Functional forms and Scheme implementation

Today: **[A]** Functional forms: 1. Basics

2. Currying

[B] Scheme implementation: 1. dotted pairs, 2. dynamic typing, 3. memory allocation, 4. lazy evaluation.

① Functional forms

Functional forms are functions that use other functions as parameters or return values. You need to know common examples including:

- compose
- map
- apply

See textbook 696-698 for compose and map, and read builtin documentation for apply.

② Currying

Given a function of 2 or more variables, we can transform the function into a sequence of functions that have only one argument each.

This is called currying

e.g.   say $f(x,y) = x^2 + y$.

Define   g to be a function that takes x as input, and outputs a function of one variable:

$g(x) = $ the function that accepts y as input and outputs $x^2 + y$.

In scheme:

(define (f x y) (+ (* x x) y)))

(define (g x)
       (lambda (y) (f x y))

Then ((g x) y) is equivalent to (f x y)
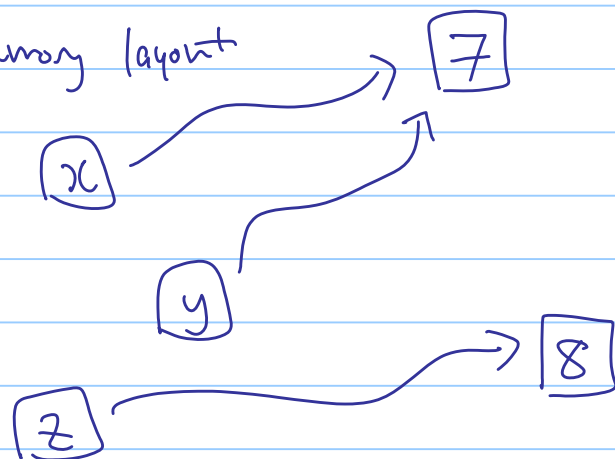
Scheme implementation

1. Pairs, and dotted pair notation

All values in scheme are pointers to objects.

e.g.
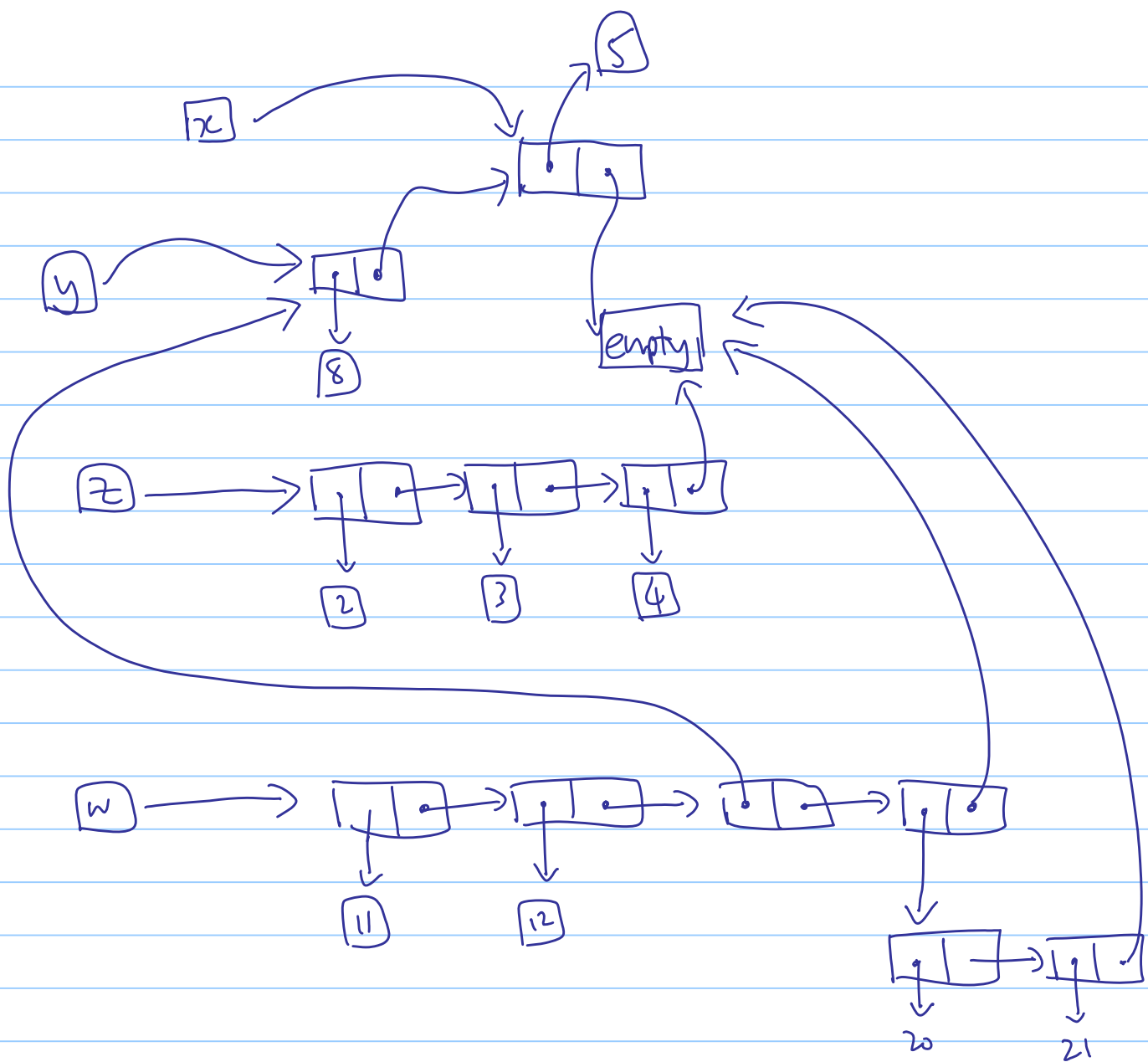(define x 7)
(define y 7)
(define z 8)

