Resolution and SAT-solving	
Topics today! () Inference rules (2) Negolution rule (3) Negolution algorithm (4) SAT-solvers	
(1) Inference mes) A knowledge large (ICR) is a cet of Resterace of that are	
Inference mes A knowledge lare (ILB) is a set of sentences that are known to be true. (We can combine KB into a single sentence using 1). e-q- KB = S P, P= Q, 7R, SnT?	
[same as KB= { P ~ P=)Q ~ ~ ~ R ~ SAT }	
Can add to KB wishy inference meg:	
e-y. "and elimbotion": if MnB EKB, can add & to KB Notadiun: anB	<u>`</u> .
exercise: apply to above KB	
"modus ponens": if LEKB and L=)BEKB, can add B to KB	
Notation: α , $\alpha = \beta$	
exercise: apply to above KB	
"regolation": see next rection	

(1)	The Negolutan inference me
	Oarl by San San San
	Resolution is an important inference rule.
	Basic idea is that apposite literals in separate clauses concel each other ant, yielding a combined clause.
	eg-Pra, Rv-a yrells PrR
	comsine
	√ carcel √
	PIQUARUS, QURUTIVAL
	comstie
	yields PVQVSVTV7U
	Exercise: Apply regulation to the KB
	Exercise: Apply regolution to the KB {PV-Q, ¬PVRV-S, SVT}
	The resolution rule is inportant because it can be used as part of an algorithm that infers entailment. i.e. it decides whether ICB = or for any ICB, or.
	re. it devides whether ICB = a for any ICB, a.
	We study this rest.

Our simple resolution algorithm for entailness We want to determine whether KB Fd.

Equivalently, is KB =) & valid?

Equivalently, is KB =) & unsatisfiable? Algorithm: - Convert KB 17x to CNF
- Apply resolution guaranteed ... terminate If you ever get an enoty clause, conclude that ICB = a . Part Chas a - If can't make any more clauses, conclude that ICB IF a. sterdy Why? Became you've derived the expty clause, equiv to False, nearing 140 nd is unsatisfiable Why? Becanse you can now satisfy KB 170 Netailed proof in book (not regling) Sut basicelly just fill in the values) Gxerise: ILS = { P => Q , Q V R V S , S => P V Q } (i) Does KB entail QVR? (ii) Does KB entail 12~5?

4	Efficiency of SAT-solvers	
(Note that the resolution algorithm above is just a particular method of determining satisfiability, also known as SAI-solving.	
	Satisfiability (or just "SAT") is of central importance in the theory of algorithms. It was the first problem to be proved NP-complete, in the early 1970s.	
	i.e. polynomial time	
	-> wears: no efficient algorithm is known	
	to solve all instances	
	. If we did find an efficient alg,	
	that alg would solve most	
	other "hard" poslens in CS	
	· therefore, efficient alg for all	
	instances probably doesn't exist.	
	(nont case)	
_	So, our resolution algorithm takes hexponential fine	
	So, our resolution algorithm takes hexponential fine (in the number of variables and/or clauses)	
	Better algorithms are Known (e.g. Davis-Putnam),	
	Better algorithms are known (e.g. Davis-Putnam), but still exponential in the nort case	
	Still, "modern solvers hardle problems with tens of millions of variables" - see last paragraph of Look 7.6-1, p262.	
	ot variables - See last paragraph of book 1.6-1, plac.	

- An interesting special case where a lite solution exists: if the KB consists a	neer time
solution exists: if the KB consists a	empletely of
Horn danses	
eg. 7BV7CVD	ositive literal
eq. 7BV7CVD,	7 PV7Q
J ,	