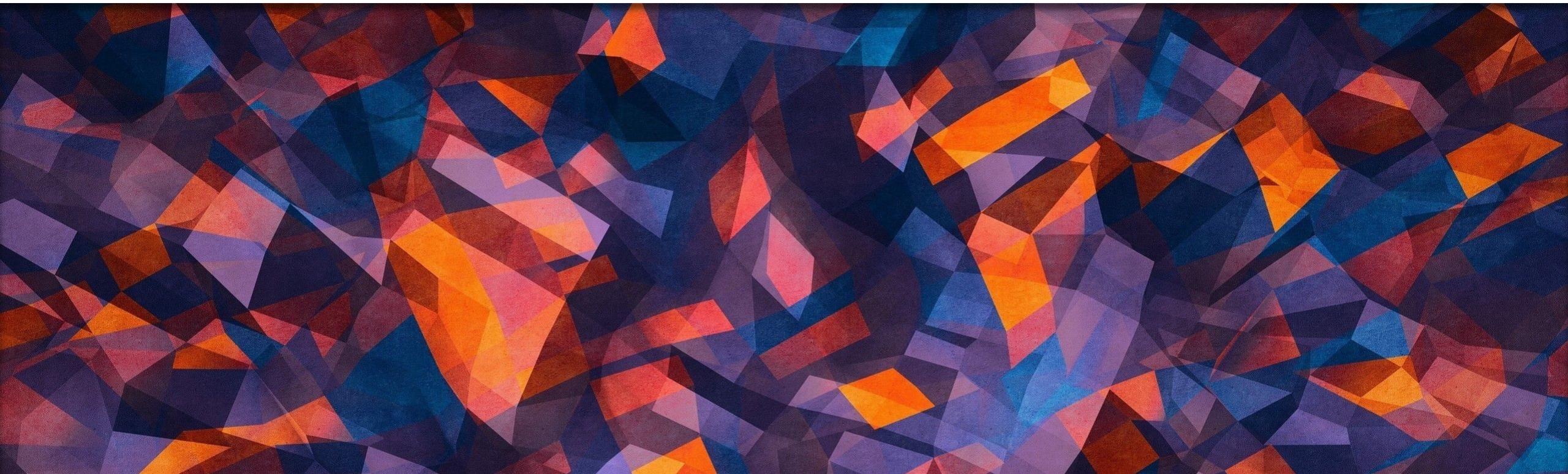




Universität St.Gallen



Web-based Autonomous Systems

# Knowledge Representation and Reasoning for the Web

Chair for Interaction- and Communication-based Systems (ICS-HSG)

# Our Journey

Prerequisites:  
• ASSE  
• (...)



Week 1:  
**Introduction**



Week 2:  
**A Web for Machines**



Week 3:  
**Knowledge Representation  
and Reasoning for the Web**



Week 4:  
**Linked Data and Distributed  
Knowledge Graphs**



Week 6 (Coordination I):  
**Agent Communication  
and Interaction**



Week 5:  
**Hypermedia Agents (Arch.  
and Programming)**



Week 10:  
**Game Theory and  
Social Choice**



Week 11:  
**Reinforcement Learning  
and Multi-Agent Learning**



Week 9 (Coordination IV):  
**Trust & Reputation**



Week 12:  
**An Industry Perspective**



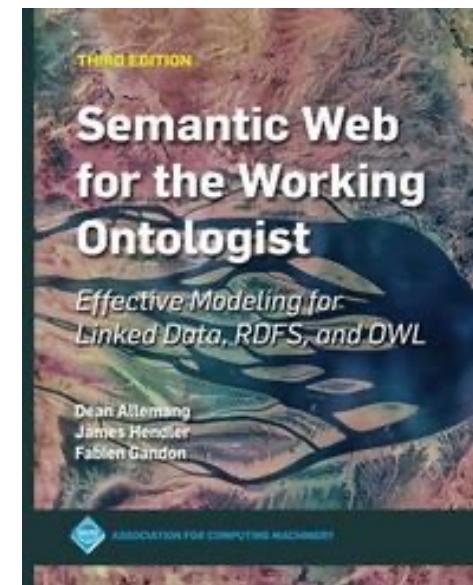
**Exercises**

Ex1: Writing Your First Agent(s)!  
Ex2: Automated Planning  
Ex3: Web Ontologies  
Ex4: Deductive Reasoning on the Web  
Ex5: Cognitive Agents in Hypermedia Env.  
Ex6: Interacting Agents on the Web

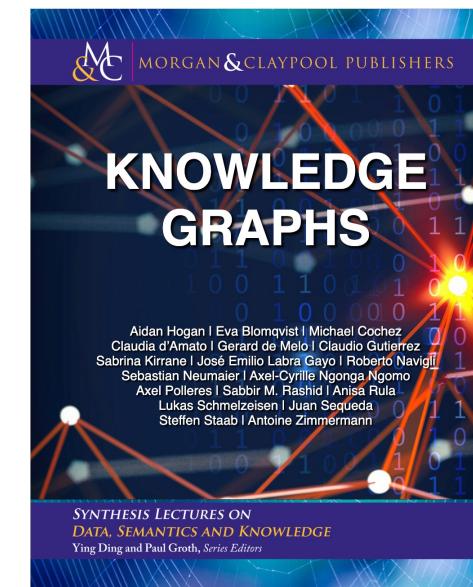
Ex7: Ant Colony Optimization  
Ex8: Organized Agent  
Ex9: Trustworthy Agents  
Ex10: Axelrod's Agents  
Ex11: Reinforcement Learning Agents  
Course Review and Q&A

# Today's Agenda

- Web Ontologies
  - Description Logics and OWL
  - Building Web Ontologies with Protégé (Tutorial)
- Knowledge Graphs
  - Graph Data Models
  - Querying Graph Datasets



[Allemang et al., 2020]



<https://kgbook.org/>

Chapter 1  
Chapter 2  
Chapter 4  
(Chapter 5)

An ontology is the **formal, explicit specification** of a **shared conceptualization** of an **area of interest**  
 [Studer et al., 1998].

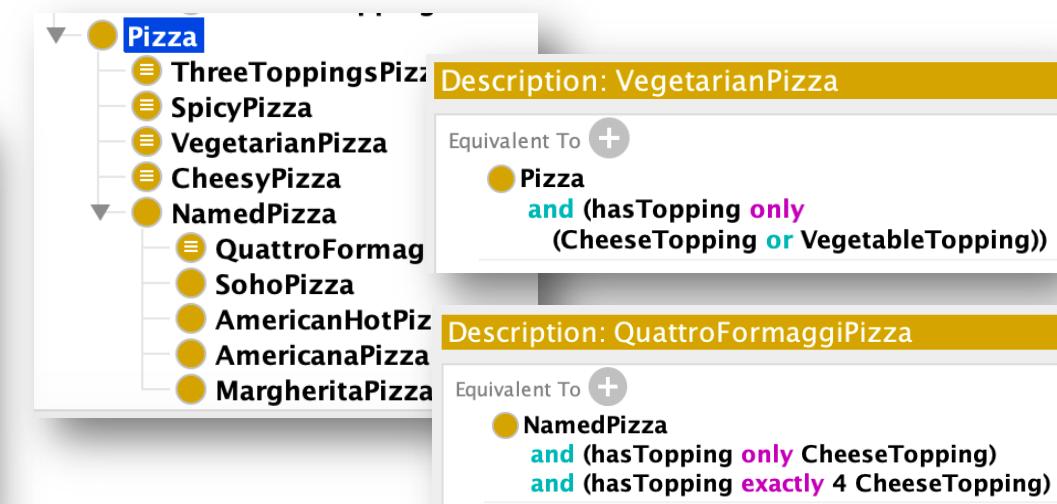
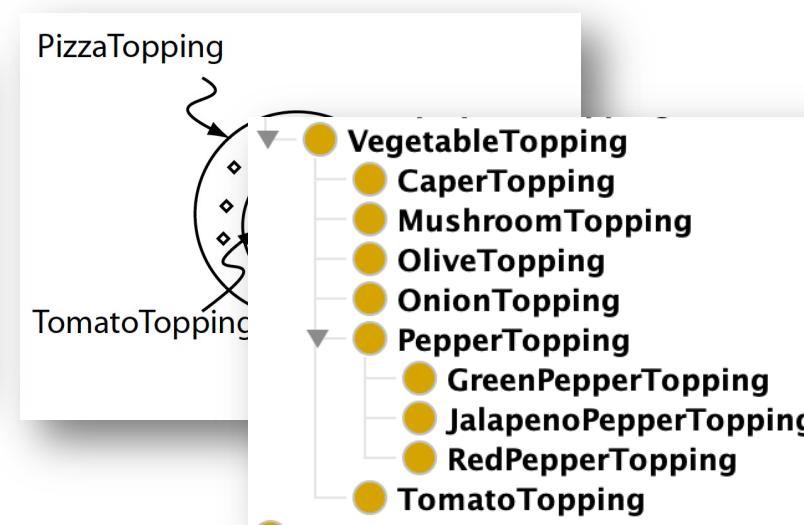
using a formal knowledge representation language, such as the **Web Ontology Language (OWL)**

the conceptual model is represented explicitly

usually defined and adopted by a group of people / a community

abstract simplified view (conceptual model)

ex., pizza



# Last Week on First-Order Logic...



The Dreadbury Mansion Mystery

1. Someone who lives in Dreadbury Mansion killed Aunt Agatha.
2. Agatha, the butler, and Charles live in I
3. A killer always hates his victim, and is r
4. Charles hates no one that Aunt Agatha
5. Agatha hates everyone except the butl
6. The butler hates everyone not richer th
7. The butler hates everyone Aunt Agatha
8. No one hates everyone.
9. Agatha is not the butler.

Who killed Aunt Agatha?

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A glimpse of reasoning in first-order logic

**A Glimpse of Reasoning in First-Order Logic**

A killer always hates his victim and is never richer than his victim.

- $\forall x, y(killed(x, y) \rightarrow hates(x, y))$
- $\forall x, y(killed(x, y) \rightarrow \neg richer(x, y))$

Charles hates no one that Aunt Agatha hate

- $\forall x(hates(charles, x) \rightarrow \neg hates(agatha, x))$

$$\frac{killed(x, y) \rightarrow hates(x, y)}{killed(charles, y) \rightarrow \neg hates(agatha, y)}$$

Agatha hates everyone except the butler.

- $\forall x(\neg hates(agatha, x) \leftrightarrow x = butler)$

$$\frac{killed(charles, y) \rightarrow \neg hates(agatha, y)}{killed(charles, y)}$$

Agatha is not the butler.

- $\neg agatha = butler$

$$\frac{killed(charles, y)}{\neg k}$$

WebSPASS - Interactive SPASS Input Form Submission

Go to: [Upload Form](#) [Interactive Input Form](#) [Help](#)

You are running 'Mozilla/5.0 (Macintosh; Intel Mac OS X 10\_15\_7) AppleWebKit/537.36 (KHTML, like Gecko) Chrome/98.0.4758.109 Safari/537.36' from '51.154.106.193'

Your WebSPASS Input Form Submission is now being processed...

```
-----SPASS-START-----
Input Problem:
1[0:Inp] || -> lives(skc1)*.
2[0:Inp] || -> lives(a)*.
3[0:Inp] || -> lives(b)*.
4[0:Inp] || -> lives(c)*.
5[0:Inp] || -> lives(d)*.
6[0:Inp] || -> lives(e)*.
7[0:Inp] || -> lives(f)*.
SPASS V 3.9
7[0:Inp] || -> lives(g)*.
SPASS beiseite: Proof found.
Problem: /tmp/webspass-webform_2022-03-08_00:47:02_174341.txt
SPASS derived 44 clauses, backtracked 11 clauses, performed 2 splits and kept 51 clauses.
```

→ computationally expensive

First-order Logic is very expressive,  
so why not use it for the Semantic Web?

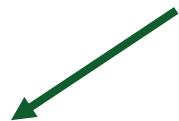
<https://spass-prover.org/>

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5

# Description Logics and OWL

Reasoning in First-Order Logic is **semi-decidable** and **intractable**



There are algorithms that:

- can always prove that a true formula is true
- never say that a false formula is false
- BUT there will **always** be formulas that are false for which the algorithm does not answer (for instance, runs forever)

Theoretical Computer Science 39 (1985) 297-308  
North-Holland

297

## THE INTRACTABILITY OF RESOLUTION

Armin HAKEN

Department of Computer Science, University of Toronto, Toronto, Ontario M5S 1A4, Canada

Communicated by R. M. Karp

Received January 1984

Revised August 1984

**Abstract.** We prove that, for infinitely many disjunctive normal form propositional calculus tautologies  $\xi$ , the length of the shortest resolution proof of  $\xi$  cannot be bounded by any polynomial of the length of  $\xi$ . The tautologies we use were introduced by Cook and Reckhow (1979) and encode the pigeonhole principle. Extended resolution can furnish polynomial length proofs of these formulas.

