WHAT IS STATISTICAL LEARNING?

Chapter 02 – Part I

- ➤ What Is Statistical Learning?
 - ➤ Why estimate f?
 - > How do we estimate f?
 - The trade-off between prediction accuracy and model interpretability
 - > Supervised vs. unsupervised learning
 - > Regression vs. classification problems

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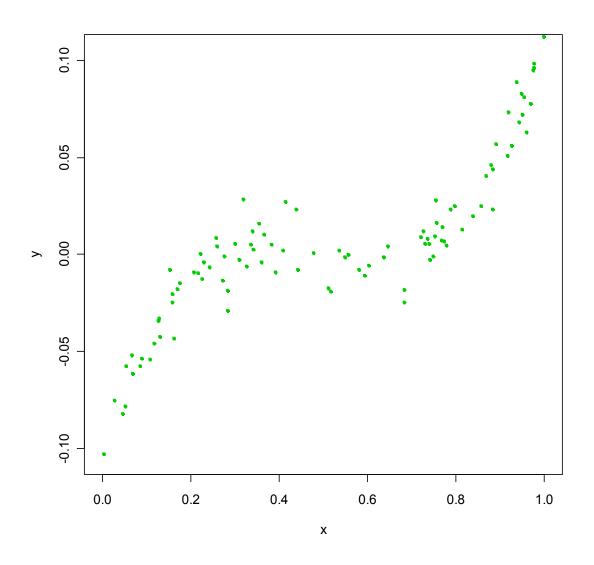
What is Statistical Learning?

- Suppose we observe Y_i and $X_i = (X_{i1},...,X_{ip})$ for i = 1,...,n
- >We believe that there is a relationship between Y and at least one of the X's.
- >We can model the relationship as

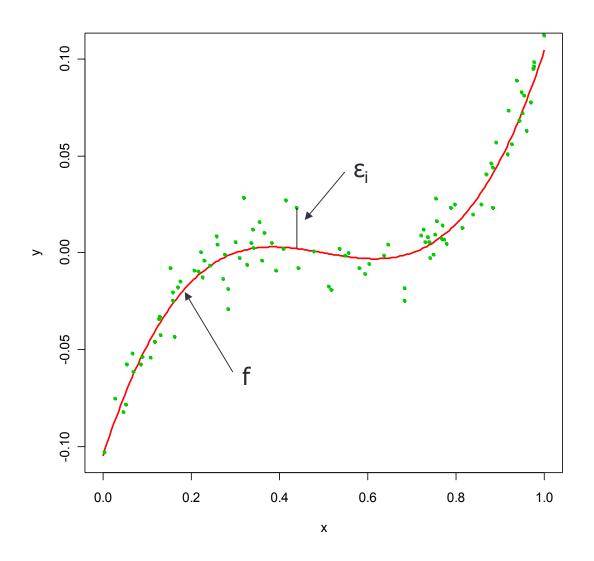
$$Y_i = f(\mathbf{X}_i) + \varepsilon_i$$

>Where f is an unknown function and ϵ is a random error with mean zero.

