# Trends in transmission and mortality rates of the Covid-19 pandemic estimated from publicly available data

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#### Abstract

A simple compartment model of Covid-19 infections and deaths is applied to publicly available data to estimate trends and transmission and mortality rates using random effects. Model estimates of infections and deaths match observations closely. Trends in estimated transmission rate vary substantially between geographic areas. Transmission rates were suppressed below  $0.007 \mathrm{da}^{-1}$  by the end of May in some areas, but often rebounded when social constraints were relaxed. Mortality rates of individuals infected with Covid-19 fell to less than  $0.001 \mathrm{da}^{-1}$  in most areas by the end of July. These results show that publicly available data, often collected and compiled with different protocols, can be used to quantitatively estimate trends in transmission and mortality rate.

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#### Introduction

The sudden advent of the Covid-19 pandemic provoked many political jurisdictions to advise people to "shelter in place" and to practice "social distancing". If this advice has been effective, it should be possible to detect the effects of the advice by comparing changes in transmission rates over time and between areas. SIR models are often applied to the spread of epidemics and have certainly been applied to the current Covid-19 pandemic (e.g. Chen et al. 2020; Roques et al. 2020). These models divide the affected the effected population into three compartments: susceptible (S), Infected (I) and Recovered (R). SIR models are usually expressed as coupled ordinary differential equations,

$$\frac{dS}{dt} = -\beta \frac{IS}{N} - \mu S \tag{1}$$

$$\frac{dI}{dt} = \beta \frac{IS}{N} - \mu I - \gamma I \tag{2}$$

$$\frac{dR}{dt} = -\mu R + \gamma I \tag{3}$$

$$\frac{dI}{dt} = \beta \frac{IS}{N} - \mu I - \gamma I \tag{2}$$

$$\frac{dR}{dt} = -\mu R + \gamma I \tag{3}$$

$$N = S + I + R \tag{4}$$

where N is the population size,  $\beta$  is the instantaneous rate ([t<sup>-1</sup>]),  $\mu$  is the instantaneous mortality rate ([ $t^{-1}$ ]), and  $\gamma$  is the instantaneous recovery rate  $([t^{-1}]).$ 

As the pandemic began to unfold, scientific institutes and governments at different levels began to make data publicly available on the World Wide Web. Unfortunately, data collection protocols may vary between institution over time. Additionally, few data sets include data for each of the compart-

ments in a SIR model. The New York Times' "historical" data set<sup>1</sup> is an easily accessible source of data and is updated daily. These data comprise daily totals of "cases" and "deaths" for each county in the United States. I assume that the data included as "cases" are a reasonable approximations of the Infected compartment (I) in a SIR model. There are simply no credible data of comparable scope on either the Susceptible or the Recovered compartments.

### Model Structure

I make some simplifying assumptions in the face of incomplete data: (1) The entire population is susceptible so that S/N = 1. (2) Over the short term, the size of the Susceptible compartment does not change,  $\frac{dS}{dt} = 0 = \frac{dN}{dt}$ , eliminating the Susceptible compartment. (3) People who recover from a Covid-19 infection return to the Susceptible compartment, eliminating the Recovered compartment. With these assumptions, and with the addition of a "deaths" compartment, the simplified SIR model is

$$\frac{dI}{dt} = \beta I - \mu I - \gamma I \tag{5}$$

$$\frac{dD}{dt} = \mu I \tag{6}$$

Most importantly this model has state variables that might be matched to available observations.

The available data contain measurement errors of various types. Definitions and methods of detecting and reporting the numbers of infected

 $<sup>^{1}</sup>$ https://github.com/nytimes/covid-19-data/

persons and numbers of deaths attributable to Covid-19 have changed since January of 2020, are continuing to evolve, and can be expected to change in the future. Reporting protocols also vary between political jurisdictions (or "geographies" in the parlance of the New York Times). Finally, there is additional variability in the biosocial processes that mediate disease transmission.

State-space models separate variability in the biosocial processes in the system (transition model) from errors in observing features of interest in the system (observation model). (See Harvey 1990).

The general form of a state-space process or transition model is

$$\alpha_t = T(\alpha_{t-1}) + \Theta_t \tag{7}$$

where  $\alpha_t$  is the state at time t and the function T embodies the dynamics mediating the development of the state at time t from the state at the previous time with random process error,  $\Theta_t$ .

The transition model for the simplified SIR model is constructed from the explicit finite difference approximations of equations (5) and (6) with associated log-normal random errors.

$$I_t = I_{t-\Delta t} \left( 1 + \Delta t (\beta_{t-\Delta t} - \mu_{t-\Delta t} - \gamma_{t-\Delta t}) \right) e^{\eta_t}$$
 (8)

$$D_t = \left(D_{t-\Delta t} + \Delta t \mu_{t-\Delta t} I_{t-\Delta t}\right) e^{\eta_t} \tag{9}$$

where  $\eta$  is a normal random deviate,  $\eta \sim N(0, \sigma_{\eta})$ , representing temporal variability in the biosocial factors that mediate the spread of the pandemic. I have no particular justification, beyond the parsimony principle, for the

assumption that the variance,  $\sigma_{\eta}$ , of the processes for I and D, should be the same.

