# 10\_Function\_Factories

2023-01-31

# 10 Function factories

# 10.1 Introduction

```
library(tidyverse)
## -- Attaching packages ----- tidyverse 1.3.2 --
## v ggplot2 3.4.0 v purrr 1.0.1
## v tibble 3.1.8 v dplyr 1.0.10
## v tidyr 1.2.1 v stringr 1.5.0
## v readr 2.1.3 v forcats 0.5.2
## -- Conflicts ----- tidyverse_conflicts() --
## x dplyr::filter() masks stats::filter()
## x dplyr::lag()
                  masks stats::lag()
power1 <- function(exp) {</pre>
 function(x) {
    x ^ exp
  }
square <- power1(2)</pre>
cube <- power1(3)</pre>
library(rlang)
## Attaching package: 'rlang'
## The following objects are masked from 'package:purrr':
##
##
       %0%, flatten, flatten_chr, flatten_dbl, flatten_int, flatten_lgl,
##
       flatten_raw, invoke, splice
library(ggplot2)
library(scales)
##
## Attaching package: 'scales'
```

```
## The following object is masked from 'package:purrr':
##
## discard

## The following object is masked from 'package:readr':
##
## col_factor
```

# 10.2 Factory fundamentals

```
square
## function(x) {
##
       x ^ exp
##
## <environment: 0x000001f7088bc7b8>
cube
## function(x) {
##
       x ^ exp
## <bytecode: 0x000001f708a34718>
## <environment: 0x000001f708913a30>
env_print(square)
## <environment: 0x000001f7088bc7b8>
## Parent: <environment: global>
## Bindings:
## * exp: <lazy>
env_print(cube)
## <environment: 0x000001f708913a30>
## Parent: <environment: global>
## Bindings:
## * exp: <lazy>
fn_env(square)$exp
## [1] 2
fn_env(cube)$exp
## [1] 3
```

# 10.2.2 Diagram conventions

```
square(10)
## [1] 100
10.2.3 Forcing evaluation
x <- 2
square <- power1(x)</pre>
x <- 3
square(2)
## [1] 8
power2 <- function(exp) {</pre>
  force(exp)
  function(x) {
    x ^ exp
  }
}
x <- 2
square <- power2(x)</pre>
x <- 3
square(2)
## [1] 4
10.2.4 Stateful functions
new_counter <- function() {</pre>
  i <- 0
  function() {
    i <<- i + 1
    i
  }
}
counter_one <- new_counter()</pre>
```

## [1] 1

counter\_one()

counter\_two <- new\_counter()</pre>

```
counter_one()
## [1] 2
counter_two()
## [1] 1
counter_one()
## [1] 3
counter_two()
## [1] 2
10.2.5 Garbage collection
f1 <- function(n) {</pre>
 x <- runif(n)
 m \leftarrow mean(x)
  function() m
}
g1 <- f1(1e6)
lobstr::obj_size(g1)
## 8.01 MB
```

```
#> 8,013,104 B

f2 <- function(n) {
    x <- runif(n)
    m <- mean(x)
    rm(x)
    function() m
}

g2 <- f2(1e6)
lobstr::obj_size(g2)</pre>
```

## 13.12 kB

### 10.2.6 Exercises

1. The definition of force() is simple:

#### force

```
## function (x)
## x
## <bytecode: 0x000001f77fa74b60>
## <environment: namespace:base>
```

Why is it better to force(x) instead of just x?

Using force(x) is better than x because it makes the evaluation of x occur immediately when the function is created rather than lazily executing the first time the function is called. If the value of x changes before the function is called, the value of x when the function was created will not be used and the new value of x will be used

```
timeser <- function(multiplier){
  function(x) x * multiplier
}
x <- 2
doubler <- timeser(x)
# Function called before x changed
doubler(2)</pre>
```

```
## [1] 4
```

```
x <- 3
doubler(2)
```

### ## [1] 4

```
x <- 2
doubler <- timeser(x)
# Function not called before x changed
x <- 3
doubler(2)</pre>
```

### ## [1] 6

```
# Forced operation
timeser2 <- function(multiplier){
  force(multiplier)
  function(x) x * multiplier
}
x <- 2
doubler <- timeser2(x)
# Function not called before x changed
x <- 3
doubler(2)</pre>
```

### ## [1] 4

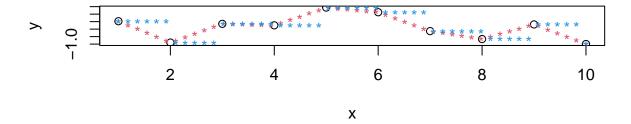
2. Base R contains two function factories, approxfun() and ecdf(). Read their documentation and experiment to figure out what the functions do and what they return.