Description Logics (DLs) are **fragments of First-Order Logic**

- designed to achieve **favorable trade-offs** between **expressivity** and **performance**  
 $\Rightarrow$  decidability and tractability depend on the **expressive power** of the DL at hand

more limited  
↓ + ↓  
cost

The Web Ontology Language (OWL) was strongly influenced by Description Logics

⇒ DARIA: Agents that have to share logic

Armin Haken, The Intractability of Resolution, Theoretical Computer Science, Volume 39, 1985.  
R.J. Brachman, H.J. Levesque. Knowledge Representation and Reasoning. Elsevier. 2004.

# Description Logics

**Description Logics (DLs)** are a family of logics that represent knowledge of an application domain (the “world”) in terms of:

**Concepts or classes** describe sets of things

- *FacultyMember, Employee, Person, University, Country, ...*

! described + refine (level)  
 ↳ class, not within  
 ↳ class !

Terminological vocabulary

**Roles or properties** describe binary relations among things

- *employedBy, locatedIn, ...*

**Individuals** are instances of classes

- *Andrei, HSG, Switzerland, ...*

Assertional vocabulary

Three kinds of **formulas** or **axioms** are common to all DLs:

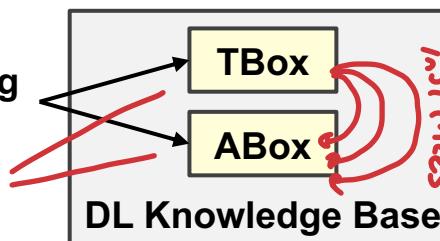
- concept inclusion:  $C \sqsubseteq D$ , where  $C$  and  $D$  are names of concepts
- concept assertion:  $C(a)$ , where  $C$  is a concept name and  $a$  is the name of an individual
- role assertion:  $R(a, b)$ , where  $R$  is a role name, and  $a$  and  $b$  are names of individuals

Terminological Knowledge (TBox)

Assertional Knowledge (ABox)

Spatial endpoint

Interface ← Reasoning Engine  
 > Separation of concerns!  
 > Reasoning tasks



$$TBox = \{ FacultyMember \sqsubseteq Employee, Employee \sqsubseteq Person \}$$

$$ABox = \{ FacultyMember(Andrei), University(HSG), employedBy(Andrei, HSG) \}$$

A. Zimmermann, Knowledge Representation and Reasoning, MINES Saint-Étienne, 2021.

F. Baader and W. Nutt, Basic Description Logics, The Description Logic Handbook: Theory, Implementation, and Applications. 2003.

$C$ : Employees of HSG  
 $D$ : People interested in X

- [ $\mathcal{EL}$ ] Existential Language
  - concept intersection ( $C \sqcap D$ ), existential restrictions ( $\exists R.C$ )
- [ $\mathcal{ALC}$ ] Attributive Language with Complement
  - concept intersection ( $C \sqcap D$ ), concept union ( $C \sqcup D$ ), concept negation ( $\neg C$ ), universal restrictions ( $\forall R.C$ ), and existential restrictions ( $\exists R.C$ )
  - [ $\mathcal{S}$ ] extends  $\mathcal{ALC}$  with transitive closure ( $Trans(R)$ )

Extensions:

- [ $\mathcal{H}$ ] adds role inclusion ( $R \sqsubseteq S$ )
  - [ $\mathcal{R}$ ] adds (limited) complex role inclusion ( $R_1 \circ R_2 \sqsubseteq S$ ), role reflexivity ( $Ref(R)$ ), role irreflexivity ( $Irref(R)$ ), role disjointness ( $Disj(R, S)$ ), and the universal role ( $U$ )
- [ $\mathcal{O}$ ] adds (limited) nominals ( $\{a_1, \dots, a_n\}$ )
- [ $\mathcal{I}$ ] adds inverse roles ( $R^-$ )
- [ $\mathcal{F}$ ] adds (limited) functional roles ( $Func(R)$ )
  - [ $\mathcal{N}$ ] adds (limited) number restrictions ( $* R$ , where  $* \in \{ \geq, \leq, = \}$ )
    - [ $\mathcal{Q}$ ] adds (limited) qualified number restrictions ( $* R.C$ , where  $* \in \{ \geq, \leq, = \}$ )
- [ $(\mathcal{D})$ ] adds datatype properties, data values, or data types

# DLs: A Family of Logics

A  
 Fragment of ...

The label of the logic encodes its expressivity:  $\mathcal{ALCN}$ , etc.

of  
 Fragment

# TBox Examples in $\mathcal{ALC}$

Atomic concepts: **Person**, **Female**, **Dragon**

Atomic roles: **hasChild**

Concepts are constructed according to the following syntax rule:

$C, D ::= A \mid$  (atomic concept)

$\top \mid$  (top concept) — root

$\perp \mid$  (bottom concept) — nothing

$\neg C \mid$  (atomic negation)  
sub-class of all other concepts

$C \sqcap D \mid$  (intersection)

$C \sqcup D \mid$  (union)

$\forall R.C \mid$  (universal restriction)  
at least one individual of that class

$\exists R.C \mid$  (existential restriction)

\*  $n R$ , where \*  $\in \{\geq, \leq, =\}$  (number restrictions)

**Woman**  $\equiv$  **Person**  $\sqcap$  **Female** (equivalence axiom)

at least one child can be anything

**Parent**  $\equiv$  **Person**  $\sqcap \exists$  **hasChild**. $\top$

**PersonWithoutChildren**  $\equiv$  **Person**  $\sqcap \neg$  **Parent**  
— no children

**MotherOfOnlyDragons**  $\equiv$  **Woman**  $\sqcap$  **Parent**  $\sqcap$   
 $\forall$  **hasChild**.**Dragon**

**MotherOfOnlyManyDragons**  $\equiv$  ? (at least 3)



We can't! We need to extend to  $\mathcal{ALCN}$

# TBox Examples in $\mathcal{ALCN}$

Atomic concepts: **Person**, **Female**, **Dragon**

Atomic roles: **hasChild**

Concepts are constructed according to the following syntax rule:

- $C, D ::= A \mid$  (atomic concept)
- $\top \mid$  (top concept)
- $\perp \mid$  (bottom concept)
- $\neg C \mid$  (atomic negation)
- $C \sqcap D \mid$  (intersection)
- $C \sqcup D \mid$  (union)
- $\forall R. C \mid$  (universal restriction)
- $\exists R. C \mid$  (existential restriction)
- \*  $n R$ , where \* $\in \{\geq, \leq, =\}$  (number restrictions)

constructors

**Woman**  $\equiv$  **Person**  $\sqcap$  **Female** ( $\equiv$  denotes equivalence)

**Parent**  $\equiv$  **Person**  $\sqcap$   $\exists$  **hasChild**. $\top$

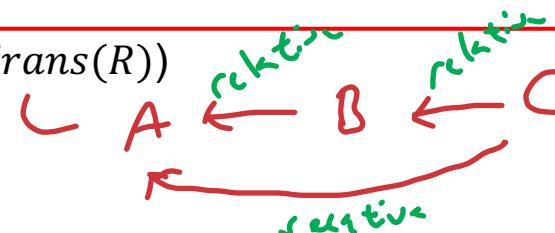
**PersonWithoutChildren**  $\equiv$  **Person**  $\sqcap$   $\neg$  **Parent**

**MotherOfOnlyDragons**  $\equiv$  **Woman**  $\sqcap$  **Parent**  $\sqcap$   $\forall$  **hasChild**.**Dragon**

**MotherOfOnlyManyDragons**  $\equiv$  **MotherOfOnlyDragons**  $\sqcap$   $\geq 3$  **hasChild**



- **[EL]** Existential Language
    - concept intersection ( $C \sqcap D$ ), existential restrictions ( $\exists R. C$ )
  - **[ALC]** Attributive Language with Complement
    - concept intersection ( $C \sqcap D$ ), concept union ( $C \sqcup D$ ), concept negation ( $\neg C$ ), universal restrictions ( $\forall R. C$ ), and existential restrictions ( $\exists R. C$ )
    - **[S]** extends **ALC** with transitive closure ( $Trans(R)$ )
- Extensions:
- **[H]** adds role inclusion ( $R \sqsubseteq S$ )
    - **[R]** adds (limited) complex role inclusion ( $R_1 \circ R_2 \sqsubseteq S$ ), role reflexivity ( $Ref(R)$ ), role irreflexivity ( $Irref(R)$ ), role disjointness ( $Disj(R, S)$ ), and the universal role ( $U$ )
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  - **[F]** adds (limited) functional properties ( $Func(R)$ )
    - **[N]** adds (limited) number restrictions ( $* R$ , where  $* \in \{ \geq, \leq, = \}$ )
      - **[Q]** adds (limited) qualified number restrictions ( $* R. C$ , where  $* \in \{ \geq, \leq, = \}$ )
  - **[(D)]** adds datatype properties, data values, or data types



OWL DL:  $SHON^{(\mathcal{D})}$   
 OWL 2 DL:  $SROIQ^{(\mathcal{D})}$

# The Pizza Ontology Revisited

An ontology is the **formal, explicit specification** of a **shared conceptualization** of an **area of interest** [Studer et al., 1998].

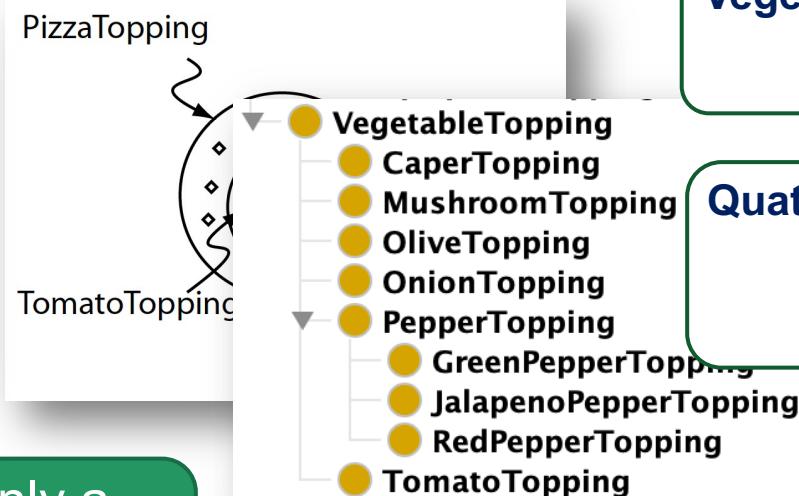
using a formal knowledge representation language, such as the **Web Ontology Language (OWL)**

the conceptual model is represented explicitly

abstract simplified view (conceptual model)

ex., pizza

usually defined and adopted by a group of people / a community



We can represent only a finite number of axioms

**VegetarianPizza**  $\equiv$  **Pizza**  $\sqcap \forall \text{hasTopping}.\text{(CheeseTopping} \sqcup \text{VegetableTopping)}$

**QuattroFormaggiPizza**  $\equiv$  **NamedPizza**  $\sqcap \forall \text{hasTopping}.\text{ChessTopping}$   
 $\sqcap = 4 \text{ hasTopping}.\text{ChessTopping}$

**MargheritaPizza**  $\equiv$  **NamedPizza** and **(hasTopping only CheeseTopping)** and **(hasTopping exactly 4 CheeseTopping)**

# Reasoning with the Pizza Ontology

Deductive reasoning is used to **bridge the gap** between what is represented explicitly and what is known implicitly

**Pizza**

- ThreeToppingsPizza
- SpicyPizza
- VegetarianPizza
- CheeseTopping
- Name
- QuattroFormaggiPizza
- SoAnAmericanaPizza
- Ma

Description: VegetarianPizza

Equivalent To +

Pizza  
and (hasTopping only (CheeseTopping or VegetableTopping))

Description: QuattroFormaggiPizza

Equivalent To +

NamedPizza  
and (hasTopping only CheeseTopping)  
and (hasTopping exactly 4 CheeseTopping)

Description: CheesyPizza

Equivalent To +

Pizza  
and (hasTopping some CheeseTopping)

Description: ThreeToppingsPizza

Equivalent To +

Pizza  
and (hasTopping min 3 owl:Thing)

