

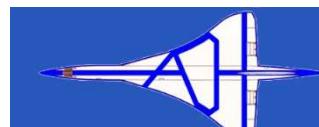
Some aspects of

Aircraft Design

mainly from the Loads and Structures point of view

by

Danny Heaton

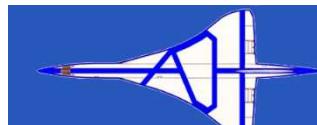


Aircraft Design

For Load Calculations (certainly for Certification of a Large Aircraft), we need to have some knowledge of

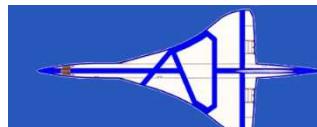
- Aircraft Weights
- Aerodynamic Data
- Design Speeds
- Stiffness Data
- Systems Data (Fuel, EFCS, Hydraulics, Airconditioning, Galleys Toilets etc)
- Geometry
- Mass Data
- V-n Information
- Engine Thrust/Power

Initially, it will be a TOP down approach evolving into a BOTTOM up situation



Some Initial Remarks....

- Remember that aircraft design is a “open end” problem: multiple solutions do exist!
- This is by no means a complete design exercise. It only covers a first preliminary design iteration!
- All the dimensions, weights and performance metrics associated to the individual aircraft configuration are meant to be representative only!
- To cover various configurations and sizes, the following aircraft have been used, they may not all be represented in this note.
They are A320 (150 seats), ATR72-600 (72 seats),
BAe Jetstream 41 (30 seats), Britten-Norman Islander (10 seats)
and Rans S6 Coyote (2 seats)



Aircraft Design

So how or where do we start

CS-25

This regulation applies to aircraft with a TOW >12500lb(5700kg)

For the Design Project, the specification might include

Payload 150 pax @ 100kg

Range 3000 nm

Design Cruising Speed

$$M_{CR} = 0.75 \text{ to } 0.85$$

TOFL/LFL ??

Approach Speed 130 to 140 kts

(Defines V_s)

$$M_{NO} = M_{CR} + 0.04$$

CS-VLA

This regulation has some limits

AUW = 750 kg

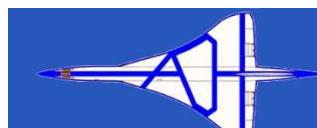
VS(LDG)not to exceed 45 kts

Not more than 2 seats

Max. Weight of one occupant = 86 kg

We might add a flight duration limit of say 3 hours – this will give a fuel load

Note: Latest issue of CS-25 asks for rational analysis (e.g. time histories), at this stage of the project, suggest using earlier issues of CS-25 or CS-23 Amdt 4



Aircraft Design

The starting point is to make some “informed” guesses on the important design parameters

MTOW

OWE

Fuel (Mission)

Wing Area (and may be Aspect Ratio and Sweep)

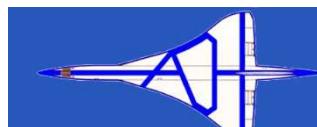
Max $C_{L_{TO}}$ and $C_{L_{LDG}}$

TOW = OWE + Payload + Fuel (Mission + Reserves)

LW = OWE + Payload + Fuel (Reserves)

$C_{L_{MAX}}$ is a function of Flap type, Flap Angle,
 c_f/c , b_f/b and Leading Edge devices

$V_{APP} = 1.3 \text{ times } V_{SLDG}$



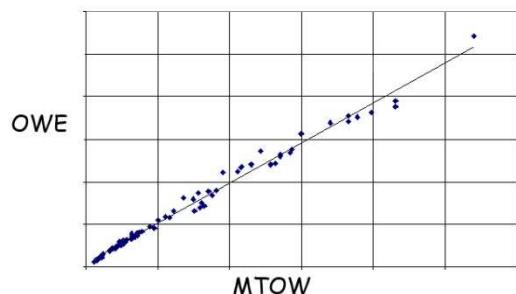
Aircraft Design

Initial aircraft weights can be derived as follows
for our example of 150 pax for 3000 nm

$$\text{TOW} = \text{ZFW} + \text{FUEL} = \text{OWE} + \text{Payload} + \text{Fuel}$$

OWE

OWE is a function of TOW
from Jenkinson et al



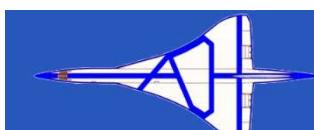
$$\text{OWE} = 0.47\text{MTOW} + 4800\text{kg} \quad (\text{approx})$$

Pax

$150 \times 100 = 15000\text{kg}$
made up of
77kg pax (CS25.785)
5kg Hand Baggage
(in Cabin)
18kg Baggage in Hold

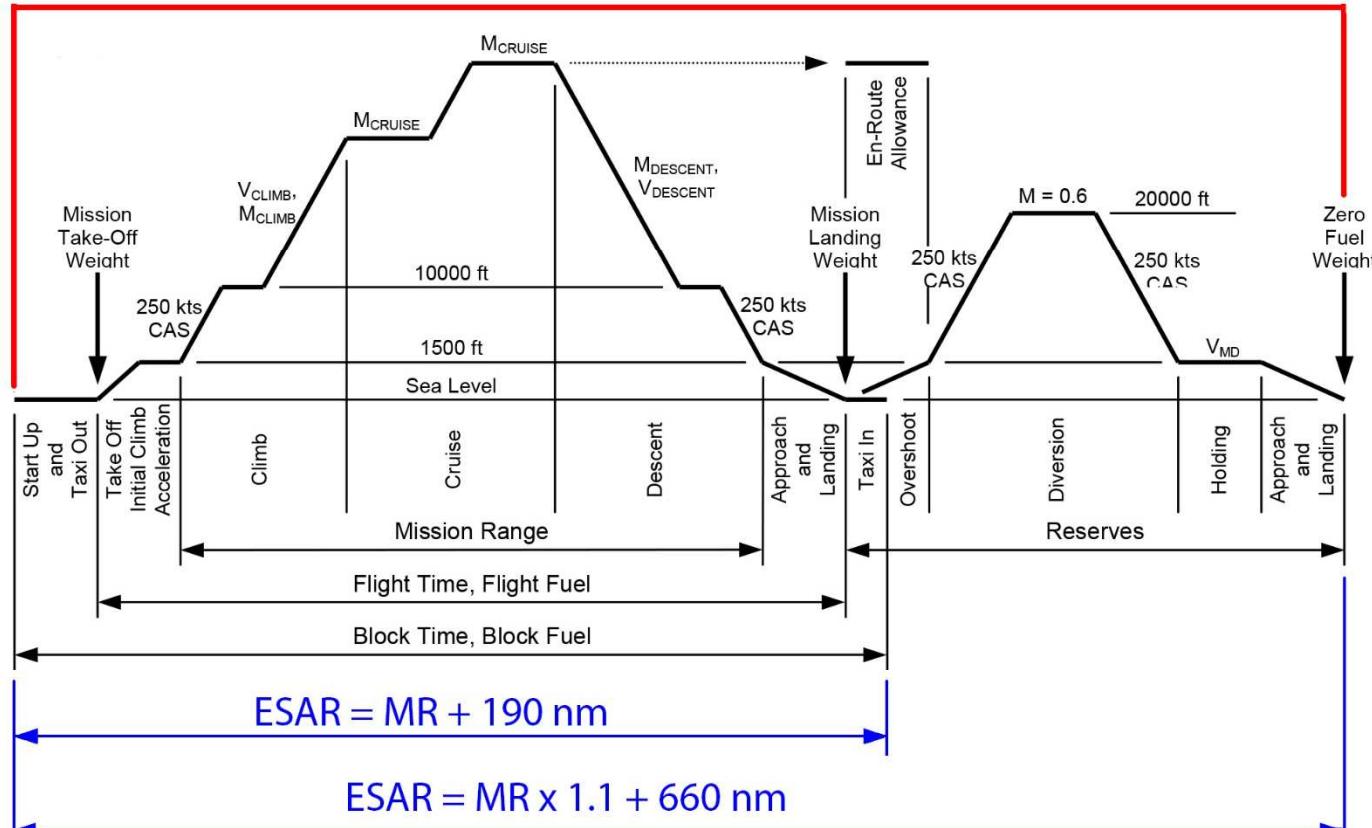
Fuel

Mission + Reserve
from Breguet Range Eqn
which involves
Range
L/D
Speed (cruise)
Engine sfc



Typical International Flight Profile

ESAR Mission Profile

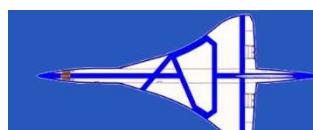


ESAR -- Equivalent Still Air Range

MR -- Mission Range

L/D is approx 17 to 20

sfc is approx 0.45 to 0.59 depending on engine technology (includes BPR)



Aircraft Design

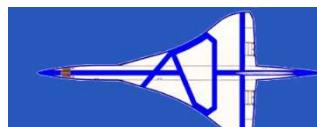
For a Conventional Aircraft layout or configuration,
the Fuselage is usually sized by the payload.

