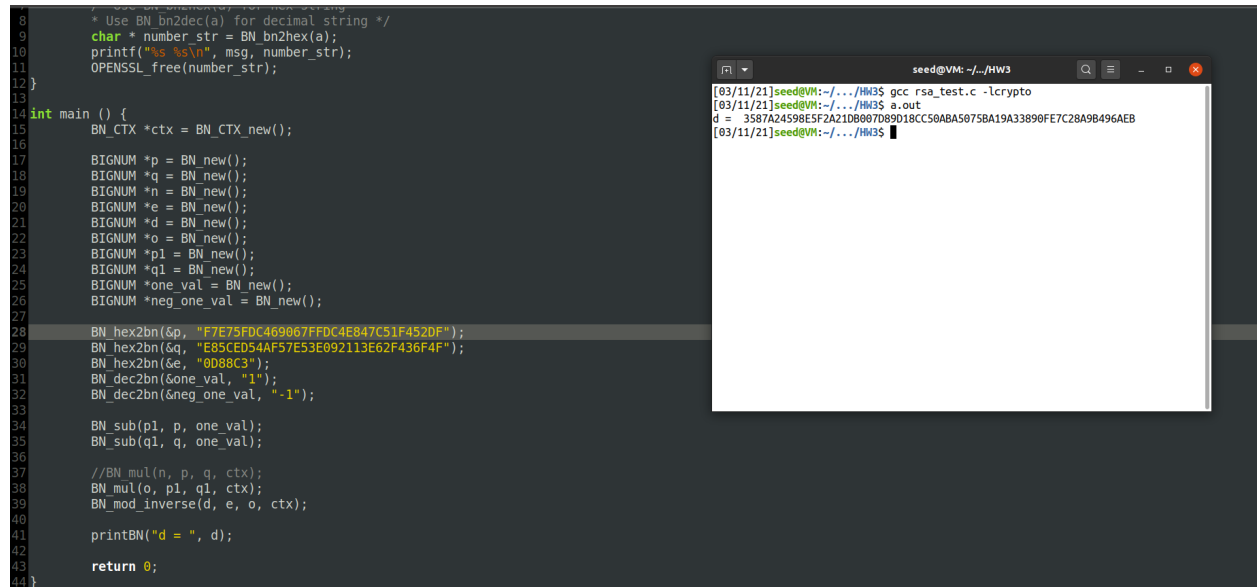


Task 1:


```

8  * Use BN_bn2dec(a) for decimal string */
9  char * number_str = BN_bn2hex(a);
10 printf("%s %s\n", msg, number_str);
11 OPENSSL_free(number_str);
12 }
13
14 int main () {
15     BN_CTX *ctx = BN_CTX_new();
16
17     BIGNUM *p = BN_new();
18     BIGNUM *q = BN_new();
19     BIGNUM *n = BN_new();
20     BIGNUM *e = BN_new();
21     BIGNUM *d = BN_new();
22     BIGNUM *o = BN_new();
23     BIGNUM *p1 = BN_new();
24     BIGNUM *q1 = BN_new();
25     BIGNUM *one_val = BN_new();
26     BIGNUM *neg_one_val = BN_new();
27
28     BN_hex2bn(&p, "F7E75FDC469867FFDC4E847C51F4520F");
29     BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
30     BN_hex2bn(&e, "0088C3");
31     BN_dec2bn(&one_val, "1");
32     BN_dec2bn(&neg_one_val, "-1");
33
34     BN_sub(p1, p, one_val);
35     BN_sub(q1, q, one_val);
36
37     //BN_mul(n, p, q, ctx);
38     BN_mul(o, p1, q1, ctx);
39     BN_mod_inverse(d, e, o, ctx);
40
41     printBN("d = ", d);
42
43     return 0;
44 }

