```
import scipy.optimize as optimize
import numpy as np
# ********* problem #1 **********
def func(x):
   return np.cos(x)**2 + 6 - x
def f(x):
   return np.power(x, 2) + 6.0 * x + 4
def f_prime(x):
   return 2.0 * x + 6.0
# 0 < \cos(x) **2 < 1, so the root has to be between x=6 and x=7
print(optimize.bisect(func, 6, 7))
6.77609231632
a = optimize.bisect(f, -1, 0)
print("This is the bisection method:{:.16e}".format(a))
# -7.6393202249983005e-01
print("This is the bisection method:{0}".format(a))
# -0.7639320225
# ************** problem #2 ***********
def g(x):
   return (-4.0) / x + 6.0
def h(x):
   return -1.0 * np.sqrt(-6.0 * x - 4.0)
# This finds the value of x such that func(x) = x, that is, where
\# -x**3 + 1 = x
print(optimize.fixed_point(g, -5.2))
# 5.2360679775
print(optimize.fixed_point(h, -0.77))
# ********** problem #4 ***********
# use the secant method.
# well scipy.optimize.newton() uses the secant method
# if we don't give it the functions derivative.
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```
a = 0
a = optimize.newton(f, 0, tol=1e-16, maxiter=8)
# using equation (1) from the assignment. where -7.6 is the fixed point "s"
def convergence(n_plus_one, n):
   numerator = np.log(np.abs(n_plus_one - -7.6393202250021031e-01))
   denominator = np.log(np.abs(n - -7.6393202250021031e-01))
   return numerator / denominator
print("This is the convergence:", convergence(-0.74996874883, -0.66665555574))
print("This is the convergence:", convergence(-0.763636264454, -0.74996874883))
print("This is the convergence:", convergence(-0.763931103843, -0.763636264454))
print("This is secant method answer {:.16e}".format(a))
# ******** problem #5 *************
# newton() will use the newton raphson method because we gave it the derivative.
a = optimize.newton(f, 0, fprime=f_prime, tol=1e-16, maxiter=14)
print"This is Newton method answer{:.16e}".format(a)
print("This is the convergence:", convergence(-0.761904761905, -0.66666666667))
print("This is the convergence:", convergence(-0.763931104357, -0.761904761905))
print("This is the convergence:", convergence(-0.7639320225, -0.763931104357))
# ****** problem #6 ***********
def k(x):
   return np.power(x, 20) - 10.0
def k_prime(x):
   return 20.0 * np.power(x, 19)
a = optimize.newton(k, 8, fprime=k_prime, tol=1e-16, maxiter=44)
print"This is Newton method answer: {:.16e}".format(a)
# ******** problem #7 *******
def f(x):
   return np.power(x,2) - 6.0*x + 9.0
def f_prime(x):
```

```
return 2.0 * x - 6.0

a = optimize.newton(f, 4, fprime=f_prime, tol=1e-16, maxiter=29)

print"This is Newton method answer: {:.16e}".format(a)

# using equation (1) from the assignment. where -7.6 is the fixed point "s"

def convergence(n_plus_one, n):
    numerator = np.log(np.abs(n_plus_one - 3.0000000298023224e+00))
    denominator = np.log(np.abs(n - 3.0000000298023224e+00))
    return numerator / denominator

print("This is the convergence:", convergence(3.25, 3.5))
print("This is the convergence:", convergence(3.125, 3.25))

print("This is the convergence:", convergence(3.0625, 3.125))

print("This is the convergence:", convergence(3.00000011921, 3.00000023842 ))
```