The rate constants in the SIR model differential equations (in this case  $\beta$ ,  $\mu$  and  $\gamma$ ) are often assumed to be invariant. This biological assumption clearly conflicts with the social assumptions that behavioral modification can reduce transmission rates and that medical advances can reduce both transmission and mortality rates. One approach to modeling time-dependent rates of transmission and mortality,  $\beta$  and  $\mu$ , is to treat them as random effects (Skaug and Fournier 2006). Random effects are appropriate if repeating a time series of observations would not yield the same outcome as the initial observations. Random effects are also appropriate when observing the same process in two different areas. I model the  $\beta$  and  $\mu$  time series as log-normal random walks. I assume that

$$\log \beta_t = \log \beta_{t-\Delta t} + \varepsilon; \quad \varepsilon \sim N(0, \sigma_{\beta})$$
 (10)

$$\log \mu_t = \log \mu_{t-\Delta t} + \varrho; \quad \varrho \sim N(0, \sigma_{\mu})$$
 (11)

A similar approach has been used by fisheries scientists to represent illdetermined parameters in fisheries stock assessment models, such as timedependent fishing induced mortality (Nielsen and Berg 2014; Sibert 2017).

The recovery rate,  $\gamma_{t-\Delta t}$ , in equation (8) is computed algebraically as

$$\gamma_{t-\Delta t} = \beta_{t-\Delta t} - \mu_{t-\Delta t} + \left(1 - \frac{I_t}{I_{t-\Delta t}}\right) \tag{12}$$

The general form of the state-space observation model is

$$x_t = O(\alpha_t) + \Omega_t \tag{13}$$

where the function O describes the measurement process with error  $\Omega$  in observing the state  $\alpha$ .

I applied separate observation error models for cases and deaths. The observation model for cases is a simple log-normal error

$$\log \varphi_t = \left(\log \frac{1}{\sqrt{2\pi\sigma_I^2}} - \left(\frac{\log I_t - \log \widehat{I}_t}{\sigma_I}\right)^2\right) \tag{14}$$

where I is the observed number of cases and  $\widehat{I}$  is the number of cases predicted by equation 8.

Not all those afflicted by Covid-19 have died; there are far fewer deaths than infections. In addition, the observed time series for both I and Dbegins at the first recorded case, i.e. at time  $t = 0, I_t \ge 1$ . The first recorded death occurs several days or weeks after the first recorded case. Therefore the deaths time-series inevitably contains a substantial number of initial recorded zeros. The observation model for deaths accommodates observed zeroes by assuming to be "zero-inflated" log normal likelihood given by

$$\log \varepsilon_t = \begin{cases} D_t > 0 : & (1 - p_0) \cdot \left( \log \frac{1}{\sqrt{2\pi\sigma_D^2}} - \left( \frac{\log D_t - \log \widehat{D}_t}{\sigma_D} \right)^2 \right) \\ D_t = 0 : & p_0 \cdot \log \frac{1}{\sqrt{2\pi\sigma_D^2}} \end{cases}$$
(15)

where D is the observed number of deaths,  $\widehat{D}$  is the number of deaths predicted by equation 9, and  $p_0$  is the proportion of observed deaths equal to zero.

Model parameters are estimated by maximizing the joint likelihood of the process errors, observation errors, and random effects.

$$L(\theta, \alpha, x) = \prod_{t=1}^{m} \left[ \phi \left( \alpha_t - T(\alpha_{t-1}), \Theta \right) \right] \cdot \prod_{t=0}^{m} \left[ \phi \left( x_t - O(\alpha_t), \Omega \right) \right]$$
 (16)

Table 1: List of model variables for the simple SIR model, simpleSIR4. There are two state variables computed from the of estimated parameters and random effects. There are two random effects and five estimated variance parameters. All models variables are represented in the TMB C++ module as their natural logarithms.

Variable	Definition
	State variables:
I	Number of infected individuals
D	Number of deaths
	Random effects:
$eta_t$	Transmission rate; log-normal random walk
$\mu_t$	Mortality rate; log-normal random walk
	Estimated parameters:
$\sigma_I$	Infectious compartment estimation standard deviation
$\sigma_D$	Deaths compartment estimation standard deviation
$\sigma_{\eta}$	Standard deviation of transmission and deaths process errors
$\sigma_{eta}$	Standard deviation of transmission rate random walk
$\sigma_{\mu}$	Standard deviation of mortality rate random walk

where m is the number of days elapsed since the first recorded case,  $x_t$  is the vector of daily observations of cases and deaths,  $\alpha_t$  is the vector of the daily calculations of the state variables and random effects, and  $\theta$  is a vector of model parameters (Table 1). The R package TMB (Kristensen et al. 2016) was used to estimate the parameters of the model. The R and supporting C++ files are available on github.<sup>2</sup>

#### Results

Six months after the pandemic began spreading in the United States, it was obvious that some areas were more successful than other in controlling the spread of the Covid-19 virus. Trends in the per-capita number of cases in the thirty most populous counties in the United States are shown in Figure 1. These trajectories fall into two more or less distinct groups: those that are concave downward, e.g. Nassau Co. NY (NaNY), indicating successful control, and those that are concave upward, e.g. Miami-Dade Co. FL (MDFL), indicateing less successful control.

Prevalence histories for counties representative of concave downward and concave upward trajectories are shown in Figure 2. The 11-day moving averages of the daily increases in cases and deaths is a good indicator of the relative success in controlling the outbreak. The cumulative trends in number of cases is equivalent to the per capita trends in Figure 1. All histories show extreme day to day variability. Variability is most notable in the deaths time series, particularly for smaller counties.

