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18.01 Single Variable Calculus Fall 2006

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18:01 Solutions W practice questions (exami)

(1) a)
$$D_{ut}^{3t} = \frac{3lut - 3t + 2}{lu^2t} = \frac{3(lut - 1)}{lu^2t}$$

When $t = e^2$
 $lut = 2lue : = \frac{3(2-1)}{4} = \frac{3}{4}$

$$\frac{3u}{\tan 2u} = \frac{3u \cdot \cos 2u}{\sin 2u} = \frac{3u}{2\sin u\cos 2u}$$

$$= \frac{3}{2} \cdot \frac{u}{\sin u} \cdot \frac{\cos 2u}{\cos u} - \frac{3}{2} \cdot |\cdot|$$

c)
$$D \sin kx = k \cos kx$$

 $D^2 \cdot \cdot \cdot = k^2(-\sin kx)$
 $D^3 \sin kx = k^3(-\cos kx)$

$$\begin{bmatrix}
2 & \frac{1}{4x} \times^3 \\
\frac{1}{40} & \frac{1}{40} \times \frac{1}{40} \times \frac{1}{40} \times \frac{1}{40}$$

$$= \lim_{\Delta x \to 0} (x_0^3 + 3x_0^2 + x_0^3 + 3x_0^2) + (x_0^3 + 3x_0^2 + x_0^2) + (x_0^3 + 3x_0^2 + x_0^2) + (x_0^3 + 3x_0^2 + x_0^2)$$

$$= 3x_0^2$$

And: by defin $\frac{d}{dx} |x| = \frac{1}{3}x^{-\frac{1}{3}}$ And: by defin $\frac{d}{dx} |x| = \lim_{h \to 0} \frac{\sqrt{1+\alpha}x - \sqrt{1}}{h} = \lim_{h \to 0} \frac{\sqrt{1+\alpha}x - \sqrt{1}}{h}$ The correct answer is -1/3.

See details on next page.

$$\begin{array}{cccc}
(4) & (7)^2 & (4) &$$

(since cosy > 0 for -TV, &y <TV/2, choose the

E
$$f(x) = \begin{cases} ax+b, x>0 \\ 1-x+x^2, x\leq 0 \end{cases}$$

Continuous $\Rightarrow ax+b = 1-x+x^2, or b=1$
Diff. $\Rightarrow continuous and stone are = at 0:
 $a = -1+2x = 0$$

By implicit diffy:

$$2xy + x^2y' + 3y^2y' + 2x = 0$$

Sloye horizontal $= y' = 0$
 $= 2x(y+1) = 0$
 $= 2x(y+$

[7] tan line at
$$(x_0, y_0)$$
:
 $y-y_0 = f(x_0)(x-x_0)$ Iff $x-intincept$,
 $y=0$
 $y=0$

b)
$$\frac{dA}{dt} = A_0 e^{rt} \cdot (-r)$$

= $A_1 \cdot (-r)$
= $\frac{1}{4} \cdot (-r) = -\frac{r}{4}$.

Correction to #3

$$\lim_{x \to 0} \left(\frac{1 - \sqrt[3]{1 + x}}{x} \right)$$

Apply L'Hopital's Rule

$$= \lim_{x \to 0} \left(\frac{-\frac{1}{3(x+1)^{\frac{2}{3}}}}{1} \right)$$

Refine

$$= \lim_{x \to 0} \left(\frac{-1}{3(x+1)^{\frac{2}{3}}} \right)$$

Plug in the value x = 0

$$= \frac{-1}{3(0+1)^{\frac{2}{3}}}$$

Simplify

$$=-\frac{1}{3}$$