

CMPE 102

Programming Logic and Design

Module 7

Python's Pre-defined Function

Outline

- Subroutine concept
- Built-in functions and standard modules
- Composition
- Defining functions
- Parameters and arguments
- Seeking and providing help

What are subroutines?

- A subroutine is a sequence of one or more actions grouped into a single task
 - The task won't be performed until the subroutine itself is used



This button won't do anything until it is pushed

- Subroutines are also known by other names, like

subroutines

methods

functions

procedures

Have you seen Python functions?



- Yes, you have

```
print(82+64+90+75+33)
```

argument

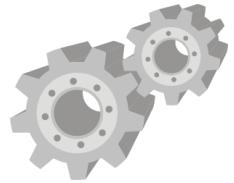
```
print('Hello')
```

Some functions may contain no argument

```
val = input()
```

- These are parts of the Python's *built-in functions*—they are readily available to use
- Functions are always followed by parentheses
- Within parentheses, it contains *arguments* of the function
 - A function may have no argument or 1 or more argument

Essential built-in functions

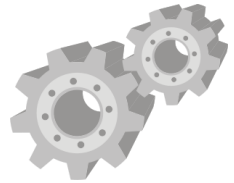


- Some examples of built-in functions:

<code>abs()</code>	<code>float()</code>	<code>input()</code>	<code>int()</code>
<code>len()</code>	<code>list()</code>	<code>max()</code>	<code>pow()</code>
<code>print()</code>	<code>range()</code>	<code>round()</code>	<code>sum()</code>
<code>type()</code>			

- No need to remember all of these now
 - We will eventually learn how to use them later
- For each function, you need to learn how to use it, i.e. what argument(s) to send

Function — How does it work?

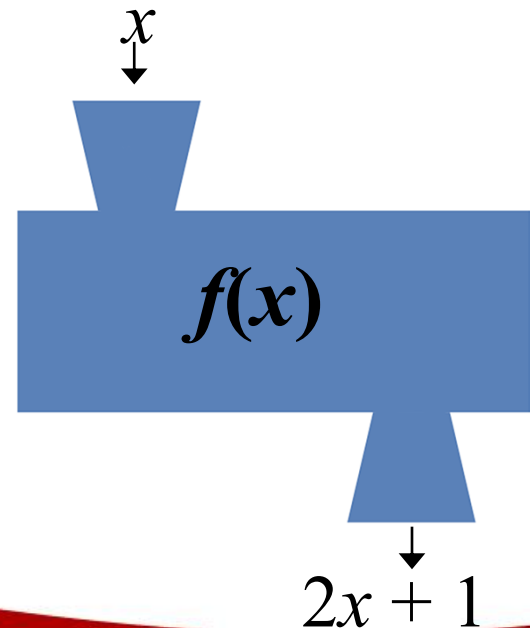


- Function usually has *input(s)* and/or *output(s)*
- For example, in math, suppose you have a function $f(x)$ defined as follow

Note: This one is math, not Python!

$$f(x) = 2x + 1$$

- This means
 - x is an input to the function $f(x)$
 - The function produces a result

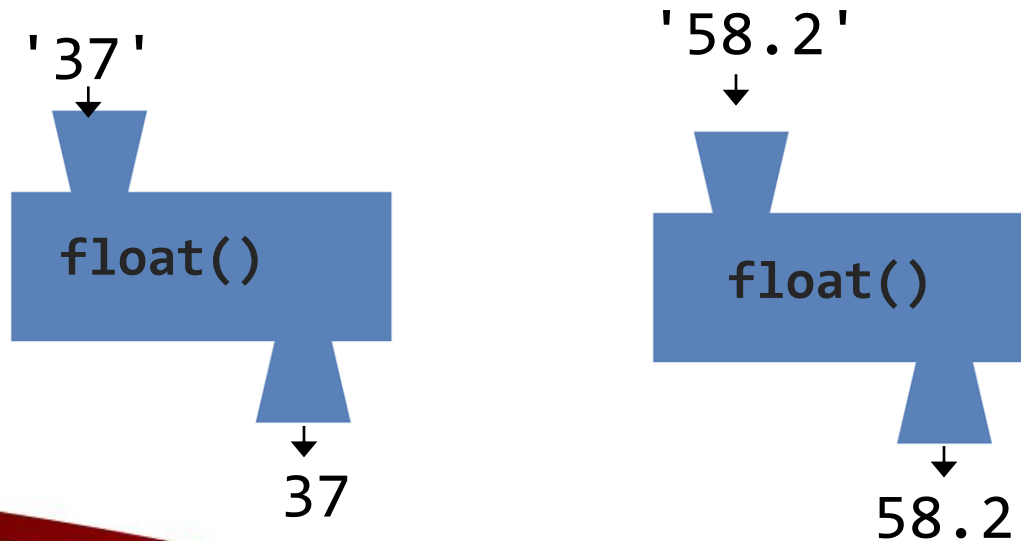


Calling a Function



- In Temperature Conversion task, we *call* the function `float()` to convert a string to a number

```
celsius_str = input()  
celsius = float(celsius_str)
```