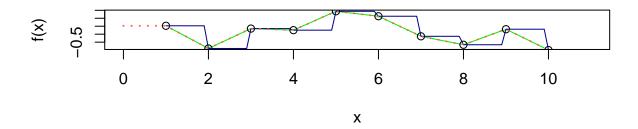
```
x <- 1:10
y <- rnorm(10)
par(mfrow = c(2,1))
plot(x, y, main = "approx(.) and approxfun(.)")
points(approx(x, y), col = 2, pch = "*")
points(approx(x, y, method = "constant"), col = 4, pch = "*")

f <- approxfun(x, y)
curve(f(x), 0, 11, col = "green2")
points(x, y)
is.function(fc <- approxfun(x, y, method = "const")) # TRUE</pre>
```

### ## [1] TRUE

# approx(.) and approxfun(.)





```
x <- rnorm(12)
Fn <- ecdf(x)
Fn  # a *function*</pre>
```

## Empirical CDF

```
## Call: ecdf(x)
## x[1:12] = -1.1656, -0.65655, -0.65042, ..., 1.1752, 1.2699
Fn(x) # returns the percentiles for x
## [1] 0.50000000 0.08333333 0.75000000 0.41666667 1.00000000 0.83333333
## [7] 0.58333333 0.25000000 0.16666667 0.91666667 0.66666667 0.333333333
tt <- seq(-2, 2, by = 0.1)
12 * Fn(tt) # Fn is a 'simple' function {with values k/12}
## [1] 0 0 0 0 0 0 0 0 0 1 1 1 1 1 3 3 3 3 3 6 7 7 7 8 8
## [26] 9 9 9 10 10 10 11 12 12 12 12 12 12 12 12
summary(Fn)
## Empirical CDF: 12 unique values with summary
    Min. 1st Qu. Median Mean 3rd Qu.
## -1.16556 -0.30789 -0.07721 0.08537 0.53374 1.26989
##--> see below for graphics
knots(Fn) # the unique data values {12 of them if there were no ties}
## [1] -1.16555703 -0.65654755 -0.65042344 -0.19371486 -0.13732884 -0.13231493
## [7] -0.02210469 0.24075921 0.41917073 0.87744878 1.17516905 1.26988685
y <- round(rnorm(12), 1); y[3] <- y[1]
Fn12 <- ecdf(y)
Fn12
## Empirical CDF
## Call: ecdf(y)
## x[1:10] = -0.8, -0.3, -0.1, ..., 1.1, 1.3
knots(Fn12) # unique values (always less than 12!)
## [1] -0.8 -0.3 -0.1 0.1 0.3 0.6 0.7 1.0 1.1 1.3
summary(Fn12)
## Empirical CDF:
                  10 unique values with summary
## Min. 1st Qu. Median Mean 3rd Qu.
## -0.800 -0.050 0.450 0.390 0.925 1.300
summary.stepfun(Fn12)
```

```
## Step function with continuity 'f'= 0 , 10 knots with summary
##
     Min. 1st Qu. Median
                             Mean 3rd Qu.
                                             Max.
   -0.800 -0.050
##
                    0.450
                            0.390
                                    0.925
                                            1.300
##
## and 11 plateau levels (y) with summary
     Min. 1st Qu. Median
##
                             Mean 3rd Qu.
                                             Max.
   0.0000 0.2083 0.5000 0.4924 0.7500 1.0000
```

3. Create a function pick() that takes an index, i, as an argument and returns a function with an argument x that subsets x with i.

```
pick <- function(index){
   function(x) x[index]
}

a <- 1:10
b <- LETTERS[1:10]
pick_2s <- pick(c(2,4,8))
pick_2s(a)

## [1] 2 4 8

pick_2s(b)</pre>
```

## [1] "B" "D" "H"

4. Create a function that creates functions that compute the  $i^th$  central moment of a numeric vector. You can test it by running the following code:

```
moment <- function(index){
  function(x){
    sum((x - mean(x)) ^ index) / length(x)
  }
}
m1 <- moment(1)
m2 <- moment(2)

x <- runif(100)
stopifnot(all.equal(m1(x), 0))
stopifnot(all.equal(m2(x), var(x) * 99 / 100))</pre>
```

