

# Better-than-chance classification for signal detection

Jonathan Rosenblatt      Roei Gilron      Roy Mukamel

July 28, 2016

## Abstract

[TODO]

## 1 Introduction

A common workflow in genetics or neuroimaging consists of fitting a classifier, and estimating its predictive accuracy using cross validation. Given that the cross validated accuracy is a random quantity, it is then common to test if the cross validated accuracy is significantly better than chance using a permutation test. Genetic examples include Jiang et al. [2008], Radmacher et al. [2002][TODO: elaborate]. Neuroscience examples include [Golland and Fischl, 2003, Kriegeskorte et al., 2006, Pereira et al., 2009, Varoquaux et al., 2016]. The number of citations<sup>1</sup> attests to the popularity of the above workflow: 956 for Kriegeskorte et al. [2006], and 274 for Radmacher et al. [2002], as examples.

To fix ideas, we will adhere to a Neuroscientific example: In Gilron et al. [2016], the authors seek to detect auditory brain regions which distinguish between vocal and non-vocal stimuli. According to the MVPA analysis workflow, the localization problem is cast as a supervised learning problem: if the type of the stimulus can be predicted from the spatial activation pattern, significantly better than chance, then a region is declared to encode vocal/non-vocal information. We call this an *accuracy test*, a.k.a. *class prediction* in Simon et al. [2003].

This same signal detection task can be also approached as a two-group multivariate test: Inferring that a region encodes vocal/non-vocal information, is essentially inferring that the spatial distribution of brain activations

---

<sup>1</sup>Based on GoogleScholar. Accesses on 26.7.2016.

is different given a vocal/non-vocal stimulus. A practitioner may then call upon a two-group location test such as Hotelling’s  $T^2$  Fujikoshi et al. [2011]. Alternatively, if the size of the brain region is too large compared to the number of observations, so that the spatial covariance cannot be fully estimated, then a high dimensional version of Hotelling’s test can be called upon, such as in Srivastava [2013] or Schäfer et al. [2005]. In contrast to *accuracy tests*, we call these *location tests*, a.k.a. *class comparison* in Simon et al. [2003].

At this point, it becomes unclear which is the preferred test. This was precisely the topic of Ramdas et al. [2016], who compared the Hotelling location test to the accuracy of *Fisher’s linear discriminant analysis* classifier (LDA) [Hastie et al., 2003]. Using an asymptotic analysis, Ramdas et al. [2016] concluded that accuracy and location tests are equivalent with respect to their order of convergence to a consistent test, while they may differ in constants.

Those constants, governing the power of the tests, are crucial when dealing with typical sample sizes in neuroscience and genetics, and thus the focus of this study. In particular, which test is to be preferred in finite samples? Our conclusion is quite simple: *location tests almost always have more power than accuracy tests*.

The main argument for our statement rests upon the observation that with typical sample sizes, the accuracy test statistic is highly discrete. Discrete test statistics are known to be conservative [Hemerik and Goeman, 2014], since they cannot exhaust the permissible false positive rate. In accuracy tests, the degree of discretization of the accuracy statistic is governed by the number of samples. In our running neuroscience example [Gilron et al., 2016], the classification is performed based on 40 trials, so that the test statistic may assume only 40 possible values. This number of examples is not unusual if considering this is the number of subject in a genetic study, or the number of trial repeats in an fMRI brain scan.

The discretization effect is aggravated if the test statistic is highly concentrated. For an intuition consider the usage of the train-accuracy test statistic (i.e., not cross validated). Because the testing problem is high dimensional, the observed train accuracy will be close to 1. The same will occur in every permutation, for the same reason. The permutation p-value will thus be 1 for almost all data sets, the null will never be rejected, and the test will have no power.

Given these considerations, it is quite surprising that signal detection using accuracy tests is so popular in neuroscience and genetics. In the following, we quantify the power loss to be expected in typical studies, and identify the problems’ characteristics that govern its severity. We start by establishing a best practice for permutation testing using the accuracy test

66 statistic, We also discuss the problem characteristics that govern the mag-  
 67 nitude of the conservativeness, and try to offer an intuition to the scope of  
 68 the observation that a multivariate test should always be preferred over a  
 69 classification approach.

