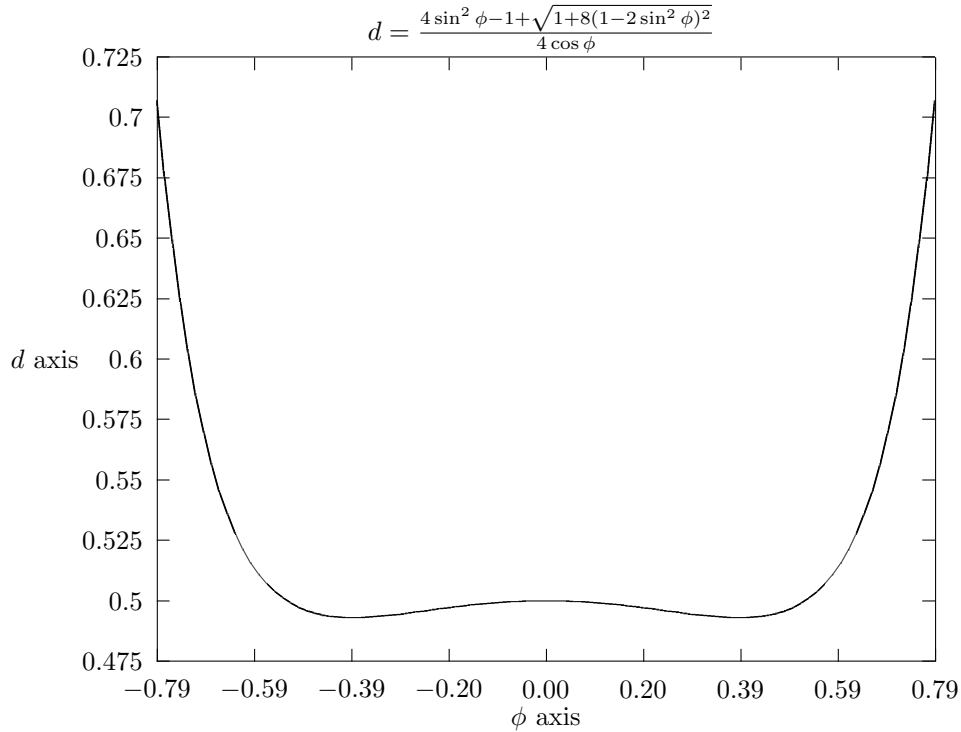


# Calculations and Graphs from J. Kirk's Original 6-Strut Tensegrity

Here is the verbatim text of the gnuplot program I wrote which generates plots for the original formula for  $d$  in terms of  $\phi$  in John Kirk's notes.

```
set terminal latex
set output "plot1.tex"
set xlabel "$\phi$ axis"
set ylabel "$d$ axis"
set nokey
set xtics -pi/4, pi/16
set ytics 0, 0.025
set size 1.0, 1.25
set nozeroaxis
set format x "%.2f$"
set title "$d=\frac{4\sin^2\phi-1+\sqrt{1+8(1-2\sin^2\phi)^2}}{4\cos\phi}$"
d(x)=((4.*(sin(x)**2))-1.+sqrt(1.+8.*(1.-2.*(sin(x)*sin(x)))*(1.-2.*(sin(x)*sin(x)))))/(4.*cos(x))
plot [x=-pi/4:pi/4] [0.475:0.725] d(x) with lines
```

Here is the graph of  $d$  with respect to  $\phi$ :



Here is Calc's processing of the  $d(x)$  used in the gnuplot program:

```
((4.*(sin(x)**2))-1.+sqrt(1.+8.*(1.-2.*(sin(x)*sin(x)))*(1.-2.*(sin(x)*sin(x)))))/(4.*cos(x))
```

Which Calc simplifies to:

```
(4. sin(x)^2 - 1. + sqrt(1. + 8. (1. - 2. sin(x)^2)^2)) / 4. cos(x)
```

and in “big” notation:

$$\frac{4. \sin(x)^2 - 1. + \sqrt{1. + 8. (1. - 2. \sin(x)^2)}}{4. \cos(x)}$$

Now to get the derivative. Here is the formula for  $d(x)$  as it was when GNU Calc began it’s derivation of the derivative.

$$(4. \sin(x)^2 - 1. + \sqrt{1. + 8. (1. - 2. \sin(x)^2)}) / 4. \cos(x)$$

```
% [calc-mode: language: nil]
% [calc-mode: symbolic: nil]
% [calc-mode: fractions: nil]
% [calc-mode: angles: rad]
```

Here is the derivative  $d'(x)$ :

$$\begin{aligned} & (8. \sin(x) \cos(x) \\ & - 32. (1. - 2. \sin(x)^2) \sin(x) \cos(x) / \sqrt{1. + 8. (1. - 2. \sin(x)^2)}) \\ & / 4. \cos(x) \\ & + 0.25 (4. \sin(x)^2 - 1. + \sqrt{1. + 8. (1. - 2. \sin(x)^2)}) \sin(x) \\ & / \cos(x)^2 \end{aligned}$$

And in “big” notation:

```
% [calc-mode: language: big]
```

$$\begin{aligned} & 2. \cos(x) \sin(x) - \frac{8. (1. - 2. \sin(x)^2) \cos(x) \sin(x)}{\sqrt{1. + 8. (1. - 2. \sin(x)^2)} + 1.} \\ & + \end{aligned}$$

$$\frac{0.25 (4. \sin(x)^2 + \sqrt{1. + 8. (1. - 2. \sin(x)^2)} + 1. - 1.) \sin(x)}{\cos(x)^2}$$

Here is the gnuplot program to generate this:

```

set output "plot2.tex"
set autoscale
set xlabel "$\phi$ axis"
set nokey
set ytics 0, 0.025
set size 1.25, 1.5
set nozeroaxis
set xzeroaxis
set format x "%.2f$"
set ylabel "$d'$ axis"
set xtics -pi/4, pi/16
set ytics -1.75, 0.25
set title "$d' = \frac{2 \cos \phi \sin \phi - \frac{8 \cos \phi \sin \phi (1-2 \sin^2 \phi)}{\sqrt{8(1-2 \sin^2 \phi)^2 + 1}}}{\cos \phi} + \frac{4 \sin^2 \phi + \sqrt{8(1-2 \sin^2 \phi)^2 - 1}}{4 \cos^2 \phi}$"
f(x) = (((2.*(cos(x)*sin(x)) - ((8.*(cos(x)*(sin(x)*(1.-2.*(sin(x)*sin(x)))))) /
sqrt(8.*((1.-2.*(sin(x)*sin(x)))*(1.-2.*(sin(x)*sin(x)))+1.)))/ cos(x)) +
((sin(x)*((4.*(sin(x)*sin(x)) + sqrt(8.*((1.-2.*(sin(x)*sin(x)))*(1.-2.*(sin(x)*sin(x))))) -1.)) /
4.*(cos(x)*cos(x))))
plot [x=-pi/4:pi/4] [-1.75:1.75] f(x) with lines

```

Here is the plot of the derivative:

$$d' = \frac{2 \cos \phi \sin \phi - \frac{8 \cos \phi \sin \phi (1-2 \sin^2 \phi)}{\sqrt{8(1-2 \sin^2 \phi)^2 + 1}}}{\cos \phi} + \frac{(4 \sin^2 \phi + \sqrt{8(1-2 \sin^2 \phi)^2 - 1})}{4 \cos^2 \phi}$$

