



18.03 | Spring 2010 | Undergraduate

Differential Equations



More Info

Readings

Listed in the table below are reading assignments for each lecture session.

[EP] refers to the course textbook: Edwards, C., and D. Penney. *Elementary Differential Equations with Boundary Value Problems*. 6th ed. Upper Saddle River, NJ: Prentice Hall, 2003. ISBN: 9780136006138

[SN] refers to the "18.03 Supplementary Notes" written by Prof. Miller.

[Notes] refers to the "18.03 Notes and Exercises" written by Prof. Mattuck.

Also listed are links to specially written $Java^{TM}$ applets, or <u>Mathlets</u>, that were used in the lecture session.

I. First-order differential equations

R1	Natural growth, separable equations	[EP]: 1.1 and 1.4
L1	Direction fields, existence and uniqueness of solutions	[EP]: 1.2 and 1.3 [Notes]: G.1 (PDF) [SN]: 1 (PDF) Isoclines Mathlet
L2	Numerical methods	[EP]: 6.1 and 6.2 [Notes]: G.2 (PDF) <u>Euler's method</u> Mathlet
L3	Linear equations, models	[EP]: 1.5 [SN]: 2 (<u>PDF</u>)
L4	Solution of linear equations, integrating factors	[EP]: 1.5 [SN]: 3 (<u>PDF</u>)
L5	Complex numbers, roots of unity	[SN]: 5 (PDF) [SN]: 6 (PDF) [Notes]: C.1-3 (PDF)
L6	Complex exponentials; sinusoidal functions	[SN]: 4 (PDE) [Notes]: C.4 (PDE) and IR.6 (PDE) Complex roots Mathlet Complex exponential Mathlet
L7	Linear system response to exponential and sinusoidal input; gain, phase lag	[SN]: 4 (PDF) [Notes]: IR.6 (PDF) <u>Trigonometric identity</u> Mathlet
L8	Autonomous equations; the phase line, stability	[EP]: 1.7 and 7.1 [SN]: Appendix A (PDF) Phase lines Mathlet

[SN]: Appendix C (PDF)

Linear vs. nonlinear

L9

II. Second-order linear equations

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L11	Modes and the characteristic polynomial	[EP]: 2.1, 2.2, and 2.3 up to "Polynomial Operators" [SN]: 9 (PDF)
L12	Good vibrations, damping conditions	[EP]: 2.3 and 2.4 <u>Damped vibrations</u> Mathlet
		[EP]: 2.6, pp. 157-159 [SN]: 7 (<u>PDF</u>) (for beats)
L13	Exponential response formula, spring drive	[Notes]: O.1 (<u>PDF</u>)
		<u>Harmonic frequency response: Variable input frequency</u> Mathlet
		[EP]: 2.6, pp. 165-167 [SN]: 10 (<u>PDF</u>)
L14	Complex gain, dashpot drive	[Notes]: O.1, 2, 4 (<u>PDF</u>)
		Amplitude and phase: Second order II Mathlet
	Operators, undetermined coefficients, resonance	[EP]: 2.5, pp. 144-153 and EP: 2.7
L15		[SN]: 8 (<u>PDF</u>)
		[SN]: 11 (<u>PDF</u>)
		[SN]: 14 (<u>PDF</u>) <u>Amplitude and phase: Second order II</u> Mathlet
L16	Frequency response	Amplitude and phase: First order Mathlet
		Amplitude and phase: Second order III Mathlet
L17	LTI systems, superposition, RLC circuits.	[SN]: Appendix B (<u>PDF</u>) <u>Series RLC circuit</u> Mathlet
	Engineering applications	[SN]: 12 (<u>PDF</u>) [SN]: 13 (<u>PDF</u>)
L18		[Notes]: O.3 (<u>PDF</u>)
III. Fo	urier series	
		[EP]: 8.1
L20		[SN]: 16 (<u>PDF</u>)
		Fourier coefficients Mathlet
L21	Operations on fourier series	[EP]: 8.2 and 8.3 Fourier coefficients: Complex with sound Mathlet
L22	Periodic solutions; resonance	[EP]: 8.3 and 8.4
L23	Step function and delta function	[SN]: 17 (<u>PDF</u>)
		[SN]: 18 (<u>PDF</u>)
L24	Step response, impulse response	[Notes]: IR (PDF)
	Convolution	[SN]: 18 (<u>PDF</u>) <u>Convolution: Accumulation</u> Mathlet
L25		Convolution: Flip and drag Mathlet
L26	Laplace transform: basic properties	[EP]: 4.1

L27	Application to ODEs	[EP]: 4.2 and 4.3 [SN]: 20 (PDF) [Notes]: H	
L28	Second order equations; completing the squares	[EP]: 4.5 and 4.6 [SN]: 20 (<u>PDF</u>)	
L29	The pole diagram	 [EP]: 4.4 [SN]: 22 (PDF) [SN]: 23 (PDF) 18.03 Difference Equations and Z-Transforms (PDF)(Courtesy of Jeremy Orloff.) Amplitude response: Pole diagram Mathlet Poles and vibrations Mathlet 	
L30	L30 The Transfer function and frequency response		
IV. First order systems			
L32	Linear systems and matrices	[EP]: 5.1-5.3 [SN]: 25 (<u>PDF</u>) [Notes]: LS.1 (<u>PDF</u>)	
L33	Eigenvalues, eigenvectors	[EP]: 5.4 [Notes]: LS.2 (PDF) <u>Linear phase portrait: Matrix entry</u> Mathlet <u>Matrix vector</u> Mathlet	
L34	Complex or repeated eigenvalues	[EP]: 5.4 [Notes]: LS.3 (<u>PDF</u>) <u>Linear phase portrait: Matrix entry</u> Mathlet	
L35	Qualitative behavior of linear systems; phase plane	[SN]: 26 (<u>PDF</u>) <u>Linear phase portrait: Matrix entry</u> Mathlet <u>Linear phase portrait: Cursor entry</u> Mathlet	
L36	Normal modes and the matrix exponential	[EP]: 5.7 [Notes]: LS.6 (<u>PDF</u>)	
L37	Nonlinear systems	[EP]: 7.2 and 7.3 [Notes]: LS.6 (<u>PDF</u>)	
L38	Linearization near equilibria; the nonlinear pendulum	[EP]: 7.4 and 7.5 [Notes]: GS (PDF) [SN]: Appendix B (PDF) [SN]: Appendix C (PDF)	
L39	Limitations of the linear: limit cycles and chaos	<u>Vector fields</u> Mathlet	



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