

The nonclassical portion of f_{A_5} vanishes under the $7 \rightarrow 6$ collinear limit for any of the A_5 subalgebras of $\text{Gr}(4, 7)$. This is quite nice.

For D_5 things are more complicated. None of the 14 f_{D_5} s vanish in the collinear limit (from here on out I am implicitly referring not to the whole function but to the nonclassical portion). Let me start by taking my ‘base’ D_5 as

$$D_5^{(0,0)} = \frac{\langle 1234 \rangle \langle 1267 \rangle}{\langle 1237 \rangle \langle 1246 \rangle} \longrightarrow -\frac{\langle 1247 \rangle \langle 3456 \rangle}{\langle 4(12)(35)(67) \rangle} \longrightarrow \frac{\langle 1246 \rangle \langle 1345 \rangle \langle 4567 \rangle}{\langle 1245 \rangle \langle 1467 \rangle \langle 3456 \rangle} \begin{matrix} \nearrow -\frac{\langle 4(12)(35)(67) \rangle}{\langle 1234 \rangle \langle 4567 \rangle} \\ \searrow -\frac{\langle 1567 \rangle \langle 4(12)(35)(67) \rangle}{\langle 1267 \rangle \langle 1345 \rangle \langle 4567 \rangle} \end{matrix} \quad (1)$$

All other D_5 s appear as cyclic+flip images of $D_5^{(0,0)}$, which I’ll denote by

$$D_5^{(i,j)} = \sigma_{D_5}^i \circ \tau_{D_5}^j (D_5^{(0,0)}). \quad (2)$$

From here on out I’ll refer to $f_{D_5}^{D_5^{(i,j)}}$ simply by (i, j) . In this notation, we have

- $(3, 0) - (5, 1)$ vanishes in the collinear limit but is ill-defined term-by-term.
- $(0, 1) - (5, 0)$ vanishes in the collinear limit but is ill-defined term-by-term.

And the each of the remaining 10 D_5 s have nonzero and well-defined collinear limit individually. They can cancel off each other in 4 linearly independent ways, for example:

- $-(0, 0) - (1, 0) + (1, 1) + (4, 0) + (4, 1)$
- $-(0, 0) - (1, 0) + (1, 1) + (2, 0) + (4, 0)$
- $-(0, 0) - (1, 0) + (2, 1) + (3, 1) + (4, 0) - (6, 1)$
- $-(1, 1) + (6, 0)$