<sup>&</sup>lt;sup>2</sup>simpleSIR4 at https://github.com/johnrsibert/SIR-Models

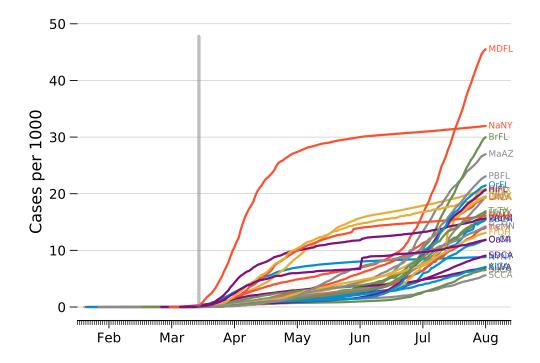
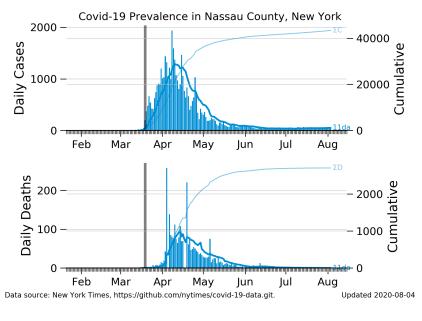


Figure 1: Trends in number of cases per 1000 people in the 30 most populous US counties. The vertical gray bar mark the March 19, 2020 California shelter in place order. See Table A.1 for key to county abbreviations.

The simpleSIR4 model estimates two random effects and five parameters. In principle, all random effects and parameters are estimated simultaneously. Initial experiments with the model showed that several different numerical algorithms used to find the minimum of the log likelihood function were unable to easily reach a solution. Minima were reached for some counties, but most attempts terminated prematurely. Inspection of the diagnostic plots for the model showed that predicted values of cases and deaths matched observed values almost exactly with unrealistically low estimates of  $\sigma_{\ln I}$  and  $\sigma_{\ln D}$ .



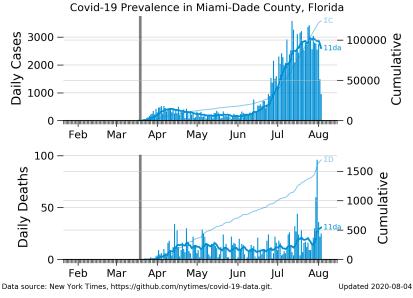


Figure 2: Prevalence trajectories for two US counties. Blue bars indicate daily increases in cases and deaths; dark blue lines enclosing the bars indicate 11 day moving averages of daily increases (labeled "11da"); pale blue lines indicate cumulative numbers (labeled  $\Sigma C$  and  $\Sigma D$ ); vertical gray bar marks the March 19, 2020 California shelter in place order.

The extreme variability in the data is reflected in the extreme variability of the estimated trends in transmission and mortality rates estimated by the unconstrained 5 parameter model. See Appendix figures C.3 and C.4 for details.

The simpleSIR4 model is easily configured with selected parameters fixed at constant values. All subsequent analysis focused on models with  $\sigma_{\ln I}$  = 0.223 and  $\sigma_{\ln D}$  = 0.00953. These standard deviations are equivalent to measurement errors of approximately 25% in reporting cases and 10% in reporting deaths. The algorithm converges to a solution in all cases, and converges rapidly using gradient methods.

Diagnostic information for the model estimates is plotted on logarithmic scales both to illustrate the lognormal likelihood functions used in the observation model, equations (14) and (15) and to illustrate trends in estimated transmission and mortality rates close to zero. The blue '+' symbols represent the observed cases (I) and deaths (D). The red lines overlaying the symbols are model predictions ( $\hat{I}$ ) and ( $\hat{D}$ ) of cases and deaths. The shaded areas bounded by red outlines are  $\pm 2$  estimated standard deviations,  $\sigma_{\ln I}$  and  $\sigma_{\ln D}$  in the observation model, around the estimated trends. The solid blue lines in the transmission rate  $\ln \beta$  and mortality rate  $\ln \mu$  diagnostic plots are the estimated transmission and death rate random effects. The shaded areas bounded by blue outlines are estimated random effects  $\pm 2$  standard deviations,  $\sigma_{\ln \beta}$  and  $\sigma_{\ln \mu}$ , of the generating random walks in the transition model. These areas should not be considered as indicators of the precision of the estimated random effects. The red lines labeled  $\tilde{\beta}$  and  $\tilde{\mu}$  are the medians