## 70 **2 Problem setup**

71 Adhering to our neuroscientific example, we now formalize terminology and  
 72 notation. Let  $y \in \mathcal{Y}$  be a class encoding. In our vocal/non-vocal example,  
 73 using effect coding, we have  $\mathcal{Y} = \{-1, 1\}$ . Let  $x \in \mathcal{X}$  be a  $p$  dimensional  
 74 feature vector. In our vocal/non-vocal example  $p$  is governed by the number  
 75 of voxels in a regions, which is the number of voxels in each brain region  
 76 tested. We thus have  $\mathcal{X} = \mathbb{R}^{27}$ .

77 Given  $n$  pairs of  $(x_i, y_i)$ , typically assumed i.i.d., the *testing* approach to  
 78 localization amounts to testing whether  $x|y = 1$  has the the same distribution  
 79 as  $x|y = -1$ . I.e., the multivariate voxel activation pattern has the same  
 80 distribution when given a vocal stimulus, as when given a non-vocal stimulus.  
 81 The *classification* approach to the localization problem amounts to learning a  
 82 predictive model  $\hat{f}(x)$  from some assumed model class  $\hat{f} \in \mathcal{F}$ . The prediction  
 83 accuracy, denoted  $T_{\hat{f}}^{acc}$ , is defined as the probability of a given classifier  $\hat{f}$   
 84 of making a correct prediction  $T_{\hat{f}}^{acc} := P(\hat{f}(x) = y)$  when given a new,  
 85 randomly drawn data point,  $(x, y)$ .

### 86 **2.1 Candidate Tests**

87 The design of a permutation test using the prediction accuracy, requires the  
 88 following design choices:

89 **What test statistic?**

90 **Cross validated or not?** Is the statistic cross validated or not?

91 **Refolding?** For a K-fold cross validated test statistic: is the data refolded  
 92 in each permutation?

93 **Permute labels of features?** Should the  $y$  be permuted or should the  $x$ ?

94 **Balanced folding?** For a K-fold cross validated test statistic: is the data  
 95 folding balanced? (a.k.a. stratified).

96 **How many folds?** We will now address these questions while bearing in  
97 mind that unlike the typical supervised learning setup, we are not in-  
98 terested in an unbiased estimate of the prediction error, but rather in  
99 the mere detection of a difference between two groups, leading to a  
100 better-than-chance accuracy.

101 **What test statistic?** Given a predictor  $\hat{f}$ , a natural test statistic is  
102 some estimate of its accuracy  $T_{\hat{f}}^{acc}$ . Then again, very low accuracies,  
103 even 0, is evidence that the classes are separated, and we only need to  
104 invert the predictions. We can thus consider some estimate of  $|T_{\hat{f}}^{acc} -$   
105  $0.5|$  as the test statistic. This, however, implies that if the classes  
106 are identical, random guessing has a 0.5 accuracy. This is not true if  
107 the classes are not balanced. The chance level in which case is the  
108 prevalence of the dominant class, we denote by  $\hat{p}_{max}$ . This suggests the  
109 following test statistic  $|T_{\hat{f}}^{acc} - \hat{p}_{max}|$ . Since we will latter be aggregating  
110 these statistic over random data foldings, where the dominant class  
111 may have varying frequencies, it seems appropriate to standardize the  
112 scale of this statistic. We thus also consider a z-scored accuracy:  $|T_{\hat{f}}^{acc} -$   
113  $\hat{p}_{max}| / \sqrt{\hat{p}_{max}(1 - \hat{p}_{max})}$ .

114 **Cross validated or not?** Were we interested in an unbiased esti-  
115 mator of the prediction error, there is no question that some validation  
116 is in order. Since we are merely interested in detecting a difference  
117 between groups, a biased error estimate is not an issue provided that it  
118 is consistent over all permutations. The underlying intuition is that if  
119 the exact same computation is performed over all permutations, then  
120 a permutation test will be “fair”, i.e., will not inflate the false positive  
121 rate. We will thus be considering both cross validated accuracies, and  
122 train accuracies as our test statistics.

