

**algorithm** *count\_crit\_pairs*

**inputs**

$S$ , the current basis  
 $L$ , the current set of critical pairs of  $S$   
 $f$ , a new polynomial to add to  $S$

**outputs**

the number  $m$  of new critical pairs of minimal degree  $d$  generated by  $f$  relative to  $S$  and  $L$

**do**

let  $t = \text{lm}(f)$

let  $m = d = 0$

— *First count number of new pairs that survive the criteria*

**for**  $i = 1, \dots, |S|$  **do**

let  $u = \text{lm}(S_i)$

**if**  $t, u$  are not coprime **then**

let  $v = \text{lcm}(t, u)$

— *Terminating at  $i - 1$  should solve the Buchberger triplet problem*

— *Easy optimization: avoid a loop by rewriting the following two ifs*

**if**  $\text{lm}(S_j) \nmid v \ \forall j = 1, \dots, i - 1$  **then**

**if**  $d = 0$  or  $\deg v < d$  **then**

let  $d = \deg v$

let  $m = 1$

**else if**  $\deg v = d$  **then**

add 1 to  $m$

— *Now count number of old pairs that survive the criteria*

**for**  $(p, q) \in L$  **do**

let  $u = \text{lcm}(\text{lm}(p), \text{lm}(q))$

let  $e = \deg(u)$

**if**  $d = 0$  or  $e \leq d$  **then**

**if**  $\text{lcm}(t, \text{lm}(s)) \nmid u \ \forall s \in S$  **then**

**if**  $d = 0$  or  $e < d$  **then**

let  $d = e$

let  $m = 1$

**else if**  $e = d$  **then**

add 1 to  $m$

**return**  $m, d$