Task: Phone Bill



- Long-distance rate for a domestic call is Php 2/minute, while a fraction of a minute is charged as a whole minute
- For example
 - 1-minute call → Php2
 - 3-minute call → Php5
 - 5.2-minute call → Php12
- Write a program that
 - asks the user how many seconds is used for the call
 - then computes the total charge for the call



Phone Bill - Ideas

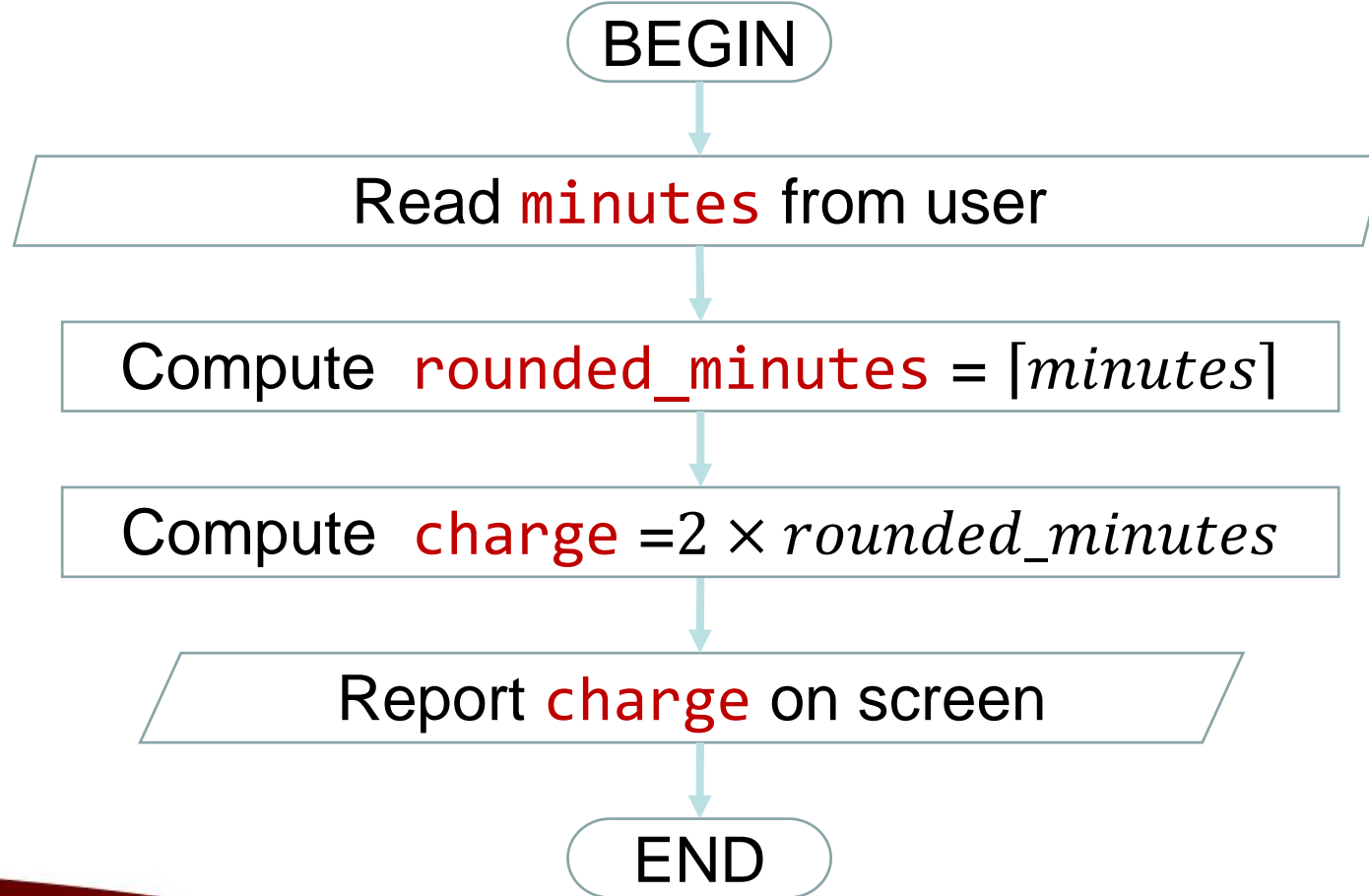
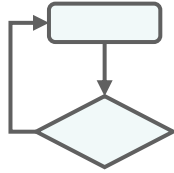


- At first, the problem looks like a typical division problem
- However, the fraction of the result must not be discarded this time, but will be rounded up to the nearest integer
 - E.g., 3 is rounded up to 3, while 3.1 is rounded up to 4
- Let x represent the call length in minutes; we want to know ***the smallest integer that is larger or equal to x***
- Mathematically, we are computing