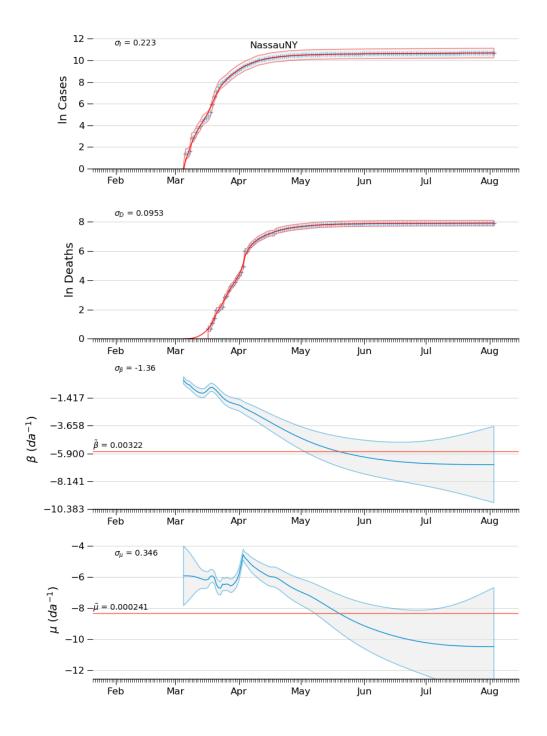


Figure 3: Diagnostic plots of model estimates for Nasssau County, NY, with constraints of the observation model variance,  $\sigma_{\ln I}=0.223$  and  $\sigma_{\ln D}=0.00953$ . See page 11 for explanation of figure.

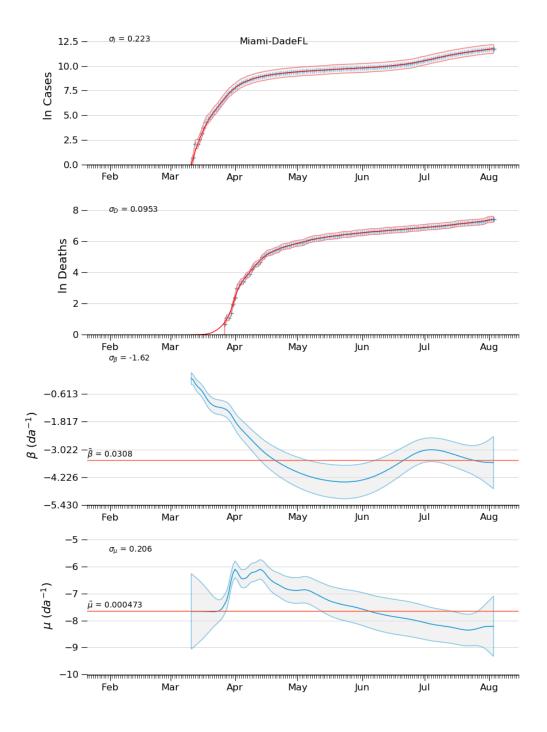


Figure 4: Diagnostic plots of model estimates for Miami-Dade County,FL, with constraints of the observation model variance,  $\sigma_{\ln I} = 0.223$  and  $\sigma_{\ln D} = 0.00953$ . See page 11 for explanation of figure.

of the estimated random effects over the time period.

Diagnostic plots for the constrained model are shown in figures 3 and 4 for convex downward and convex upward trajectories respectively. Estimated cases and deaths agree well with observation throughout the time series because of constraints on the observation model errors. Distinct trends in transmission rate estimates are plainly evident for the two prevalence patterns. A small, but distict, transitory upward "bump" in July is evident for the convex downward example, Miami-Dade Co. FL. Estimated mortality rates trend generally downward for both patterns.

Figure 5 compares estimated transmission rate among counties. Transmission rates increased rapidly at the beginning of the pandemic exceeding  $1 da^{-1}$  ( $\ln \beta \approx 0$ ) in early March, an instantaneous transmission rate equivalent to a doubling time of less than one day. Beginning in April, transmission rates fell substantially, and doubling times increased to longer than 20 days in some counties in late May. Counties with estimated transmission rates less than  $0.007 da^{-1}$  (or  $\ln \beta \leq 5$ ) at the end of May correspond roughly to those counties with concave downward prevalence trajectories. Figure 6 is a simplified presentation of estimated transmission rate between counties that compare counties with sustainable suppression of transmission (Cook Co, IL, Nassau Co, NY) with two counties that have suffered a resurgence of cases (Honolulu Co, HI and Miami-Dade Co FL). The Honolulu example indicates that simply suppressing the transmission rate to a point where the doubling time is greater than 100 days does not ensure a sustainable outcome.

Figure 7 compares estimated mortality rate among counties. Initial mor-

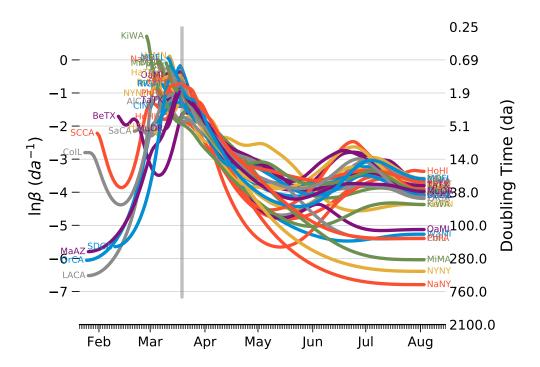


Figure 5: Estimated natural logarithms of the transmission rate for thirty two US counties using the constrained simpleSIR4 model. Equivalent doubling times  $(t_2 = \frac{\ln 2}{\exp(\ln \beta)})$  are shown on the right-hand ordinate.

tality rates were quite variable during the first months of the pandemic, but rose quickly to around  $0.01 da^{-1}$  ( $\ln \mu \approx 4.6$ ) in April. Subsequently the estimated mortality rates decreased for all counties and appear to have leveled off in August to lows near  $0.001 da^{-1}$  ( $\ln \mu \approx -6.9$ ).