For a passenger Aircraft, the number of pax is the main driver which in turn will influence Cabin Width (Narrow Body or Wide Body or even an A380 style).

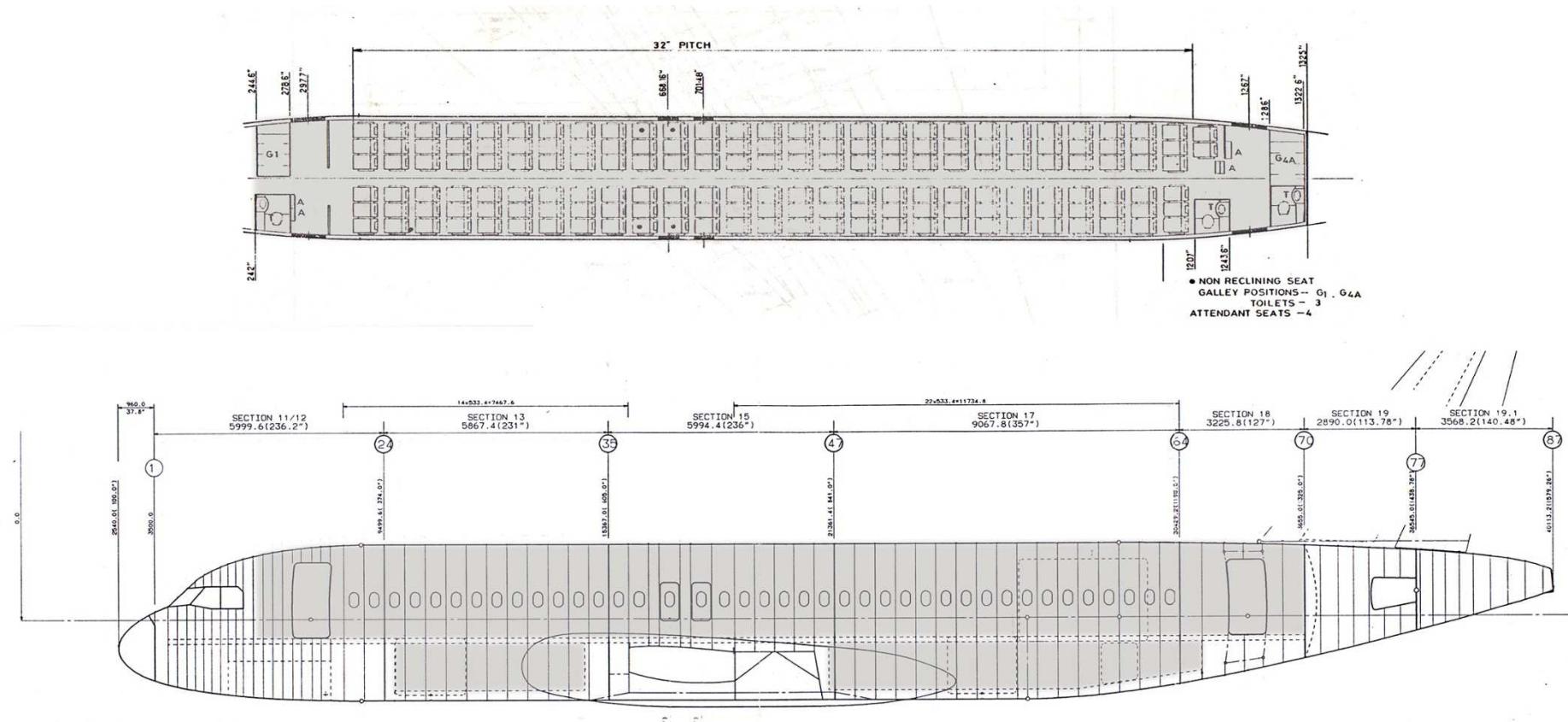
Need to provide Toilets, Galleys etc

Number of Emergency Exits (size and access to them)

Cabin Crew Seats (along with Flight Crew, these are usually counted as part of the OWE from a Mass point of view)



Typical Fuselage Layout



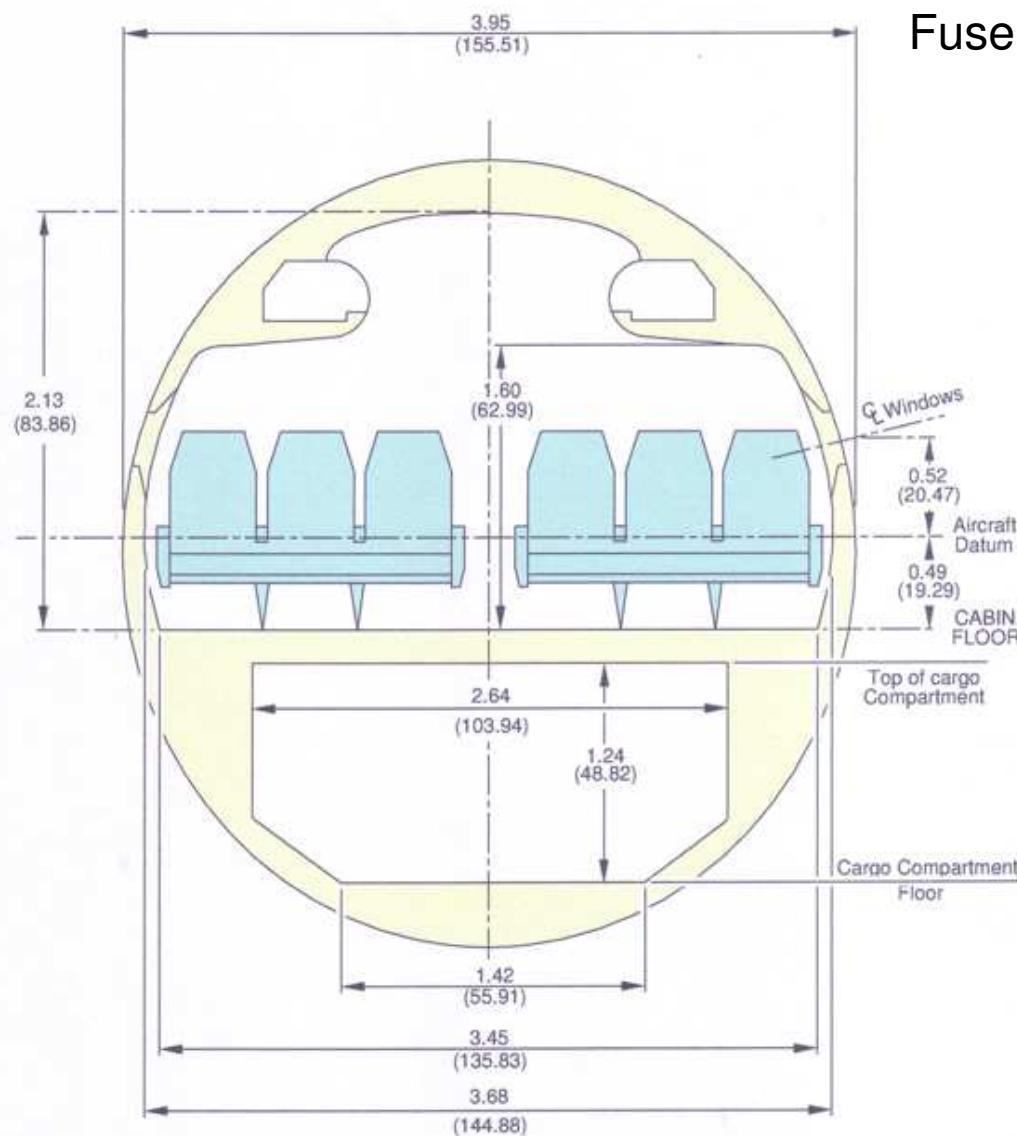
Fuselage Length is approximately 2.5 times Fuselage Width plus Cabin Length

