

there is not a linear correlation between  $x$  and  $y$ . But if we use the methods of this section, we get  $r_s = 1$  and critical values of  $\pm 0.648$ , suggesting that there is a correlation between  $x$  and  $y$ . *With rank correlation, we can sometimes detect relationships that are not linear.*

## using TECHNOLOGY

**STATDISK** Enter the sample data in columns of the data window. Select **Analysis** from the main menu bar, then select **Rank Correlation**. Select the two columns of data to be included, then click **Evaluate**. The STATDISK results include the exact value of the test statistic  $r_s$  and the critical value.

**MINITAB** Enter the paired data in columns C1 and C2. If the data are not already ranks, select **Data** and **Rank** to convert the data to ranks, then select **Stat**, followed by **Basic Statistics**, followed by **Correlation**. Minitab will display the exact value of the test statistic  $r_s$ . Although Minitab identifies it as the Pearson correlation coefficient described in Section 10-2, it is actually the Spearman correlation coefficient described in this section (because it is based on ranks). **Caution:** Ignore the  $P$ -value, because it is calculated using the methods of Chapter 10, not the methods of this section.

**EXCEL** Excel does not have a function that calculates the rank correlation coefficient from original sample values, but the exact value of the test statistic  $r_s$  can be found as follows. First replace each of the original sample values by its corresponding rank. Enter those ranks in columns A and B. Click on the **fx** function key located on the main menu bar. Select the function category **Statistical** and the function name **CORREL**, then click **OK**. In the dialog box, enter the cell range of values for  $x$ , such as A1:A10. Also enter the cell

range of values for  $y$ , such as B1:B10. Excel will display the exact value of the rank correlation coefficient  $r_s$ .

**XLSTAT** XLSTAT can be used by selecting **Correlation/Association tests**. For the type of test, select **Spearman**. The value of  $r_s$  will be listed in the table identified as "Correlation matrix (Spearman)," and if the value is displayed in a bold font, we can reject the claim of no correlation.

**TI-83/84 PLUS** If using a TI-83/84 Plus calculator or any other calculator with 2-variable statistics, you can find the exact value of  $r_s$  as follows: (1) Replace each sample value by its corresponding rank, then (2) calculate the value of the linear correlation coefficient  $r$  with the same procedures used in Section 10-2. Enter the paired ranks in lists L1 and L2, then press **STAT** and select **TESTS**. Using the option **LinRegTTest** will result in several displayed values, including the exact value of the rank correlation coefficient  $r_s$ . **Caution:** Ignore the  $P$ -value, because it is calculated using the methods of Chapter 10, not the methods of this section.

**STATCRUNCH** Replace each sample value by its corresponding rank, then use the same StatCrunch procedure described in Section 10-2. **Caution:** Ignore the  $P$ -value, because it is calculated using the methods of Chapter 10, not the methods of this section.

## 13-6 Basic Skills and Concepts

### Statistical Literacy and Critical Thinking

**1. Regression** If the methods of this section are used with paired sample data, and the conclusion is that there is sufficient evidence to support the claim of a correlation between the two variables, can we use the methods of Section 10-3 to find the regression equation that can be used for predictions? Why or why not?

**2. Level of Measurement** Which of the levels of measurement (nominal, ordinal, interval, ratio) describe data that cannot be used with the methods of rank correlation? Explain.

**3. Notation** What do  $r$ ,  $r_s$ ,  $\rho$ , and  $\rho_s$  denote? Why is the subscript  $s$  used? Does the subscript  $s$  represent the same standard deviation  $s$  introduced in Section 3-3?

**4. Efficiency** Refer to Table 13-2 in Section 13-1 and identify the efficiency of the rank correlation test. What does that value tell us about the test?