$\lceil x \rceil$

this is called
'the ceiling of x '

Phone Bill – Steps



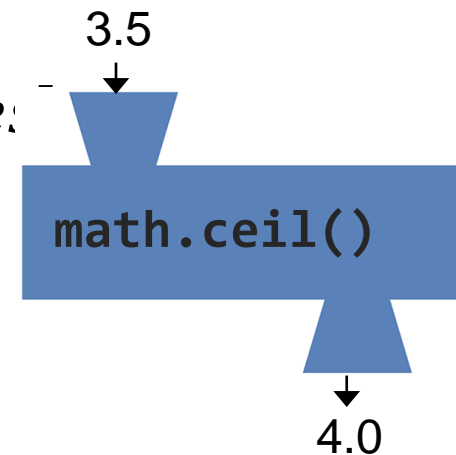
Phone Bill – Program



```
1: import math
2: minutes_str = input('Enter call length in minutes: ')
3: minutes = float(minutes_str)
4: rounded_minutes = math.ceil(minutes)
5: charge = 2*rounded_minutes
6: print(f'Charge is {charge:.2f} Pesos.')
```

- `import math` imports the *math module* that contains additional mathematical functions
- Line 3, the expression is evaluated to `[minutes]`

`math.ceil(minutes)`



Math Module



- In addition to built-in functions, Python provides many mathematical functions and constants in the ***math*** module
- Some common functions and constants are:

Expression	Evaluated to	Remark
<code>math.ceil(x)</code>	$\lceil x \rceil$	compute smallest integer larger or equal to x
<code>math.floor(x)</code>	$\lfloor x \rfloor$	compute largest integer smaller or equal to x
<code>math.cos(x)</code>	$\cos(x)$	compute cosine of angle x in radians
<code>math.sin(x)</code>	$\sin(x)$	compute sine of angle x in radians
<code>math.degrees(x)</code>	$180x/\pi$	convert angle x from radians to degrees
<code>math.radians(x)</code>	$x\pi/180$	convert angle x from degrees to radians
<code>math.sqrt(x)</code>	\sqrt{x}	compute square-root of x
<code>math.pi</code>	π	yield the value of π (approx.3.14159)
<code>math.e</code>	e	yield the value of e (approx.2.71828)

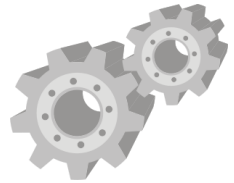
Math Functions: Examples



```
>>> import math
>>> math.fabs(-12.34)
12.34
>>> math.ceil(3.29)
4
>>> math.floor(3.29)
3
>>> math.cos(math.pi/4)
0.7071067811865476
>>> math.pow(5, 3)
125.0
>>> math.sqrt(2)
1.4142135623730951
```

```
>>> import math
>>> math.exp(1)
2.718281828459045
>>> math.log(4)
1.3862943611198906
>>> math.log10(100)
2.0
>>> math.log(8, 2)
3.0
>>> math.pi
3.141592653589793
>>> math.e
2.718281828459045
```

Two ways of importing



- Importing a module as a whole
 - Names inside are accessed via the module name

```
import math  
value = math.cos(math.pi/2)
```

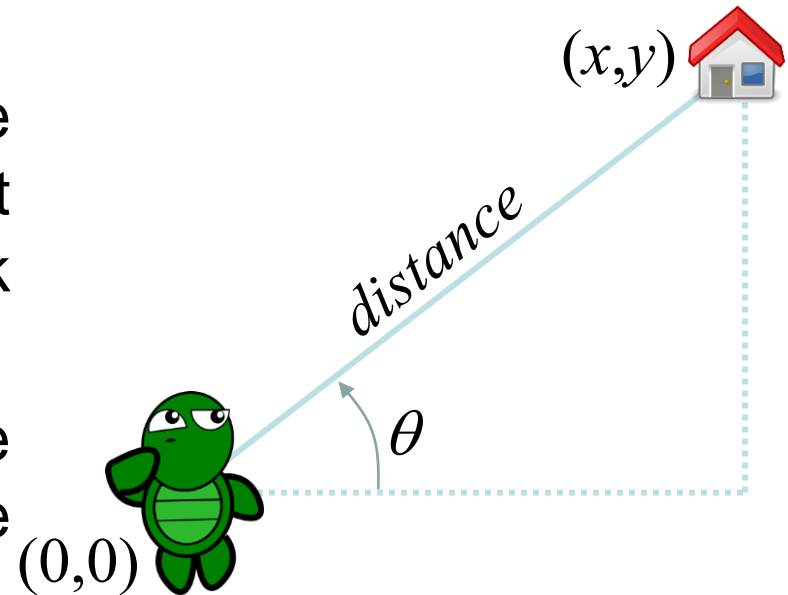
- Importing only specified names inside a module
 - These imported names can be used directly

```
from math import cos, pi  
value = cos(pi/2)
```