Cabin Length is Flight Deck Door to Pressure Bulkhead

A320

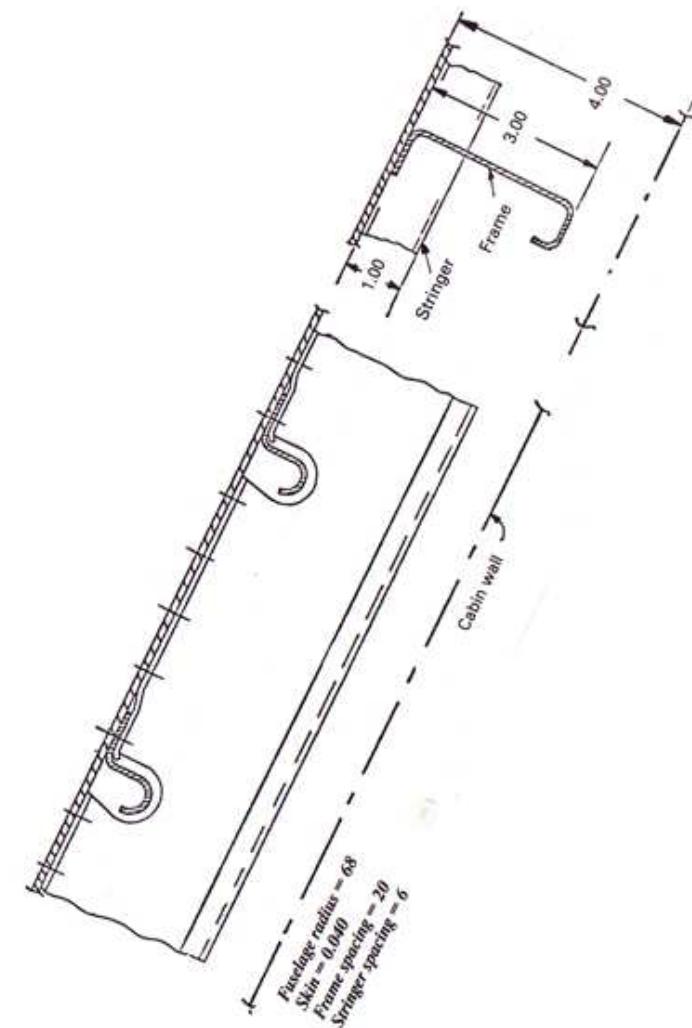


Fuselage Cross-Section and Frame Depth



A320

NOTE: DIMENSIONS m (in)



Aircraft Design

Still staying with a Conventional Aircraft,
the Wing is usually sized by the Performance needs like
Cruise, Take-off and Landing and Fuel Capacity

As a guide, based on the Fuel required (Mission plus Reserves),
Wing Area correlates as

$$S = ((C \times \text{Fuel})/16)^{2/3} \quad \text{fuel in kg} \quad \text{or}$$

$$S = ((C \times \text{Fuel})/20)^{2/3} \quad \text{fuel in litres}$$

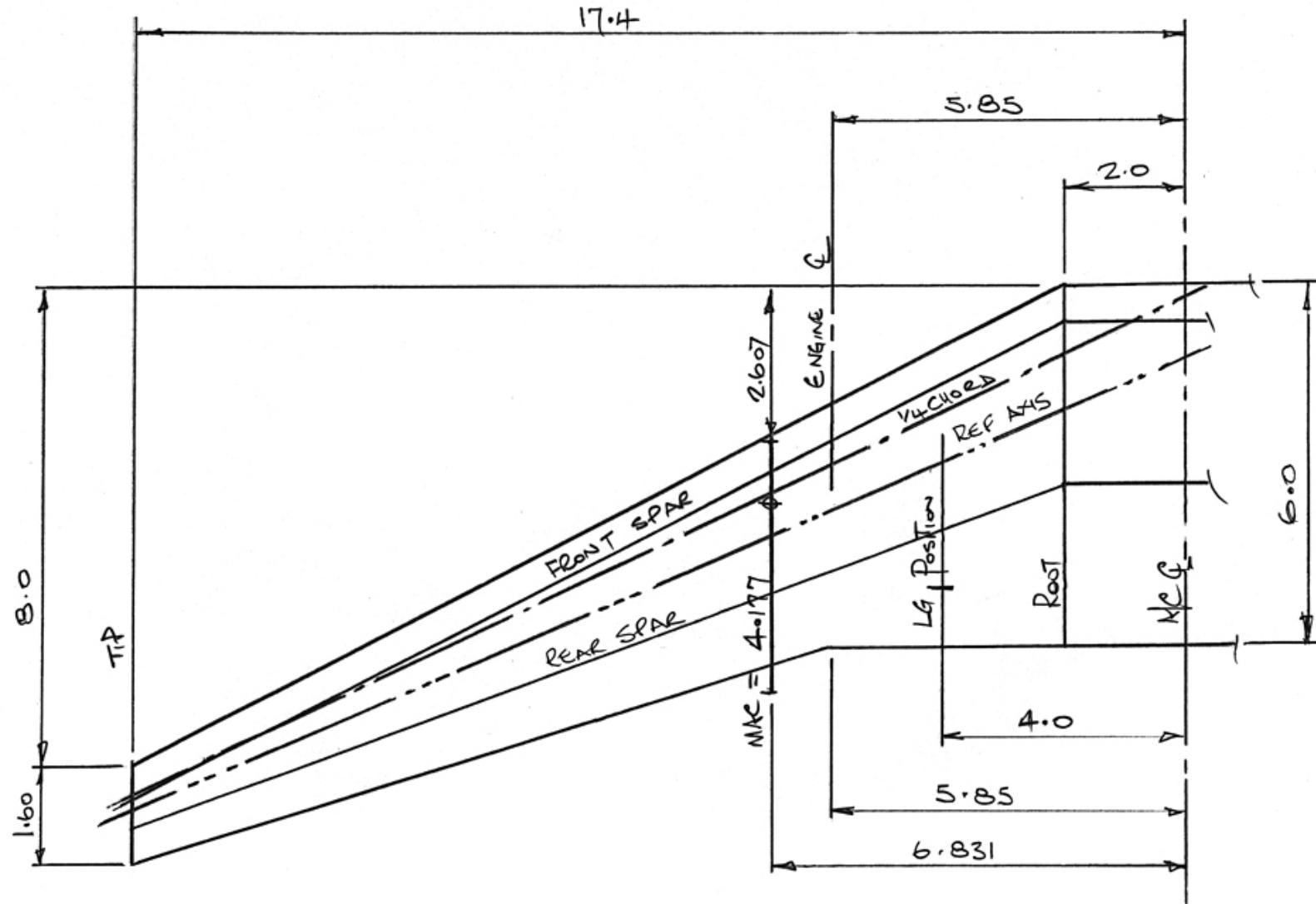
Where S is Wing Area (m^2)

C = 1.0 for Wing and Centre Tanks

C = 1.5 for Wing only (Dry Centre Tank)

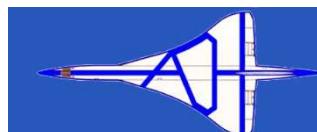
and a Fuel Density of 800kg/m^3 is implied