123 **Refolding?** The standard practice in neuroimaging is to refold the  
124 data after each permutation. This is imperative if permuting labels  
125 while aiming at balanced data folds. This is not, however, imperative  
126 in general. In this work, we will adhere to the standard practice of  
127 refolding the data within each permutation.

128 **Permute labels of features?** While seemingly identical, the com-  
129 pounding of permutations with data foldings renders these two ap-

proaches distinct. As an example, consider balanced (stratified) K-fold cross validation where the initial data folding is balanced. After a label permutation, the folds will probably not be balanced, and will thus have to be refolded. If the features are permuted, then the labels conserve their original fold assignments, and the data need not be refolded. Since we only report results while refolding the data in each permutation, then the only difference between permuting labels and permuting features seems to be a computational one. We thus adhere to the more common, albeit less efficient practice, of permuting labels.

**Balanced folding?** A standard practice when cross validating is to constrain the data folds to be balanced (i.e. stratified). This is well justified when aiming at unbiased accuracy estimation. This also simplifies matter when aiming at signal detection, as can be seen from the above discussion of the appropriate test statistic. Then again, it may complicate matters, as can be seen from the above discussion on label versus feature permutation. In general, it is not imperative in general, and we will indeed be comparing the effect of balanced foldings versus unbalanced. We will thus report results with both balanced and unbalanced data foldings.

**How many folds?** Different authors suggest different rules for the number of folds. We will be varying the number of folds, since it will affect the concentration of the estimated accuracy, which will have a crucial effect on the conservativeness of the permutation test. Our intuition suggests that since more folds imply a less concentrated estimate, then leave-one-out should be the less conservative, and 2-fold should be the most conservative.

By now, the reader will have observed that there are indeed many ways to perform a permutation test using a cross validated statistic. The subset of tests we will be comparing is collected for convenience in Table 1.

### 3 Controlling the False Positive Rate

In the first of our battery of simulations we verify that various test statistics and permutation schemes control the type I error. Figure ?? demonstrates that this is indeed the case. All our candidate tests control the type I error, with varying degrees of conservativeness. In particular: (a) if the folds are balanced or not, (b) if the labels are permuted or the features, (c) if the test

Name	Basis	CV	Accuracy	Parameters
Hotelling	Hotelling	–	–	shrink=FALSE
Hotelling.shrink	Hotelling	–	–	shrink=TRUE
lda.CV.1	LDA	TRUE	accuracy	–
lda.CV.2	LDA	TRUE	z-accuracy	–
lda.noCV.1	LDA	FALSE	accuracy	–
lda.noCV.2	LDA	FALSE	z-accuracy	–
sd	SD	–	–	–
svm.CV.1	SVM	TRUE	accuracy	cost=1e1
svm.CV.2	SVM	TRUE	accuracy	cost=1e-1
svm.CV.3	SVM	TRUE	z-accuracy	cost=1e1
svm.CV.4	SVM	TRUE	z-accuracy	cost=1e-1
svm.noCV.1	SVM	FALSE	accuracy	cost=1e1
svm.noCV.2	SVM	FALSE	accuracy	cost=1e-1
svm.noCV.3	SVM	FALSE	z-accuracy	cost=1e1
svm.noCV.4	SVM	FALSE	z-accuracy	cost=1e-1

Table 1: This table enumerates the various test statistics we will be studying. Three are location tests: Hotelling, Hotelling.shrink, and sd. *Hotelling* is the classical two-group  $T^2$  statistic. *Hotelling.shrink* is a high dimensional version with the regularized covariance in Schäfer et al. [2005]. *sd* is another high dimensional version of the  $T^2$ , from Srivastava et al. [2013]. The rest of the tests are variations of the linear SVM, and Fisher’s LDA, with varying accuracy measures, cross validated or not, and varying tuning parameters. For example, *svm.CV.4* is a linear SVM, with *libsvm*’s cost parameter set at 0.1, using the cross validated z-scored accuracy ( $|T_{\hat{f}}^{acc} - \hat{p}_{max}| / \sqrt{\hat{p}_{max}(1 - \hat{p}_{max})}$ , see Section 2.1). Another example is *lda.noCV.1*, which is Fisher’s LDA, returning the train accuracy, without cross validation, and without z-scoring.