Task: Bring Turtle Home



- Our little robotic turtle is lost in the field. Please help guide him from his location at $(0,0)$ to his home at (x,y)
- He cannot walk very fast, so we must head him to the right direction so that he can walk with the shortest distance
- Write a program to take the values x and y , then report the values of θ and *distance*



Bring Turtle Home - Ideas



- Again, we need to analyze the relationship among all the variables to solve the two unknowns

- From Pythagorean theorem

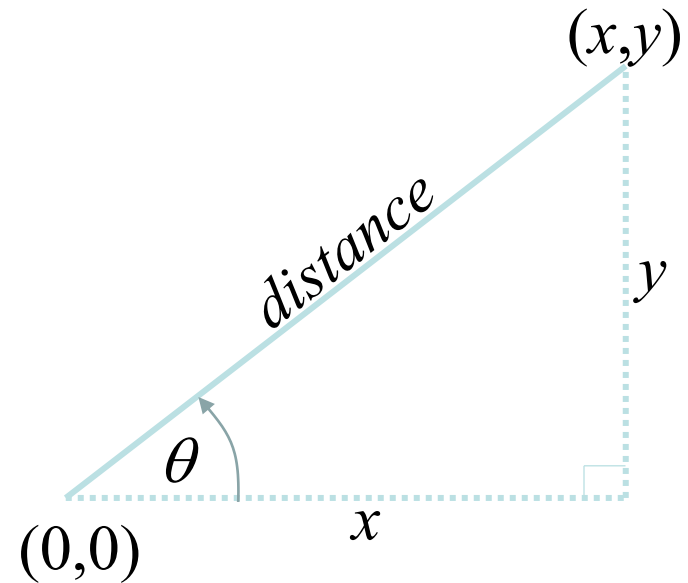
$$\text{distance}^2 = x^2 + y^2$$

- And from Trigonometry

$$\tan \theta = \frac{y}{x}$$

- Therefore,

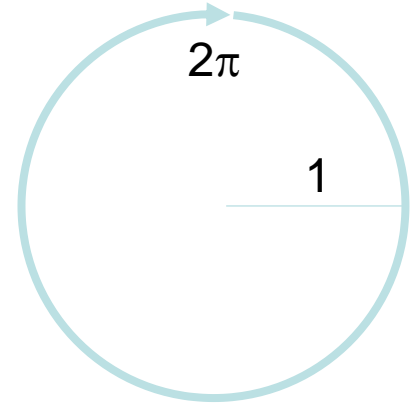
$$\text{distance} = \sqrt{x^2 + y^2} \quad \text{and} \quad \theta = \arctan \frac{y}{x}$$



Caveats – Radians vs. Degrees



- In most programming languages, the unit of angles used by trigonometry functions is ***radians***, not degrees
- A full circle, 360 degrees, is 2π radians
- In Python, we can use `math.radians()` and `math.degrees()` to convert between radians and degrees



```
>>> math.degrees(math.asin(1))  
90.0
```

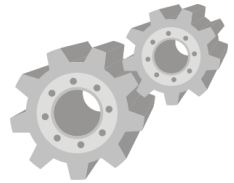
Bring Turtle Home – Program



```
import math

x = float(input('Enter x: '))
y = float(input('Enter y: '))
distance = math.sqrt((x*x) + (y*y))
heading = math.degrees(math.atan(y/x))
print(f'Heading: {heading:.2f} degree')
print(f'Distance: {distance:.2f} units')
```

Composition



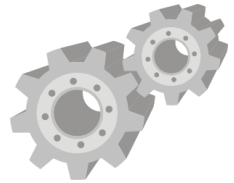
- Some functions *return* a value, which can be used as part of an expression and/or an argument of another function
- As part of an expression:

```
rounded_minutes = math.ceil(minutes)  
charge = 2*rounded_minutes
```



```
charge = 2*math.ceil(minutes)
```

Composition



- Function that has a value can also be part of an argument of another function:

```
minutes_str = input('Enter call length in minutes: ')\nminutes = float(minutes_str)
```



```
minutes = float(input('Enter call length in minutes: '))
```

From now on, we will write input statement this way when reading a number

Task: Savings Account



- When you have a savings account, the bank usually deposits interest back into your account every year
- You would like to know how much money you will have after a certain number of years
- Write a program that
 - lets user input the principal, rate (%), and years
 - outputs the amount you will have after the specified number of years