```

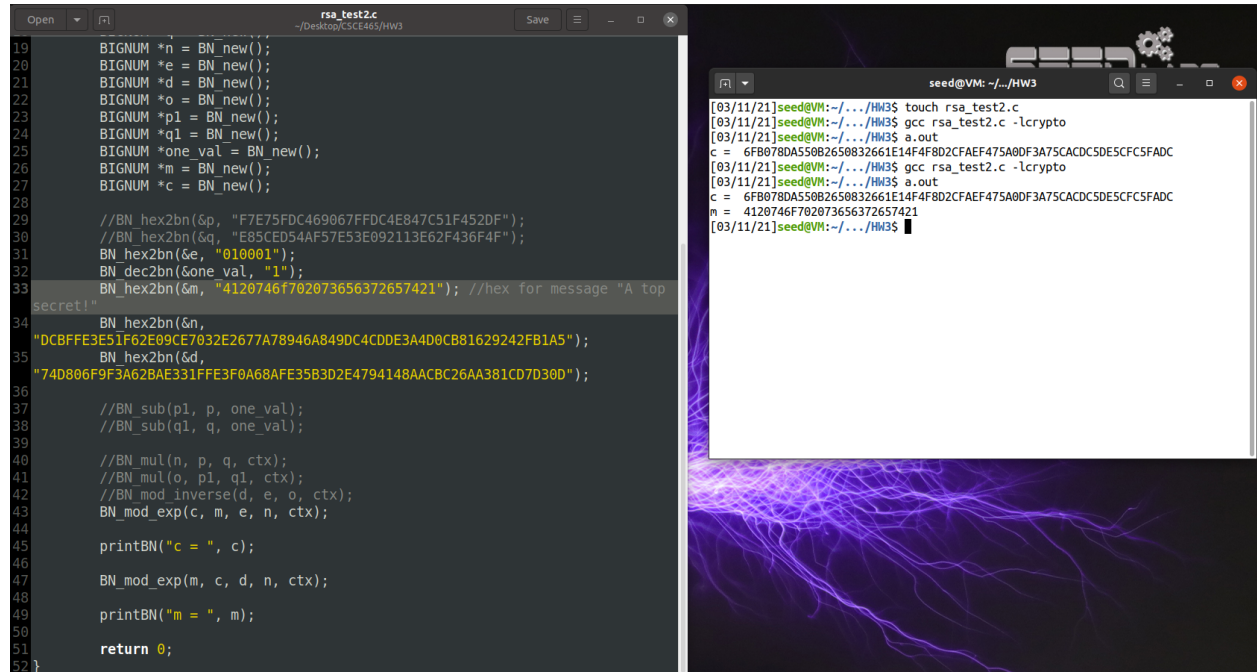
```

seed@VM: ~/HW3
[03/11/21]seed@VM:~/HW3$ gcc rsa_test.c -lcrypto
[03/11/21]seed@VM:~/HW3$ a.out
d = 3587A24598E5F2A21DB007D89D18CC50ABA5075BA19A33890FE7C28A9B496AEB
[03/11/21]seed@VM:~/HW3$

```

In this task, I calculated the private key value by setting up the determination of $(p-1)*(q-1)$ as the modulus for the following equation. This required first declaring the number 1 as a BIGNUM variable, then applying it to the values of p and q with the subtraction function. From here, it was as simple as multiplying their subtracted values as the modulus, which was then used in the inverse modulo function to determine d as a result of the formula $d*e = 1 \bmod((p-1)*(q-1))$. The value of this function was output to the terminal shown.

Task 2:

The image shows a C program in a text editor and its execution in a terminal. The C program, named 'rsa_test2.c', implements RSA encryption and decryption using the BIGNUM library. It defines variables for modulus (n), public exponent (e), private exponent (d), and primes (p, q). It also defines a one-time pad (one_val) and a message (m). The message is converted to a hex string and then encrypted using the modular exponentiation function BN_mod_exp. The encrypted message (c) is printed. The program also performs decryption using the private exponent (d) and the encrypted message (c) to retrieve the original message (m). The terminal output shows the execution of the program, the compilation with gcc, and the resulting encrypted and decrypted messages.

```
19 BIGNUM *n = BN_new();
20 BIGNUM *e = BN_new();
21 BIGNUM *d = BN_new();
22 BIGNUM *o = BN_new();
23 BIGNUM *p1 = BN_new();
24 BIGNUM *q1 = BN_new();
25 BIGNUM *one_val = BN_new();
26 BIGNUM *m = BN_new();
27 BIGNUM *c = BN_new();
28
29 //BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
30 //BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
31 BN_hex2bn(&e, "010001");
32 BN_dec2bn(&one_val, "1");
33 BN_hex2bn(&m, "4120746f702073656372657421"); //hex for message "A top
secret!"
34 BN_hex2bn(&n,
"DCBFFE3E51F62E09CE7032E2677A78946A849DC4CDD3A400CB81629242FB1A5");
35 BN_hex2bn(&d,
"74D806F9F3A62BAE331FFE3F0A68AFE35B3D2E4794148AACBC26AA381CD7D38D");
36
37 //BN_sub(p1, p, one_val);
38 //BN_sub(q1, q, one_val);
39
40 //BN_mul(n, p, q, ctx);
41 //BN_mul(o, p1, q1, ctx);
42 //BN_mod inverse(d, e, o, ctx);
43 BN_mod_exp(c, m, e, n, ctx);
44
45 printBN("c = ", c);
46
47 BN_mod_exp(m, c, d, n, ctx);
48
49 printBN("m = ", m);
50
51 return 0;
52 }
```

```
[03/11/21]seed@VM:~/HW3$ touch rsa_test2.c
[03/11/21]seed@VM:~/HW3$ gcc rsa_test2.c -lcrypto
[03/11/21]seed@VM:~/HW3$ a.out
c = 6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC
[03/11/21]seed@VM:~/HW3$ gcc rsa_test2.c -lcrypto
[03/11/21]seed@VM:~/HW3$ a.out
c = 6FB078DA550B2650832661E14F4F8D2CFAEF475A0DF3A75CACDC5DE5CFC5FADC
m = 4120746f702073656372657421
[03/11/21]seed@VM:~/HW3$
```