Description: SpicyPizza

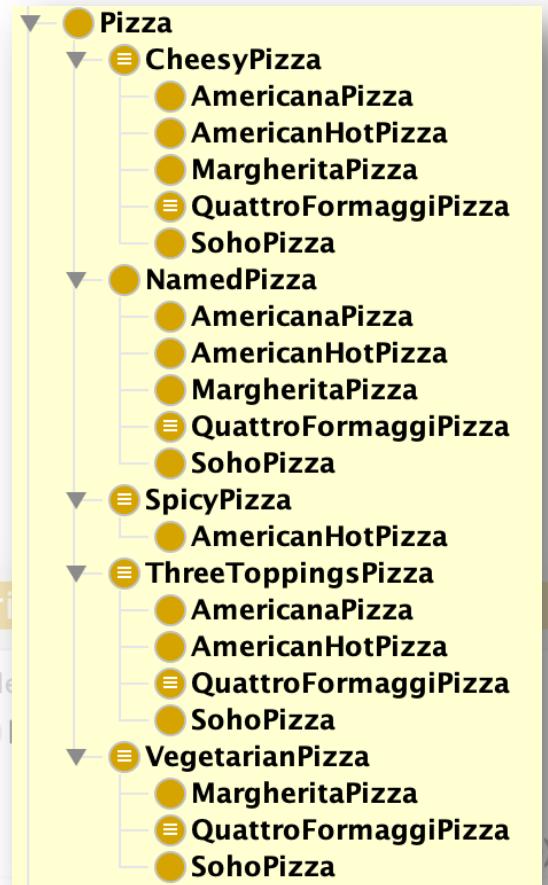
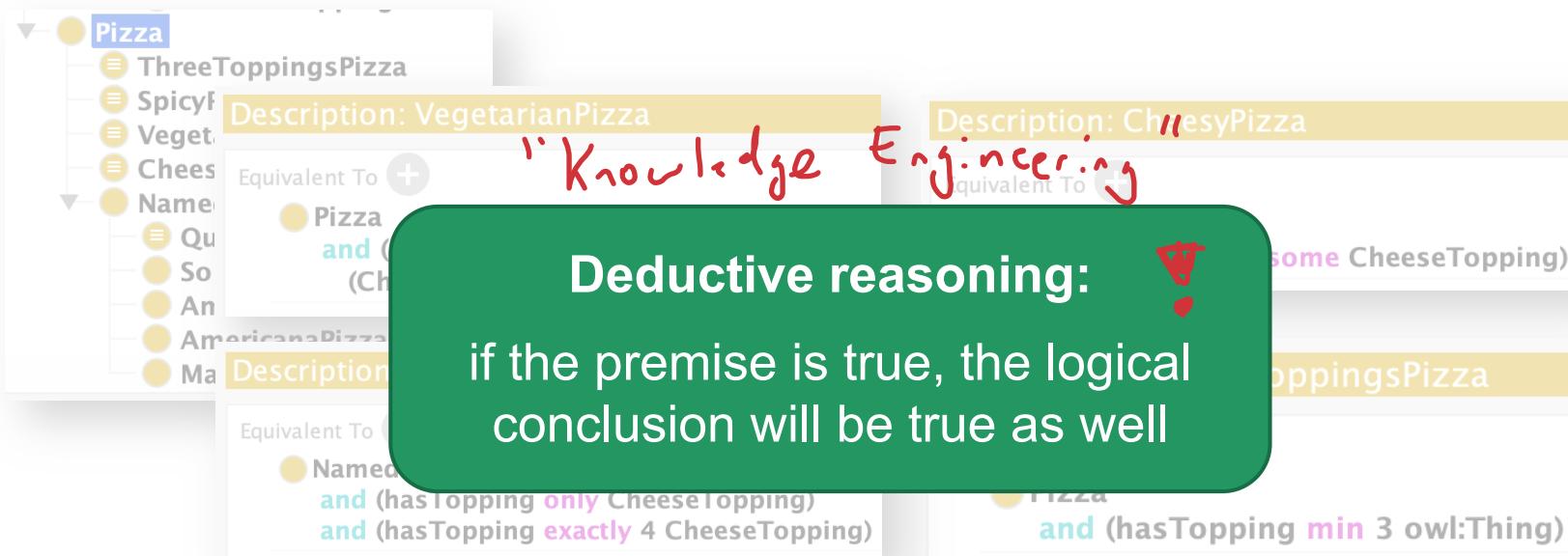
Equivalent To +

Pizza  
and (hasTopping some (PizzaTopping  
and (hasSpiciness some Hot)))

Explicit knowledge

# Reasoning with the Pizza Ontology

Deductive reasoning is used to bridge the gap between what is represented explicitly and what is known implicitly



What we have seen so far, is **DL syntax**

- rules for constructing well-formed sequences of symbols

$$\text{VegetarianPizza} \equiv \text{Pizza} \sqcap \forall \text{ hasTopping}.(\text{CheeseTopping} \sqcup \text{VegetableTopping})$$

**DL semantics** define rules for deriving the meaning of complex sequences of symbols from atomic symbols

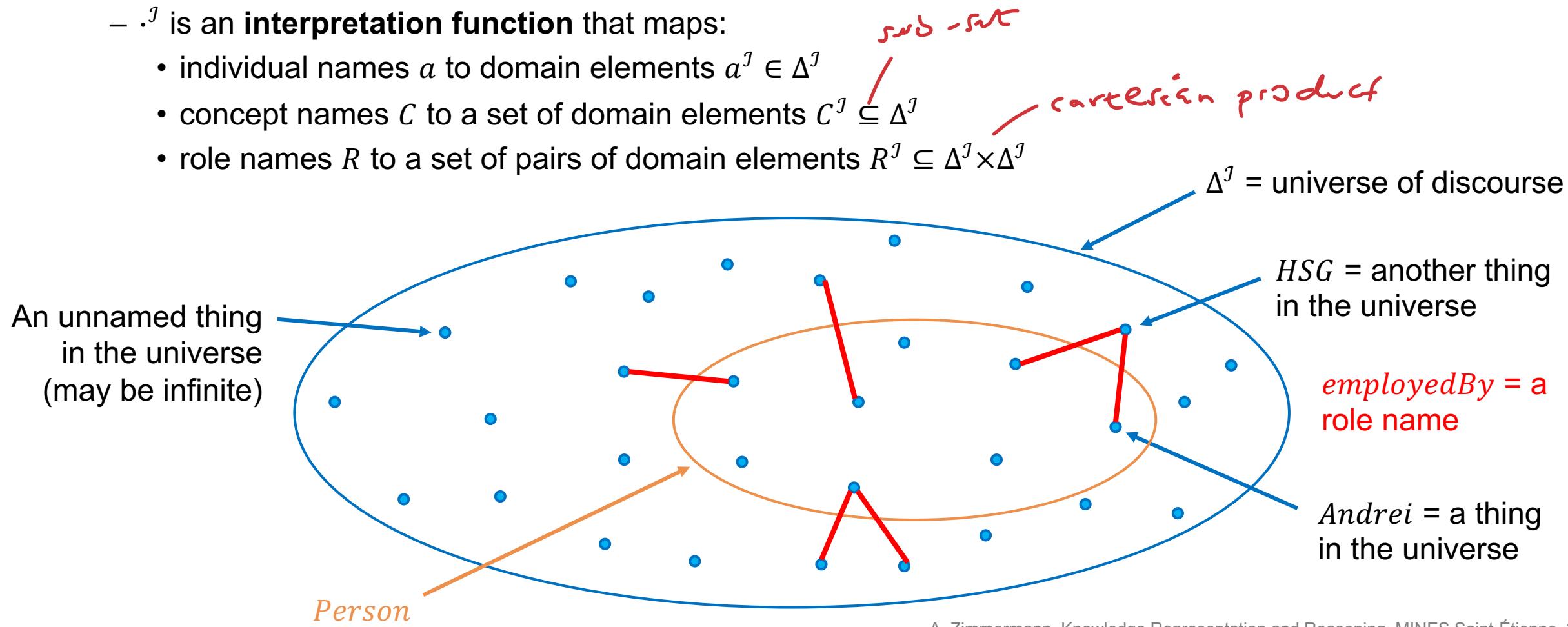
- meaning is derived based on an **interpretation** within a **formal model** over a **domain**
- there are usually **many possible interpretations** over the same domain

↪ need t. remove ambiguity

# DL Semantics: Interpretation

An **interpretation** is a pair  $\mathcal{I} = (\Delta^{\mathcal{I}}, \cdot^{\mathcal{I}})$  such that:

- $\Delta^{\mathcal{I}}$  is a non-empty set of individuals (**domain of interpretation or universe of discourse**)
- $\cdot^{\mathcal{I}}$  is an **interpretation function** that maps:
  - individual names  $a$  to domain elements  $a^{\mathcal{I}} \in \Delta^{\mathcal{I}}$
  - concept names  $C$  to a set of domain elements  $C^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}}$
  - role names  $R$  to a set of pairs of domain elements  $R^{\mathcal{I}} \subseteq \Delta^{\mathcal{I}} \times \Delta^{\mathcal{I}}$



# $\mathcal{ALCN}$ Semantics: Interpretation

## Syntax

Concepts are constructed according to the following syntax rule:

- $C, D ::= A \mid$  (atomic concept)
- $\top \mid$  (top concept)
- $\perp \mid$  (bottom concept)
- $\neg C \mid$  (atomic negation)
- $C \sqcap D \mid$  (intersection)
- $C \sqcup D \mid$  (union)
- $\forall R. C \mid$  (universal restriction)
- $\exists R. C \mid$  (existential restriction)
- \*  $n R$ , where \* $\in \{\geq, \leq, =\}$  (number restrictions)

## Semantics

Extending the interpretation function  $\cdot^J$  to concept definitions:

- $(A^J \subseteq \Delta^J)$
- $\top^J = \Delta^J$
- $\perp^J = \emptyset$
- $(\neg C)^J = \Delta^J \setminus C^J$
- $(C \sqcap D)^J = C^J \cap D^J$
- $(C \sqcup D)^J = C^J \cup D^J$
- $(\forall R. C)^J = \{ x \in \Delta^J \mid \forall y (x, y) \in R^J \rightarrow y \in C^J \}$
- $(\exists R. C)^J = \{ x \in \Delta^J \mid \exists y (x, y) \in R^J \wedge y \in C^J \}$
- $(\geq n R)^J = \{ x \in \Delta^J \mid |\{ y \mid (x, y) \in R^J \}| \geq n \}$
- (similar definitions for the other number restrictions)

role

new concept: for any  
Set of x

# DL Semantics: Satisfiability

Given an interpretation  $\mathcal{I}$ , the **satisfaction** relation  $\models$  is defined as follows:

- $\mathcal{I} \models C \sqsubseteq D$  if and only if  $C^{\mathcal{I}} \sqsubseteq D^{\mathcal{I}}$  (concept inclusion axiom)
- $\mathcal{I} \models C(a)$  if and only if  $a^{\mathcal{I}} \in C^{\mathcal{I}}$  (concept assertion axiom)
- $\mathcal{I} \models R(a, b)$  if and only if  $(a^{\mathcal{I}}, b^{\mathcal{I}}) \in R^{\mathcal{I}}$  (role assertion axiom)
- $\mathcal{I} \models C \equiv D$  if and only if  $C^{\mathcal{I}} = D^{\mathcal{I}}$  (equivalence axiom)

*FacultyMember*  $\sqsubseteq$  *Person*

*FacultyMember(Andrei)*

*Human*  $\equiv$  *Person*

*Human*

*Person*

*FacultyMember*

$\Delta^{\mathcal{I}}$  = universe of discourse

*HSG* = another thing  
in the universe

*Andrei* = a thing  
in the universe

*employedBy(Andrei, HSG)*

# DL Semantics: Satisfiability

Given an interpretation  $\mathcal{I}$ , the **satisfaction** relation  $\models$  is defined as follows:

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- $\mathcal{I} \models C \equiv D$  if and only if  $C^{\mathcal{I}} = D^{\mathcal{I}}$  (equivalence axiom)

An interpretation  $\mathcal{I}$  satisfies a TBox  $T$  if and only if  $\mathcal{I}$  satisfies all axioms in  $T$ .  
( $\mathcal{I}$  is a model of  $T$ )

An interpretation  $\mathcal{I}$  satisfies an ABox  $A$  if and only if  $\mathcal{I}$  satisfies all axioms in  $A$ .  
( $\mathcal{I}$  is a model of  $A$ )

# Reasoning Tasks for the TBox

**Satisfiability:** A concept  $C$  is satisfiable with respect to a TBox  $T$  if there exists a model  $\mathcal{J}$  of  $T$  such that  $C^{\mathcal{J}}$  is nonempty ( $\mathcal{J}$  is a model of  $C$ ).

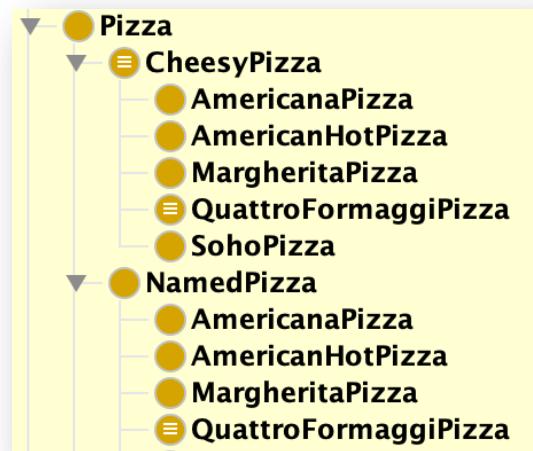


Concept Satisfiability [TBox]  
(**CheeseTopping** and  
**VegetableTopping** are disjoint)

# Reasoning Tasks for the TBox

**Satisfiability:** A concept  $C$  is satisfiable with respect to a TBox  $T$  if there exists a model  $\mathcal{J}$  of  $T$  such that  $C^{\mathcal{J}}$  is nonempty ( $\mathcal{J}$  is a model of  $C$ ).

**Subsumption:** A concept  $C$  is subsumed by a concept  $D$  with respect to a TBox  $T$  if  $C^{\mathcal{J}} \subseteq D^{\mathcal{J}}$  for all models  $\mathcal{J}$  of  $T$ .



intupr.  
of  $C$

intupr.  
of  $C$

subset  
of

Concept Subsumption [TBox]  
(inferred classification)

# Reasoning Tasks for the TBox

**Satisfiability:** A concept  $C$  is satisfiable with respect to a TBox  $T$  if there exists a model  $\mathcal{J}$  of  $T$  such that  $C^{\mathcal{J}}$  is nonempty ( $\mathcal{J}$  is a model of  $C$ ).