DIMENSIONS in metres

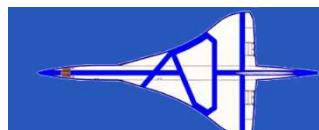
BASIC WING GEOMETRY



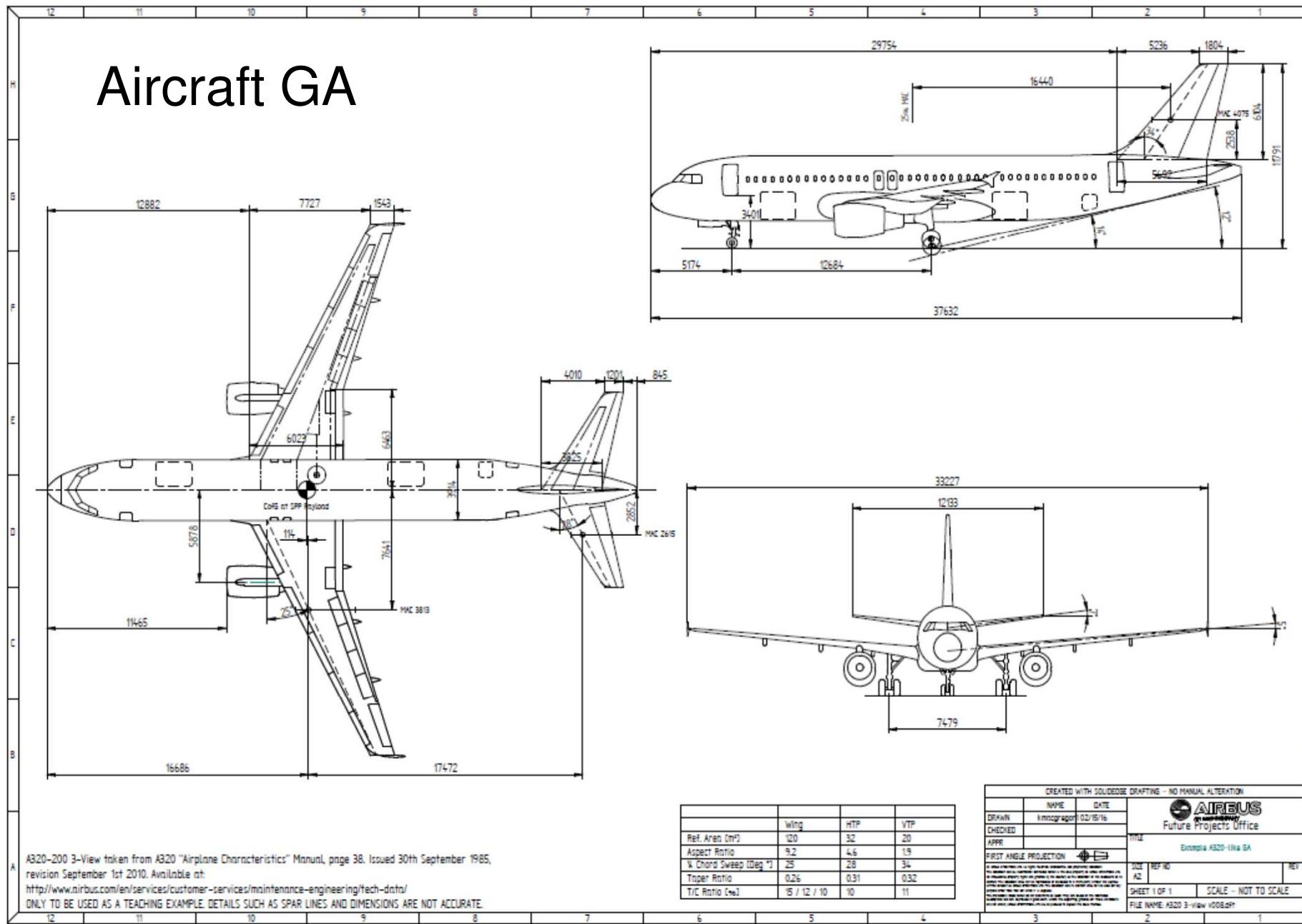
Spar Positions

Position		F/S	R/S
Root	A320	0.101	0.560
	Mid Span	0.143	0.634
	Tip	0.348	0.609
Root	A310	0.147	0.526
	Mid Span	0.201	0.657
	Tip	0.323	0.605
Root	A330	0.117	0.614
	Mid Span	0.154	0.654
	Tip	0.263	0.665
Root	A340-600	0.100	0.659
	Mid Span	0.152	0.696
	Tip	0.211	0.737
Root	A380	0.190	0.704
	Mid Span	0.122	0.671
	Tip	0.176	0.559
Root	A400M	0.150	0.625
	Mid Span	0.150	0.625
	Tip	0.150	0.625

Note; Values are fractions of local chord
These values have been derived by scaling
small scale drawings
They are some indication of what can occur



Aircraft GA



Typical Supercritical Wing Section

Wing sections on the latest commercial airliners use what is known as supercritical sections. These are usually developed by the wing designer to meet the needs of the particular aircraft specification.

The wing design is a 3 dimensional exercise ending with a wing section that can change all along the span from root to tip. Equally the thickness will vary but in a smooth manner, however t/c will probably have kinks where there are kinks in the planform.

The wing section given has been manually digitised from a very small drawing.

The process was to define a basic symmetric profile and a mean camber line following the general principles of the theory as given in 'Theory of Wing Sections' by Ira H. Abbott and Albert E. Von Doenhoff in Chapter 6 (in particular paragraphs 6.4 and 6.6)

The constants in the equations were derived using the trend line in Microsoft Excel.

The basic thickness and the mean line are defined by the following equation

$$y = t (a_0 \sqrt{x} + a_1 x + a_2 x^2 - a_3 x^3 + a_4 x^4)$$

where

y is the vertical ordinate

x is the distance along the chord line (maximum value = 1.0 for a non-dimensional profile)

t is the thickness (0.1 is equivalent to a t/c = 10%)

a_0, a_1, a_2, a_3, a_4 are constants derived from the trend line fit

Note: for the mean line $t = 1$



Typical Supercritical Wing Section

Values for the 'a' constants are

	basic	mean line
a_0	1.529035	0.0
a_1	-0.788940	0.004714
a_2	-1.449138	-0.013111
a_3	1.263147	0.119557
a_4	-0.554104	-0.111160

Leading Edge Radius is given by $(a_0^2 \times t^2)/2$

Upper and lower profiles are then derived by

$$y_u = y_m + y_b$$

$$y_l = y_m - y_b$$

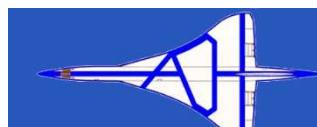
The method given in Abbott & Doenhoff for combining the base section and the mean line involves the local slope of the mean line (see equation 6.1), this was ignored in the derivation of the profiles.