Savings Account - Ideas

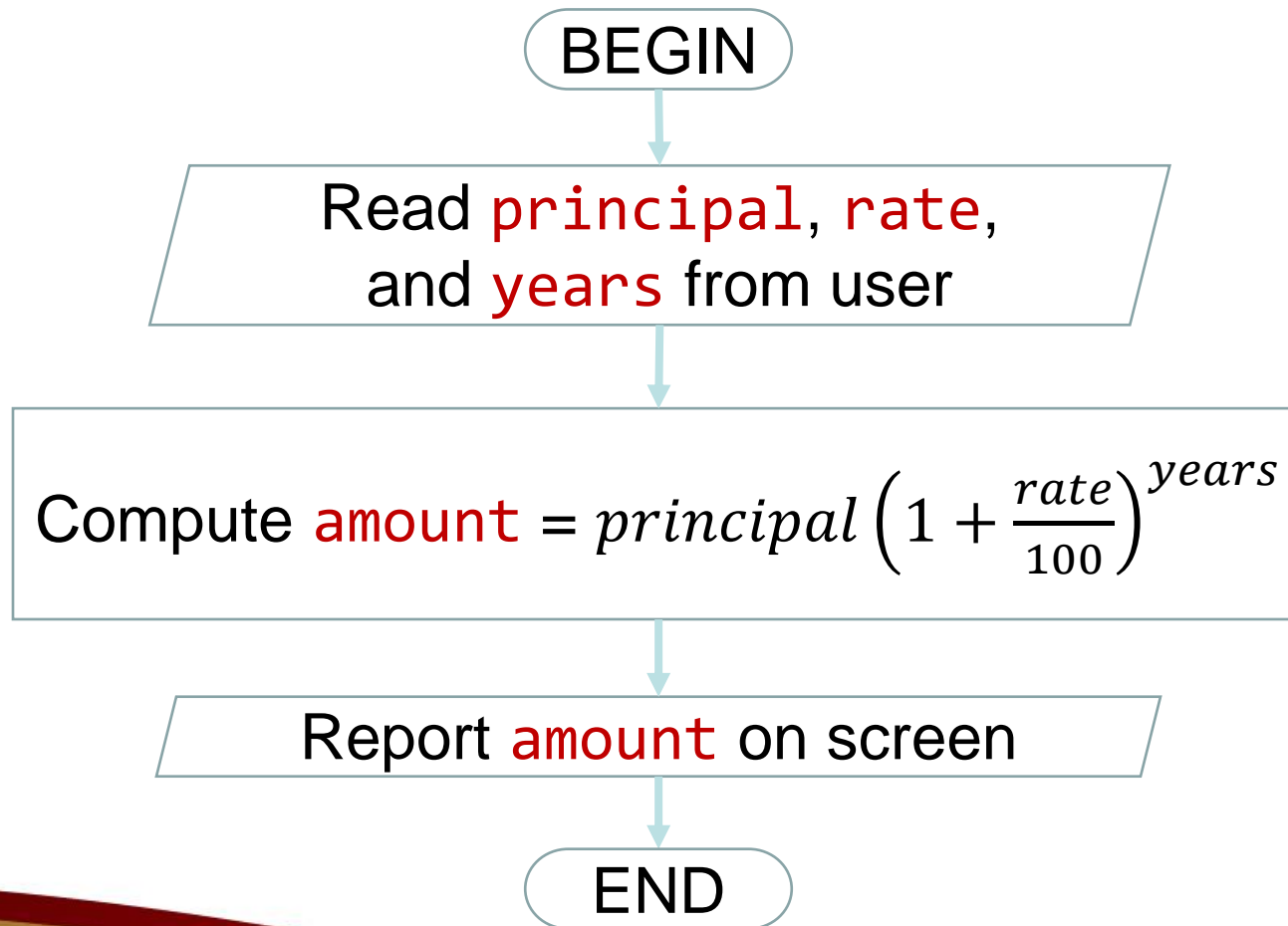
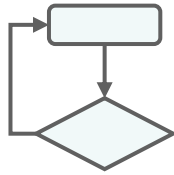


- Let us analyze the relationship among the amount in the account, principal (p), rate (r), and years (n)

Year	Amount
0	p
1	$p \left(1 + \frac{r}{100}\right)$
2	$p \left(1 + \frac{r}{100}\right) \left(1 + \frac{r}{100}\right) = p \left(1 + \frac{r}{100}\right)^2$
3	$p \left(1 + \frac{r}{100}\right)^2 \left(1 + \frac{r}{100}\right) = p \left(1 + \frac{r}{100}\right)^3$
:	:

- It follows that on n^{th} year, the amount will be $p \left(1 + \frac{r}{100}\right)^n$

Savings Account – Steps



Savings Account – Program



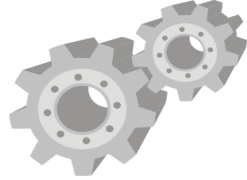
```
import math
```

```
principal = float(input('Principal (Baht): '))  
rate = float(input('Rate (% per year): '))  
years = int(input('Time (years): '))  
amount = principal * math.pow(1 + rate/100, years)  
print(f'Amount: {amount:.2f}')
```

Same as:

