(b)

Solution. Using Euler's relation, we can write

$$x(t) = \left(e^{-4t} - \frac{j}{2}e^{-(5-5j)t} + \frac{j}{2}e^{-(5+5j)t}\right)u(t).$$

Then the Laplace transform of x(t) can be expressed as

$$X(s) = \int_{-\infty}^{\infty} e^{-4t} u(t) \, \mathrm{d}t - \frac{j}{2} \int_{-\infty}^{\infty} e^{-(5-5j)t} u(t) \, \mathrm{d}t + \frac{j}{2} \int_{-\infty}^{\infty} e^{-(5+5j)t} u(t) \, \mathrm{d}t.$$

Each of these integrals represents a Laplace transform of the type encountered in Example 9.1. It follows that

$$\begin{split} e^{4t}u(t) & \overset{\mathcal{L}}{\longleftrightarrow} \frac{1}{s+4}, \quad \mathcal{R}e\{s\} > -4, \\ e^{-(5-5j)t}u(t) & \overset{\mathcal{L}}{\longleftrightarrow} \frac{1}{s-5+5j}, \quad \mathcal{R}e\{s\} > -5, \\ e^{-(5+5j)t}u(t) & \overset{\mathcal{L}}{\longleftrightarrow} \frac{1}{s-5-5j}, \quad \mathcal{R}e\{s\} > -5. \end{split}$$

For all three Laplace transforms to converge simultaneously, we must have $\Re e\{s\} > -4$. Consequently, the Laplace transform of x(t) is

$$X(s) = \frac{1}{s+4} - \frac{j}{2(s-5+5j)} + \frac{j}{2(s-5-5j)}, \quad \mathcal{R}e\{s\} > -4.$$

(i)

Solution.

$$x(t) = \delta(t) + u(t) \stackrel{\mathcal{L}}{\longleftrightarrow} X(s) = 1 + \frac{1}{s}, \quad \mathcal{R}e\{s\} > 0.$$

(j)

Solution. Note that $\delta(3t) + u(3t) = \delta(t) + u(t)$. Therefore, the Laplace transform is the same as the result of the previous part.

- 9.22
- (e)
- 9.23
- (1)
- 9.25
- (c)
- 9.26
- 9.31
- 9.35
- 9.40