5. What happens if you don't use a closure? Make predictions, then verify with the code below.

```
i <- 0
new_counter2 <- function() {
    i <<- i + 1
    i
}
new_counter2()</pre>
```

```
## [1] 1
new_counter2()
## [1] 2
## [1] 2
i <- 9
new_counter2()
## [1] 10
## [1] 10
Uses the parent environment and changes when global i changes in this case. Function factory can help
prevent this
i <- 0
new_counter2 <- function() {</pre>
  i <- 0
  function(){
    i <<- i + 1
    i
  }
}
i
## [1] 0
new_counter3 <- new_counter2()</pre>
## [1] 0
new_counter3()
## [1] 1
new_counter3()
```

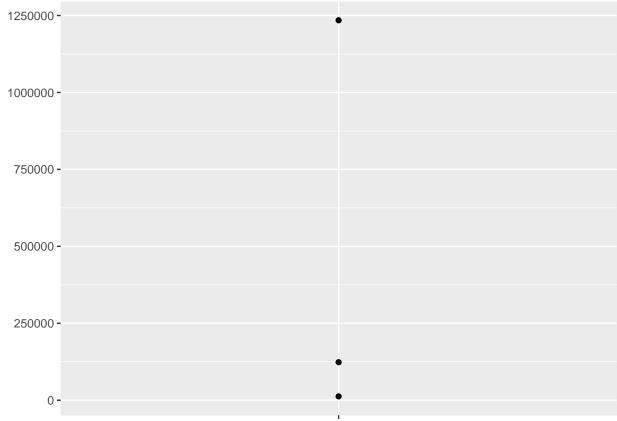
## [1] 2

```
i <- 0
new_counter3()
## [1] 3
  6. What happens if you use <- instead of <<-? Make predictions, then verify with the code below.
new_counter3 <- function() {</pre>
  i <- 0
  function() {
    i <- i + 1
    i
  }
}
i # 0
## [1] 0
new_counter4 <- new_counter3()</pre>
i # 0
## [1] 0
new_counter4() # 1
## [1] 1
i # 0
## [1] 0
new_counter4() # 1
## [1] 1
i # 0
## [1] 0
```

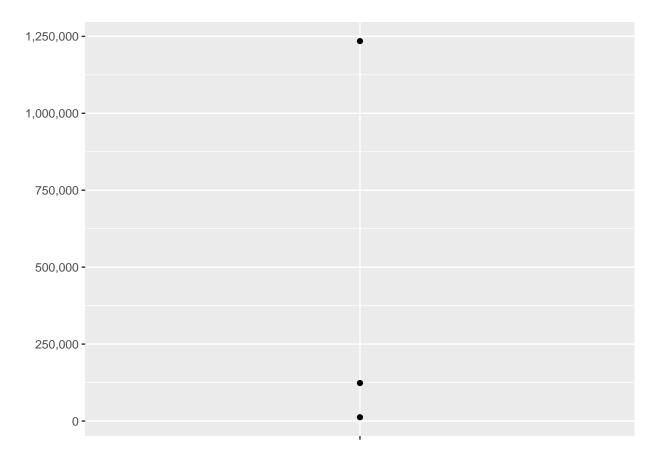
It doesn't update i in the global environment so each run i doesn't change.