$(1 + \text{rate}/100)^{\text{years}}$

Defining your own function



- Python lets you *use* and also *define* functions
- We *group* up a number of statements/computations and then we *give them a name*
 - This enables reuse of these statements (just like we use built-in functions)
- Using your own functions, program is:
 - shorter by eliminating repetitive codes
 - easier to understand
 - less error-prone
- If a change is needed, make it in one place

A Simple Function Definition



- Functions must be defined before use

def is the keyword that means:
I am **defining** a function

Name of your defined
function:
follow the naming rules

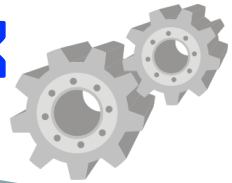
```
1: def my_hello(name):  
2:     print(f'Hello, {name}.')  
3:  
4: my_hello('Jon Snow')
```

Parameters of your
defined function (as
many as you need)

Statement in your
defined function

Your program that calls
your defined function

Function Declaration Syntax



Function
Name

0 or more parameter
names

header

```
def function_name(...):
```

body

```
    ...  
    ...  
    statements  
    ...
```

Very important

Spaces in front of every statement must be the same



Task: Circle Area

- Program will ask the user to input the radius value of a circle, calculate the circle's area, and then print the resulting circle's area to screen.

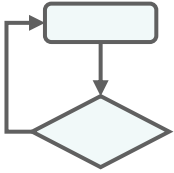


Circle Area - Ideas

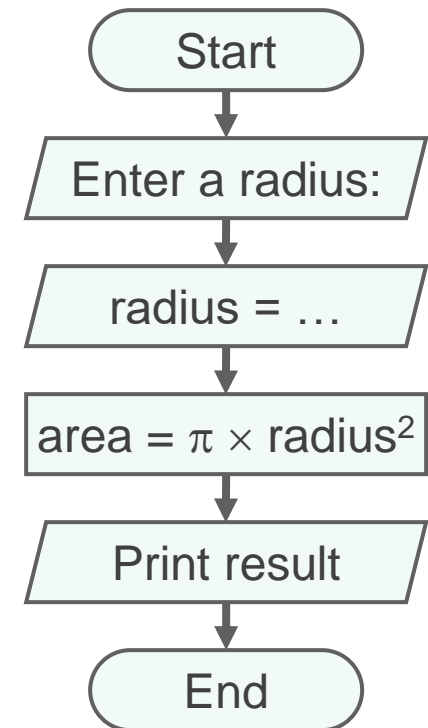


- Need to know what is the radius of the underlying circle
- Compute the circle's area
 - $\text{area} = \pi \times \text{radius} \times \text{radius}$
- Show the result to screen

Circle Area - Steps



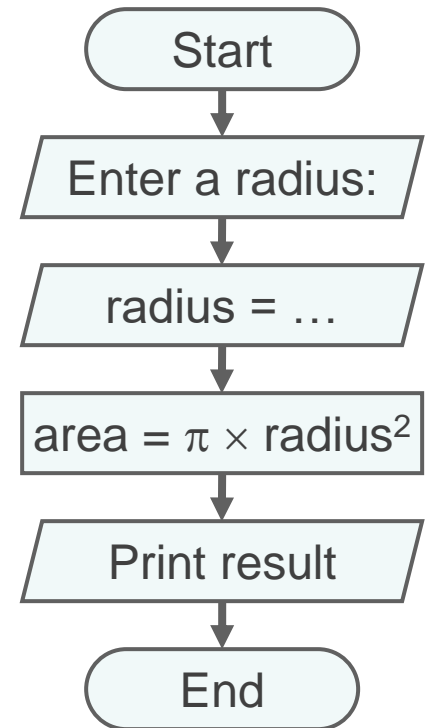
- Tell user to input the radius to the program
- Get input radius from the user
- Calculate the Area
 - $\text{area} = \pi \times \text{radius} \times \text{radius}$
- Print the resulting Area
- Pause the screen



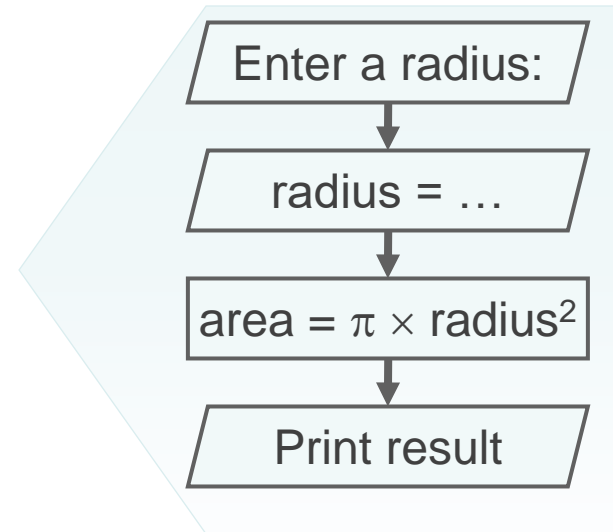
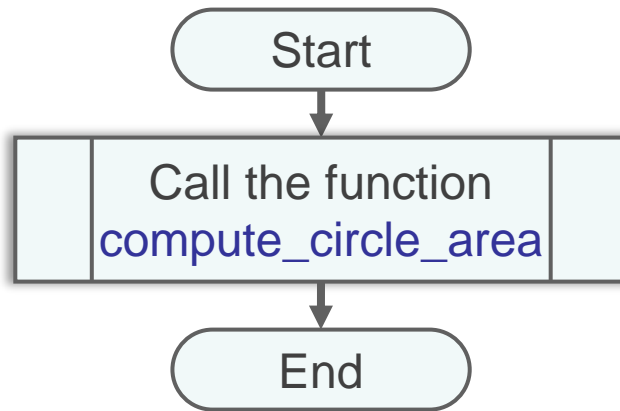
Circle Area – Program#1



