

$$\hat{\beta} = \frac{\sum_i x_i y_i}{\sum_j x_j^2}$$

$$y_i = y_i \cdot \beta^* + e_i$$

$$\hat{\beta} = \beta^* + Ze$$

$$\hat{\beta} = \frac{\sum_i x_i (x_i \cdot \beta^* + e_i)}{\sum_j x_j^2} = \frac{\sum_i x_i^2 \cdot \beta^* + e_i x_i}{\sum_j x_j^2}$$

$$\hat{\beta} = \beta^* \cdot \frac{\sum_i x_i^2}{\sum_j x_j^2} + \frac{\sum_i e_i x_i}{\sum_j x_j^2} = \beta^* + eZ$$

$$e = \sum e_i$$

$$Z = \frac{\sum x_i}{\sum x_j^2}$$