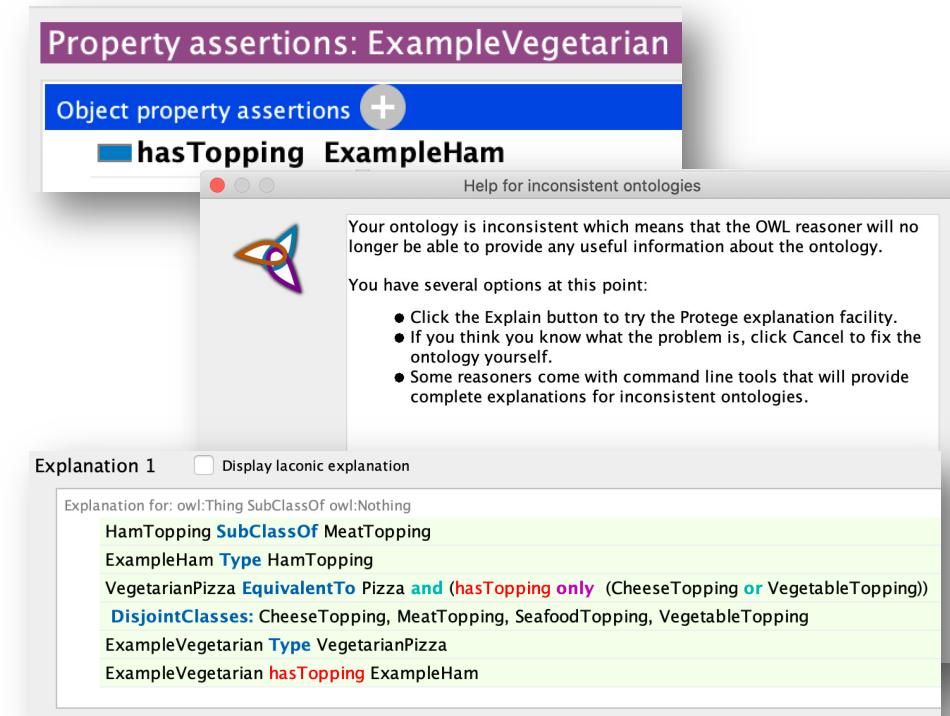
**Subsumption:** A concept  $C$  is subsumed by a concept  $D$  with respect to a TBox  $T$  if  $C^{\mathcal{J}} \subseteq D^{\mathcal{J}}$  for all models  $\mathcal{J}$  of  $T$ .

**Equivalence:** Two concepts  $C$  and  $D$  are equivalent with respect to a TBox  $T$  if  $C^{\mathcal{J}} = D^{\mathcal{J}}$  for all models  $\mathcal{J}$  of  $T$ .

**Disjointness:** Two concepts  $C$  and  $D$  are disjoint with respect to a TBox  $T$  if  $C^{\mathcal{J}} \cap D^{\mathcal{J}} = \emptyset$  for all models  $\mathcal{J}$  of  $T$ .

# Reasoning Tasks for the ABox

**Consistency:** An ABox  $A$  is consistent with respect to a TBox  $T$  if there exists an interpretation  $\mathcal{I}$  such that  $\mathcal{I}$  is a model of both  $A$  and  $T$ .

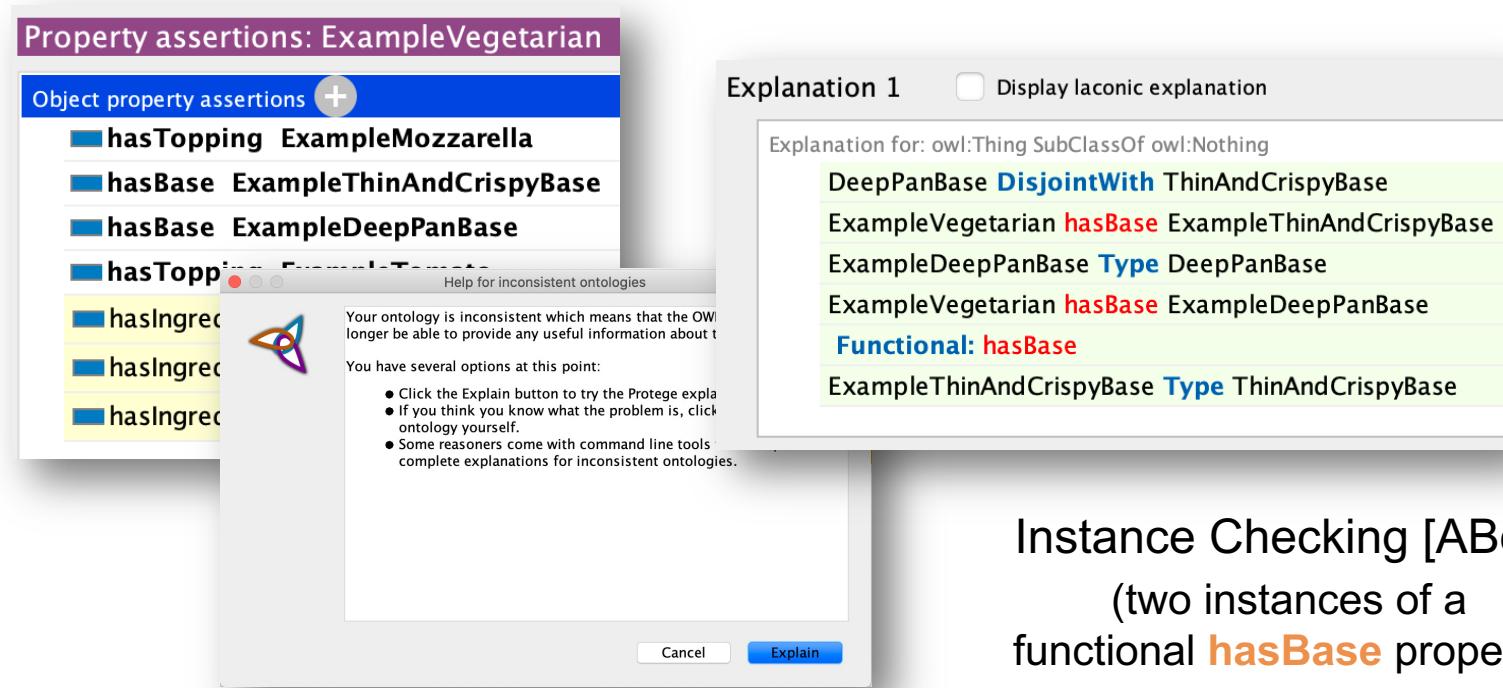


Consistency [ABox]  
(creating a **VegetarianPizza** with ham)

# Reasoning Tasks for the ABox

**Consistency:** An ABox  $A$  is consistent with respect to a TBox  $T$  if there exists an interpretation  $\mathcal{I}$  such that  $\mathcal{I}$  is a model of both  $A$  and  $T$ .

**Instance Checking:** An assertion  $\alpha$  is entailed by an ABox  $A$  and we write  $A \models \alpha$  if all interpretations  $\mathcal{I}$  that satisfy  $A$ , that is all models of  $A$ , also satisfy  $\alpha$ .



The screenshot shows the Protege ontology editor interface. On the left, a list of property assertions for an individual named 'ExampleVegetarian' is displayed under the heading 'Property assertions: ExampleVegetarian'. The assertions include:

- Object property assertions:
  - hasTopping ExampleMozzarella
  - hasBase ExampleThinAndCrispyBase
  - hasBase ExampleDeepPanBase
  - hasTopping ExampleThinAndCrispyBase
  - hasIngredient ExampleMozzarella
  - hasIngredient ExampleThinAndCrispyBase
  - hasIngredient ExampleDeepPanBase

A message at the bottom of this list states: "Your ontology is inconsistent which means that the OWL reasoner will no longer be able to provide any useful information about it."

On the right, a modal dialog titled 'Explanation 1' is open. It contains an explanation for the assertion 'owl:Thing SubClassOf owl:Nothing'. The explanation text is as follows:

```

Explanation for: owl:Thing SubClassOf owl:Nothing
DeepPanBase DisjointWith ThinAndCrispyBase
ExampleVegetarian hasBase ExampleThinAndCrispyBase
ExampleDeepPanBase Type DeepPanBase
ExampleVegetarian hasBase ExampleDeepPanBase
Functional: hasBase
ExampleThinAndCrispyBase Type ThinAndCrispyBase

```

Below the explanation, there is a note: "You have several options at this point:" followed by a bulleted list:

- Click the Explain button to try the Protege explanation.
- If you think you know what the problem is, click the Fix button.
- Some reasoners come with command line tools to complete explanations for inconsistent ontologies.

At the bottom of the dialog are 'Cancel' and 'Explain' buttons.

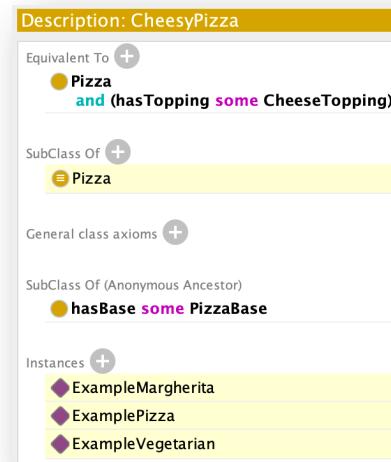
**Instance Checking [ABox]**  
 (two instances of a functional **hasBase** property)

# Reasoning Tasks for the ABox

**Consistency:** An ABox  $A$  is consistent with respect to a TBox  $T$  if there exists an interpretation  $\mathcal{I}$  such that  $\mathcal{I}$  is a model of both  $A$  and  $T$ .

**Instance Checking:** An assertion  $\alpha$  is entailed by an ABox  $A$  and we write  $A \models \alpha$  if all interpretations  $\mathcal{I}$  that satisfy  $A$ , that is all models of  $A$ , also satisfy  $\alpha$ .

**Retrieval Problem:** Given an ABox  $A$  and a concept  $C$ , find all individuals  $a$  such that  $A \models C(a)$ .



Retrieval Problem [ABox]  
(inferred instances of **CheesyPizza**)

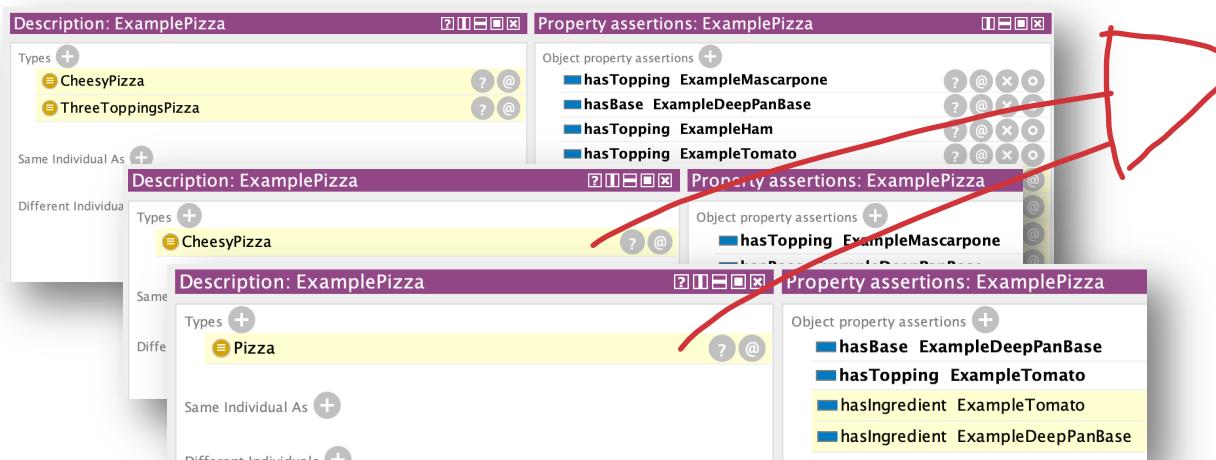
# Reasoning Tasks for the ABox

**Consistency:** An ABox  $A$  is consistent with respect to a TBox  $T$  if there exists an interpretation  $\mathcal{I}$  such that  $\mathcal{I}$  is a model of both  $A$  and  $T$ .

**Instance Checking:** An assertion  $\alpha$  is entailed by an ABox  $A$  and we write  $A \models \alpha$  if all interpretations  $\mathcal{I}$  that satisfy  $A$ , that is all models of  $A$ , also satisfy  $\alpha$ .

**Retrieval Problem:** Given an ABox  $A$  and a concept  $C$ , find all individuals  $a$  such that  $A \models C(a)$ .

**Realization Problem:** Given an individual  $a$  and a set of concepts, find the most specific concepts  $C$  from the set such that  $A \models C(a)$ .