# 10.3 Graphical factories

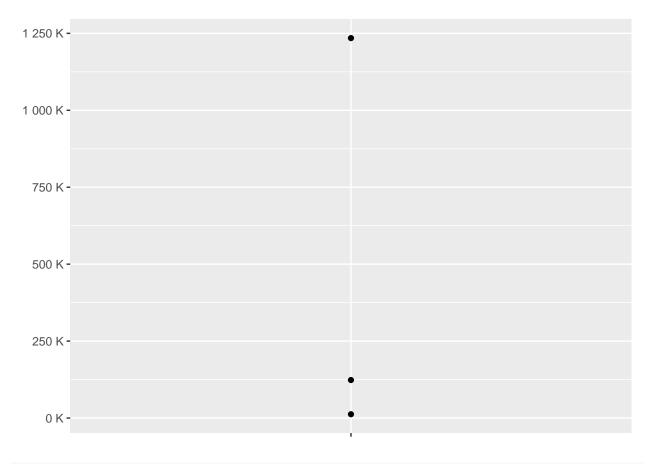
# 10.3.1 Labelling



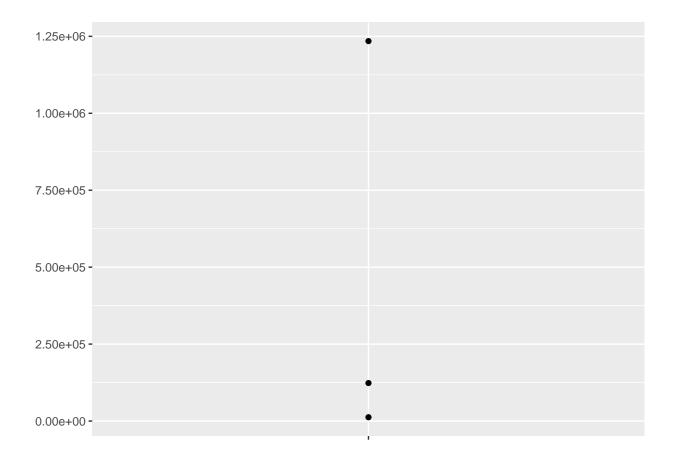
```
core + scale_y_continuous(
   labels = comma_format()
)
```



```
core + scale_y_continuous(
  labels = number_format(scale = 1e-3, suffix = " K")
)
```



```
core + scale_y_continuous(
   labels = scientific_format()
)
```

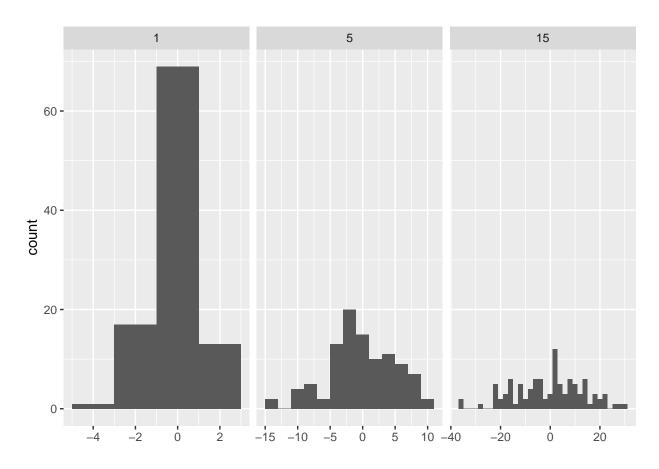


# 10.3.2 Histogram bins

```
# construct some sample data with very different numbers in each cell
sd <- c(1, 5, 15)
n <- 100

df <- data.frame(x = rnorm(3 * n, sd = sd), sd = rep(sd, n))

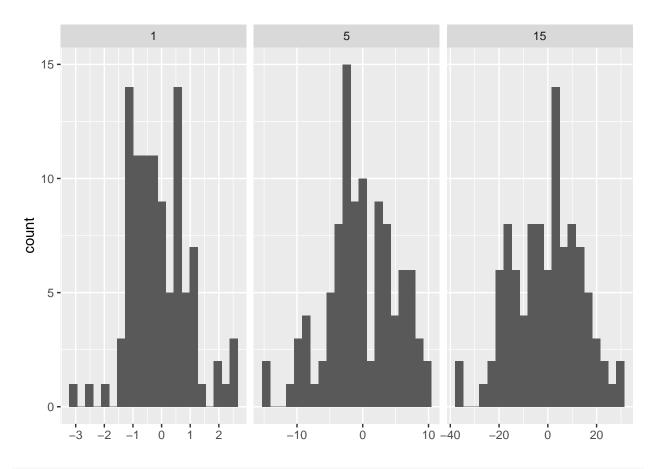
ggplot(df, aes(x)) +
   geom_histogram(binwidth = 2) +
   facet_wrap(~ sd, scales = "free_x") +
   labs(x = NULL)</pre>
```



```
binwidth_bins <- function(n) {
  force(n)

function(x) {
    (max(x) - min(x)) / n
  }
}

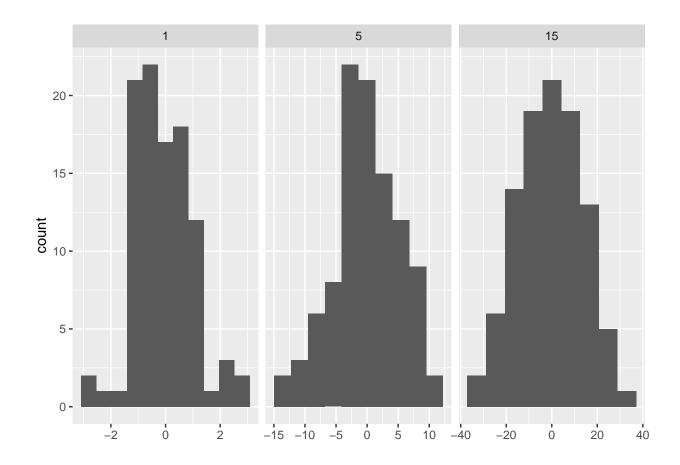
ggplot(df, aes(x)) +
  geom_histogram(binwidth = binwidth_bins(20)) +
  facet_wrap(~ sd, scales = "free_x") +
  labs(x = NULL)</pre>
```



```
base_bins <- function(type) {
  fun <- switch(type,
    Sturges = nclass.Sturges,
    scott = nclass.scott,
  FD = nclass.FD,
    stop("Unknown type", call. = FALSE)
)

function(x) {
    (max(x) - min(x)) / fun(x)
}

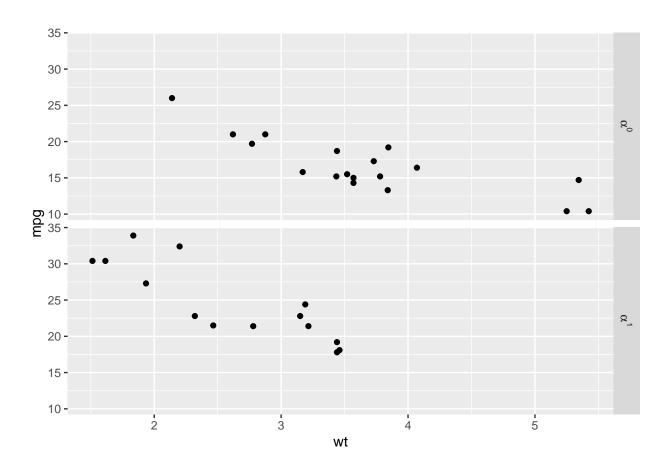
ggplot(df, aes(x)) +
  geom_histogram(binwidth = base_bins("FD")) +
  facet_wrap(~ sd, scales = "free_x") +
  labs(x = NULL)</pre>
```



