



a)  $E$ ?

b)  $x'^T E x = 0$

$$\begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix} = E$$

a)  $E = [T_x^T] R =$

$R = I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$

$T^1 = \begin{bmatrix} -d \\ 0 \\ 0 \end{bmatrix}$

b)  $x = \begin{bmatrix} x_0 \\ y_0 \\ f \end{bmatrix} \quad x' = \begin{bmatrix} x'_0 \\ y'_0 \\ f \end{bmatrix}$

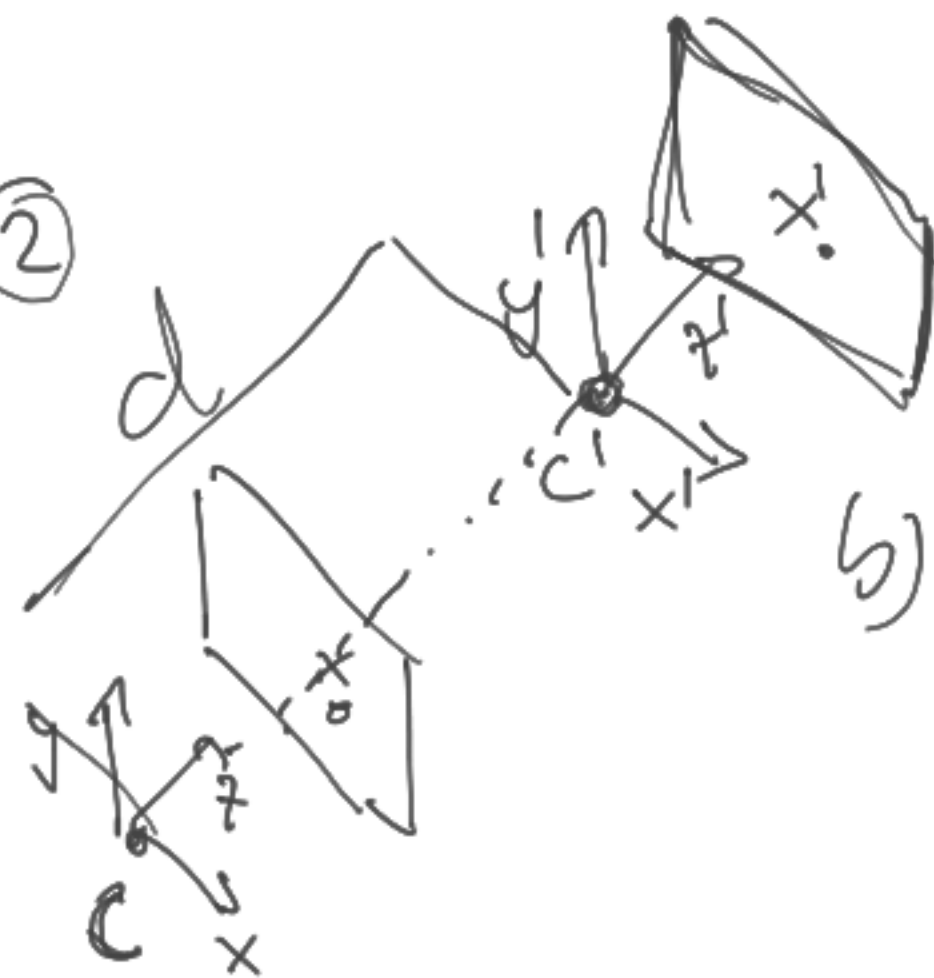
$$\begin{bmatrix} x'_0 & y'_0 & f \end{bmatrix} \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & d \\ 0 & -d & 0 \end{bmatrix} \begin{bmatrix} x_0 \\ y_0 \\ f \end{bmatrix} =$$

$$= \begin{bmatrix} x'_0 & y'_0 & f \end{bmatrix} \begin{bmatrix} 0 \\ d f \\ -d y_0 \end{bmatrix} = y'_0 d f - y_0 d f \cdot 0$$

$$y'_0 d f = y_0 d f$$

$$y'_0 = y_0$$

②



$\rightarrow E?$

$$b) x'^T E x = 0$$

$$\Leftrightarrow \boxed{\frac{x_0}{y_0} = \frac{x'_0}{y'_0}}$$

PROVE  $\underline{E} = U \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} V^T$ ,  $E = \begin{bmatrix} T_x^T \end{bmatrix} \cdot R \leftarrow \text{orthogonal}$   
 $\uparrow$   
 skew-symmetric

(1) USE HELPER MATRICES  $W = \begin{bmatrix} 0 & -1 & 0 \\ 1 & 0 & 0 \\ 0 & 0 & 1 \end{bmatrix}$  and  $Z = \begin{bmatrix} 0 & 1 & 0 \\ -1 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$   $Z = - \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} W$   
 $\uparrow$   $\uparrow$   
 orthogonal skew-symmetric

(2) PROPERTY THAT SKEW-SYMMETRIC MATRIX CAN BE DECOMPOSED AS:

$$S = k U \cdot Z \cdot U^T \text{ (up-to-scale and } U \text{ orthogonal)}$$

$$S = (-k) U \cdot \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} W U^T$$

$$E = \begin{bmatrix} T_x^T \end{bmatrix} R = U \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \underbrace{W U^T R}_{\text{orthogonal}}$$

$$= \left[ U \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} V^T \right] = \underline{E}$$

$E$  is given  $\rightarrow$   $\boxed{T' = \pm u_3}$  (last column of  $U$ )

We know that  $[T'_x] = U \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} W U^T = U \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{bmatrix} \underbrace{(U W^T)^T}$

$\swarrow$  This looks like  
a singular value  
decomposition

$[T'_x] T' = 0$

$\|T'\| = 1$

Solution to this is  $SVD([T'_x])$   
last column of  $V$  of  $\hat{J}$

last column  
of  $U$

For  $R$

$V^T = W \cdot U^T \cdot R$

$\rightarrow R = U \cdot W^T V^T$

$\rightarrow R = U \cdot W V^T$