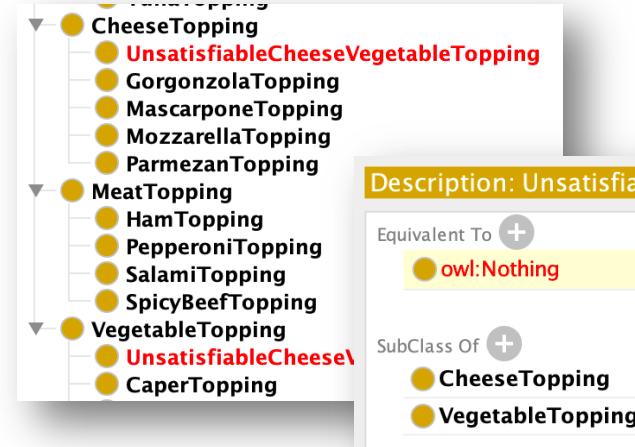
what is most restrictive type?

Realization Problem [ABox]  
 (removing toppings from a pizza results in less specific classifications)

# Reasoning Tasks with the Pizza Ontology

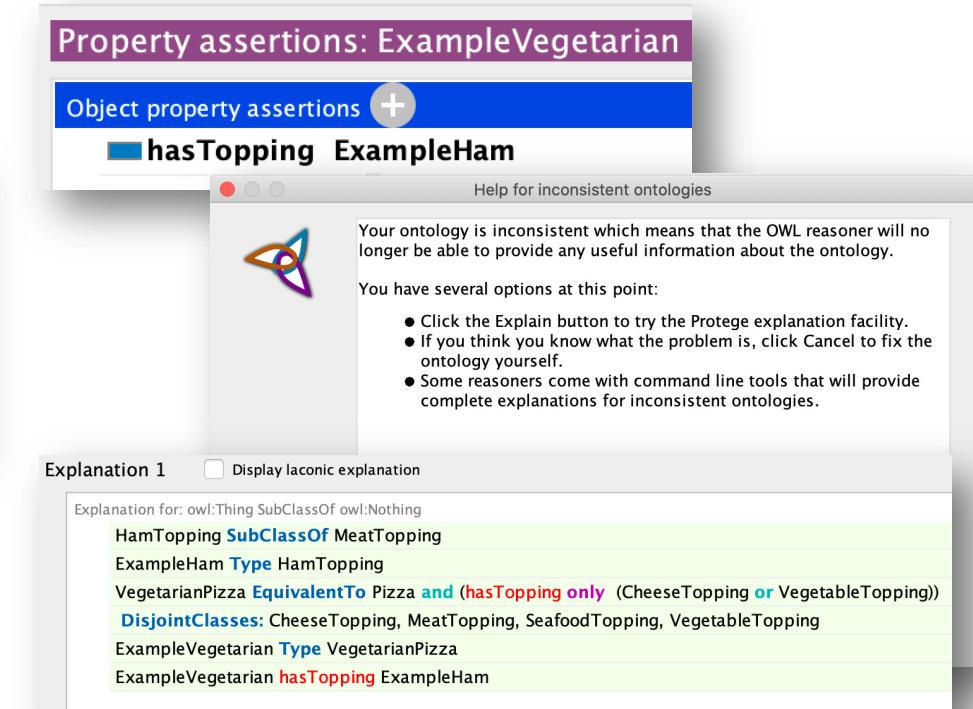


Concept Subsumption [TBox]  
(inferred classification)



Concept Satisfiability [TBox]  
**(CheeseTopping and VegetableTopping are disjoint)**

And we saw live the other **reasoning tasks** discussed for the ABox (instance checking, retrieval, realization)



Property assertions: ExampleVegetarian

Object property assertions +

**hasTopping ExampleHam**

Your ontology is inconsistent which means that the OWL reasoner will no longer be able to provide any useful information about the ontology.

You have several options at this point:

- Click the Explain button to try the Protege explanation facility.
- If you think you know what the problem is, click Cancel to fix the ontology yourself.
- Some reasoners come with command line tools that will provide complete explanations for inconsistent ontologies.

Explanation 1  Display laconic explanation

Explanation for: owl:Thing SubClassOf owl:Nothing

HamTopping SubClassOf MeatTopping  
ExampleHam Type HamTopping  
VegetarianPizza EquivalentTo Pizza and (hasTopping only (CheeseTopping or VegetableTopping))  
DisjointClasses: CheeseTopping, MeatTopping, SeafoodTopping, VegetableTopping  
ExampleVegetarian Type VegetarianPizza  
ExampleVegetarian hasTopping ExampleHam

ABox Consistency  
(creating a **VegetarianPizza** with ham)

# The Semantic Web Roadmap (1998)

Tim Berners-Lee

Date: September 1998. Last modified: \$Date: 1998/10/14 20:17:13 \$

Status: An attempt to give a high-level plan of the architecture of the Semantic WWW. Editing status: Draft. Comments welcome

[Up to Design Issues](#)

## Semantic Web Road map

A road map for the future, an architectural plan untested by anything except thought experiments.



“This document is a plan for achieving a set of connected applications for data on the Web in such a way as to form a **consistent logical web of data (semantic web)**.”

Sir Tim Berners-Lee, Semantic Web Road Map, 1998

Now this should have depth!

We'll discuss this next week,  
when we talk about **Linked Data**!

# Closed- vs. Open-World Semantics

A database operates under the **Closed-World Assumption**

- what is not known to be true is necessarily false  
⇒ only one possible interpretation

A DL knowledge base operates under the **Open-World Assumption**

- what is not known to be true is simply not known (could be either true or false)  
⇒ many possible interpretations

*many interpretations  
in description  
logic logic  
base*



The Story of Oedipus (up to 2m10s): <https://youtu.be/Jn9Gq5AkEx4>

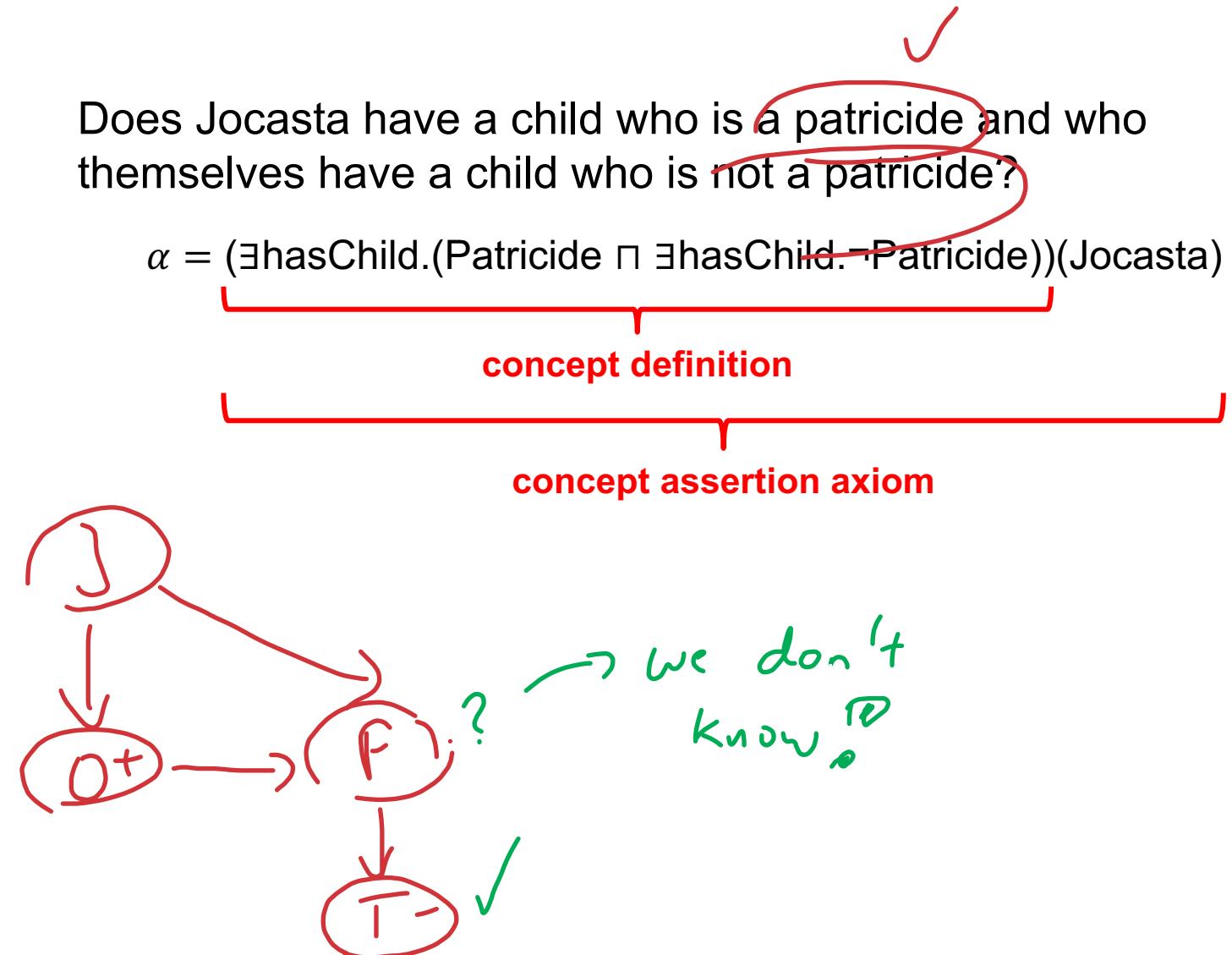
- well-known example in DL research [Baader & Nutt, 2003]

# DL Reasoning: Open-World Semantics

Abox A
hasChild(Jocasta,Oedipus)
hasChild(Jocasta,Polyneikes)
hasChild(Oedipus,Polyneikes)
hasChild(Polyneikes,Thersandros)
Patricide(Oedipus)
$\neg$ Patricide(Thersandros)

$\models \nexists DB : No$

$\models \nexists Description Logic : Yes$



# DL Reasoning: Open-World Semantics

Abox A

```

hasChild(Jocasta,Oedipus)
hasChild(Jocasta,Polyneikes)
hasChild(Oedipus,Polyneikes)
hasChild(Polyneikes,Thersandros)
Patricide(Oedipus)
¬Patricide(Thersandros)
  
```

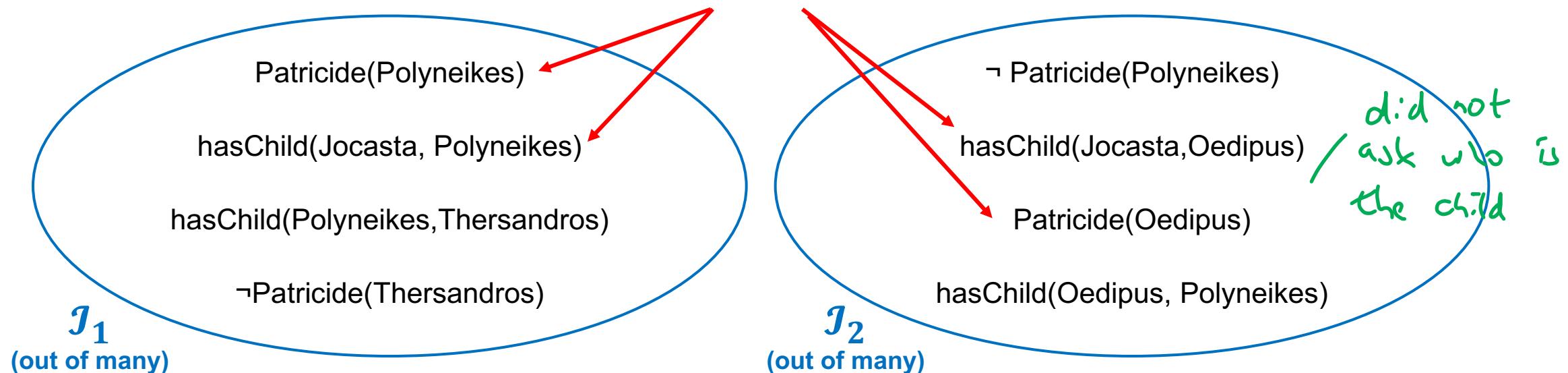
Does Jocasta have a child who is a patricide and who themselves have a child who is not a patricide?

$$\alpha = (\exists \text{hasChild}.(\text{Patricide} \sqcap \exists \text{hasChild}. \neg \text{Patricide}))(\text{Jocasta})$$

Do all possible interpretations  $\mathcal{I}_x$  of A satisfy  $\alpha$ ?

Both  $\mathcal{I}_1$  and  $\mathcal{I}_2$  satisfy  $\alpha$   
(although different patricides)

Child of Jocasta who is a patricide and  
has a child who is not a patricide



# Today's Agenda

- Web Ontologies
  - Description Logics and OWL
  - Building Web Ontologies with Protégé (Tutorial)
- Knowledge Graphs
  - Graph Data Models
  - Querying Graph Datasets

# Knowledge Graphs

<https://www.google.com/search?q=The+Keyword>

Introducing the Knowledge Graph: things, not strings

May 16, 2012 · 4 min read

Amit Singhal  
SVP, Engineering

**Microsoft Bing Blogs**

Bring rich knowledge of people, places, things and local businesses to your apps

Today we are excited to announce the availability of [Bing Entity Search API](#), a new Microsoft Cognitive Service in Free Preview. While in Preview, it will be available within the United States.

Bing Entity Search API (Preview) helps you enrich your app with the knowledge of the web. It lets you access the ever-growing Bing knowledge graph which consists of billions of real world entities like people, places, things and local businesses. When your app users need supplemental information on the content in your app, having to leave your app to run a separate query is not optimal. You can use Bing knowledge graph to bring search within your experience.