### Discussion

Nonlinear statistical models with multiple parameters rely on numerical methods to estimate parameters by searching for minima in the negative of the

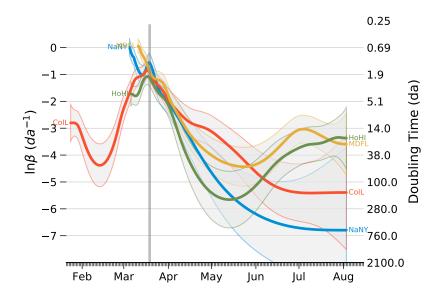


Figure 6: Estimated natural logarithms of the transmission rate for four US counties using the constrained simpleSIR4 model. Equivalent doubling times  $(t_2 = \frac{\ln 2}{\exp(\ln \beta)})$  are shown on the right-hand ordinate.

likelihood function. The parameter values at the minima are considered to be maximum likelihood estimators. The minimization algorithms applied to unconstrained simpleSIR4 do not reliably converge to solutions. The standard deviations in the observation model are components of the likelihood, and the algorithm pushes these parameters toward unrealistically low estimates. Setting the values of  $\sigma_{\ln I}$  and  $\sigma_{\ln D}$  to arbitrarily small constants allows the algorithm to estimate the other parameters.

The trends in estimated transmission rate Figure 5 seem reasonable. The extremely high transmission rates in March agree well with doubling times reported in newspaper articles at the time. The steady decline of transmission

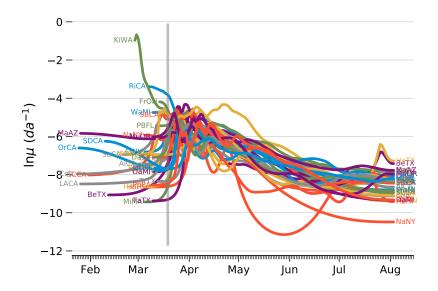


Figure 7: Estimated natural logarithms of the mortality rate for thirty two US counties using the constrained simpleSIR4 model.

rates after shelter-in-place advice is also consistent with casual observation. The transmission rates estimated for several counties appear to trend upward, at least briefly, in July (figure 5). Counties that display this upward deflection are also counties that have not been successful in controlling spread of the outbreak

The incubation time of the Covid-19 virus is usually assumed to be about 14 days **someone2020**. The trends in Figure 5 in conjunction with the empirical prevalence trends suggest that sustainable containment of the pandemic does not occur unless the instantaneous transmission rate is forced below  $0.018da^{-1}$ , that is, unless the doubling time is greater than 35 days, approximately twice the incubation period.

Given the presence of substantial numbers of zero observations at the start of the "deaths" time series, both the magnitude and the variability of the mortality rate estimates, Figure 7, is surprising.

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# A Abbreviation Key

Table A.1: Key to county name abbreviations used in time series graphs, figures 1 and

Key	County	State	Key	County	State
AlCA	Alameda	CA	MuOR	Multnomah	OR
BeTX	Bexar	TX	NYNY	New York City	NY
$\mathrm{BrFL}$	Broward	$\operatorname{FL}$	NaNY	Nassau	NY
ClNV	Clark	NV	OaMI	Oakland	MI
CoIL	Cook	$\operatorname{IL}$	OrCA	Orange	CA
DaTX	Dallas	TX	OrFL	Orange	$\operatorname{FL}$
FrOH	Franklin	OH	PBFL	Palm Beach	$\operatorname{FL}$
HaTX	Harris	TX	PhPA	Philadelphia	PA
$\operatorname{HeMN}$	Hennepin	MN	RiCA	Riverside	CA
${ m HiFL}$	Hillsborough	$\operatorname{FL}$	SBCA	San Bernardino	CA
HoHI	Honolulu	HI	SCCA	Santa Clara	CA
KiWA	King	WA	SDCA	San Diego	CA
LACA	Los Angeles	CA	SaCA	Sacramento	CA
MDFL	Miami-Dade	$\operatorname{FL}$	TaTX	Tarrant	TX
MaAZ	Maricopa	AZ	TrTX	Travis	TX
MiMA	Middlesex	MA	WaMI	Wayne	MI

## B Estimation results

Table B.1: Model results. Estimating  $\beta$  and  $\mu$  trends as random effects with constraints on  $\sigma_I$  and  $\sigma_D$ . Data updated 2020-08-04 from https://github.com/nytimes/covid-19-data.git.2020-08-04

