bayesian-bandit

March 14, 2020

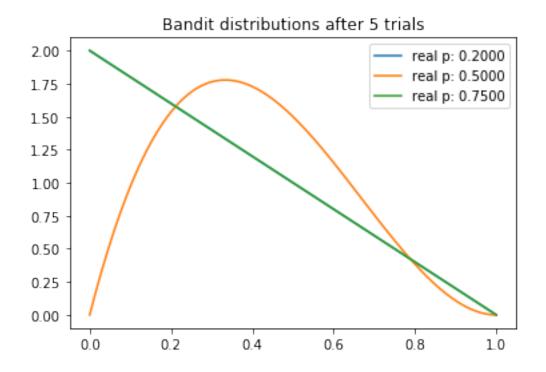
0.1 Bayesian Method for Exploit-Explore Problem

- instead of playing slot machine (bandit) one at a time
- on each round we rank each bandit according to samples from their posterior
- model each slot machine as a separate Beta distribution, i.e. model each machine's win rate
- draw a sample from each Beta distribution and sort them in order, i.e. the ranking
- pick top item from ranked list, and play that slot machine
- this is analogous to (CTR) clicks/impressions on a website
- Bayesian approach lets us treat click through rate measurements as random variables,
- and explore-exploit is handled by random variables

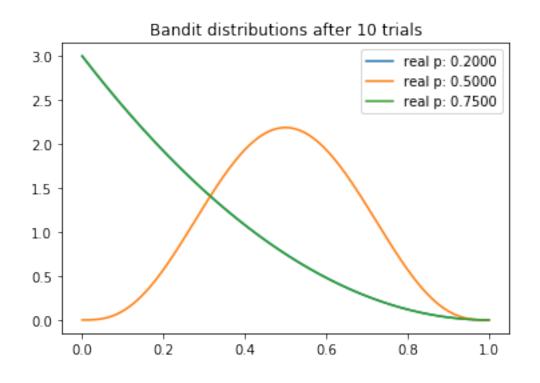
```
[2]: import matplotlib.pyplot as plt
    import numpy as np
    from scipy.stats import beta
    NUM_TRIALS = 2000
    BANDIT_PROBABILITIES = [0.2, 0.5, 0.75]
[3]: class Bandit(object):
      def __init__(self, p):
        self.p = p
        self.a = 1
        self.b = 1
      def pull(self):
        return np.random.random() < self.p</pre>
      def sample(self):
        return np.random.beta(self.a, self.b)
      def update(self, x):
        self.a += x
        self.b += 1 - x
    def plot(bandits, trial):
      x = np.linspace(0, 1, 200)
      for b in bandits:
```

```
y = beta.pdf(x, b.a, b.b)
        plt.plot(x, y, label='real p: %.4f' % b.p)
     plt.title('Bandit distributions after %s trials' % trial)
     plt.legend()
     plt.show()
    def experiment():
     bandits = [Bandit(p) for p in BANDIT_PROBABILITIES]
      sample_points = [5, 10, 20, 50, 100, 200, 500, 1000, 1500, 1999]
     for i in range(NUM_TRIALS):
       bestb = None
        maxsample = -1
        allsamples = []
        for b in bandits:
          sample = b.sample()
          allsamples.append('%.4f' % sample)
          if sample > maxsample:
            maxsample = sample
            bestb = b
        if i in sample_points:
          print('current samples: %s' % allsamples)
          plot(bandits, i)
        x = bestb.pull()
        bestb.update(x)
[4]: experiment();
```

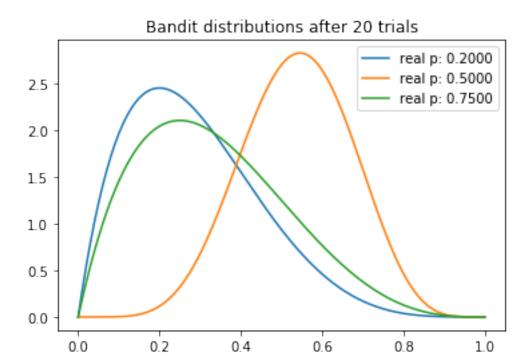
current samples: ['0.3260', '0.2359', '0.8346']