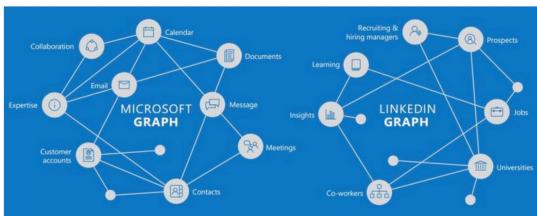
**LinkedIn Engineering**

Building The LinkedIn Knowledge Graph

Qi He October 6, 2016

**MICROSOFT GRAPH** and **LINKEDIN GRAPH**

Authors: Qi He, Bee-Chung Chen, Deepak Agarwal



<https://www.aboutamazon.com/news/innovation-at-amazon/making-search-easier>

How Amazon's Product Graph is helping customers find products more easily.

Consider a typical cup of yogurt. It's vegetarian, has active and live cultures, and delivers 15% of the daily recommended dose of calcium. But your aunt Lily is visiting, and she has celiac. So you want to know if the yogurt is gluten free before buying it on Amazon.

Ordinarily, you'd have to look up a yogurt by brand, and check the label to see if it was certified gluten-free. But what if there was a simpler way? What if you could search for certified gluten-free yogurts on Amazon? Or what if you could say, "Alexa, what yogurts are gluten-free?"

Now, with the product graph being developed by a team of scientists and engineers in Amazon's consumer organization, you can.

Published in [The Airbnb Tech Blog](#)

Spencer Chang  
Sep 4, 2018 · 9 min read

## Scaling Knowledge Access and Retrieval at Airbnb

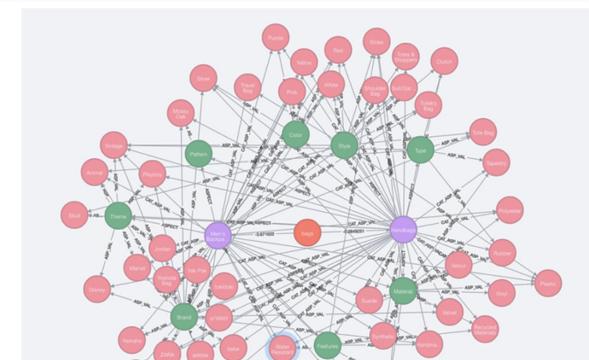
Introducing our Knowledge Graph for encoding relationships and surfacing relevant information



<https://www.ebayinc.com/stories/news/cracking-the-code-on-conversational-commerce/>

**eBay**

Company Stories Impact Tech Investors Careers



ShopBot uses its Knowledge Graph to understand user requests and generate follow-up questions to refine requests before searching for the items in eBay's inventory. In a search query for "bags" for example, purple nodes represent "categories," green "attributes" and pink are "values" for those attributes.

Context is Key

- <https://blog.google/products/search/introducing-knowledge-graph-things-not-strings/>
- <https://www.aboutamazon.com/news/innovation-at-amazon/making-search-easier>
- <https://engineering.linkedin.com/blog/2016/10/building-the-linkedin-knowledge-graph>
- <https://www.ebayinc.com/stories/news/cracking-the-code-on-conversational-commerce/>
- <https://medium.com/airbnb-engineering/scaling-knowledge-access-and-retrieval-at-airbnb-665b6ba21e95>
- <https://blogs.bing.com/search-quality-insights/2017-07/bring-rich-knowledge-of-people-places-things-and-local-businesses-to-your-apps>

# Knowledge Graphs

knowledge graphs

1 OF 28 TEXT ONLY

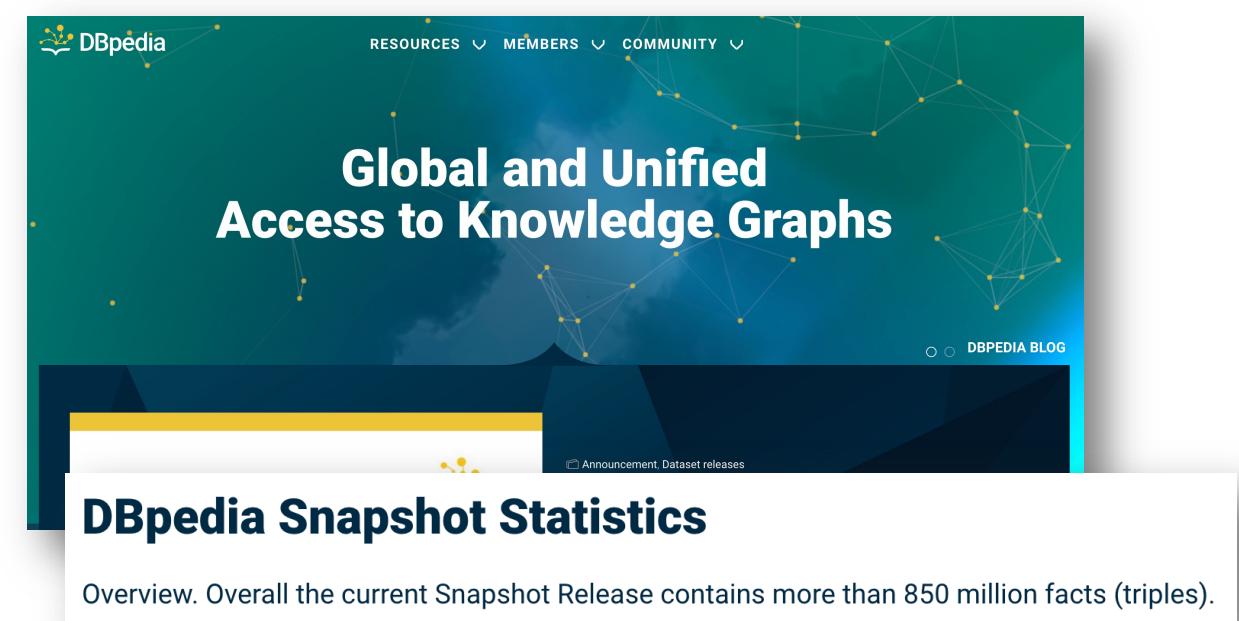
## Industry-scale Knowledge Graphs Lessons and Challenges

FIVE DIVERSE TECHNOLOGY

TABLE 1: COMMON CHARACTERISTICS OF THE KNOWLEDGE GRAPHS

	DATA MODEL	SIZE OF THE GRAPH	DEVELOPMENT STAGE
Microsoft	The types of entities, relations, and attributes in the graph are defined in an ontology.	~2 billion primary entities, ~55 billion facts	Actively used in products
Google	Strongly typed entities, relations with domain and range inference	1 billion entities, 70 billion assertions	Actively used in products
Facebook	All of the attributes and relations are structured and strongly typed, and optionally indexed to enable efficient retrieval, search, and traversal.	~50 million primary entities, ~500 million assertions	Actively used in products
eBay	Entities and relation, well-structured and strongly typed	Expect around 100 million products, >1 billion triples	Early stages of development and deployment
IBM	Entities and relations with evidence information associated with them.	Various sizes. Proven on scales documents >100 million, relationships >5 billion, entities >100 million	Actively used in products and by clients

NATASHA YUQING G ANSHU J A NANT N ALAN PAT JAMIE TAY



DBpedia

RESOURCES ▾ MEMBERS ▾ COMMUNITY ▾

Global and Unified Access to Knowledge Graphs

DBpedia BLOG

Announcement, Dataset releases

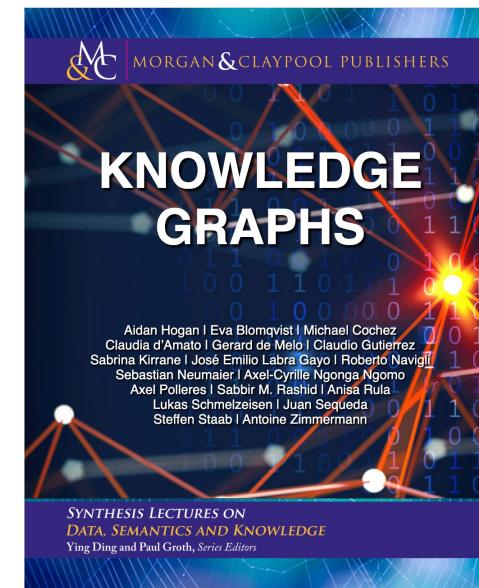
## DBpedia Snapshot Statistics

Overview. Overall the current Snapshot Release contains more than 850 million facts (triples).

<https://www.dbpedia.org/>  
 N. Noy, Y. Gao, A. Jain, A. Narayanan, A. Patterson, and J. Taylor. Industry-scale Knowledge Graphs: Lessons and Challenges — Five diverse technology companies show how it's done. Queue, 2019.

# Knowledge Graphs

“A knowledge graph is a **graph of data** intended to accumulate and convey **knowledge of the real world**, whose **nodes** represent **entities of interest** and whose **edges** represent **relations between these entities**” [Hogan et al., 2021].



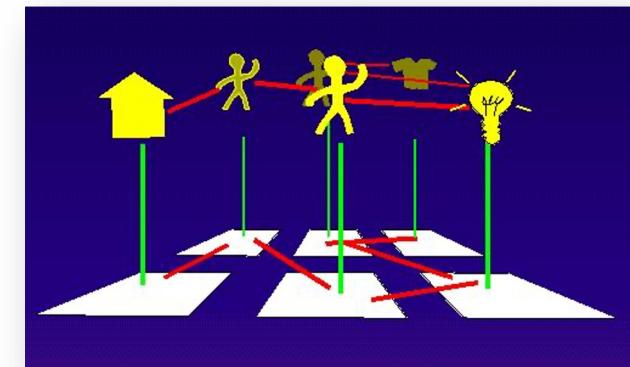
<https://kgbook.org/>

Aidan Hogan et al. Knowledge Graphs. 2021.  
Antoine Zimmermann. *Knowledge Representation and Reasoning*, MINES Saint-Étienne, 2021.

# Knowledge Graphs

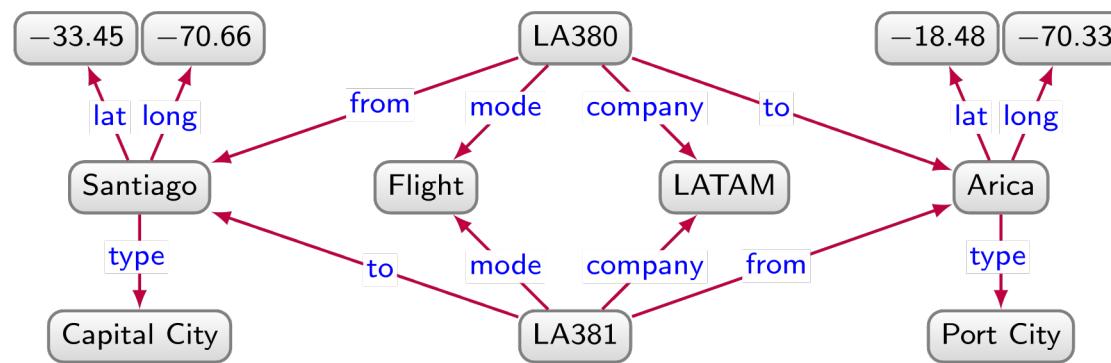
“A knowledge graph is a **graph of data** intended to accumulate and convey **knowledge of the real world**, whose **nodes** represent **entities of interest** and whose **edges** represent **relations between these entities**” [Hogan et al., 2021].