165 statistic is varied, (d) if the regularization level of the support vector machine  
166 classifier (SVM) is varied, (e) if the number of folds is varied.

## 167 4 Power

168 Having established that all of the tests in our battery control the false pos-  
169 itive rate, it remains to be seen if they have similar power– at least when  
170 comparing the power of the various classifiers and multivariate tests. The re-  
171 sults of Ramdas et al. [2016] suggest that power should be of the same order.  
172 On the other hand, the results of our previous sections suggest that the con-  
173 servativeness of some of the considered tests can be considerable, rendering  
174 them underpowered.

175 [TODO: discuss power of various tests]

Figure 1: The power of a permutation test with various test statistics. The power on the  $x$  axis. Effect are color and shape coded. They are assumed to be equal in all the 23 dimensions, and vary over 0 (red circle), 0.25 (green triangle), and 0.5 (blue square). The various statistics on the  $y$  axis. Their details are given in Table 1. Simulation code available at [TODO].



We see by now that the use of accuracy tests for signal detection is underpowered compared to location tests. The above simulations can hardly support such a universal statement. We will thus verify on a neuroimaging dataset, and discuss the causes for this phenomenon thus the scope of the statement.

## 5 Neuroimaging Example

Figure 2 is an application of our battery of tests to the data of Pernet et al. [2015]. The authors of Pernet et al. [2015] collected fMRI data while subjects were exposed to the sounds of human speech (vocal), and other non-vocal sounds. Each subject was exposed to 20 sounds of each type, totalling in  $n = 40$  trials in each scan. The study was rather large and consisted of about 200 subjects. The data was kindly made available by the authors at the OpenfMRI website<sup>2</sup>.

To verify the observation that location tests have more power than accuracy tests, we perform permutation inference using the pipeline of Stelzer

<sup>2</sup><https://openfmri.org/>

191 et al. [2013], which was also used in Gilron et al. [2016]. For completeness,  
 192 the pipeline is described in Appendix A. To demonstrate our point, we com-  
 193 pare the *sd* location test with the *svm.cv.1* accuracy test (see Table 1 for the  
 194 definition of these statistics).

195 In agreement with our simulation results, the location test (*sd*) discovers  
 196 more brain regions that encode information discriminating between vocal and  
 197 non-vocal stimuli when compared to an accuracy test (*svm.cv.1*). The former  
 198 discovers 1,232 regions, while the latter only 441, as reported in Figure 2. We  
 199 emphasize that both test statistics were compared with the same permutation  
 200 scheme, and the same error controls, so that any difference in detections is  
 201 due to their different power.

202 Having established that accuracy tests are underpowered both in simula-  
 203 tion and in application, we wish to identify the conditions under which this  
 204 will occur, and discuss implications on the practice of accuracy tests.

