

Tensegrity Geometry Derivation Results

John Kirk

Six-strut Tensegrity (corresponds to the tetrahedron-tetrahedron duality)

Lengths when strut length is 2:

$$d = \frac{4 \sin^2(\phi) - 1 + \sqrt{1 + 8(1 - 2 \sin^2(\phi))^2}}{4 \cos(\phi)}$$

$$short = \sqrt{2} \sqrt{d^2 - d(\cos(\phi) + \sin(\phi)) - \cos(\phi) \sin(\phi) + 1}$$

$$long = \sqrt{2} \sqrt{d^2 - d(\cos(\phi) - \sin(\phi)) + \cos(\phi) \sin(\phi) + 1}$$

Twelve-strut Tensegrity (corresponds to the octrahedron-cube duality)

Lengths when strut length is 2:

$$d = \frac{\frac{\sqrt{2}}{2} - \sin(\phi) \cos(\phi) + \sqrt{4 \sin^2(\phi) \cos^2(\phi) + \frac{1}{2}}}{\cos(\phi) + \sqrt{2} \sin(\phi)}$$

$$short = \sqrt{d^2 - 2\sqrt{2} \cos(\phi) d - \cos^2(\phi) + 3}$$

$$long = \sqrt{d^2 - 2 \sin(\phi) d + \cos^2(\phi) + 1}$$