Syntax	Semantics
graph of data	knowledge of the real world

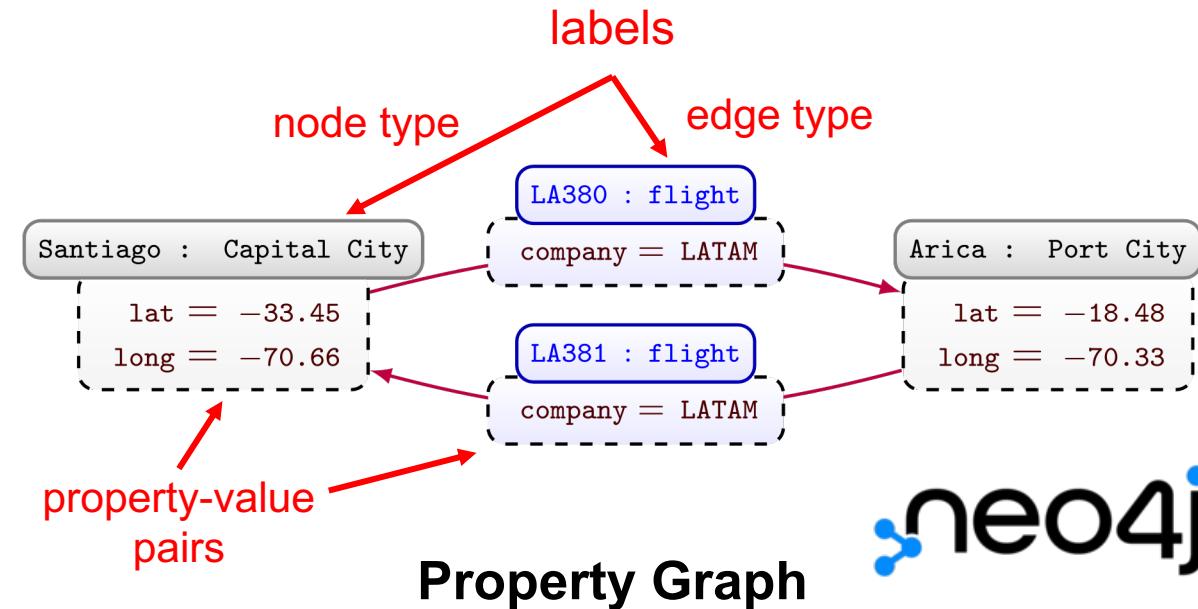


<https://videos.cern.ch/record/2671957>

# Data Models for Knowledge Graphs

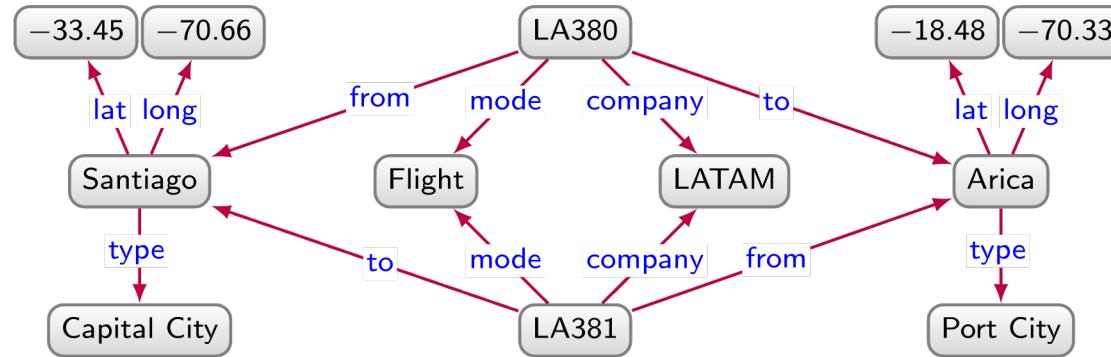


Directed Edge-Labelled Multigraph



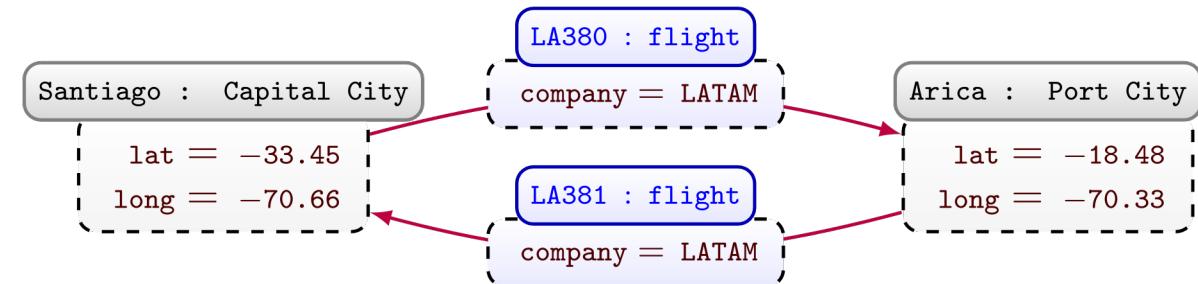
 neo4j

# Data Models for Knowledge Graphs



**Directed Edge-Labelled Multigraph**

more **minimal** model



**Property Graph**

more **flexible** model

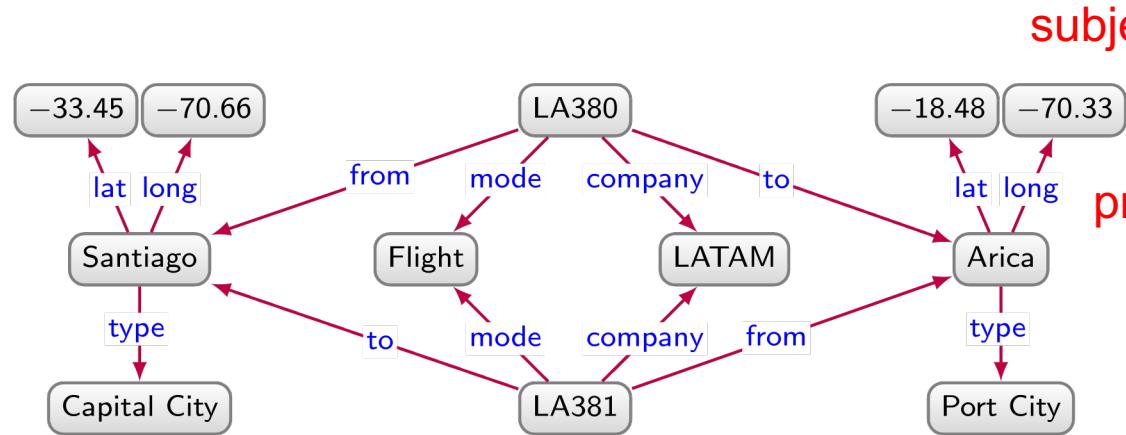
Property graphs can be converted to/from directed edge-labelled multigraphs [Angles et al., 2019].

The **Resource Description Framework (RDF)** is a standardized data model based on directed edge-labelled multigraphs.

Aidan Hogan et al. Knowledge Graphs. 2021.

R. Angles, H. Thakkar, and D. Tomaszuk. RDF and Property Graphs Interoperability: Status and Issues. CEUR Workshop Proceedings, vol. 2369. 2019.

# Data Models for Knowledge Graphs



**Directed Edge-Labelled Multigraph**

more **minimal** model

subject

predicate

## RDF Graph (Turtle syntax)

```

prefix : <http://example.org/>
prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>

:LA380 :company :LATAM ;
        :mode :Flight ;
        :from :Santiago ;
        :to :Arica

:LA381 :company :LATAM ;
        :mode :Flight ;
        :from :Arica ;
        :to :Santiago

:Santiago rdf:type :City
          :lat -33.45 ;
          :long -70.66 .

:Arica rdf:type :City
         :lat -18.48 ;
         :long -70.33 .
  
```

An **RDF graph** is a **set of triples**:  
subject predicate object

In **first-order logic**, a triple is just a  
binary predicate: predicate(subject,object)

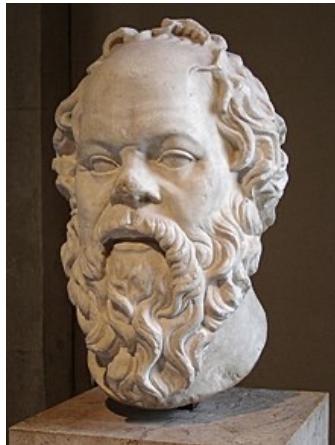
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# Deriving Knowledge from RDF Graphs



**Premise:** All men are mortal.

**Premise:** Socrates is a man.

**Conclusion:** Socrates is mortal.

## First-Order Logic

$$\frac{\forall x (man(x) \rightarrow mortal(x)) \quad man(socrates)}{mortal(socrates)}$$

## Modus Ponens:

$$\frac{P \rightarrow Q \quad P}{Q}$$

## RDF (Turtle syntax)

```
prefix : <http://example.org/#>
prefix rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>
prefix rdfs: <http://www.w3.org/2000/01/rdf-schema#>

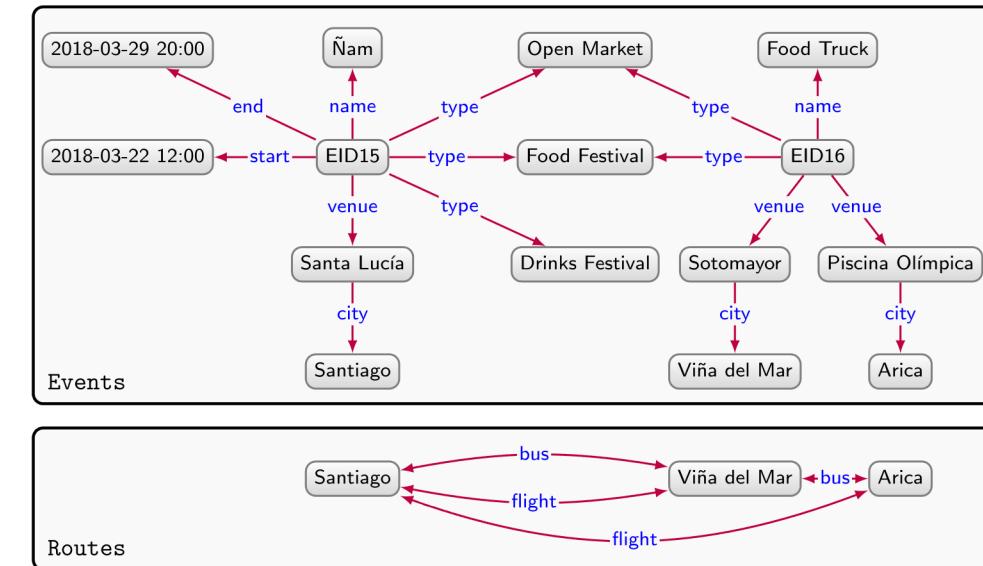
:Man rdfs:subClassOf :Mortal . # premise
:Socrates rdf:type :Man .      # premise
:Socrates rdf:type :Mortal .    # conclusion (can be inferred)
```

# Graph Datasets

A **graph dataset** is a **set of named graphs**

There is always a **default graph**

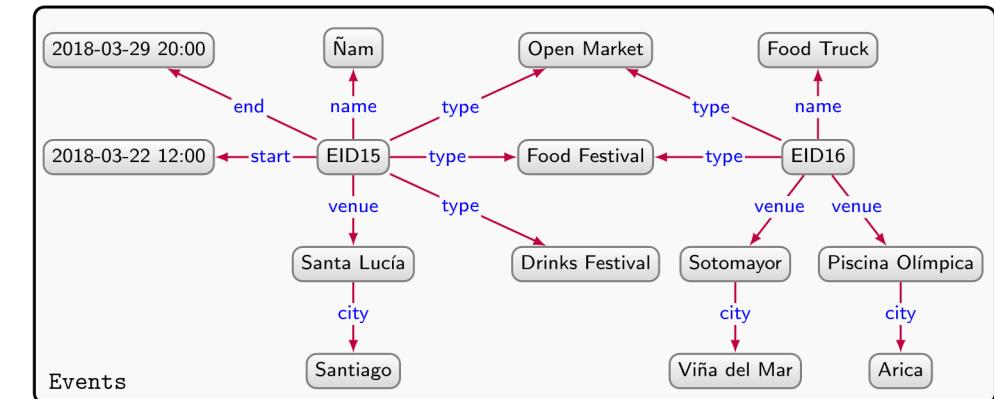
- sometimes the default graph is the union of all named graphs



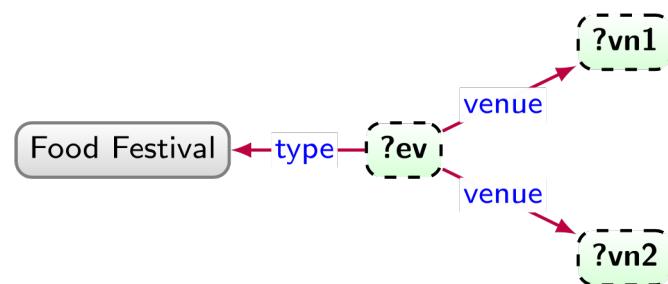
# Graph Datasets and Querying

Graph query languages (SPARQL, Cypher, etc.) share 3 types of **graph patterns**:

- basic graph patterns



Q: "What are the venues of food festivals?"



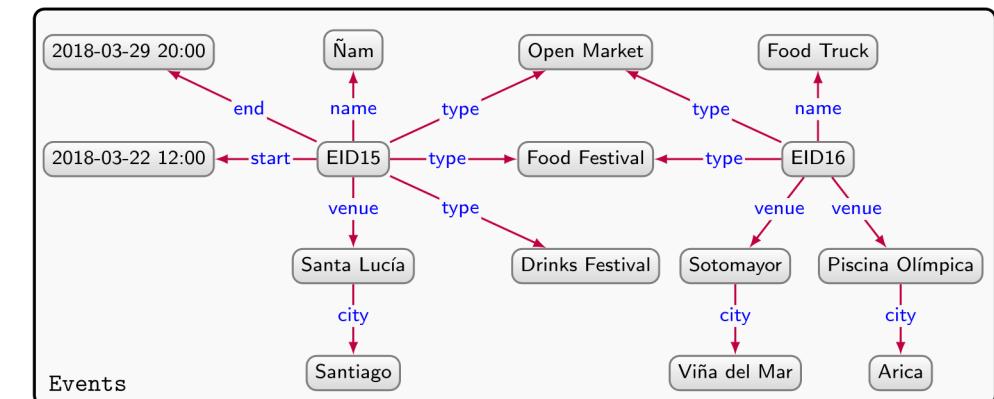
*depends on  
semantics of  
query language*

?ev	?vn1	?vn2
EID16	Piscina Olímpica	Sotomayor
EID16	Sotomayor	Piscina Olímpica
EID16	Piscina Olímpica	Piscina Olímpica
EID16	Sotomayor	Sotomayor
EID15	Santa Lucía	Santa Lucía

# Graph Datasets and Querying

Graph query languages (SPARQL, Cypher, etc.) share 3 types of **graph patterns**:

- basic graph patterns



## SPARQL Query

```

PREFIX : <http://example.org/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>

FROM NAMED <http://example.org/events>

SELECT ?ev ?vn1 ?vn2 WHERE {
  ?ev rdf:type :FoodFestival .
  ?ev :venue ?vn1 .
  ?ev :venue ?vn2 .
}
  
```

?ev	?vn1	?vn2
EID16	Piscina Olímpica	Sotomayor
EID16	Sotomayor	Piscina Olímpica
EID16	Piscina Olímpica	Piscina Olímpica
EID16	Sotomayor	Sotomayor
EID15	Santa Lucía	Santa Lucía

# Graph Datasets and Querying

Graph query languages (SPARQL, Cypher, etc.) share 3 types of **graph patterns**:

- basic graph patterns
- complex graph patterns (relational algebra operators)

Q: "What are food festivals and drinks festivals not held in Santiago (optional: with start date and name)?"