A Simple Example

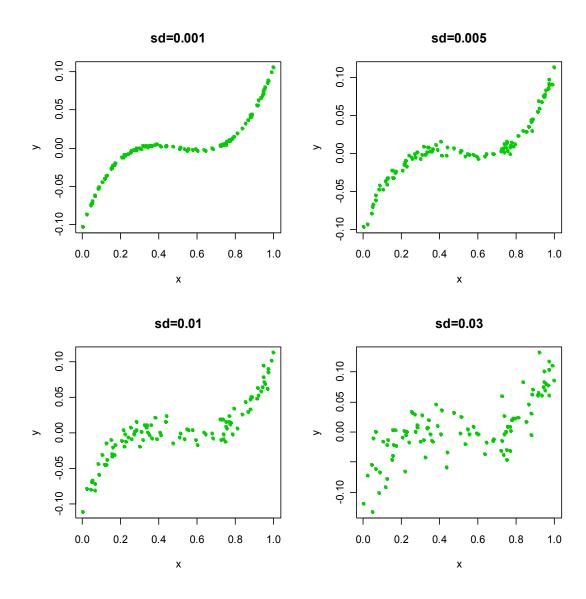


A Simple Example

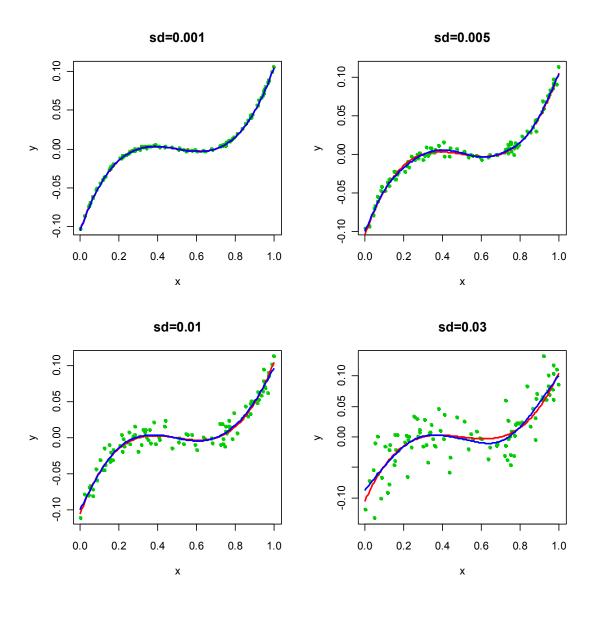


Different Standard Deviations

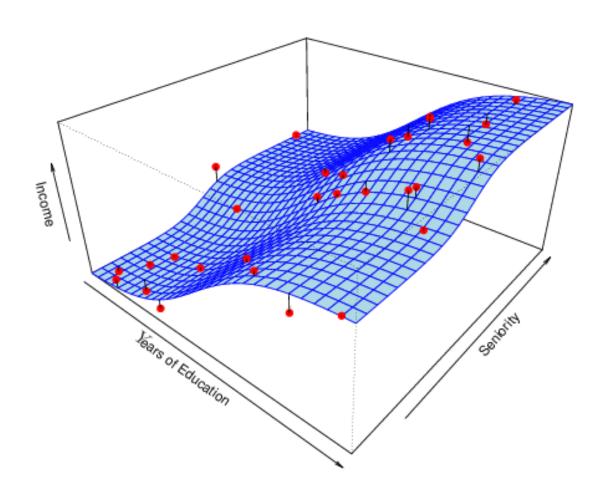
 The difficulty of estimating f will depend on the standard deviation of the ε's.



Different Estimates For f



Income vs. Education and Seniority



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Why Do We Estimate f?

- Statistical Learning, and this course, are all about how to estimate f.
- The term statistical learning refers to using the data to "learn" f.
- >Why do we care about estimating f?
- >There are 2 reasons for estimating f,
 - Prediction and
 - > Inference.

1. Prediction

If we can produce a good estimate for f (and the variance of ε is not too large) we can make accurate predictions for the response, Y, based on a new value of **X**.

Example: Direct Mailing Prediction

- Interested in predicting how much money an individual will donate based on observations from 90,000 people on which we have recorded over 400 different characteristics.
- >Don't care too much about each individual characteristic.
- >Just want to know: For a given individual should I send out a mailing?

2. Inference

- Alternatively, we may also be interested in the type of relationship between Y and the X's.
- >For example,
 - ➤ Which particular predictors actually affect the response?
 - > Is the relationship positive or negative?
 - ➤ Is the relationship a simple linear one or is it more complicated etc.?

Example: Housing Inference

- ➤ Wish to predict median house price based on 14 variables.
- >Probably want to understand which factors have the biggest effect on the response and how big the effect is.
- For example how much impact does a river view have on the house value etc.

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How Do We Estimate f?

>We will assume we have observed a set of training data

$$\{(\mathbf{X}_1, Y_1), (\mathbf{X}_2, Y_2), \dots, (\mathbf{X}_n, Y_n)\}$$

- >We must then use the training data and a statistical method to estimate f.
- ➤ Statistical Learning Methods:
 - > Parametric Methods
 - Non-parametric Methods

Parametric Methods

- It reduces the problem of estimating f down to one of estimating a set of parameters.
- >They involve a two-step model based approach

STEP 1:

Make some assumption about the functional form of f, i.e. come up with a model. The most common example is a linear model i.e.

$$f(\mathbf{X}_i) = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \dots + \beta_p X_{ip}$$

However, in this course we will examine far more complicated, and flexible, models for *f*. In a sense the more flexible the model the more realistic it is.

Parametric Methods (cont.)

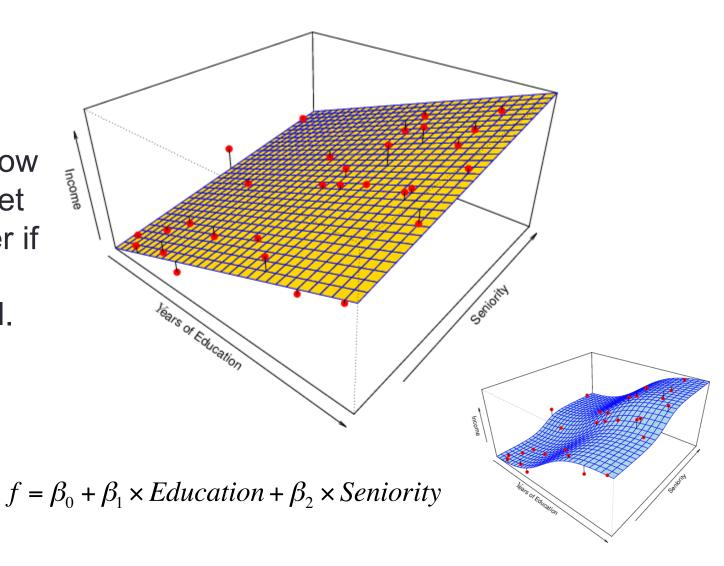
STEP 2:

Use the training data to fit the model i.e. estimate f or equivalently the unknown parameters such as β_0 , β_1 , β_2 ,..., β_p .

