	Interenze in Gistorder logic
Note Tit	le
	Topies today: (1) Substitutions Jaked closely or
	6) Propositionalization (textsook 9.1)
	not based on textsoll, 3 Generalized Modry Ponens Islumed 9.2.1
	but still [(4) Conjunctioners and decidability of POL - arithmetic
	(600) 190
	Course
	Susstitutions
	Notation for susstitutions:
	· { MA, y(B, z C)
	means replace or with A, y with B, 2 with C.
	· SUBST ({XL/A}, d)
	means replace x with A in sertence of.
	examples: - Susst (x/John, y/Mother (John)), Knows (x)y)
	becomes do as exerise
	- Surst ({x/z, y/z}, Knows (x,y)) becomes do as exercise
	becomes do as exerise

2	Propositiona lization
	Reall that a major institution for introducing FOL was that PL required too many facts
	was that PL required too many facts
	PL: (CSMajor (Davielle) For fact for every Strellet (SMajor (Chris)
	OI
	Cs Major (Chrs)
	GOL: Yr CSMajor (rc)
	But, we can go back the other way it desirest.
	ie-transform from Gol to PL by
	alia alia com l'éca mal l'acide
	eliminating quantifies and variables.
	This requires application of two obvious mes:
	UI (Universal Instantiation)
	For any variable V and ground term g and sentence d:
	a term with no variables
	₩ x x
	SUBST ({V/g}, A)

Example: Objects are students in this class.

Nelation CSMajor(11), function ProjectPartner (11) Unalledge base is: Yrc CsMajor(rc) Then we can use UI to add any or all of the following to the KB: CSMajor (Omar)
CSMajor (Sam)
CSMajor (ProjectPartner (Omar))
CSMajor (ProjectPartner (ProjectPartner (Omar)) Gxistential Instantiation (EI) For any sentence of, variable v, and constant symbol k that does not appear elember in the knowledge base SUBST ({V/k}, a) Example: Similar scenario to last example, Objects are students, this class.

Nelation (SMajor(14), Relation (spojet Pather (x,y) Cnot the same as the function

in the earlier example.

Art now suppose entire KB is:
CSMajor (Omar) CSMajor (Justine) For Astronomy Minor (21) For IsProjectPartner (Justine, 22) **The strong Minor (21) **The strong Minor (21)
CSMajor (Justine)
Joc Astronomy Minor (21)
7 x (sprojectPartner (Justine, x) - X
Applying GI to A we can add to the KB:
Aftionomi (Someone)
(3(L) 13 JM (
or even:
Astronomy Minor (Cole) = laser here.
[M. q Nt Not
but not: Action My (Tack) le the (real)
Astronomy Mahar (Justine) Cole
(nt what if Justine were an Astronomy minor? Statement (++) covers that! (Justine) and Someone, can refer to
minus! Statement (++) covers that!
Unitile and someone an reter to
the same object.
Applying EI to (*) we can odd to the KB:
(D) 0.+0 1 (T)
(strojentPatrer (Justine, Someonel)
SProject Partner (Justine, Glez) Euly is it OK? see comments above
151/ojat Vartner (Oustine, Colet) Why is it of some see comments above
Jee w

Remark the above rules can convert any KB from
FOL to PL. Then we can apply our PL
resolution technique to infer entailment. But there are
two problems:

(1) KB and become very big. It's better to do
inference within For rather than converting to PL.

The textbook explains has to do this (e.g. there
is an For version of resolution in Section 9.5)
but we don't study it.

(2) Functions lead to infinitely many possible substitutions e.g. Father (X), Father (Father (X)), Father (Father (X)))

etc.

In practice this means that

- any entailed sentence can be proved
- we cannot, in general, prove that a sentence is not entailed.

anoting from textsook p325:

The question of entailment for first-order logic is semidecidable — that is algorithms exist that say yes to every entailed sentence, but no algorithm exists that also says no to every nomentailed sentence."

	Generalized Modes Ponens Stripped
3)	Generalized Modes Ponens SIG ME
	We study this example of a useful interence me in
	We study this example of a useful interence me in FOL. Nevall the PL verim:
	$(\alpha, \alpha \Rightarrow \beta)$
	B
	The Fol version is:
	Given otomic sentences Di, Di', a and a culstitution O
	Given odomi sentences pi, pi, q and a substitution of such that Sussit (o) pi') = Subst (o, pi),
	$\rho', \rho', \dots \rho', \qquad (\rho_1 \wedge \rho_2 \wedge \dots \wedge \rho_n \Rightarrow q)$
	proposition of proposition of the proposition of th
	SUBST (O, q)
	Example Same scenario as earlier, but with ICB:
	Hrs, ty Projlather (x,y) => Projlather (y, 1c) Projlather (Over, Justine)
	Proj Pathner (Omar, Justine)
	Take P' = Porta Arac (Durar, Justine)
	Take Pi = Paglather (Donar, Justine) Pi = Projlather (Donar, Justine) Or = Six (Onnar, Justine)
	19 = Syl Omas (Justine ?

Skipped ProjPartner (Justine, Omar) to the KB. Summary of completeness and decidability for PL, FOL, arithmetic - See next page for summary - definition of complete: every valid statement has - definition of decidable: there exists an algorithm that decides whether a given statement is valid