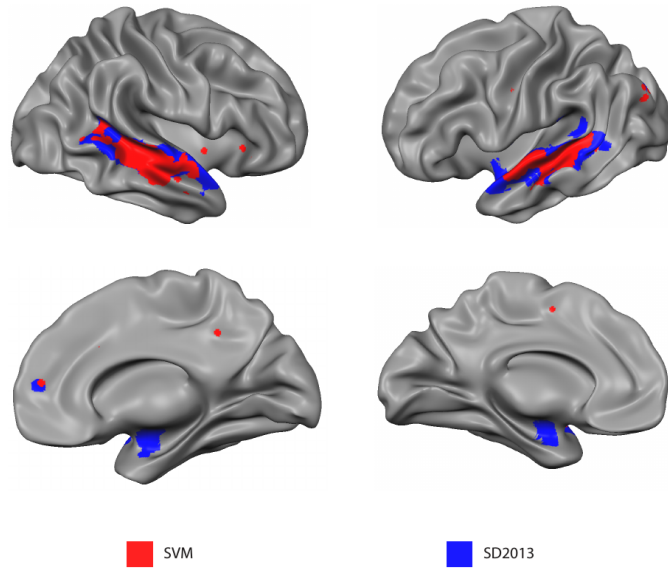


Figure 2: Brain regions encoding information discriminating between vocal and non-vocal stimuli. Map reports the centres of 27-voxel sized spherical regions, as discovered by an accuracy test (*svm.cv.1*), and a location test (*sd*). *svm.cv.1* was computed using 5-fold cross validation, and a cost parameter of 1. Region-wise significance was determined using the permutation scheme of Stelzer et al. [2013], followed by region-wise  $FDR \leq 0.05$  control using the Benjamini-Hochberg procedure [Benjamini and Hochberg, 1995]. Number of permutations equals 400. The location test detect 1,232 regions, and the accuracy test 441. The overlap is such that 90% of the accuracy test regions, are also detected by the location test. For the details of the analysis see Appendix A and Gilron et al. [2016].



## 205 6 Discussion

206 We have set out to understand which of the tests is more powerful: the  
207 accuracy test or the location test. Using simulations, we have concluded  
208 that the location tests are preferable. We attribute this to the discretization  
209 introduced in finite samples by the accuracy test statistic. This also explains  
210 why an asymptotic analysis, such as Ramdas et al. [2016], did not find a  
211 qualitative difference.

212 At this point some reservations to the generality of our findings are in  
213 order. Firstly, not all accuracy tests are concerned with signal detection.  
214 Indeed, it is possible that the purpose of the test is not to detect a differ-  
215 ence between classes, but to actually test if a particular classifier is better  
216 than chance. This would be the case, for instance, with brain-machine inter-  
217 faces, where the detection of a signal is not enough [Olivetti et al., 2012]. In  
218 such cases, the performance of a particular classifier is the object of study,  
219 rendering the accuracy test the appropriate choice.

220 Secondly, there may be cases where the accuracy test does have more  
221 power than the location test. Our simulations were unable to point out such  
222 a scenario, but the fact that in our neuroimaging example (Section 5) some  
223 brain regions were detected with the accuracy test, and not the location test,  
224 suggest that the accuracy test does have more power for particular types of  
225 signal. [TODO: signal in scale? heavy tails?]

226 A very important point is the ease of implementation. The need for cross  
227 validation of the accuracy test greatly increases its computational complexity.  
228 Moreover, anyone who has actually implemented tests with discrete statistics,  
229 will attest they are considerably harder to implement. This is because their  
230 unforgiveness to the type of inequality. Indeed, replacing a weak inequality  
231 with a strong inequality may considerably change the results. This is not the  
232 case for continuous test statistics.

233 Given all the above, we find the popularity of accuracy tests quite puz-  
234 zling. We believe this is due to a reversal of the inference cascade. Re-  
235 searchers first fit a classifier, and then ask if the classes are any different.  
236 Were they to start by asking if classes are any different, and only then try  
237 to classify, then location tests would naturally arise as the preferred method.  
238 As put by Ramdas et al. [2016]:

239 The recent popularity of machine learning has resulted in the ex-  
240 tensive teaching and use of prediction in theoretical and applied  
241 communities and the relative lack of awareness or popularity of  
242 the topic of Neyman-Pearson style hypothesis testing in the com-  
243 puter science and related “data science” communities.