Note that

$\cos 5^\circ$ is 0.9962

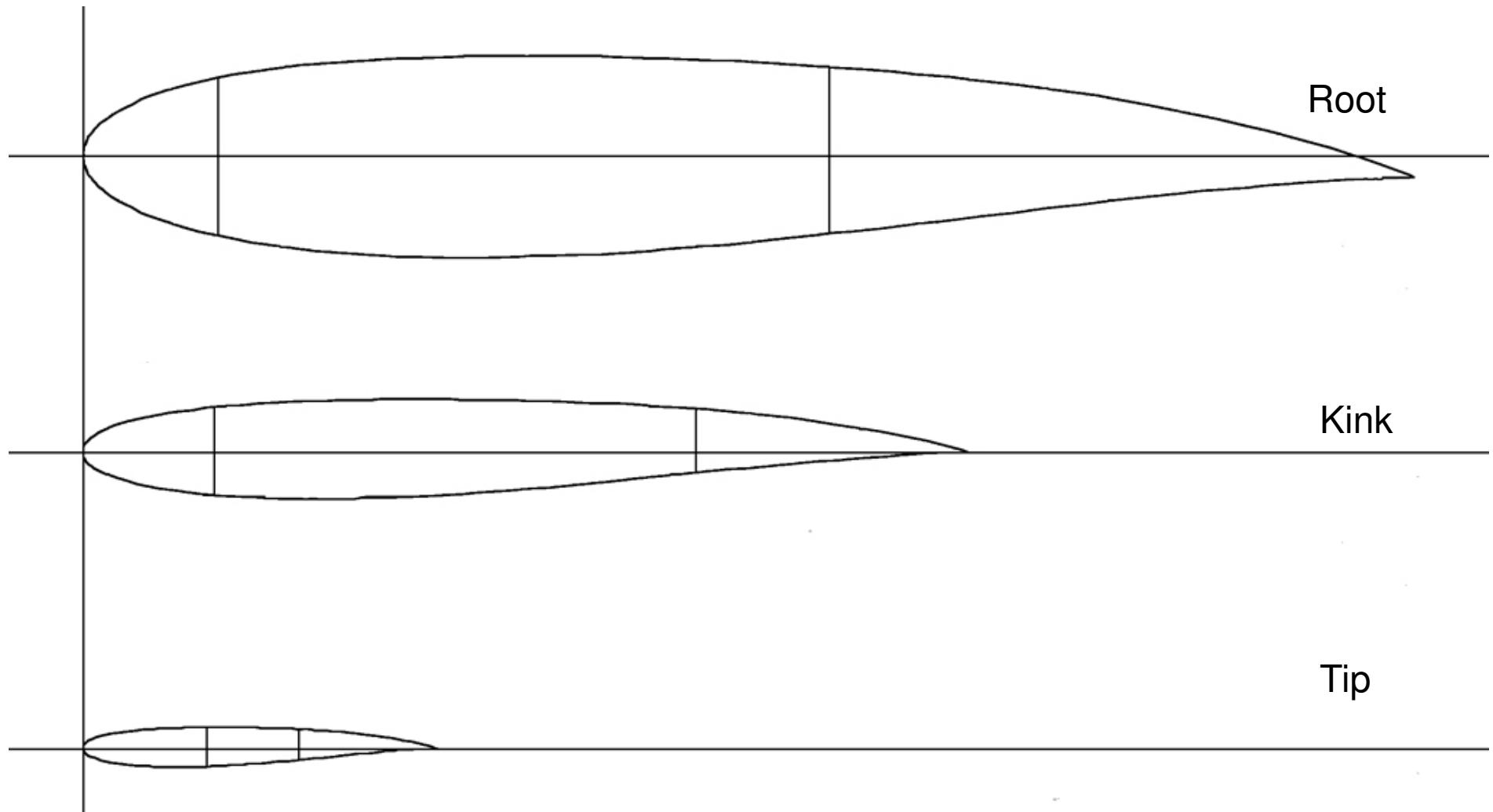
$\sin 5^\circ$ is 0.0872

$\tan 5^\circ$ is 0.0875

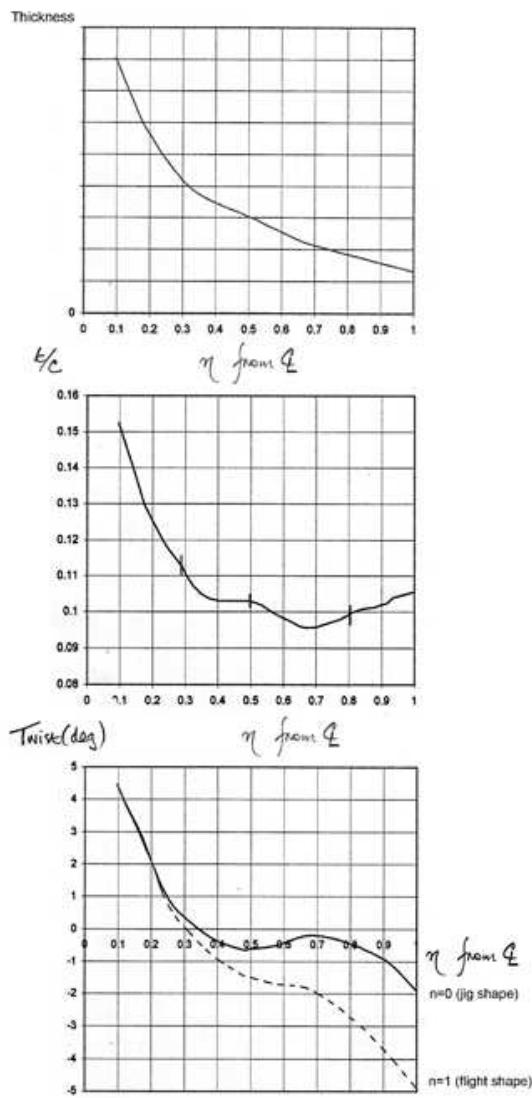


Wing Sections

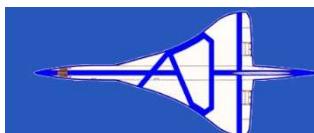
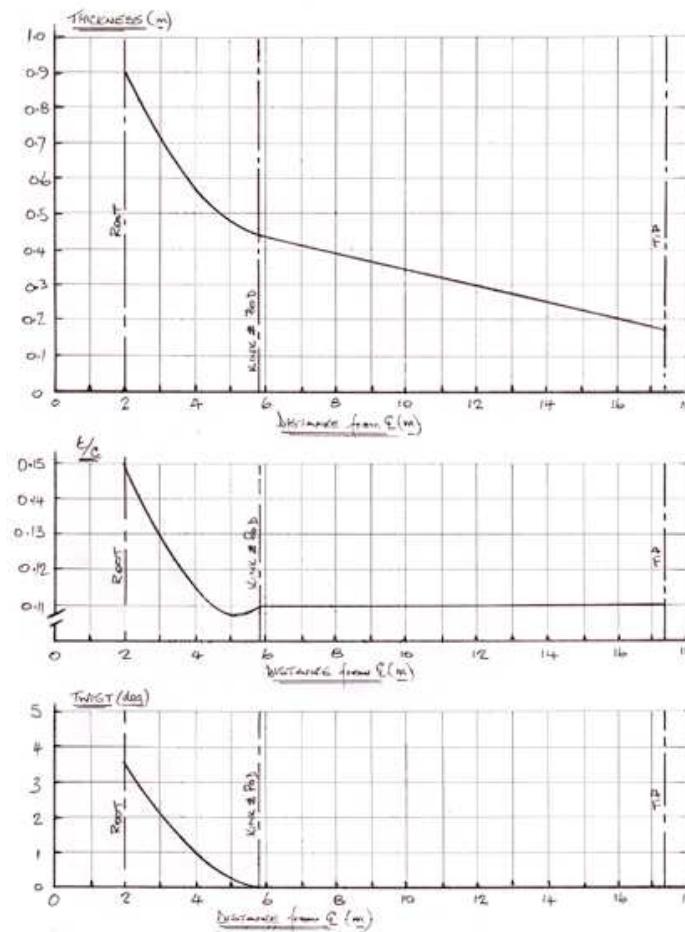
Shows Front and Rear Spar positions