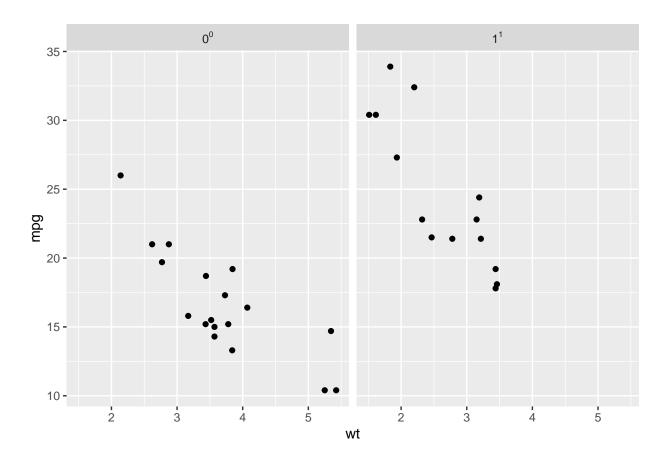
### 10.3.3 ggsave()

```
plot_dev <- function(ext, dpi = 96) {</pre>
  force(dpi)
  switch(ext,
    ps = function(path, ...) {
      grDevices::postscript(
        file = filename, ..., onefile = FALSE,
        horizontal = FALSE, paper = "special"
     )
    },
    pdf = function(filename, ...) grDevices::pdf(file = filename, ...),
    svg = function(filename, ...) svglite::svglite(file = filename, ...),
    emf = ,
    wmf = function(...) grDevices::win.metafile(...),
    png = function(...) grDevices::png(..., res = dpi, units = "in"),
    jpg = ,
    jpeg = function(...) grDevices::jpeg(..., res = dpi, units = "in"),
    bmp = function(...) grDevices::bmp(..., res = dpi, units = "in"),
    tiff = function(...) grDevices::tiff(..., res = dpi, units = "in"),
    stop("Unknown graphics extension: ", ext, call. = FALSE)
```