- > The most common approach for estimating the parameters in a linear model is ordinary least squares (OLS).
- > However, this is only one way.
- > We will see in the course that there are often superior approaches.

Example: A Linear Regression Estimate

 Even if the standard deviation is low we will still get a bad answer if we use the wrong model.

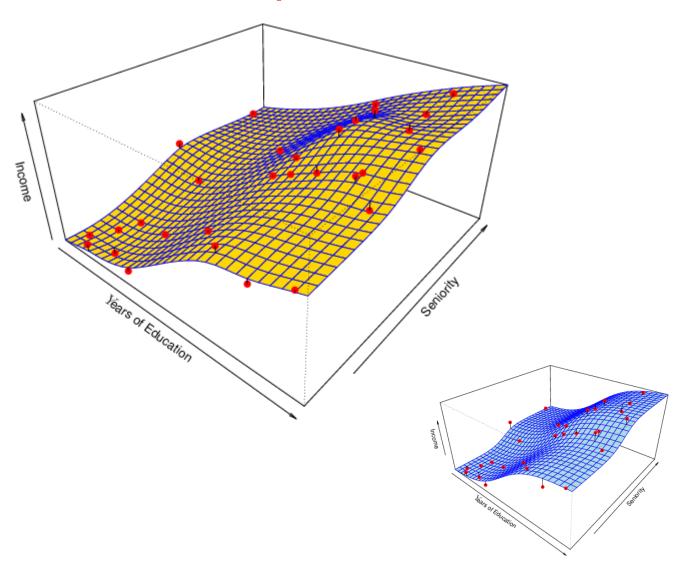


Non-parametric Methods

- They do not make explicit assumptions about the functional form of f.
- > Advantages: They accurately fit a wider range of possible shapes of f.
- ➤ <u>Disadvantages:</u> A very large number of observations is required to obtain an accurate estimate of f

Example: A Thin-Plate Spline Estimate

 Non-linear regression methods are more flexible and can potentially provide more accurate estimates.



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Tradeoff Between Prediction Accuracy and Model Interpretability

- >Why not just use a more flexible method if it is more realistic?
- >There are two reasons

Reason 1:

A simple method such as linear regression produces a model which is much easier to interpret (the Inference part is better). For example, in a linear model, β_j is the average increase in Y for a one unit increase in X_j holding all other variables constant.

Reason 2:

Even if you are only interested in prediction, so the first reason is not relevant, it is often possible to get more accurate predictions with a simple, instead of a complicated, model. This seems counter intuitive but has to do with the fact that it is harder to fit a more flexible model.

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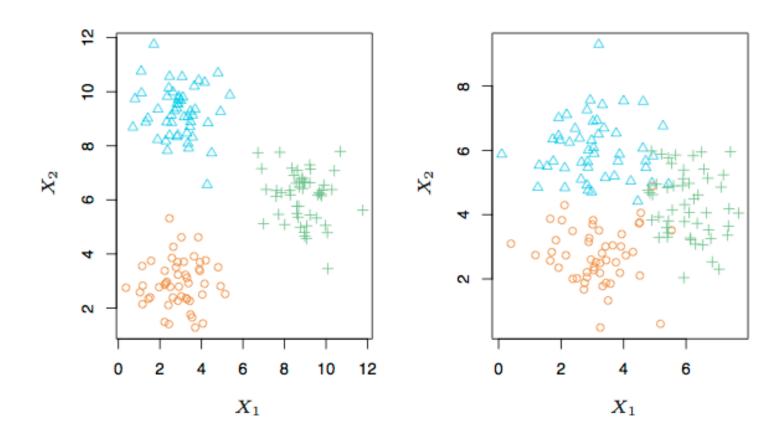
Supervised vs. Unsupervised Learning

- We can divide all learning problems into Supervised and Unsupervised situations
- >Supervised Learning:
 - Supervised Learning is where both the predictors, **X**_i, and the response, Y_i, are observed.
 - > This is the situation you deal with in Linear Regression classes (e.g. GSBA 524).
 - > Most of this course will also deal with supervised learning.

➤ Unsupervised Learning:

- \triangleright In this situation only the X_i 's are observed.
- > We need to use the **X**_i's to guess what Y would have been and build a model from there.
- > A common example is market segmentation where we try to divide potential customers into groups based on their characteristics.
- >A common approach is clustering.
- > We will consider unsupervised learning at the end of this course.

A Simple Clustering Example



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Regression vs. Classification

- >Supervised learning problems can be further divided into regression and classification problems.
- >Regression covers situations where Y is continuous/ numerical. e.g.
 - > Predicting the value of the Dow in 6 months.
 - > Predicting the value of a given house based on various inputs.
- >Classification covers situations where Y is categorical e.g.
 - > Will the Dow be up (U) or down (D) in 6 months?
 - > Is this email a SPAM or not?

Different Approaches

- >We will deal with both types of problems in this course.
- Some methods work well on both types of problem e.g. Decision Trees
- >Other methods work best on Regression, e.g. Linear Regression, or on Classification, e.g. k-Nearest Neighbors.

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