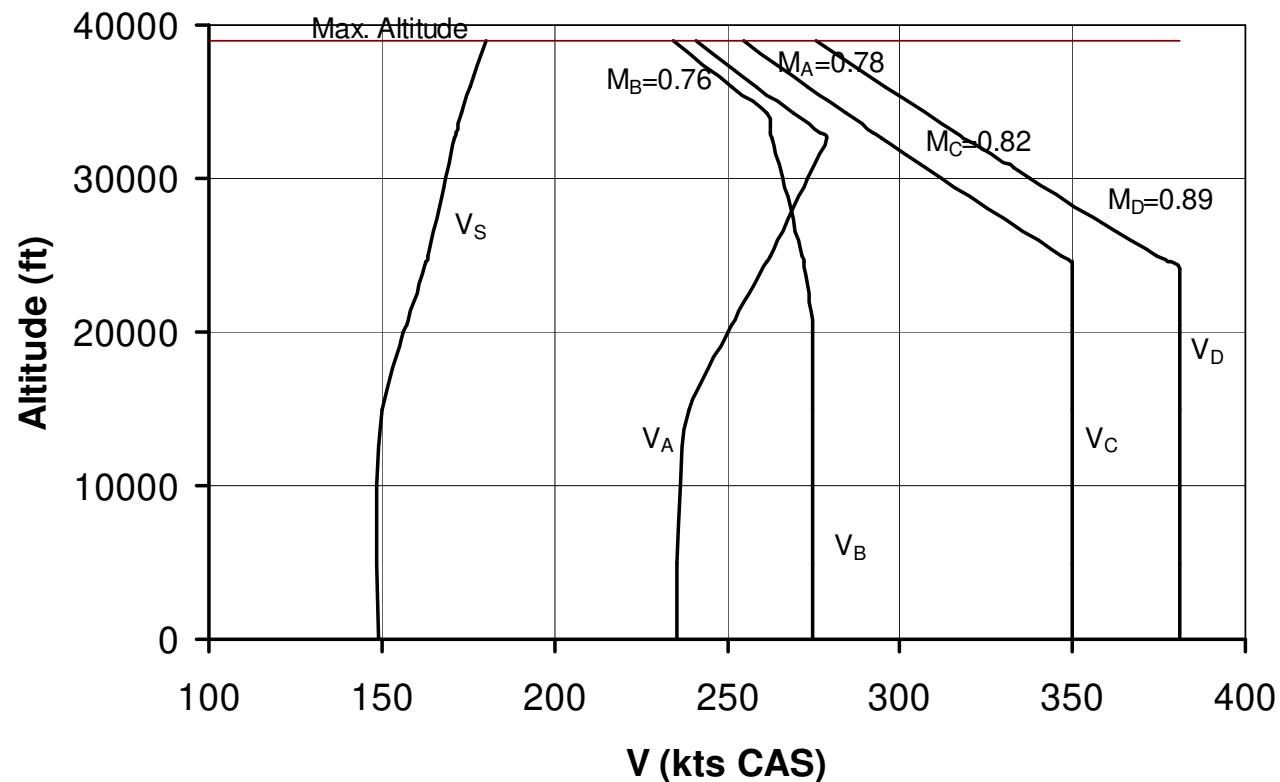
Modern Airliner



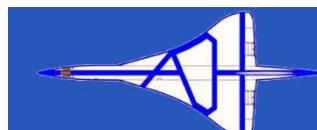
Wing Design Exercise



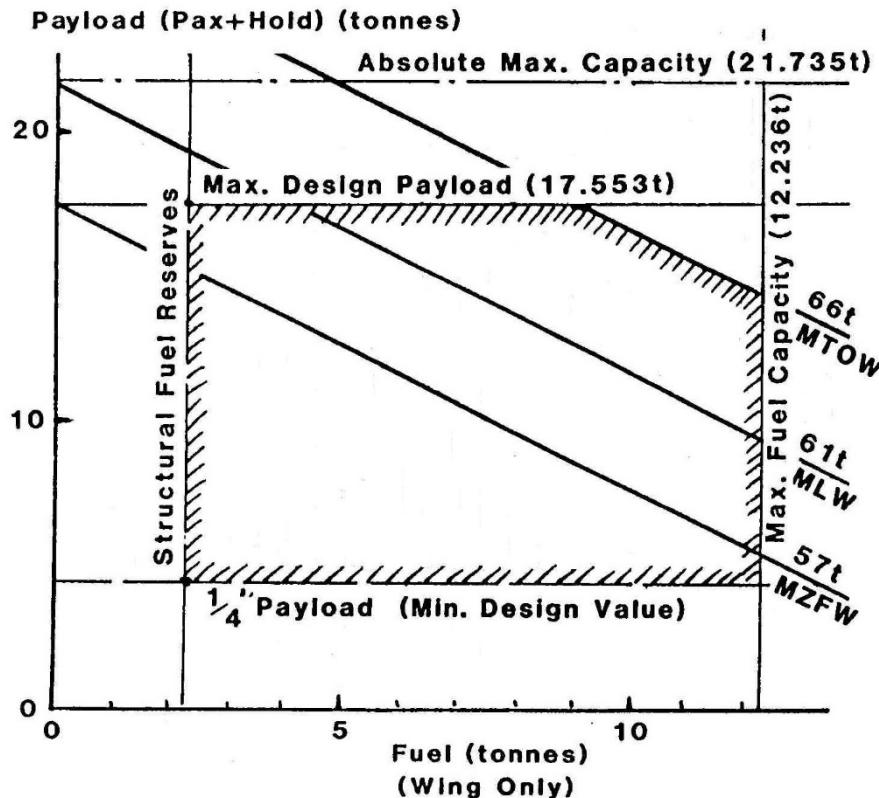
Design Speeds



A320



PAYOUT - FUEL LOADING

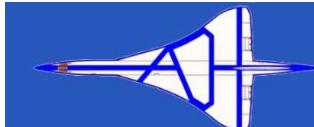
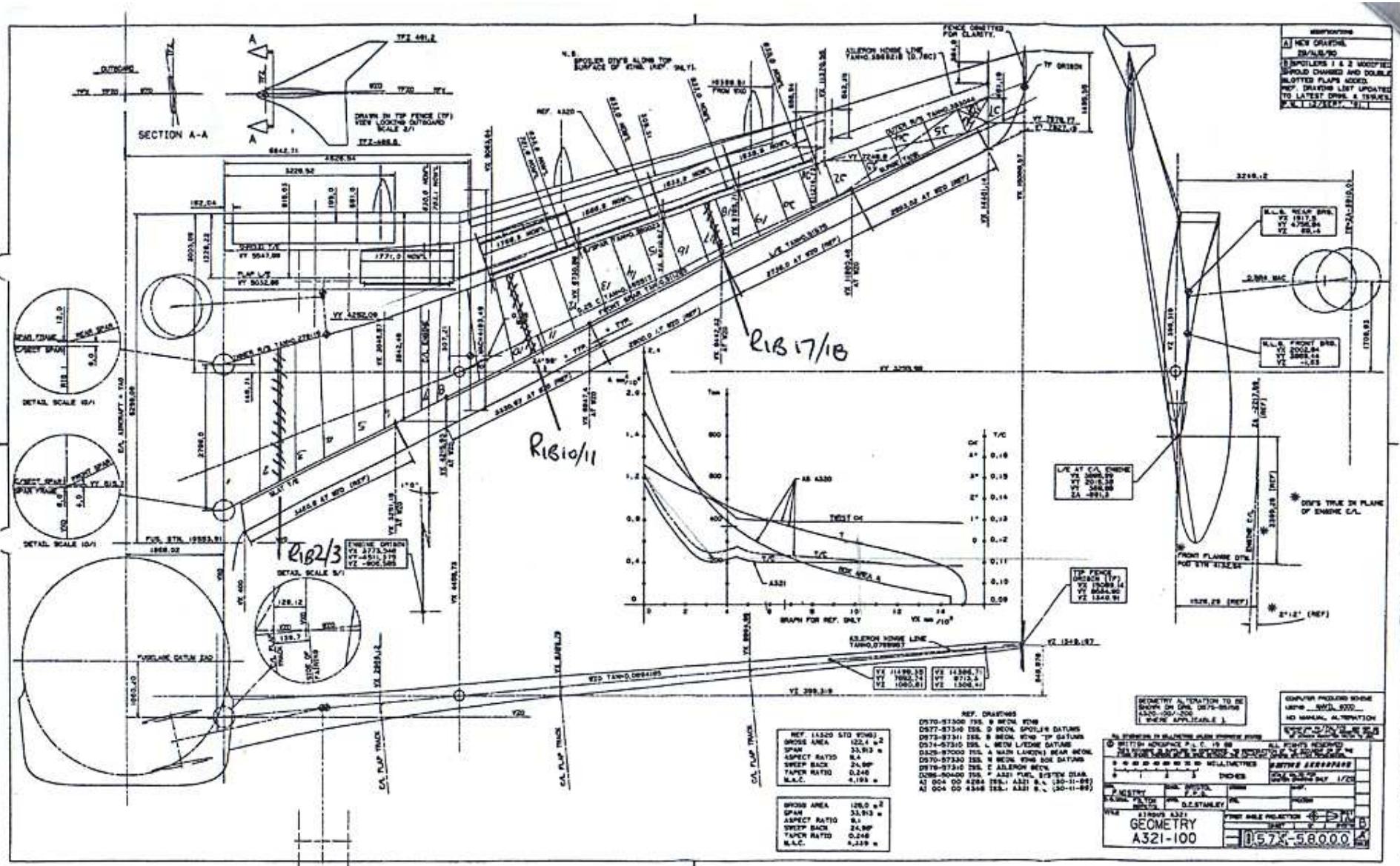


NOTES

- Passengers (75kg) and Baggage (15kg)
 $165 \times (75 + 15) = 14850 \text{ kg}$
 Max Hold Capacity = 9435 kg
- Structural Fuel Reserves - Fuel required to climb to 10000 ft and then cruise at speed appropriate to that for maximum range for 45 mins
- Payload loaded from front or back to give CG range
- Payload for Fatigue Mission is between 65% and 80% of maximum Design Payload