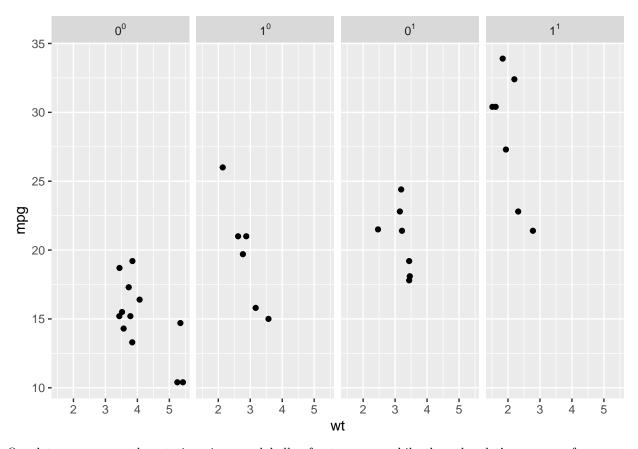
```
}
plot_dev("pdf")
## function(filename, ...) grDevices::pdf(file = filename, ...)
## <bytecode: 0x000001f709a18bd0>
## <environment: 0x000001f709699040>
plot_dev("png")
## function(...) grDevices::png(..., res = dpi, units = "in")
## <bytecode: 0x000001f709c978b8>
## <environment: 0x000001f70a1d5db8>
10.3.4 Exercises
  1. Compare and contrast ggplot2::label_bquote() with scales::number_format()
y <- c(12345, 123456, 1234567)
scales::number_format(scale = 1e-3, suffix = " K")(y)
## [1] "12 K" "123 K"
                           "1 235 K"
p <- ggplot(mtcars, aes(wt, mpg)) + geom_point()</pre>
p + facet_grid(vs ~ ., labeller = label_bquote(alpha ^ .(vs)))
```



p + facet\_grid(. ~ vs, labeller = label\_bquote(cols = .(vs) ^ .(vs)))



```
p + facet_grid(. ~ vs + am, labeller = label_bquote(cols = .(am) ^ .(vs)))
```



One lets you use math notations in your labeller facet names, while the other let's you transform your number values

# 10.4 Statistical factories

# 10.4.1 Box-Cox transformation

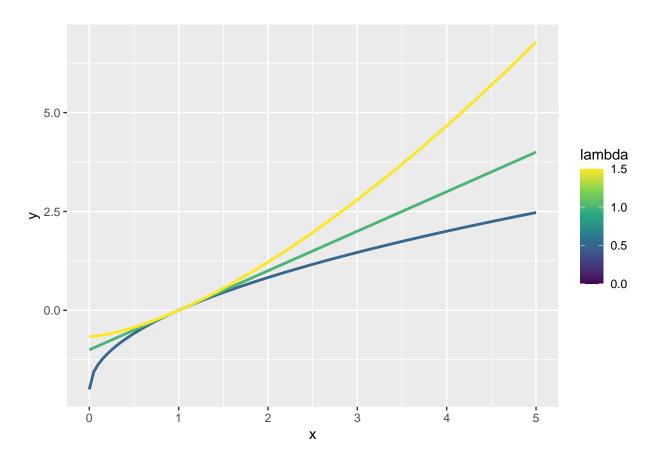
```
boxcox1 <- function(x, lambda) {
  stopifnot(length(lambda) == 1)

if (lambda == 0) {
   log(x)
  } else {
    (x ^ lambda - 1) / lambda
  }
}</pre>
```

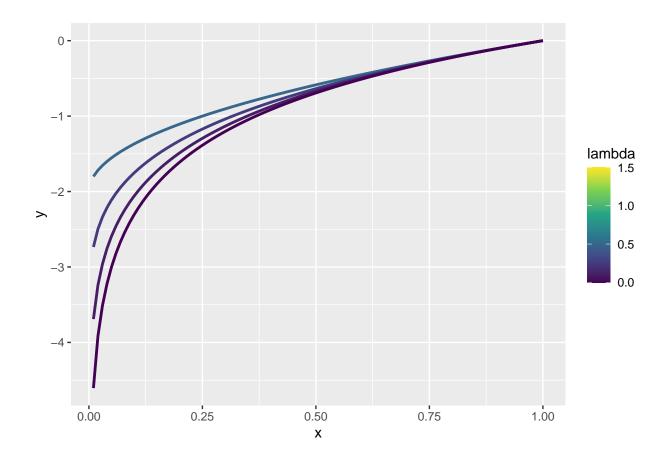
```
boxcox2 <- function(lambda) {
  if (lambda == 0) {
    function(x) log(x)
  } else {
    function(x) (x ^ lambda - 1) / lambda
  }
}</pre>
```

```
stat_boxcox <- function(lambda) {
   stat_function(aes(colour = lambda), fun = boxcox2(lambda), linewidth = 1)
}

ggplot(data.frame(x = c(0, 5)), aes(x)) +
   lapply(c(0.5, 1, 1.5), stat_boxcox) +
   scale_colour_viridis_c(limits = c(0, 1.5))</pre>
```



```
\begin{split} & \text{ggplot}(\text{data.frame}(\mathbf{x} = \text{c}(0.01, 1)), \text{ aes}(\mathbf{x})) + \\ & \text{lapply}(\text{c}(0.5, 0.25, 0.1, 0), \text{ stat\_boxcox}) + \\ & \text{scale\_colour\_viridis\_c}(\text{limits} = \text{c}(0, 1.5)) \end{split}
```