This task required me to encrypt a message, which first got converted to a hex string and used as input for encryption. To do this, I used the provided values to perform the encryption using the modular exponent function to determine the encrypted message, c. To confirm that this performed properly, I also performed decryption of the message using the same function but in reverse, using d as the exponential value instead of e, and determined the encrypted string yielded the same message when decrypted.

Task 3:

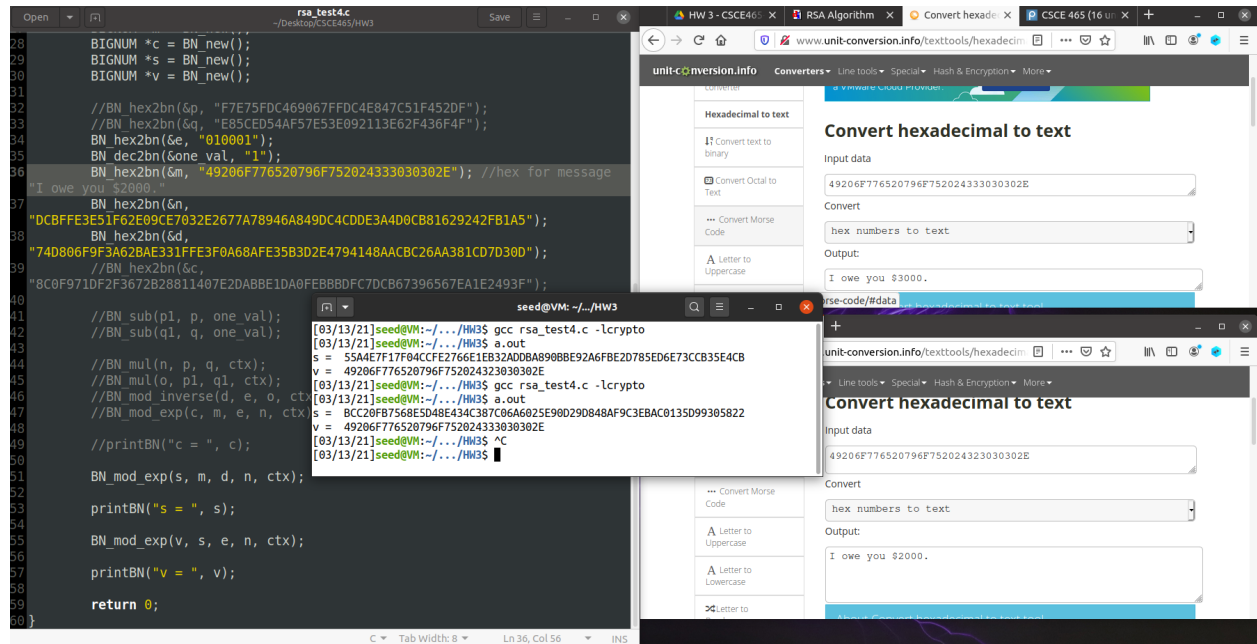
The image shows a C program on the left and a web-based hex-to-text converter on the right. The C program uses the BN library to perform modular exponentiation and convert hex strings to integers. The web converter, unit-conversion.info, is used to verify the output of the C program.

```
21 BIGNUM *d = BN_new();
22 BIGNUM *o = BN_new();
23 BIGNUM *p1 = BN_new();
24 BIGNUM *q1 = BN_new();
25 BIGNUM *one_val = BN_new();
26 BIGNUM *m = BN_new();
27 BIGNUM *c = BN_new();
28
29 //BN_hex2bn(&p, "F7E75FDC469067FFDC4E847C51F452DF");
30 //BN_hex2bn(&q, "E85CED54AF57E53E092113E62F436F4F");
31 BN_hex2bn(&e, "010001");
32 BN_dec2bn(&one_val, "1");
33 //BN_hex2bn(&m, "4120746f702073656372657421"); //hex for message "A
top secret!"
34 BN_hex2bn(&n,
"DCBFFE3E51F62E09CE7032E2677A78946A849DC4DDDE3A4D0CB81629242FB1A5");
35 BN_hex2bn(&d,
"74D806F9F3A62BAE331FFE3F0A6AFE35B3D2E4794148AACBC26AA381CD7D38D");
36 BN_hex2bn(&c,
"8C0F971DF2F3672B28811407E2DA8BE1DA0FEBB8DFC7DCB67396567EA1E2493F");
37
38 //BN_sub(p1, p, one_val);
39 //BN_sub(q1, q, one_val);
40
41 //BN_mul(n, p, q, ctx);
42 //BN_mul(o, p1, q1, ctx);
43 //BN_mod_inverse(d, e, o, ctx);
44 //BN_mod_exp(c, m, e, n, ctx);
45
46 //printBN("c = ", c);
47
48 BN_mod_exp(m, c, d, n, ctx);
49
50 printBN("m = ", m);
51
52 return 0;
53 }
```