A320





MISSION COMPARISON

	MAXIMUM DESIGN WEIGHTS	DESIGN MISSION	FATIGUE MISSION
OWE (kg)	39447	39447	39447
Payload (kg)	17553	15580	11410
ZFW (kg)	57000	55027	50857
Fuel (reserve) (kg)	4000	3109	2543
Landing Weight (kg)	61000	58136	53400
Fuel (block) (kg)	5000	7864	2600
TOW (kg)	66000	66000	56000
Fuel (max) (kg)	12200		
Range (nm)		1500	370
Cruise Altitude (ft)		35000	31000
Cruise Mach No		0.76	0.78
Flight Time (mins)		219	60
Block Time (mins)		233	74

A320



Mass Configurations

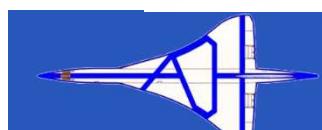
	AUW	Fuel	Payload	
Mission 1	66000	10973	15580	Single class 164 pax @ 95kg
Mission 2	66000	12303	14250	2 class 150 pax @ 95kg (Wing Tanks Full)
Take-off 1	66000	9000	17553	Max Payload
Take-off 2	66000	12303	14250	Max Fuel
Landing 1	61000	4000	17553	Max Payload
Landing 2	61000	7130	14423	High Fuel load
Flight 1	59250	2250	17553	Max P/L + Str Res
Flight 2	46085	2250	4388	quarter P/L + Str Res
Flight 3	64130	7143	17553	Max P/L less fuel burn to altitude
Flight 4	57000	0	17553	Zero Fuel, Max P/L
Flight 5	52002	7130	5425	Not sure of the reasoning for this case
Flight 6	43835	0	4388	Zero Fuel, quarter P/L
Flight 7	40447	1000	0	Min Fuel for ferry flight
Flight 8	64130	10433	14250	Max Fuel less fuel burn to altitude

Masses in kg

OWE= 39447kg

A320

Each case can be loaded from front or back giving rise to forward CG or Aft CG

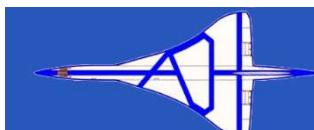


OWE Weight Breakdown

MTOW = 66000kg

A320

		Fuselage	Wing C/S	Wing	Pylon	Engine	Fin	Tailplane		TOTAL
Structure	Wing		1020	7569						8589
	Fuselage	8140	4							8144
	Tailplane						606			606
	Fin					429				429
	MLG	1153		790						1943
	NLG	324								324
	Pylon			896						896
	Total	9617	1024	8359	896	0	429	606		20931
Power Unit	Engine					6818				6818
	Bleed Air	72		54	94					220
	Controls	13		3	5					21
	Fuel System	16	18	190	20					244
	Total	101	18	247	119	6818	0	0		7303
Systems	APU	213								213
	Hyd Gen	366		59	62					487
	Hyd Dist	304		107	12		12	12		447
	Air Cond	660								660
	De-Ice			39						39
	Fire Pre	31		5	70					106
	Flt Control	340		328			49	32		749
	Instruments	108								108
	Auto FS	130					13			143
	Nav	458					7			465
	Com	161		2						163
	Elec Gen	341		18	12					371
	Elec Dist	986	3	100	56			4		1149
	Total	4098	3	658	212	0	81	48		5100
Furnishing	Furn	2418								2418
	Oxygen	144								144
	Light	207		19						226
	Water	88								88
	Total	2857	0	19	0	0	0	0		2876
MWE		16673	1045	9283	1227	6818	510	654		36210
Operators	Items	3087		73		77				3237
OWE		19760	1045	9356	1227	6895	510	654		39447



Typical Wing Weight Breakdown

The following data may be used to establish the potential weight savings that might be obtained using modern materials in the construction of a medium sized civil transport wing.

1 Datum wing.

The mass of a typical civil transport wing around the size of say an A310 is in the range 80~90 kg/m². The materials used in a typical wing of that era are shown on Fig. 57 of the Airworthiness and Loads Lecture.

2 Overall mass breakdown

The wing mass can be typically split as follows :

Total upper skins (inc. centre section)	17.5	%
Total lower skins (inc. centre section)	22.0	%
Total spars (inc. centre section)	12.0	%
Total ribs (inc. centre section)	8.0	%
Fixed LE	6.0	%
Slats	6.0	%
Fixed TE	3.5	%
Flap surfaces & fairings	8.0	%
Flap tracks etc.	12.5	%
U/C support structure	2.5	%
Engine mounting reinforcement	2.0	%
Total	100.0	%

3 Typical unit masses

Outside the main wing torque box, typical structural masses for aircraft in this category are :

Fixed LE 20~30 kg/m²

Moveable LE 30~38 kg/m²

Fixed TE (composite) 10 kg/m²

Flap system (total surfaces supports & fairings) 55~65 kg/m² flap area

Spoilers (composite) 12 kg/m²

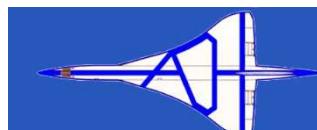
Ailerons (composite) 24 kg/m²



Typical Fuselage Structural Weight Breakdown

This data is based on civil passenger aircraft with the Engines mounted on the wing and the Main Landing Gear pintle point on the wing (typically A320, A310, B737 etc)

Skin & Stringers	33	%
Frames	8	%
Access Doors & Apertures	10	%
Cabin Windows	3.5	%
Nose & Tail Fairings	1.5	%
NLG Installation	3	%
MLG Installation	3	%
Cabin Floor Structure And Panels	16	%
Freight/baggage holds Including Floor)	6	%
Tail Unit Attacment Structure	3.5	%
Windscreen (Frame and Glazings)	2	%
Pressure Bulkheads	2.5	%
Fuselage/Wing Attachment	5	%
Paint/Sealant	1.5	%
APU Attachment	0.3	%
Miscellaneous/Special Features	1.2	%
TOTAL	100	%



Suggested Loads Cases that you should be aware of

Loads Cases Aircraft Design Project

The list of cases that follows might not give the worst case for the structure but should be within about 5%. We are looking for understanding of the principles involved and getting close to the worst case.

Don't forget to apply the appropriate Ultimate Factor (use 1.5 unless specified)

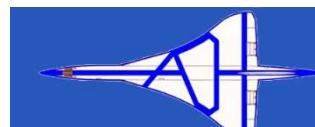
Wing Design Cases (Flight)

Consider $n = 2.5g$, $1.0g$ and $-1.0g$ trimmed Manoeuvres with full wing fuel at MTOW. This is not probably the worst case but will give a good indication and save a lot of calculations for varying fuel and payload states.

Assume Gust cases will be equal to or less than Manoeuvres due to the use of Load Alleviation devices.

Fuselage Design Cases (Flight)

Use Mission Payload uniformly distributed (will give a middling *CG*). Consider $n = 2.5g$, $1.0g$ and $-1.0g$ trimmed Manoeuvres. Worst Case likely to be a Gust with Max Payload at a low fuel load or low payload at forward or aft *CG* with low fuel.



Suggested Loads Cases that you should be aware of

Wing Design Cases (Ground)

Depends on aircraft configuration and time available whether they are considered for the Design Project

Fuselage Design Cases (Ground)

The landing cases can give rise to some large vertical g's in dynamic conditions. One way of assessing the loads is as follows. Landing Case is 1.0g flight condition prior to impact plus the increment due to impact (Use next fig for g along the fuselage - it already includes the 1.0g for trimmed flight).