County	u	$p_0$	f	C	$\sigma_{\eta}$	$\sigma_{\beta}$	$\sigma_{\mu}$	$\sigma_I$	$\sigma_D$	Υ̃	β	$\tilde{\mu}$
Nassau, NY	151	0.0789	-348	0	0.14	0.256	0.346	0.223	0.0953	-1.22e-08	0.00322	0.000241
New York City, NY	155	0.0833	-310	0	0.161	0.217	0.36	0.223	0.0953	-2.36e-08	0.00533	0.000405
Wayne, MI	146	0.0544	-336	0	0.14	0.229	0.16	0.223	0.0953	-1.8e-08	0.00619	0.000875
Oakland, MI	146	0.068	-332	0	0.137	0.226	0.426	0.223	0.0953	-1.62e-08	0.0101	0.000594
Philadelphia, PA	146	0.102	-340	0	0.126	0.175	0.425	0.223	0.0953	-2.42e-08	0.0106	0.000532
Middlesex, MA	151	0.105	-357	0	0.124	0.237	0.371	0.223	0.0953	-1.25e-08	0.0107	0.000451
King, WA	157	0.00633	-431	0	0.126	0.234	0.339	0.223	0.0953	-8.63e-09	0.013	0.000481
Franklin, OH	142	0.0629	-419	0	0.102	0.157	0.3	0.223	0.0953	-1.76e-08	0.0208	0.00101
Honolulu, HI	150	0.166	-484	0	0.0721	0.227	0.49	0.223	0.0953	-5.15e-08	0.0215	0.000174
Cook, IL	192	0.275	-473	0	0.101	0.234	0.217	0.223	0.0953	-2.2e-07	0.0226	0.000466
Alameda, CA	155	0.141	-465	0	0.0808	0.133	0.248	0.223	0.0953	-3.45e-08	0.0231	0.000527
Multnomah, OR	146	0.0272	-497	0	0.0798	0.181	0.318	0.223	0.0953	-5.07e-08	0.0233	0.000362
Santa Clara, CA	185	0.204	-586	0	0.071	0.237	0.274	0.223	0.0953	-1.55e-07	0.0246	0.000352
Los Angeles, CA	190	0.236	-454	0	0.102	0.305	0.244	0.223	0.0953	-3.45e-07	0.0249	0.000423
San Diego, CA	175	0.244	-430	0	0.0956	0.277	0.317	0.223	0.0953	-2.63e-07	0.0267	0.000719
Riverside, CA	149	0.00	-482	0	0.00	0.138	0.183	0.223	0.0953	-2.72e-08	0.0294	0.000895
Palm Beach, FL	144	0.069	-378	0	0.111	0.166	0.157	0.223	0.0953	-1.54e-08	0.0302	0.000942
Harris, TX	151	0.0921	-373	0	0.102	0.197	0.322	0.223	0.0953	-2.44e-08	0.0302	0.000301
Miami-Dade, FL	145	0.11	-342	0	0.133	0.197	0.206	0.223	0.0953	-1.08e-08	0.0308	0.000473
Orange, FL	143	0.0208	-418	0	0.101	0.21	0.435	0.223	0.0953	-1.98e-08	0.0314	0.00024
Clark, NV	151	0.0724	-436	0	0.1	0.158	0.218	0.223	0.0953	-3.3e-08	0.0319	0.000743
Travis, TX	143	0.0972	-359	0	0.1	0.19	0.271	0.223	0.0953	-1.73e-08	0.0327	0.000319
Tarrant, TX	146	0.068	-414	0	0.1	0.138	0.42	0.223	0.0953	-3.12e-08	0.0328	0.000335
Broward, FL	150	0.0728	-391	0	0.107	0.167	0.447	0.223	0.0953	-2.15e-08	0.0333	0.00041
Orange, CA	191	0.313	-519	0	0.0769	0.234	0.266	0.223	0.0953	-3.73e-07	0.0334	0.000732
	146	0.0612	-388	0	0.11	0.17	0.309	0.223	0.0953	-1.43e-08	0.0336	0.000504
San Bernardino, CA	141	0.0634	-406	0	0.0999	0.14	0.198	0.223	0.0953	-2.06e-08	0.0343	0.000794
Sacramento, CA	164	0.109	-574	0	0.0666	0.174	0.252	0.223	0.0953	-8.02e-08	0.0343	0.000428
Hennepin, MN	144	0.103	-359	0	0.114	0.207	0.402	0.223	0.0953	-1.24e-08	0.036	0.000917
Hillsborough, FL	155	0.16	-461	0	0.0813	0.189	0.227	0.223	0.0953	-7.15e-08	0.0373	0.00065
Maricopa, AZ	190	0.283	-482	0	0.0897	0.235	0.158	0.223	0.0953	-4e-07	0.0422	0.00188
Bexar, TX	173	0.224	-478	0	0.0745	0.213	0.376	0.223	0.0953	-7.61e-08	0.0461	0.000393
Median	150.5	0.09465	-418.5	0	0.101	0.202	0.3045	0.223	0.0953	-2.43e-08	0.0298	0.000477

Table B.2: Model results. Estimating  $\beta$  and  $\mu$  trends as random effects without constraints on  $\sigma_I$  and  $\sigma_D$ . Data updated 2020-08-04 from https://github.com/nytimes/covid-19-data.git.2020-08-04

