

# CSE310 Lecture 1 Notes

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## The Sorting Problem - Formal definition

Sorting problem:

- Input: a sequence of  $n$  numbers  $\langle a_1, a_2, \dots, a_n \rangle$ .
- Output: a permutation (reordering) [of the input]  $\langle a'_1, a'_2, \dots, a'_n \rangle$  such that  $a'_1 \leq a'_2 \leq a'_n$

## Insertion Sort: Analogy to storing cards...

There may be many ways to sort cards, but one intuitive procedure is to always insert a card into the right place.

- Works naturally when you draw a stack of cards one-by-one and put them into your hand.
- Similarly, if you sort all cards in your hand  $\rightarrow$  "*in place*" sorting

## Computationally represent the procedure

Pseudocode: Liberal user of English; Use of indentation for block structure; Omission of error handling (e.g. check if an array is empty).

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```
// Pseudocode for insertion sort

INSERTION-SORT(A)
for j=2 to A.length // A.length=n
    key = A[j]
    // Insert A[j] into sorted sequence A[1...j-1]
```

```

i=j-1
while i>0 and A[i]>key
    A[i+1] = A[i]
    i=i-1
A[i+1]=key

```

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Example:

3	9	6	1	2		9 should be inserted after 3 - no change
3	9	6	1	2		6 should be inserted between 3 and 9
3	6	9	1	2		1 should be inserted before 3
1	3	6	9	2		2 should be inserted between 1 and 3
1	2	3	6	9		sorted array

### Analysis of the Insertion-sort algorithm

When we analyze an algorithm, we mainly focus on the performance (running-time). The running time of the algorithm depends on various factors' success.

- depends on the nature of the input (already sorted vs. reverse sorted)
- depends on the size( $n$ ) (6 vs  $10^6$  elements)  $\rightarrow$  parameterized running time.
  - $T(n) = \leftarrow$  function of the size ( $n$ ).

Different kinds of running time analysis:

- Worst-case.
  - Max time on the input size  $n$  given an upperbound guarantee to the user.
- Average case.
  - expected time over all possible input
    - \* running time of every input and find the average. We need to know the probability of each input  $\rightarrow$  Input  $\times$  probability of that input = weighted average.
  - we don't know the exact probability, therefore, we make assumptions
    - \* all inputs are equally likely – uniform distribution.
- Best case
  - works on some inputs only, no guarantee to the user.

Next question: how to eliminate hardware dependency from running time.

- parameterize the running time based on the input size and then give the growth of the running time rather than giving absolute value.  $\rightarrow$  asymptotic analysis (notation)

Asymptotic Notation:

- ignore machine dependent constants
- observe the growth of the running time.

One of the commonly used notation in the asymptotic notation is the  $\theta$  notation.

$\theta$  notation:

- drop lower order terms and ignore constants
  - $T(n) = 3n^3 + 50n^2 + n + 600$ 
    - \* drop  $50n^2 + n + 600$
    - \* ignore 3 in front of  $3n^3$
  - $T(n) = \theta(n^3)$
- this means when  $n \rightarrow \infty$   $\theta(n^3) > \theta(n^2)$