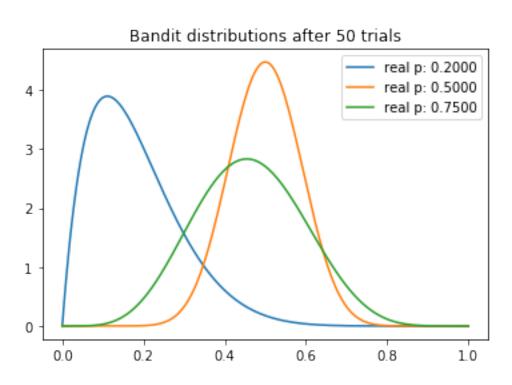
current samples: ['0.0057', '0.3723', '0.0160']



current samples: ['0.5576', '0.6959', '0.4918']

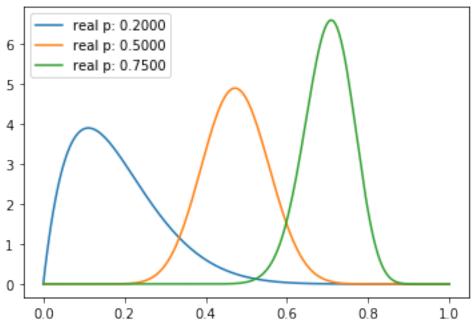


current samples: ['0.2300', '0.5487', '0.6393']



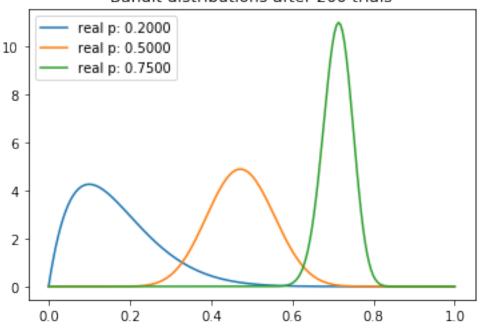
current samples: ['0.0286', '0.5113', '0.6657']

Bandit distributions after 100 trials



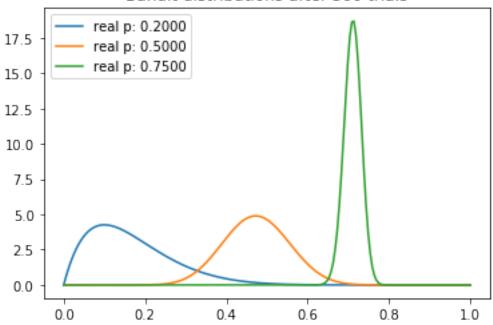
current samples: ['0.0668', '0.4711', '0.7406']

Bandit distributions after 200 trials



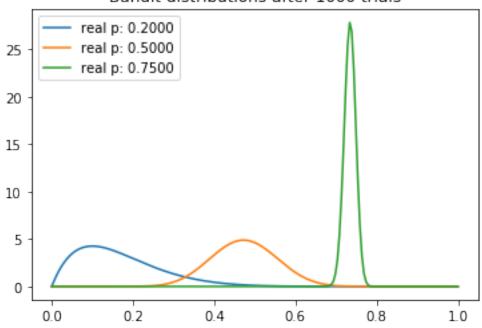
current samples: ['0.0722', '0.6293', '0.7360']

Bandit distributions after 500 trials



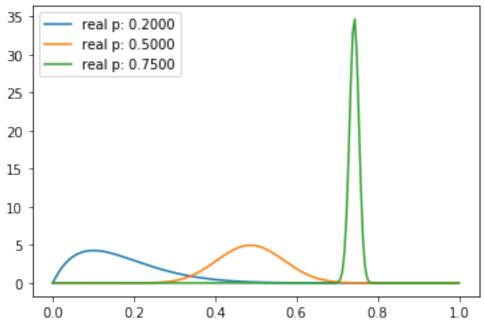
current samples: ['0.2483', '0.4353', '0.7042']

Bandit distributions after 1000 trials



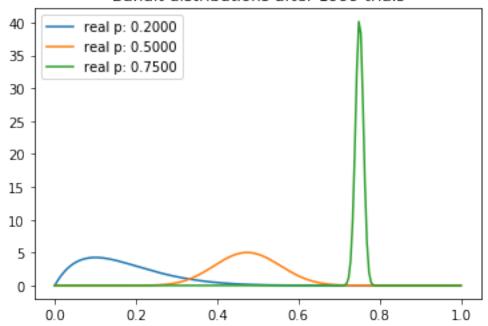
current samples: ['0.1081', '0.5063', '0.7486']





current samples: ['0.1646', '0.5434', '0.7477']

Bandit distributions after 1999 trials



[]:[