# 10.4.2 Bootstrap generators

```
boot_permute <- function(df, var) {
    n <- nrow(df)
    force(var)

function() {
    col <- df[[var]]
    col[sample(n, replace = TRUE)]
    }

boot_mtcars1 <- boot_permute(mtcars, "mpg")
head(boot_mtcars1())</pre>
```

## [1] 14.7 30.4 21.0 15.0 30.4 33.9

```
head(boot_mtcars1())
```

**##** [1] 15.2 22.8 15.8 17.8 10.4 18.7

```
boot_model <- function(df, formula) {</pre>
  mod <- lm(formula, data = df)</pre>
  fitted <- unname(fitted(mod))</pre>
  resid <- unname(resid(mod))</pre>
  rm(mod)
  function() {
    fitted + sample(resid)
  }
}
boot_mtcars2 <- boot_model(mtcars, mpg ~ wt)</pre>
head(boot mtcars2())
## [1] 20.07725 22.21963 31.30793 22.45261 18.70000 19.14968
head(boot_mtcars2())
## [1] 20.31002 18.45742 20.98059 21.30371 17.87265 16.70730
10.4.3 Maximum likelihood estimation
lprob_poisson <- function(lambda, x) {</pre>
  n <- length(x)
  (\log(\operatorname{lambda}) * \operatorname{sum}(x)) - (n * \operatorname{lambda}) - \operatorname{sum}(\operatorname{lfactorial}(x))
}
x1 <- c(41, 30, 31, 38, 29, 24, 30, 29, 31, 38)
lprob_poisson(10, x1)
## [1] -183.6405
#> [1] -184
lprob_poisson(20, x1)
## [1] -61.14028
#> [1] -61.1
lprob_poisson(30, x1)
## [1] -30.98598
#> [1] -31
```

```
ll_poisson1 <- function(x) {</pre>
  n <- length(x)
  function(lambda) {
    log(lambda) * sum(x) - n * lambda - sum(lfactorial(x))
}
11_poisson2 <- function(x) {</pre>
  n <- length(x)
  sum_x \leftarrow sum(x)
  c <- sum(lfactorial(x))</pre>
  function(lambda) {
    log(lambda) * sum_x - n * lambda - c
  }
}
111 <- 11_poisson2(x1)</pre>
111(10)
## [1] -183.6405
111(20)
## [1] -61.14028
111(30)
## [1] -30.98598
optimise(ll1, c(0, 100), maximum = TRUE)
## $maximum
## [1] 32.09999
## $objective
## [1] -30.26755
optimise(lprob_poisson, c(0, 100), x = x1, maximum = TRUE)
## $maximum
## [1] 32.09999
## $objective
## [1] -30.26755
```

#### 10.4.4 Exercises

1. In boot\_model(), why don't I need to force the evaluation of df or model?

```
boot_model <- function(df, formula) {
  mod <- lm(formula, data = df)
  fitted <- unname(fitted(mod))
  resid <- unname(resid(mod))
  rm(mod)

function() {
   fitted + sample(resid)
  }
}</pre>
```

The call to fitted and resid implicitly forces the evaluation of df and mod when the factory is called and luckily these values only need to be calculated once.

2. Why might you formulate the Box-Cox transformation like this?

```
boxcox3 <- function(x) {
  function(lambda) {
    if (lambda == 0) {
      log(x)
    } else {
      (x ^ lambda - 1) / lambda
    }
  }
}</pre>
```

In this case x is fixed when first created, but can change later on by changing x. You can then manipulate lambda and also change x is need be. ie change your dataset but keep the overall function the same.

3. Why don't you need to worry that boot\_permute() stores a copy of the data inside the function that it generates?

```
boot_permute <- function(df, var) {
    n <- nrow(df)
    force(var)

function() {
    col <- df[[var]]
    col[sample(n, replace = TRUE)]
    }
}

boot_mtcars1 <- boot_permute(mtcars, "mpg")
head(boot_mtcars1())</pre>
```

```
## [1] 15.8 19.7 21.4 19.7 15.2 18.7
```

It doesn't actually store a copy. It just describes an object already in memory. A sampling of mtcar where no new values are created.

