- **d.** Find  $P_{30}$ , the bone density test score separating the bottom 30% from the top 70%.
- e. If the mean bone density test score is found for 16 randomly selected subjects, find the probability that the mean is greater than 0.27.
- 2. Door Peephole Standing eye heights of women are normally distributed with a mean of 1516 mm and a standard deviation of 63 mm (based on anthropometric survey data from Gordon, Churchill, et al.).
  - a. A door peephole is placed at a height that is uncomfortable for women with standing eye heights greater than 1605 mm. What percentage of women will find that height uncomfortable?
  - **b.** In selecting the height of a door peephole, the architect wants its height to be suitable for the highest 99% of standing eye heights of women. What standing eye height of women separates the highest 99% of standing eye heights from the lowest 1%?
- 3. Window Placement Standing eye heights of men are normally distributed with a mean of 1634 mm and a standard deviation of 66 mm (based on anthropometric survey data from Gordon, Churchill, et al.).
  - a. If a window is positioned so that it is comfortable for men with standing eye heights greater than 1500 mm, what percentage of men will find that height comfortable?
  - b. A window is positioned to be comfortable for the lowest 95% of eye heights of men. What standing eye height of men separates the lowest 95% from the highest 5%?
  - 4. Sampling Distributions Scores on the ACT test have a distribution that is approximately normal with mean 21.1 and standard deviation 5.1. A sample of 80 ACT scores is randomly selected and the sample mean is computed.
  - a. Describe the distribution of such sample means.
  - b. What is the mean of all such sample means?
  - c. What is the standard deviation of all such sample means?

## 5. Unbiased Estimators

- a. What is an unbiased estimator?
- b. For the following statistics, identify those that are unbiased estimators: mean, median, range, variance, proportion.
- **c.** Determine whether the following statement is true or false: "The sample standard deviation is a biased estimator, but the bias is relatively small in large samples, so s is often used to estimate  $\sigma$ ."
- 6. Monorail and Airliner Doors The Mark VI monorail used at Disney World has doors with a height of 72 in. Heights of men are normally distributed with a mean of 69.5 in. and a standard deviation of 2.4 in. (based on Data Set 1 in Appendix B).
  - a. What percentage of adult men can fit through the doors without bending? Does the door design with a height of 72 in. appear to be adequate? Explain.
  - b. What doorway height would allow 99% of adult men to fit without bending?
- 7. Aircraft Safety Standards Under older Federal Aviation Administration rules, airlines were required to estimate the weight of a passenger as 185 lb. (That amount is for an adult traveling in winter, and it includes 20 lb of carry-on baggage.) Rules were revised to use an estimate of 195 lb. Men now have weights that are normally distributed with a mean of 182.9 lb and a standard deviation of 40.9 lb (based on Data Set 1 in Appendix B).
  - a. If 1 adult male is randomly selected and is assumed to have 20 lb of carry-on baggage, find the probability that his total weight is greater than 195 lb.