## 244 References

- 245 Y. Benjamini and Y. Hochberg. Controlling the false discovery rate: a prac-  
246 tical and powerful approach to multiple testing. *JOURNAL-ROYAL STA-*  
247 *TISTICAL SOCIETY SERIES B*, 57:289–289, 1995.
- 248 Y. Fujikoshi, V. V. Ulyanov, and R. Shimizu. *Multivariate Statistics: High-*  
249 *Dimensional and Large-Sample Approximations*. John Wiley & Sons, Aug.  
250 2011. ISBN 978-0-470-53986-6.
- 251 R. Gilron, J. Rosenblatt, O. Koyejo, R. A. Poldrack, and R. Mukamel. Quan-  
252 tifying spatial pattern similarity in multivariate analysis using functional  
253 anisotropy. *arXiv:1605.03482 [q-bio]*, May 2016.
- 254 P. Golland and B. Fischl. Permutation tests for classification: towards statis-  
255 tical significance in image-based studies. In *IPMI*, volume 3, pages 330–341.  
256 Springer, 2003.
- 257 T. Hastie, R. Tibshirani, and J. Friedman. *The Elements of Statistical Learn-*  
258 *ing*. Springer, July 2003. ISBN 0-387-95284-5.
- 259 J. Hemerik and J. Goeman. Exact testing with random permutations.  
260 *arXiv:1411.7565 [math, stat]*, Nov. 2014.
- 261 W. Jiang, S. Varma, and R. Simon. Calculating confidence intervals for  
262 prediction error in microarray classification using resampling. *Statistical*  
263 *Applications in Genetics and Molecular Biology*, 7(1), 2008.
- 264 N. Kriegeskorte, R. Goebel, and P. Bandettini. Information-based functional  
265 brain mapping. *Proceedings of the National Academy of Sciences of the*  
266 *United States of America*, 103(10):3863–3868, July 2006. ISSN 0027-8424,  
267 1091-6490. doi: 10.1073/pnas.0600244103.
- 268 E. Olivetti, S. Greiner, and P. Avesani. Induction in Neuroscience with  
269 Classification: Issues and Solutions. In G. Langs, I. Rish, M. Grosse-  
270 Wentrup, and B. Murphy, editors, *Machine Learning and Interpretation*  
271 *in Neuroimaging*, number 7263 in Lecture Notes in Computer Science,  
272 pages 42–50. Springer Berlin Heidelberg, 2012. ISBN 978-3-642-34712-2  
273 978-3-642-34713-9. doi: 10.1007/978-3-642-34713-9\_6.
- 274 F. Pereira, T. Mitchell, and M. Botvinick. Machine learning classifiers and  
275 fMRI: A tutorial overview. *NeuroImage*, 45(1, Supplement 1):S199–S209,  
276 Mar. 2009. ISSN 1053-8119. doi: 10.1016/j.neuroimage.2008.11.007.

- 277 C. R. Pernet, P. McAleer, M. Latinus, K. J. Gorgolewski, I. Charest, P. E. G.  
278 Bestelmeyer, R. H. Watson, D. Fleming, F. Crabbe, M. Valdes-Sosa, and  
279 P. Belin. The human voice areas: Spatial organization and inter-individual  
280 variability in temporal and extra-temporal cortices. *NeuroImage*, 119:164–  
281 174, Oct. 2015. ISSN 1053-8119. doi: 10.1016/j.neuroimage.2015.06.050.
- 282 M. D. Radmacher, L. M. McShane, and R. Simon. A Paradigm for  
283 Class Prediction Using Gene Expression Profiles. *Journal of Computa-*  
284 *tional Biology*, 9(3):505–511, June 2002. ISSN 1066-5277. doi: 10.1089/  
285 106652702760138592.
- 286 A. Ramdas, A. Singh, and L. Wasserman. Classification Accuracy as a Proxy  
287 for Two Sample Testing. *arXiv:1602.02210 [cs, math, stat]*, Feb. 2016.
- 288 J. Schäfer, K. Strimmer, and others. A shrinkage approach to large-scale co-  
289 variance matrix estimation and implications for functional genomics. *Sta-*  
290 *tistical applications in genetics and molecular biology*, 4(1):32, 2005.
- 291 R. Simon, M. D. Radmacher, K. Dobbin, and L. M. McShane. Pitfalls in the  
292 Use of DNA Microarray Data for Diagnostic and Prognostic Classification.  
293 *Journal of the National Cancer Institute*, 95(1):14–18, Jan. 2003. ISSN  
294 0027-8874, 1460-2105. doi: 10.1093/jnci/95.1.14.
- 295 M. S. Srivastava. On testing the equality of mean vectors in high dimension.  
296 *Acta et Commentationes Universitatis Tartuensis de Mathematica*, 17(1):  
297 31–56, June 2013. ISSN 2228-4699. doi: 10.12697/ACUTM.2013.17.03.
- 298 M. S. Srivastava, S. Katayama, and Y. Kano. A two sample test in high  
299 dimensional data. *Journal of Multivariate Analysis*, 114:349–358, Feb.  
300 2013. ISSN 0047-259X. doi: 10.1016/j.jmva.2012.08.014.
- 301 J. Stelzer, Y. Chen, and R. Turner. Statistical inference and multiple test-  
302 ing correction in classification-based multi-voxel pattern analysis (MVPA):  
303 Random permutations and cluster size control. *NeuroImage*, 65:69–82, Jan.  
304 2013. ISSN 1053-8119. doi: 10.1016/j.neuroimage.2012.09.063.
- 305 G. Varoquaux, P. R. Raamana, D. Engemann, A. Hoyos-Idrobo, Y. Schwartz,  
306 and B. Thirion. Assessing and tuning brain decoders: cross-validation,  
307 caveats, and guidelines. working paper or preprint, June 2016.