County	u	$p_0$	f	C	$\sigma_{\eta}$	$\sigma_{eta}$	$\sigma_{\mu}$	$\sigma_I$	$\sigma_D$	$\tilde{\gamma}$	$\dot{\beta}$	$ ilde{\mu}$
Nassau, NY	151	0.0789	-1190	1	0.231	0.603	10.3	0.000183	3.29e-08	-9.46e-09	0.00295	9.88e-05
New York City, NY	155	0.0833	-1000	0	0.187	1.04	1.01	0.000436	0.000367	-2.73e-08	0.00476	0.000234
Oakland, MI	146	0.068	-836	_	0.16	1.55	1.18	9.12e-07	0.00426	-1.91e-08	0.00669	0.000318
Cook, IL	192	0.275	-1100	П	0.116	3.68	0.992	8.16e-08	8.01e-05	-2.24e-07	0.00679	0.000201
Wayne, MI	146	0.0544	-856	П	0.192	1.15	1.46	0.000795	0.000936	-2.57e-08	0.00701	0.000362
Philadelphia, PA	146	0.102	-728	П	0.159	1	1.98	0.00274	0.00396	-3.1e-08	0.00964	0.000227
Middlesex, MA	151	0.105	-836	0	0.162	1.05	1.24	0.000663	0.00204	-1.56e-08	0.00995	0.000331
King, WA	157	0.00633	-1080	П	0.147	0.474	0.909	0.00206	0.00224	-5.99e-09	0.0133	0.000455
Honolulu, HI	150	0.166	-1480	10	0.116	4.87	117	0.000734	3.7e-06	-5.53e-08	0.0156	1.46e-11
Santa Clara, CA	185	0.204	-1280	П	0.104	4.78	7.43	9.33e-08	2.29e-06	-1.53e-07	0.0158	1.16e-07
Sacramento, CA	164	0.109	-803	10	0.123	3.17	2.46	1.44e-06	0.0049	-8.81e-08	0.0183	0.00016
Multnomah, OR	146	0.0272	-894	_	0.119	0.896	3.35	0.0036	0.00226	-6.79e-08	0.0234	5.44e-05
Franklin, OH	142	0.0629	-819	Н	0.123	0.462	1.3	0.00255	0.00368	-1.42e-08	0.0239	0.000575
Los Angeles, CA	190	0.236	-971	П	0.242	0.889	0.983	2.22e-06	0.00661	-3.77e-07	0.024	0.000399
Alameda, CA	155	0.141	-905	П	0.131	3.61	20.3	2.65e-05	6.68e-08	-3.95e-08	0.0241	9.44e-10
San Diego, CA	175	0.244	-850	П	0.161	1.08	1.23	4.71e-06	0.0103	-2.91e-07	0.0247	0.000335
Bexar, TX	173	0.224	-689	Н	0.131	2.61	1.44	0.000397	0.0103	-7.18e-08	0.0261	0.000256
Orange, CA	191	0.313	-878	П	0.127	1.54	0.961	6.16e-06	0.053	-4.02e-07	0.0268	0.000509
Orange, FL	143	0.0208	-710	П	0.119	0.678	1.08	0.0015	0.0373	-2.3e-08	0.027	0.000192
Clark, NV	151	0.0724	-662	10	0.148	1.5	5.31	0.00247	1.25e-05	-4.16e-08	0.0276	0.000322
Tarrant, TX	146	0.068	-662	П	0.14	1.24	1.34	0.00891	0.00326	-3.79e-08	0.0283	0.000269
Harris, TX	151	0.0921	-429	П	0.116	0.27	0.965	0.156	0.0215	-2.11e-08	0.0297	0.000289
Palm Beach, FL	144	0.069	-207	0	0.137	0.337	1.31	0.0822	0.00588	-1.16e-08	0.0302	0.000525
San Bernardino, CA	141	0.0634	-567	П	0.146	1.74	2.74	0.0051	0.00586	-1.74e-08	0.0304	0.000207
Miami-Dade, FL	145	0.11	-722	10	0.156	0.639	0.961	6.89e-06	0.00814	-9.55e-09	0.0313	0.000447
Hennepin, MN	144	0.103	-726	0	0.14	0.72	1.35	0.00522	0.00203	-9.13e-09	0.0314	0.00048
Riverside, CA	149	90.0	-683	П	0.113	1.25	5.23	0.0174	2.17e-05	-2.61e-08	0.0317	0.000718
Maricopa, AZ	190	0.283	-932	_	0.105	1.23	1.26	5.43e-06	0.0164	-4.2e-07	0.0322	0.000596
Travis, TX	143	0.0972	-394	П	0.14	0.107	1.44	0.177	0.0131	-1.67e-08	0.0329	0.000265
Hillsborough, FL	155	0.16	-653	0	0.111	1.11	1.28	0.00477	0.0169	-7.24e-08	0.0329	0.000393
Broward, FL	150	0.0728	-584	П	0.13	0.23	1.63	0.0759	0.00289	-2.03e-08	0.0331	0.000275
Dallas, TX	146	0.0612	-529	_	0.13	0.303	1.26	0.0757	0.00757	-1.04e-08	0.0349	0.000342
Median	150.5	0.09465	-811	П	0.134	1.065	1.325	0.0011475	0.00382	-2.67e-08	0.0254	0.0003035

# C Diagnostic Plots

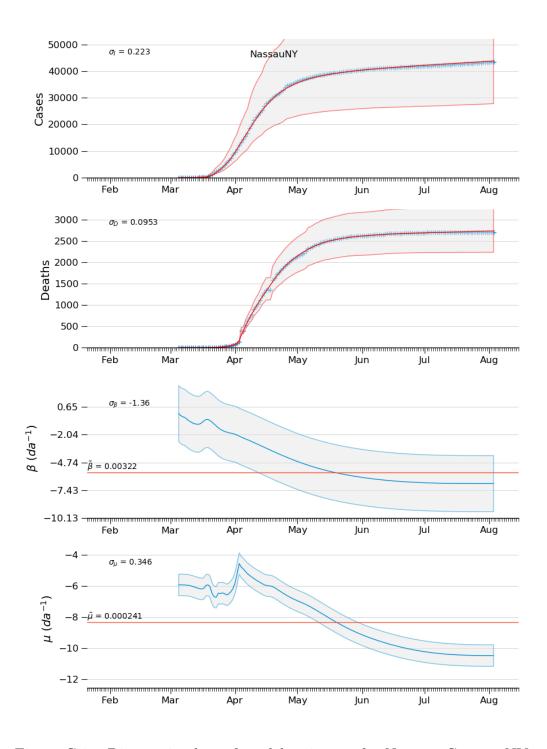


Figure C.1: Diagnostic plots of model estimates for Nasssau County, NY, with constraints of the observation model variance,  $\sigma_{\ln I}=0.223$  and  $\sigma_{\ln D}=0.00953$ . Cases and deaths plotted on arithmetic scale. See page 11 for explanation of figure.