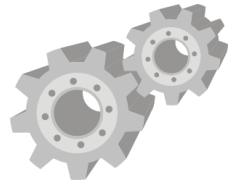
```
1: radius = float(input('Enter a radius: '))
2: area = math.pi*radius**2
3: print('Area of a circle with radius
      {radius} is {area:.2f}')
```



Circle Area – Program#2



```
1: def compute_circle_area():
2:     radius = float(input('Enter a radius: '))
3:     area = math.pi*radius**2
4:     print(f'Area of a circle with radius {radius} is {area:.2f}')
5:
6: compute_circle_area()
```

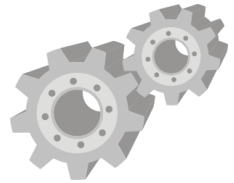



Function Names

- Follow the conventions for creating an identifier

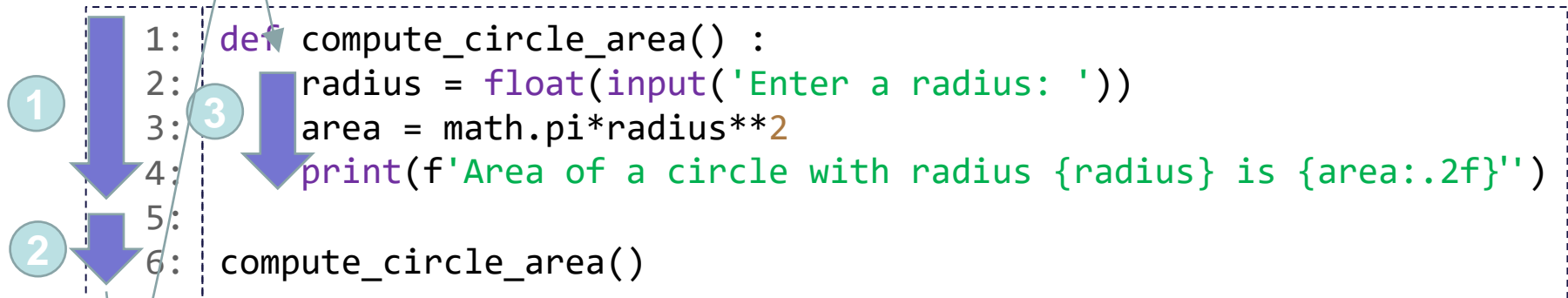
```
def compute_circle_area():  
    ...  
}
```

- Examples:
 - calculate_sales_tax()
 - assign_section_number()
 - display_results()
 - convert_input_value()



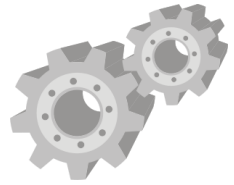
Flow of Execution

- When executing the following program:



1. Function `compute_circle_area()` is defined
2. Main part of user program—calling `compute_circle_area()`
3. Statements within the function are executed

Returning a Value



- Function can *return* a value
- Recall a built-in function—`float()`

```
celsius = float('35')
```

- `float('35')` returns a value that equal to 35.0
 - In other words, the term `float('35')` is equal to 35.0
- You can write your own function that returns a value
 - Requires *return* keyword