4. How much time does ll\_poisson2() save compared to ll\_poisson1()? Use bench::mark() to see how much faster the optimisation occurs. How does changing the length of x change the results?

```
ll_poisson1 <- function(x) {</pre>
 n <- length(x)
  function(lambda) {
    log(lambda) * sum(x) - n * lambda - sum(lfactorial(x))
}
11 poisson1 <- function(x) {</pre>
 n <- length(x)
 function(lambda) {
    log(lambda) * sum(x) - n * lambda - sum(lfactorial(x))
  }
11_poisson2 <- function(x) {</pre>
 n \leftarrow length(x)
 sum_x \leftarrow sum(x)
 c <- sum(lfactorial(x))</pre>
 function(lambda) {
    log(lambda) * sum_x - n * lambda - c
  }
x1 \leftarrow c(41, 30, 31, 38, 29, 24, 30, 29, 31, 38)
x2 \leftarrow sample(1:1000, 100)
x3 <- sample(1:1e6, 10000)
things <- expand_grid(functional = c("ll_poisson1", "ll_poisson2"),</pre>
                       x_values = c("x1","x2","x3"))
things <- pmap(things,
     function(functional, x_values) {
       fun <- get(functional)</pre>
       x <- get(x_values)</pre>
       fun(x)
     })
names(things) <- c("1111", "1121",
                    "1131", "1112",
                    "1122", "1132")
map_df(things, ~bench::mark(optimise(.x, c(0,100), maximum = TRUE))) %>%
 mutate(input = names(things)) %>%
  select(input, everything())
## # A tibble: 6 x 7
     input expression
                                                           min median itr/s~1 mem a~2
     <chr> <bch:expr>
                                                      <bch:tm> <bch:t>
                                                                          <dbl> <bch:b>
## 1 1111 optimise(.x, c(0, 100), maximum = TRUE)
                                                       35.6us 50.5us 16472.
## 2 1121 optimise(.x, c(0, 100), maximum = TRUE) 228.8us 254.8us 3429. 25.67KB
## 3 1131 optimise(.x, c(0, 100), maximum = TRUE) 19.1ms 20.6ms
                                                                           49.1 2.37MB
```

# 10.5 Function factories + functionals

## [1] 10

```
names <- list(</pre>
 square = 2,
 cube = 3,
 root = 1/2,
 cuberoot = 1/3,
 reciprocal = -1
)
funs <- purrr::map(names, power1)</pre>
funs$root(64)
## [1] 8
funs$root
## function(x) {
##
       x ^ exp
##
## <bytecode: 0x000001f708a34718>
## <environment: 0x000001f708bb3b00>
with(funs, root(100))
## [1] 10
attach(funs)
## The following objects are masked _by_ .GlobalEnv:
##
##
       cube, square
root(100)
## [1] 10
detach(funs)
rlang::env_bind(globalenv(), !!!funs)
root(100)
```

```
rlang::env_unbind(globalenv(), names(funs))
10.5.1 Exercises
  1. Which of the following commands is equivalent to with(x, f(z))?
E. It depends
  2. Compare and contrast the effects of env_bind() vs. attach() for the following code.
funs <- list(</pre>
  mean = function(x) mean(x, na.rm = TRUE),
  sum = function(x) sum(x, na.rm = TRUE)
)
attach(funs)
## The following objects are masked from package:base:
##
##
       mean, sum
#> The following objects are masked from package:base:
       mean, sum
mean <- function(x) stop("Hi!")</pre>
detach(funs)
mean(1:5)
## Error in mean(1:5): Hi!
sum(1:5)
## [1] 15
rlang::env_bind(globalenv(), !!!funs)
mean(1:5)
## Error in mean(x, na.rm = TRUE): unused argument (na.rm = TRUE)
sum(1:5)
## Error in sum(x, na.rm = TRUE): unused argument (na.rm = TRUE)
mean <- function(x) stop("Hi!")</pre>
mean(1:5)
```

## Error in mean(1:5): Hi!

```
rlang::env_unbind(globalenv(), names(funs))
mean(1:5)

## [1] 3

sum(1:5)
```

## [1] 15

with attach the base mean and sum functions are masked because you are adding funs to the search path. Detaching funs removes the masking and funs from the search path. However if you change mean you change the base mean function as well. With env\_bind you can change the functions in the global environment, but then when you unbind them they revert back to their original format.