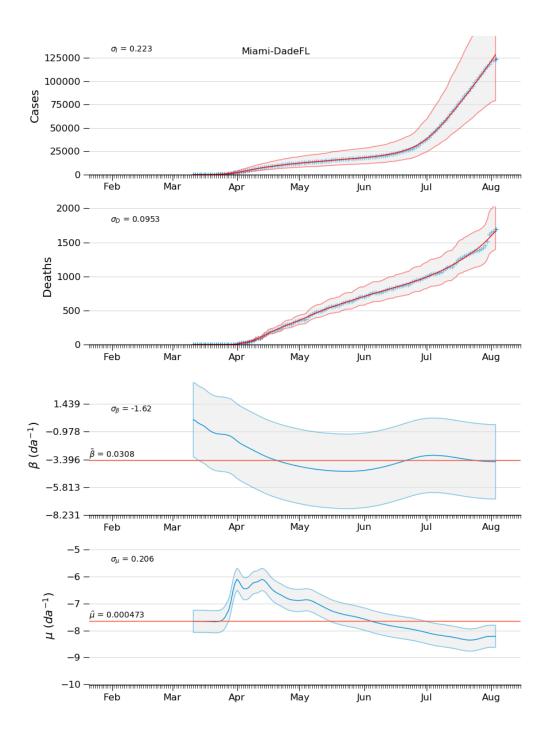


Figure C.2: Diagnostic plots of model estimates for Miami-Dade County, FL with constraints of the observation model variance,  $\sigma_{\ln I} = 0.223$  and  $\sigma_{\ln D} = 0.00953$ . Cases and deaths plotted on arithmetic scale. See page 11 for explanation of figure.

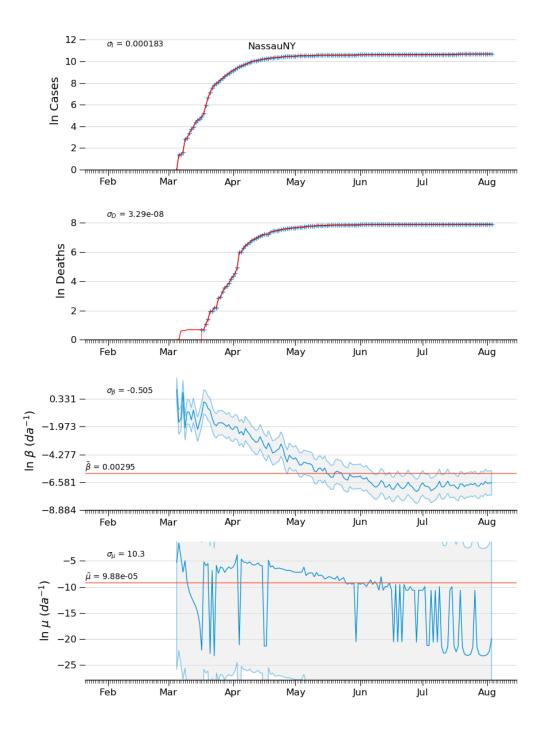


Figure C.3: Diagnostic plots of model estimates for Nasssau County, NY, without constraints of the observation model variance. See page 11 for explanation of figure.

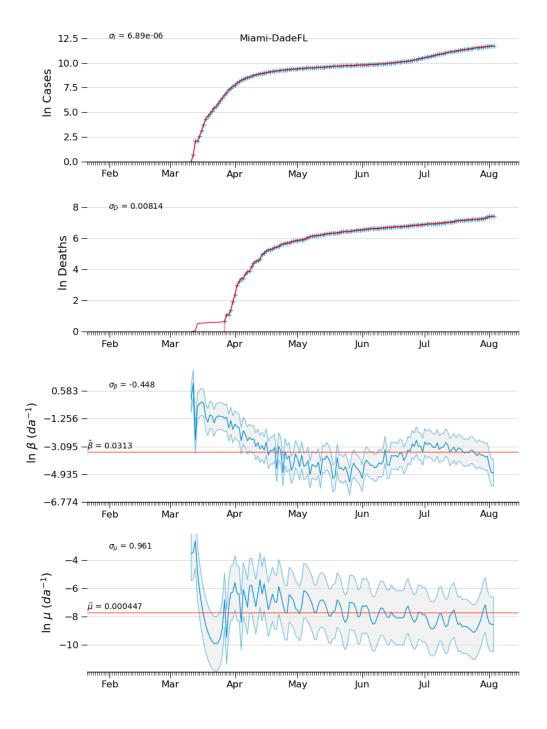


Figure C.4: Diagnostic plots of model estimates for Miami-Dade County,FL, without constraints of the observation model variance. See page 11 for explanation of figure.