The web converter shows the input data: 50617373776f72642069732064656573. The output is: Password is dees. A terminal window in the foreground shows the execution of the C program, confirming the output: m = 50617373776f72642069732064656573.

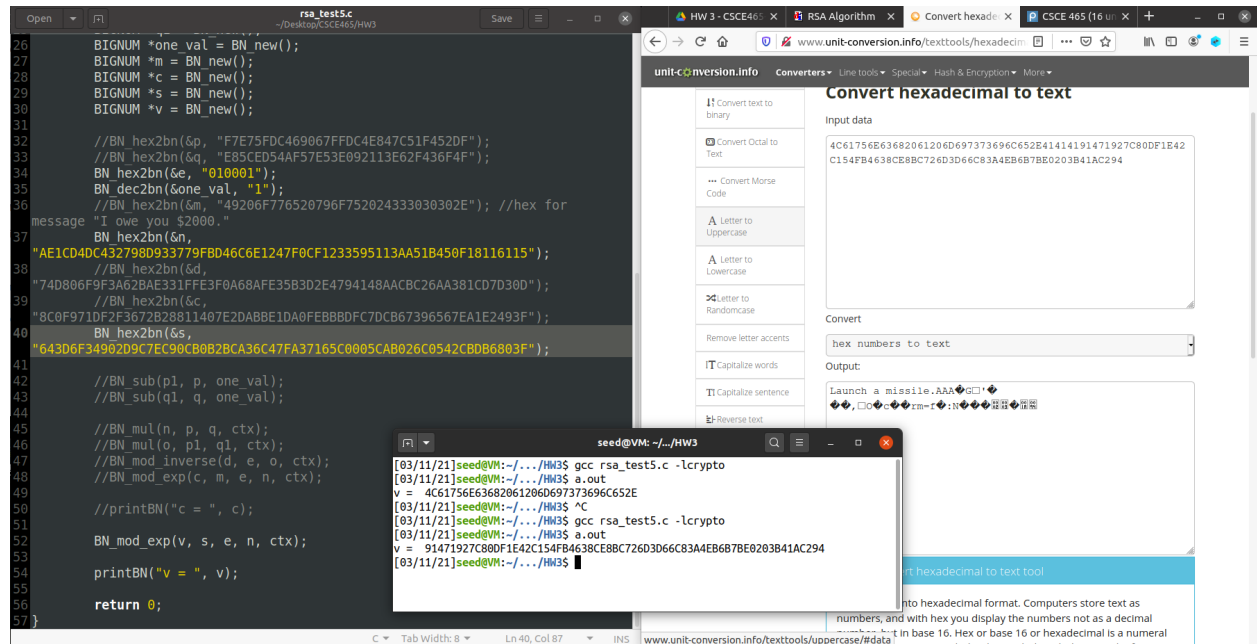
Similar to what I performed as a check in the previous task, I decrypted the provided encrypted message using the modular exponent function and the private key to yield the original message. To confirm this, I ran the output hex string through a converter (in place of the python commands, which I couldn't get to work) and confirmed that the output message was the same as what was originally sent.

Task 4:



Similar to the encryption step in Task 2, this task requested that I sign the message being sent. To do this, I signed the message using a private key and sending the message to the recipient. To verify that the signature matched what was expected, I had the message decrypted into the original message against the signature using regular decryption via the public key e . This is demonstrated as functioning properly in the associated hex to text converter on the right for each of the messages sent.

Task 5:



Finally, in this task I did the same as I did in my checking step in Task 4 where I decrypted the signed message received using the public key to verify that the message was correct as well as the signature. To make sure this worked, I sent this through the same hex to text converter and verified that the decryption algorithm worked as expected. Similarly, I also altered the signed message and ran it through the converter and got corrupted information as a result, illustrated in the attached image as well.