## Hamming's Problem:

Given: a list of prime numbers.

Output: a list of numbers in increasing order such that a number is output if and only if its prime factors are contained in the given list of prime numbers.

Example: input is 3, 5, 11

output is 3, 5, 9, 11, 15, 25, 27, 33, 45, 55, 75, 81, 99, 121, ...

## What to do?

Consider all numbers from 1,2,3... and check for prime factors

Too Slow!!!

```
9, 15, 27, 33, 45, 75, 81, 99, ....
        5, 11, 25, 55, 125. ...
          3*(3, 5, 9, 11, 15, 25, 27, 33, ....)
      5, 11, 25, 55, 125. ...
int *hamming (int *primes) {
  if (primes == NULL) return NULL;
  return concat(first(primes), merge(first(primes)*hamming(primes),
                                          hamming(rest(primes)));
first(primes) = first number in list 'primes'
rest(primes) = list 'primes' with the first number removed
merge(list-1,list-2) = increasing list of numbers taken from increasing lists 'list-1' and 'list-2'
```

concat(n, list-1) = add the token 'n' to the list 'list-1'

## **Bad News!**

The call hamming(primes) requires calling hamming(primes)
So no output is ever seen!

## What to do?

Suspend the calls to hamming (primes) using a priority list!
We can implement a priority list using a heap.

1 [3,5,11]

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