## 308 A Analysis pipeline

309 Here is the analysis pipeline of Stelzer et al. [2013] we for the auditory data in  
 310 Gilron et al. [2016]. Denoting by  $i = 1, \dots, I$  the subject index,  $v = 1, \dots, V$   
 311 the voxel index, and  $s = 1, \dots, S$  the permutation index. Since regions<sup>3</sup> are  
 312 centred around a unique voxel, the voxel index  $v$  also serves as a unique  
 313 region index. Algorithm 1 computes a region-wise test statistic, which is  
 314 compared to its permutation null distribution computed by Algorithm 2.

**Algorithm 1:** Compute a group parametric map.

**Data:** fMRI scans, and experimental design.  
**Result:** Brain map of group statistics:  $\{\bar{T}_v\}_{v=1}^V$

```

1 for  $v \in 1, \dots, V$  do
2   for  $i \in 1, \dots, I$  do
3      $T_{i,v} \leftarrow$  test statistic for subject  $i$  in a region centered at  $v$ .
4    $\bar{T}_v \leftarrow \frac{1}{I} \sum_{i=1}^I T_{i,v}$ .
```

**Algorithm 2:** Compute a permutation p-value map.

**Data:** fMRI scans of 20 subjects, experimental design.  
**Result:** Brain map of permutation p-values:  $\{p_v\}_{v=1}^V$

```

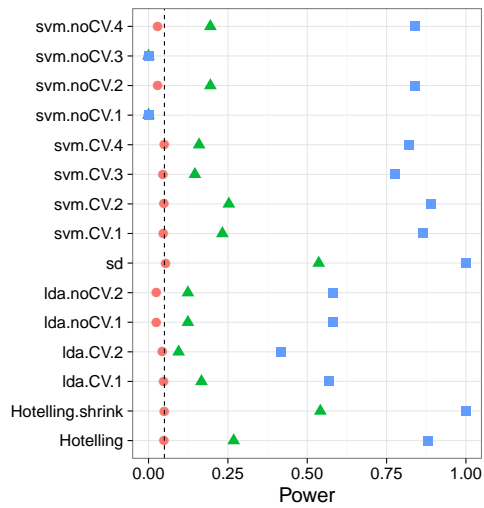
1 for  $s \in 1, \dots, S$  do
2   permute labels;
3    $\bar{T}_v^s \leftarrow$  parametric map
```

---

<sup>3</sup>*searchlight* or *sphere* in the MVPA parlance

317 **B More Simulations**

Figure 3: [TODO].



(a) 2 Folds.



(b) 20 Folds.

Figure 4: [TODO].



(a) Scale Change.



(b) t Null

Figure 5: [TODO].



(a) Compound symmetry



(b) AR(1)

Figure 6: [TODO].



(a)  $n=400$



(b) ?