Solution

a. In the United States, Thanksgiving Day always falls on the fourth Thursday in November. It is therefore impossible for Thanksgiving to be on a Wednesday.
When an event is impossible, we say that its probability is 0.

> b. It is certain that Thanksgiving will be on a Thursday. When an event is certain to occur, we say that its probability is 1.

Because any event imaginable is impossible, certain, or somewhere in between, it follows that the mathematical probability of any event A is 0, 1, or a number between 0 and 1 (see Figure 4-2). That is, $0 \le P(A) \le 1$.

Figure 4-2 shows the possible values of probabilities and the more familiar and common expressions of likelihood.

Complementary Events

Sometimes we need to find the probability that an event A does not occur.

DEFINITION The **complement** of event A, denoted by \overline{A} , consists of all outcomes in which event A does *not* occur.

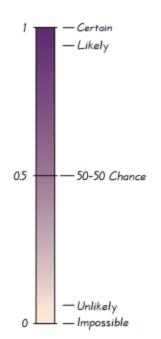


Figure 4-2 Possible Values for Probabilities

Example 9 Complement of Smoker

Results from Example 2 show that if we randomly select an adult in the United States, the probability of selecting a smoker is 0.200. Find the probability of randomly selecting an adult in the United States and getting someone who does *not* smoke.

Solution

Because 202 of the 1010 surveyed adults in the United States are smokers, it follows that the other 808 are not smokers, so

$$P(\text{not a smoker}) = \frac{808}{1010} = 0.800$$

Interpretation

The probability of randomly selecting an adult in the United States and getting someone who is *not* a smoker is 0.800.

Although it is difficult to develop a universal rule for rounding off probabilities, the following guide will apply to most problems in this text.

Rounding Off Probabilities

When expressing the value of a probability, either give the *exact* fraction or decimal or round off final decimal results to three significant digits. (*Suggestion:* When a probability is not a simple fraction such as 2/3 or 5/9, express it as a decimal so that the number can be better understood.) All digits in a number are significant except for the zeros that are included for proper placement of the decimal point.