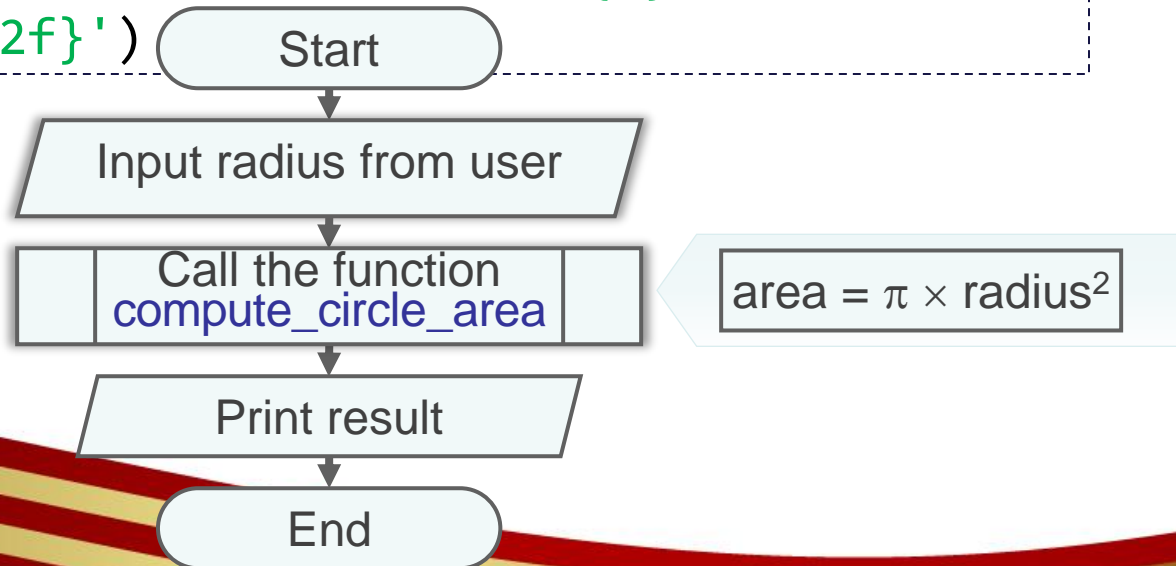


Circle Area – Program#3

```
1: def compute_circle_area(radius):  
2:     circle_area = math.pi*radius**2  
3:     return circle_area  
4:  
5: r = float(input('Enter a radius: '))  
6: area = compute_circle_area(r)  
7: print('Area of a circle with radius {r} is  
8:     {area:.2f}')
```

Value in
circle_area is
returned

Notice how the
return keyword is
used

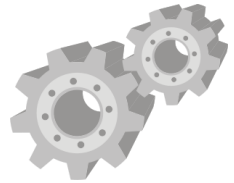


Circle Area – Program#4



```
1: def compute_circle_area(radius):  
2:     return math.pi*radius**2  
3:  
4: r = float(input('Enter a radius: '))  
5: area = compute_circle_area(r)  
6: print('Area of a circle with radius {r} is  
    {area:.2f}')
```

Passing Parameters



- Mechanism of **copying** value from an **argument** to its corresponding **parameter**

```
def compute_circle_area(radius):  
    ...  
}  
  
r = float(input("Enter a radius: "))  
area = compute_circle_area(r)
```

Parameter

copy

Argument

Seeking help



- The built-in `help()` function can be used in the shell to provide more details about any object

```
>>> import math
>>> help(math)
Help on module math:
```

```
NAME
    math
```

MODULE REFERENCE

<https://docs.python.org/3.6/library/math>

The following documentation is automatically generated from the Python source files. It may be incomplete, incorrect or include features that are considered implementation detail and may vary between Python implementations. When in doubt, consult the module reference at the location listed above.

DESCRIPTION

This module is always available in the Python shell. It contains mathematical functions defined in the C standard library.

```
>>> help(math.atan)
Help on built-in function atan in module math:

atan(...)
    atan(x)

    Return the arc tangent (measured in radians) of x.
```

```
>>> help(38)
Help on int object:

class int(object)
|   int(x=0) -> integer
|   int(x, base=10) -> integer
|
|   Convert a number or string to an integer, or return 0 if no
|   are given. If x is a number, return x.__int__(). For float
|   numbers, this truncates towards zero.
```

Providing help with docstring



- A docstring can be added at the beginning of a function to be shown by the `help()` function

```
def compute_circle_area(radius):  
    """  
    Compute and return the area of a circle  
    with the specified radius  
    """  
    return math.pi*radius**2
```

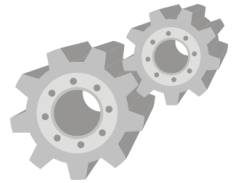
docstring

```
>>> help(compute_circle_area)  
Help on function compute_circle_area in module __main__:  
  
compute_circle_area(radius)  
    Compute and return the area of a circle with the specified radius
```


Conclusion

- Subroutine/function is a group of statements
- There are built-in functions and user-defined functions
- Python provides many useful mathematical functions in its math module

Syntax Summary



- Read a number from keyboard

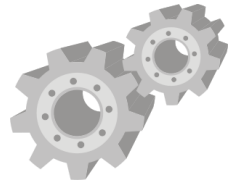
```
variable_name = int(input(str))  
variable_name = float(input(str))
```

- Define a function

```
def function_name(parameters...):  
    ...  
    ...  
    return value
```

optional

optional



Syntax Summary

- Import a module as a whole

```
import module_name
```

- Import some objects from a module

```
from module_name import obj1, obj2
```



References

- Python's math module
<https://docs.python.org/3/library/math.html>
- Python docstring
<https://www.python.org/dev/peps/pep-0257/>