gives the memory layout

A pair is a record (think of it as a struct) containing two pointers. By definition, car returns the first pointer and cdr returns the second pointer; cons creates pairs.

e.g.
(define x (cons 5 empty))
(define y (cons 8 x))
(define z (list 2 3 4))
(define w (list 11 12 y (list 20 21)))

gives the memory layout:

Pairs are often represented in dot notation — the 2 elements of the pair are parenthesized and separated with a dot

e.g. x is   (5 . empty)

y is   (8 . (5 . empty))

z is   (2 . (3 . (4 . empty)))

w is

$$\left(11 \cdot \left(12 \cdot \left(\left(8 \cdot (5 \cdot empty) \right) \cdot \left(20 \cdot (21 \cdot empty) \right) \right) \right) \right)$$

2. Is Scheme typed, or not?

All the symbols in Scheme have the type "pointer to anything".

Every object that is pointed to does have a type, which could be integer, rational, floating point, list etc..

So, Scheme does have types, and they are checked at run time, not compile time.

(This approach is known as dynamic typing.)
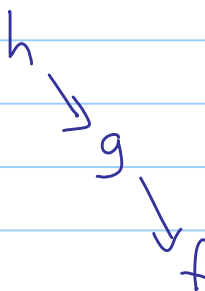
3. How is memory allocation handled?

everything is automatically allocated on the heap, and automatically garbage-collected when there are no more references.

4. Strict vs lazy evaluation

Scheme (and most other languages) use <u>strict</u> evaluation:
function arguments are evaluated <u>before</u> the function itself
is evaluated.

e.g. $(f \quad 3 \quad (g \; (h \; 2) \; 5) \quad 6 \quad (p \; 3))$

order of evaluation is

← p could be before
or after h, g, but
must be before f.

Lazy evaluation works the opposite way

e.g.
```
(define  (g x)  (... save long and complex calculation ))
(define  (h x)  (+ x 5))
(define  (f x y z)
    (if  (= x 9)  (+ z x)
        (* y x))
```

<u>If</u> lazy evaluation were used, then the expression

$$(f \; (h \; 4) \; (g \; 6) \; (h \; 7))$$

would be evaluated as:

1. begin evaluating f
2. inside the 'if' statement, we need (h 4),
   so begin evaluating h. This returns 9.
   Therefore we need '(+ z x)' — so we
   need (h 7). Evaluate that, returning 12.
   So we can return 9+12 = 21 as the
   value of f.

Note that the expensive function g was
never evaluated, because it wasn't needed!
Thus lazy evaluation can improve efficiency
   (but it also imposes extra costs.)

Summary of above example:

order of function evaluation

	strict	lazy
(f (h 4) (g 6) (h 7))	h, g, h, f	f, h, h
(f (h 1) (h 3) (g 2))	h, h, g, f	f, h, h, h
(f (h 1) (g 2) (h 3))	h, g, h, f	f, h, g, h

arbitrary order