

# MSiA-400 Everything Starts with Data

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## Lab Exercise #1

**Due Date: Monday, October 16, 09:00 am**

EXERCISE INSTRUCTIONS: Q1: submit R script and an example using data “Tensile.txt”; Q2 & Q3: submit short answers, related code and print for each problem if necessary. Push your answers to Github (required) and Canvas (optional).

### Problem 1

In the lab session, we used `aov()` for one-way ANOVA analysis. Please write your own one-way ANOVA function in R which takes two vectors (i.e. data and group labels) as input and the F-test result (e.g. reject null hypothesis or not) as output. You don't have to output the entire ANOVA table.

### Problem 2

Data set *bostonhousing.txt*, created by Harrison and Rubinfeld [1978], concerns housing values in suburbs of Boston. The attributes include

|         |   |
|---------|---|
| MEDV    | Median value of owner-occupied homes in \$1000's                      |
| CRIM    | per capita crime rate by town   |
| ZN      | proportion of residential land zoned for lots over 25,000 sq.ft.      |
| INDUS   | proportion of non-retail business acres per town                      |
| CHAS    | Charles River dummy variable (= 1 if tract bounds river; 0 otherwise) |
| NOX     | nitric oxides concentration (parts per 10 million)                    |
| RM      | average number of rooms per dwelling                                  |
| AGE     | proportion of owner-occupied units built prior to 1940                |
| DIS     | weighted distances to five Boston employment centres                  |
| RAD     | index of accessibility to radial highways                             |
| TAX     | full-value property-tax rate per \$10,000                             |
| PTRATIO | pupil-teacher ratio by town   |
| B       | $1000(Bk - 0.63)^2$ where $Bk$ is the proportion of blacks by town    |
| LSTAT   | % lower status of the population,                                     |

in which MEDV is the response variable. The summary of the data set is below.

|                        |   |
|------------------------|---|
| Name of the data set   | bostonhousing   |
| Number of observations | 506   |
| Number of attributes   | 14 (1 response variable and 13 explanatory variables) |

### Problem 2(a)

Build regression model `reg` and display `summary()` of the model. Pick two explanatory variables that are least likely to be in the best model, and support your suggestion in one sentence.

### Problem 2(b)

Build regression model `reg.picked` by excluding the two explanatory variables selected in problem 2(a). Display `summary()` of the model.

### Problem 2(c)

For a regression model, the mean squared error (MSE) is defined as  $\frac{SSE}{n-1-p}$ , in which  $p$  is the number of explanatory variables used in the model. The mean absolute error (MAE) is similarly defined:  $\frac{SAE}{n-1-p}$ . Display  $MSE$  and  $MAE$  for regression models `reg` and `reg.picked` from the previous problems. Based on  $MSE$  and  $MAE$ , pick one model you prefer.

### Problem 2(d)

Run `step()` using regression model `reg` in problem 2(a). Compare the model with `reg.picked` in problem 2(b).

## Problem 3

Import `labdata.txt`. The summary of the data set is below.

|                        |   |
|------------------------|---|
| Name of the data set   | labdata   |
| Number of observations | 400   |
| Number of attributes   | 9 (1 response variable and 8 explanatory variables) |

Column `y` is the response variable and remaining attributes `x1,x2,...` are the explanatory variables.

### Problem 3(a)

Build regression model `reg` and display `summary()` of the model

### Problem 3(b)

For each explanatory variable, plot it against the response variable. Based on the scatter plots, pick one variable that is most likely to be used in a piecewise regression model. Attach one plot associated with the variable you pick.

### Problem 3(c)

Calculate the mean of the variable you pick in problem 3(b) and build piecewise regression model `reg.piece` using the mean. Is model `reg.piece` better than model `reg` in problem 3(a)? Support your argument in one sentence.

## Reference

David Harrison and Daniel L Rubinfeld. Hedonic housing prices and the demand for clean air. Journal of environmental economics and management, 5(1):81-102, 1978.