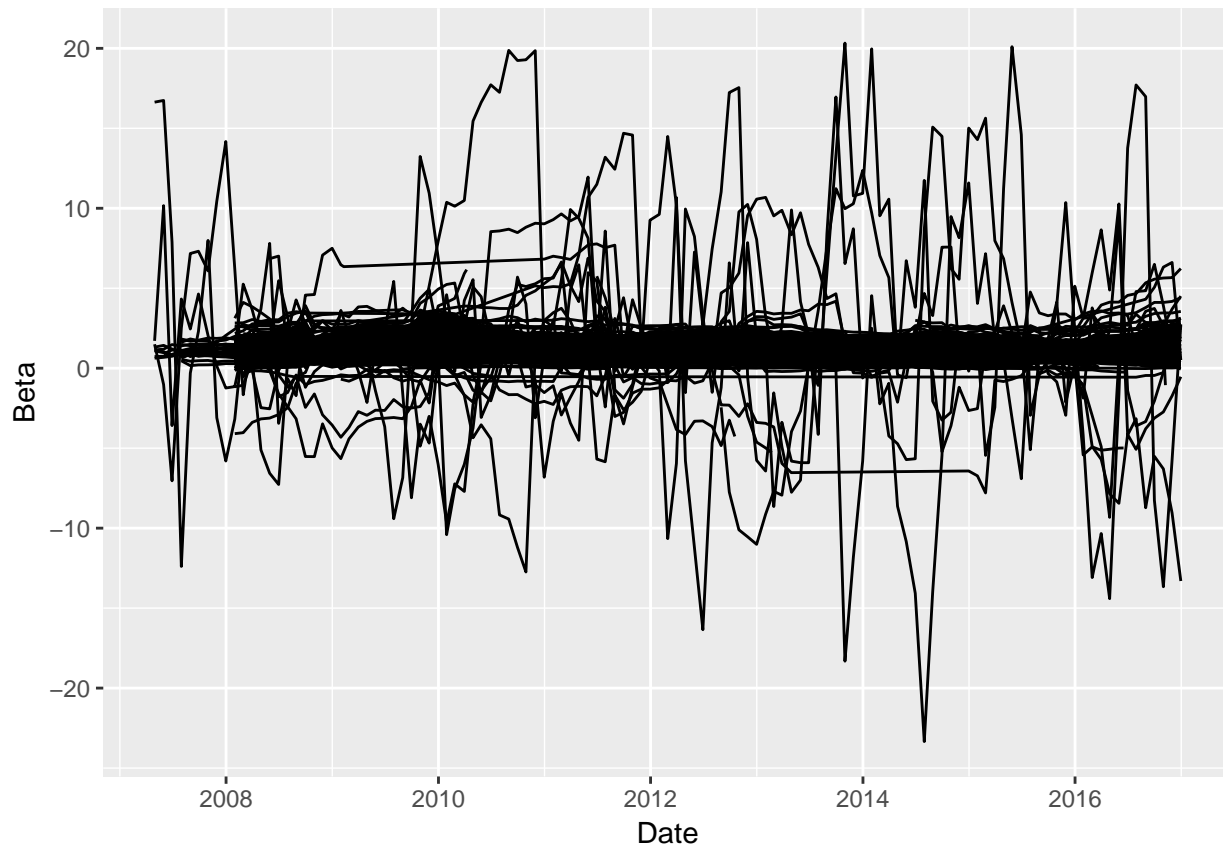
Data was collected from the past 10 years of the EUSA index. The data was collected from 12/31/2006 to 12/30/2016, was collected from WRDS for the 908 historical constituents of the USA Equal Weight (EUSA) index, of which USMV is derived. Each tickers' 252-day (annual) trailing beta was calculated and a month end spaghetti plot was produced.

```
##           Date Ticker      Beta
## 271 2008-01-31      A 0.9538067
## 291 2008-02-29      A 0.9473060
## 311 2008-03-31      A 0.9376670
## 333 2008-04-30      A 0.9588268
## 354 2008-05-30      A 0.9680630
## 375 2008-06-30      A 0.9611418
```

```
##           Date Ticker      Beta
## 879842 2016-07-29    ZTS 1.0224673
## 902837 2016-08-31    ZTS 1.0302957
## 923836 2016-09-30    ZTS 0.9779760
## 944833 2016-10-31    ZTS 0.9830767
## 965832 2016-11-30    ZTS 0.9220281
## 986829 2016-12-30    ZTS 0.9549808
```

```
##           Date           Ticker           Beta
## Min.      :2007-04-30   Length:80200      Min.      : -23.3438
## 1st Qu.:2010-04-30     Class :character 1st Qu.:  0.8184
```

```
## Median :2012-07-31   Mode  :character   Median : 1.0516
## Mean   :2012-07-23                               Mean  : 1.0982
## 3rd Qu.:2014-10-31                               3rd Qu.: 1.3297
## Max.   :2016-12-30                               Max.   : 20.3256
```