$Q_1: (?event \text{---} type \rightarrow \text{Food Festival})$

$Q_2: (?event \text{---} type \rightarrow \text{Drinks Festival})$

$Q_3: (?event \text{---} venue \rightarrow (?venue \text{---} city \rightarrow \text{Santiago}))$

$Q_4: (?event \text{---} start \rightarrow (?start))$

$Q_5: (?event \text{---} name \rightarrow (?name))$

$$Q := (((Q_1 \cup Q_2) \setminus Q_3) \bowtie Q_4) \bowtie Q_5$$

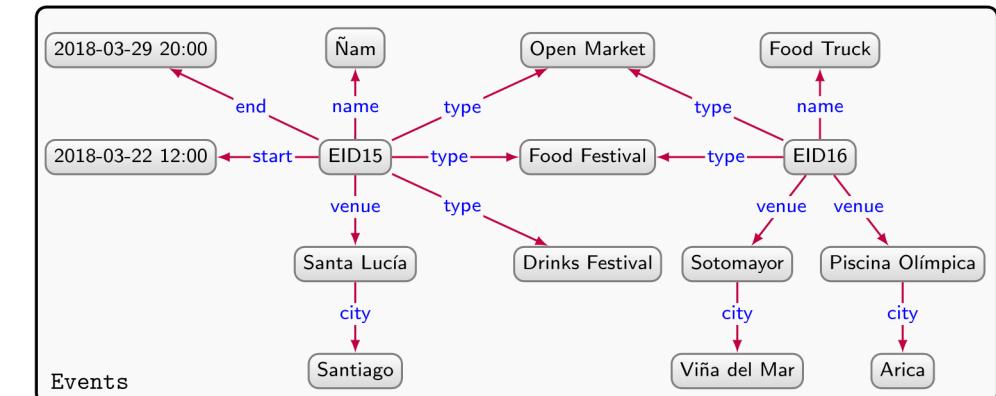
union

minus  
(antijoin)

optional  
(left join)



?event	?start	?name
EID16		Food Truck



# Graph Datasets and Querying

## SPARQL Query

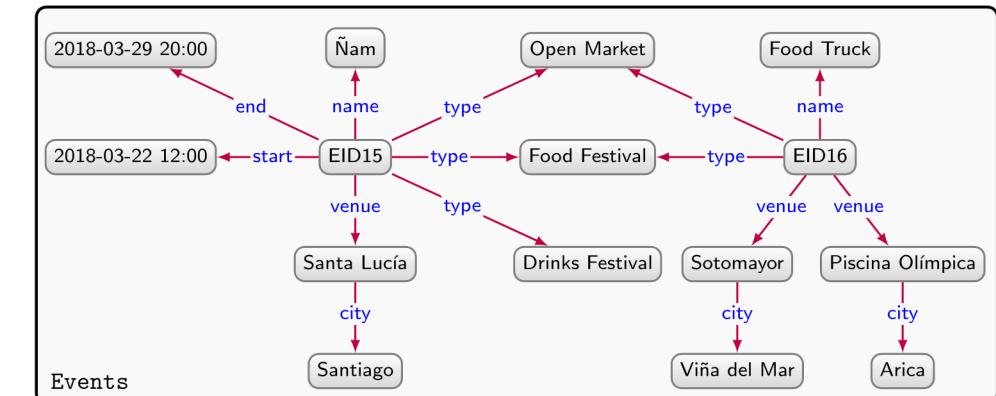
```

PREFIX : <http://example.org/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>

FROM NAMED <http://example.org/events>

SELECT ?event ?name ?start WHERE {
  {
    {
      ?event rdf:type :FoodFestival . #Q1
    }
    UNION
    {
      ?event rdf:type :DrinksFestival . #Q2
    }
    MINUS
    {
      ?event :venue ?venue .
      ?venue :city :Santiago . #Q3
    }
    } OPTIONAL {
      ?event :start ?start . #Q4
    }
  } OPTIONAL {
    ?event :name ?name #Q5
  }
}

```



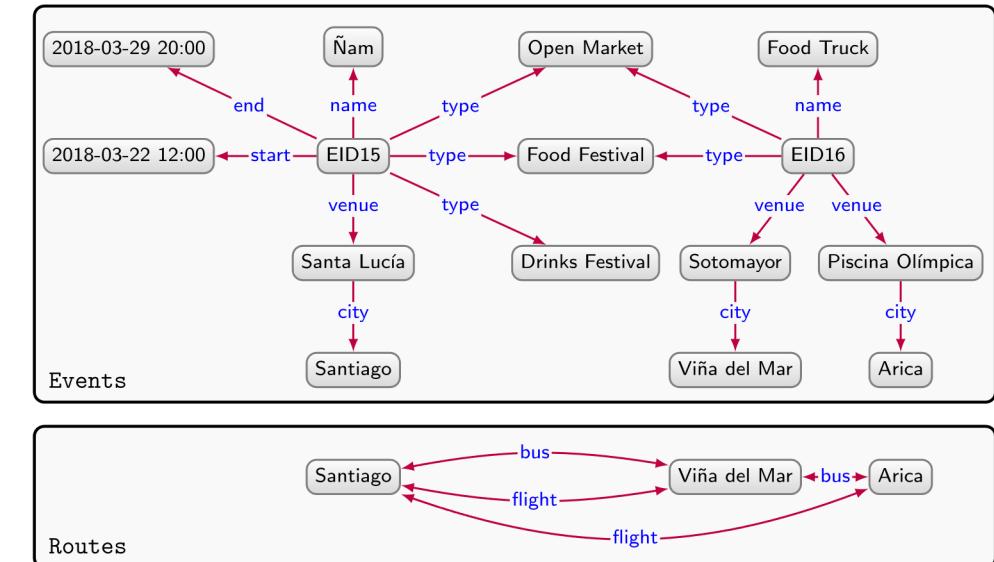
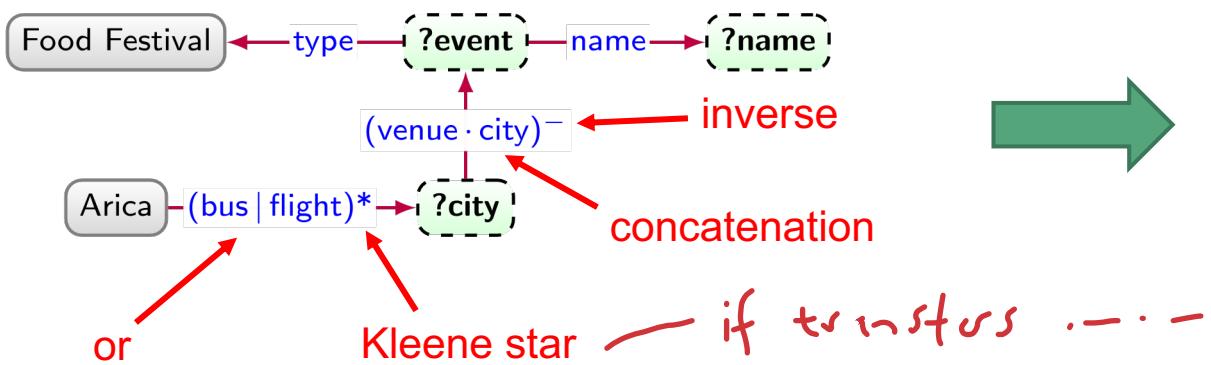
?event	?start	?name
EID16		Food Truck

# Graph Datasets and Querying

Graph query languages (SPARQL, Cypher, etc.) share 3 types of **graph patterns**:

- basic graph patterns
- complex graph patterns (relational algebra operators)
- navigational graph patterns (path expressions)

Q: "What are food festivals held in a city reachable from Arica by bus or flight?"



?event	?name	?city
EID15	Ñam	Santiago
EID16	Food Truck	Arica
EID16	Food Truck	Viña del Mar

# Graph Datasets and Querying

Graph query languages (SPARQL, Cypher, etc.) share 3 types of **graph patterns**:

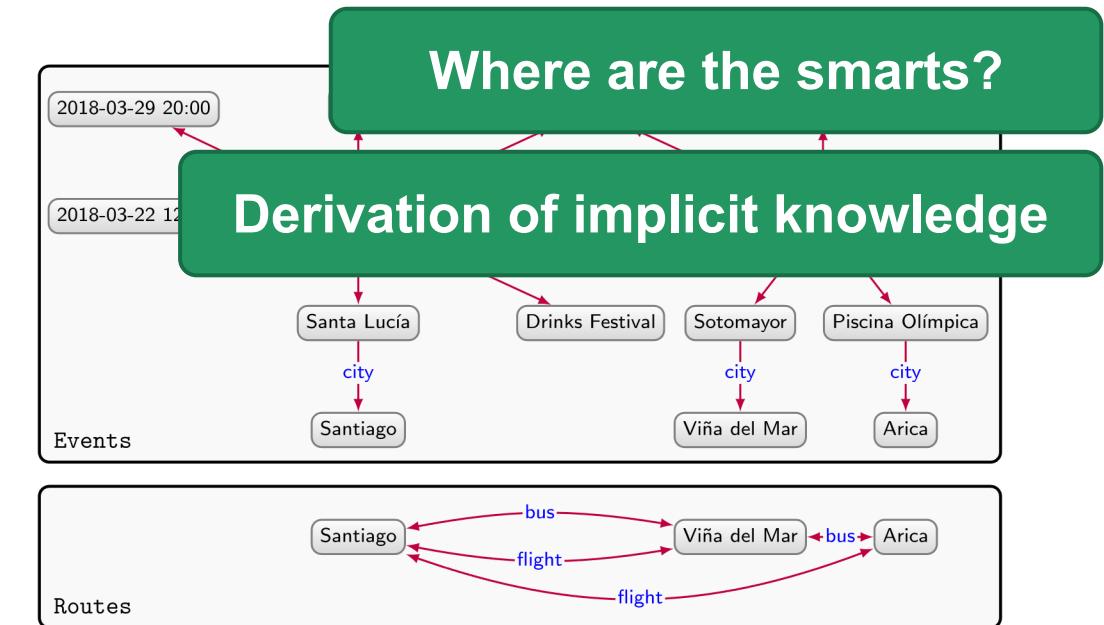
- basic graph patterns
- complex graph patterns (relational algebra operators)
- navigational graph patterns (path expressions)

## SPARQL Query

```
PREFIX : <http://example.org/>
PREFIX rdf: <http://www.w3.org/1999/02/22-rdf-syntax-ns#>

FROM NAMED <http://example.org/events>
FROM NAMED <http://example.org/routes>

SELECT ?event ?name ?city WHERE {
    ?event :name ?name ;
        rdf:type :FoodFestival .
    :Arica (:bus|:flight)* ?city .
    ?city ^(:venue/:city) ?event .
}
```



?event	?name	?city
EID15	Ñam	Santiago
EID16	Food Truck	Arica
EID16	Food Truck	Viña del Mar

# Our Journey

**Prerequisites:**  
 • ASSE  
 • (...)



**Week 1:  
Introduction**



**Week 2:  
A Web for Machines**



**Week 3:  
Knowledge Representation  
and Reasoning for the Web**



**Week 4:  
Linked Data and Distributed  
Knowledge Graphs**



**Week 6 (Coordination I):  
Agent Communication  
and Interaction**



**Week 5:  
Hypermedia Agents (Arch.  
and Programming)**



**Week 10:  
Game Theory and  
Social Choice**

**Week 11:  
Reinforcement Learning  
and Multi-Agent Learning**



**Week 9 (Coordination IV):  
Trust & Reputation**



**Week 12:  
An Industry Perspective**



**Exercises**

Ex1: Writing Your First Agent(s)!  
 Ex2: Automated Planning  
 Ex3: Web Ontologies  
 Ex4: Deductive Reasoning on the Web  
 Ex5: Cognitive Agents in Hypermedia Env.  
 Ex6: Interacting Agents on the Web

Ex7: Ant Colony Optimization  
 Ex8: Organized Agent  
 Ex9: Trustworthy Agents  
 Ex10: Axelrod's Agents  
 Ex11: Reinforcement Learning Agents  
 Course Review and Q&A

# Any Questions / Comments / Doubts / Concerns?



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