5.4 EUSA Constituent Price to Book Ratios

Data was collected from the past 10 years of the EUSA index. The data was collected from 12/31/2006 to 12/30/2016, was collected from WRDS for the 908 historical constituents of the USA Equal Weight (EUSA) index, of which USMV is derived. Each tickers' Price to Book ratio was calculated in two ways, to ensure accuracy.

```
##      gvkey      Date Year Ticker Total_Assets BV_per_share
## 1 126554 2007-10-31 2007      A    7.554e+09      8.7405
## 2 126554 2008-10-31 2008      A    7.437e+09      7.3114
## 3 126554 2009-10-31 2009      A    7.612e+09      7.2397
## 4 126554 2010-10-31 2010      A    9.696e+09      9.3256
## 5 126554 2011-10-31 2011      A    9.057e+09     12.4371
## 6 126554 2011-10-31 2011      A    9.049e+09         NA
##      Shares_Outstanding Total_Liabilities Market_Value Share_Price Book_Value
## 1          370000000      4.320e+09 13634500000      36.85 3233985000
## 2          350000000      4.878e+09  7766500000      22.19 2558990000
## 3          346148000      5.106e+09  8563701500      24.74 2506007676
## 4          346144000      6.460e+09 12045811200      34.80 3228000486
## 5          346382000      4.741e+09 12840380700      37.07 4307987572
## 6              NA              NA 12840380700         NA         NA
```



```
##      PBR1      PBR2
## 1 4.216006 4.216006
## 2 3.034986 3.034986
## 3 3.417269 3.417269
## 4 3.731663 3.731663
## 5 2.980598 2.980598
## 6      NA      NA
```

```
##      gvkey      Date Year Ticker Total_Assets BV_per_share
## 17182 13721 2014-12-31 2014   ZTS   6.607e+09   2.6151
## 17183 13721 2014-12-31 2014   ZTS   6.588e+09      NA
## 17184 13721 2015-12-31 2015   ZTS   7.913e+09   2.1472
## 17185 13721 2015-12-31 2015   ZTS   7.913e+09      NA
## 17186 13721 2016-12-31 2016   ZTS   7.649e+09   3.0171
## 17187 13721 2016-12-31 2016   ZTS   7.649e+09      NA
##      Shares_Outstanding Total_Liabilities Market_Value Share_Price
## 17182      501328000      5.270e+09 21572143800      43.03
## 17183      NA      NA      NA 21572143800      NA
## 17184      497400000      6.822e+09 23835408000      47.92
## 17185      NA      NA      NA 23835408000      NA
## 17186      492855000      6.150e+09 26382528200      53.53
## 17187      NA      NA      NA 26382528200      NA
##      Book_Value      PBR1      PBR2
## 17182 1311022853 16.45444 16.45444
## 17183      NA      NA      NA
## 17184 1068017280 22.31744 22.31744
## 17185      NA      NA      NA
## 17186 1486992820 17.74220 17.74220
## 17187      NA      NA      NA
```

```
##      gvkey      Date      Year      Ticker
## Min. : 1045 2013-12-31:1283 Min. :2006 ACGL : 33
## 1st Qu.: 7146 2012-12-31:1277 1st Qu.:2009 AET : 33
## Median : 14824 2014-12-31:1275 Median :2011 AFL : 33
## Mean : 50895 2011-12-31:1265 Mean :2011 AIZ : 33
## 3rd Qu.: 65556 2015-12-31:1253 3rd Qu.:2014 AMG : 33
## Max. :294524 2010-12-31:1222 Max. :2016 ANTM : 33
##      (Other) :9612 NA's :33 (Other):16989
##      Total_Assets      BV_per_share      Shares_Outstanding
## Min. :0.000e+00 Min. : -1489600 Min. :0.000e+00
## 1st Qu.:3.912e+09 1st Qu.: 8 1st Qu.:1.010e+08
## Median :9.538e+09 Median : 15 Median :1.973e+08
## Mean :4.725e+10 Mean : 5311 Mean :4.654e+08
## 3rd Qu.:2.632e+10 3rd Qu.: 27 3rd Qu.:4.344e+08
## Max. :2.573e+12 Max. :16297416 Max. :2.906e+10
## NA's :2568 NA's :9284 NA's :9188
##      Total_Liabilities      Market_Value      Share_Price
## Min. :0.000e+00 Min. :3.545e+06 Min. : 0.027
## 1st Qu.:2.135e+09 1st Qu.:4.445e+09 1st Qu.: 25.985
## Median :6.310e+09 Median :8.851e+09 Median : 43.180
## Mean :4.451e+10 Mean :2.166e+10 Mean : 57.339
## 3rd Qu.:1.865e+10 3rd Qu.:1.942e+10 3rd Qu.: 67.955
## Max. :2.341e+12 Max. :6.266e+11 Max. :1466.060
## NA's :7785 NA's :2764 NA's :10064
##      Book_Value      PBR1      PBR2
```

##	Min.	:-8.615e+10	Min.	:-687.634	Min.	:-687.634
##	1st Qu.:	1.313e+09	1st Qu.:	1.595	1st Qu.:	1.595
##	Median :	3.121e+09	Median :	2.626	Median :	2.626
##	Mean :	8.170e+09	Mean :	4.503	Mean :	4.503
##	3rd Qu.:	7.376e+09	3rd Qu.:	4.416	3rd Qu.:	4.416
##	Max.	: 2.416e+11	Max.	:1575.000	Max.	:1575.000
##	NA's	:9284	NA's	:10079	NA's	:10079

Chapter 6

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