Tailplane

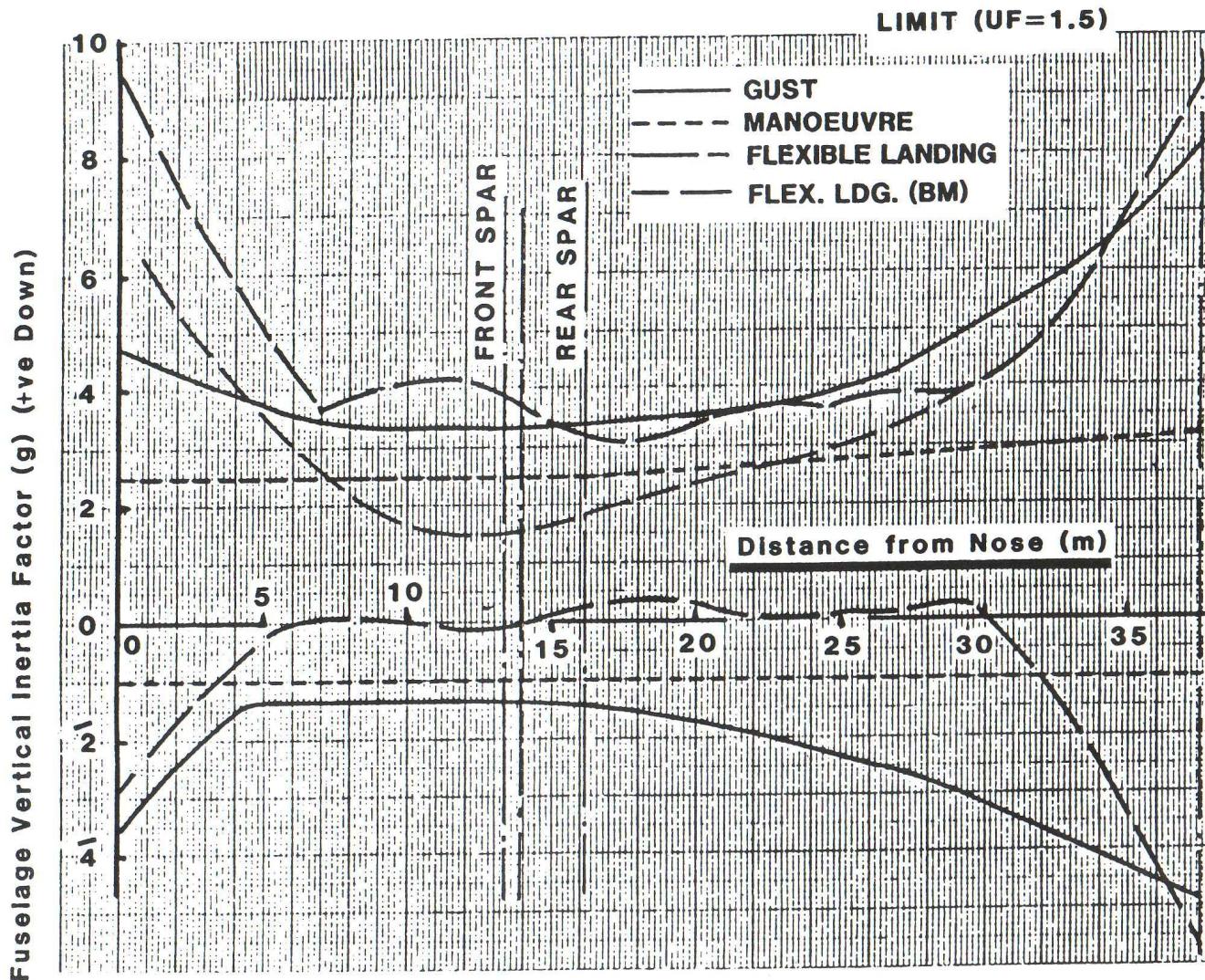
The loads on the tailplane result from the Trimmed state (2.5g, 1.0g and -1.0g), Pitching Manoeuvres and Vertical Gusts (down gust will be critical).

Fin

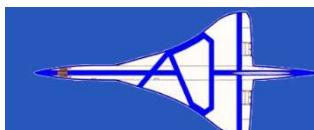
Critical cases are Lateral Gust and Rudder Manoeuvre. While Engine Failure might size the fin and rudder in terms of area, it is not normally a critical strength case.



Fuselage Vertical Inertia Factor



A320



Suggested Loads Cases that you should be aware of

Landing Gear Design Cases

Critical cases are those that give the maximum fore/aft, side and vertical loads (plus moment cases for torque links and steering).

Don't forget to derive and assess the attachment loads of the landing gear to the wing or fuselage.

For the MLG these are

- Take-off
- Braked Roll (max. drag load)
- Zmax
- Spring Back (max. forward load)
- Turn Case (max.side load)
- Pivot Case (max. moment for torque links)

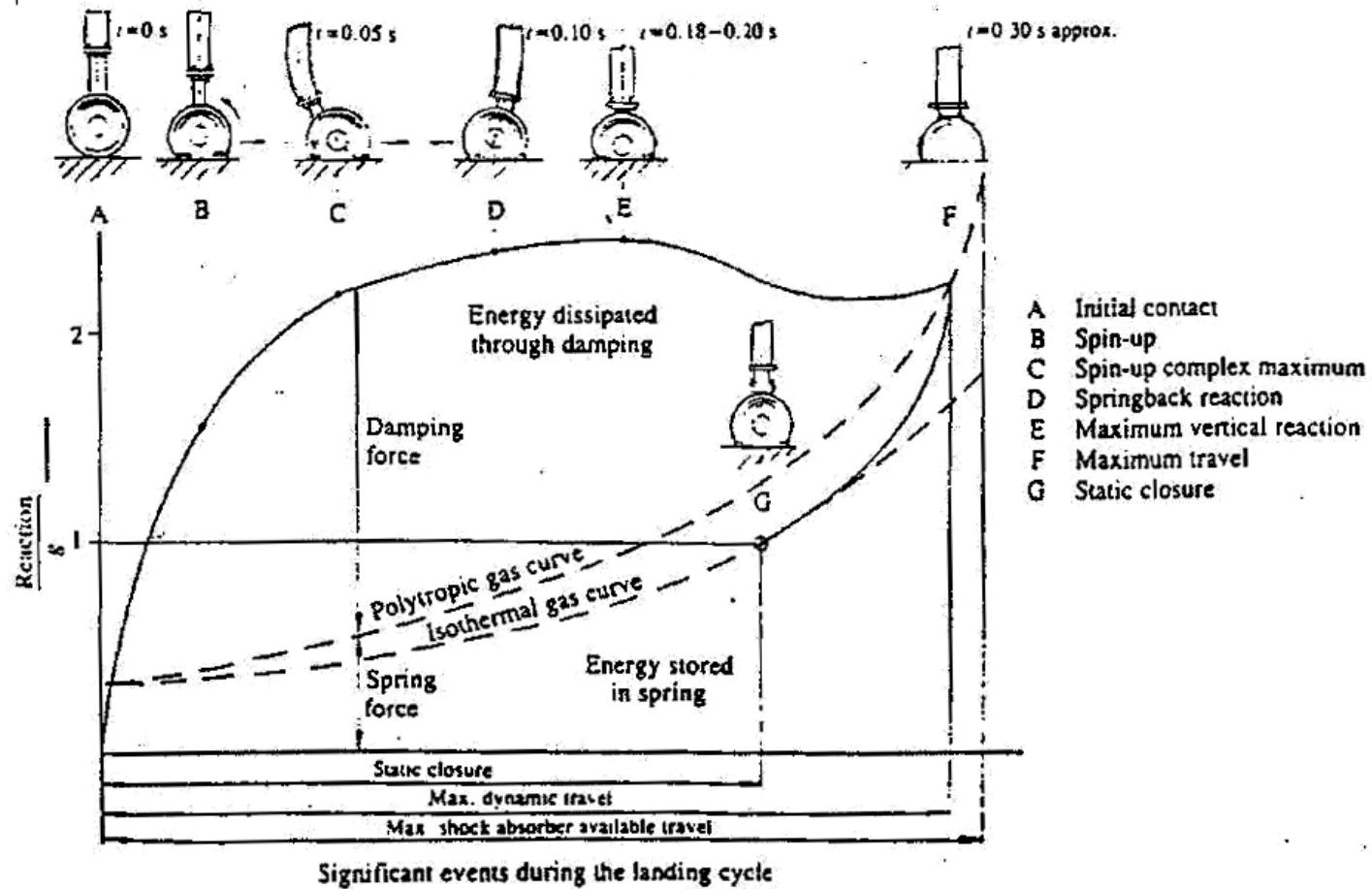
Note that a 60/40 distribution is used between tyre/wheels (see CS23.511 Amdt 4), CS25.511 has a more rational analysis

For the NLG these are

- Braked Roll (No drag Load)
- Towing (consider push and pull)
- Nose Wheel Yaw (only consider para(a)of CS 25.499, that is 1g vertical and 0.8*Z laterally)
- Zmax

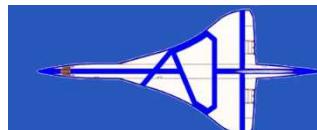
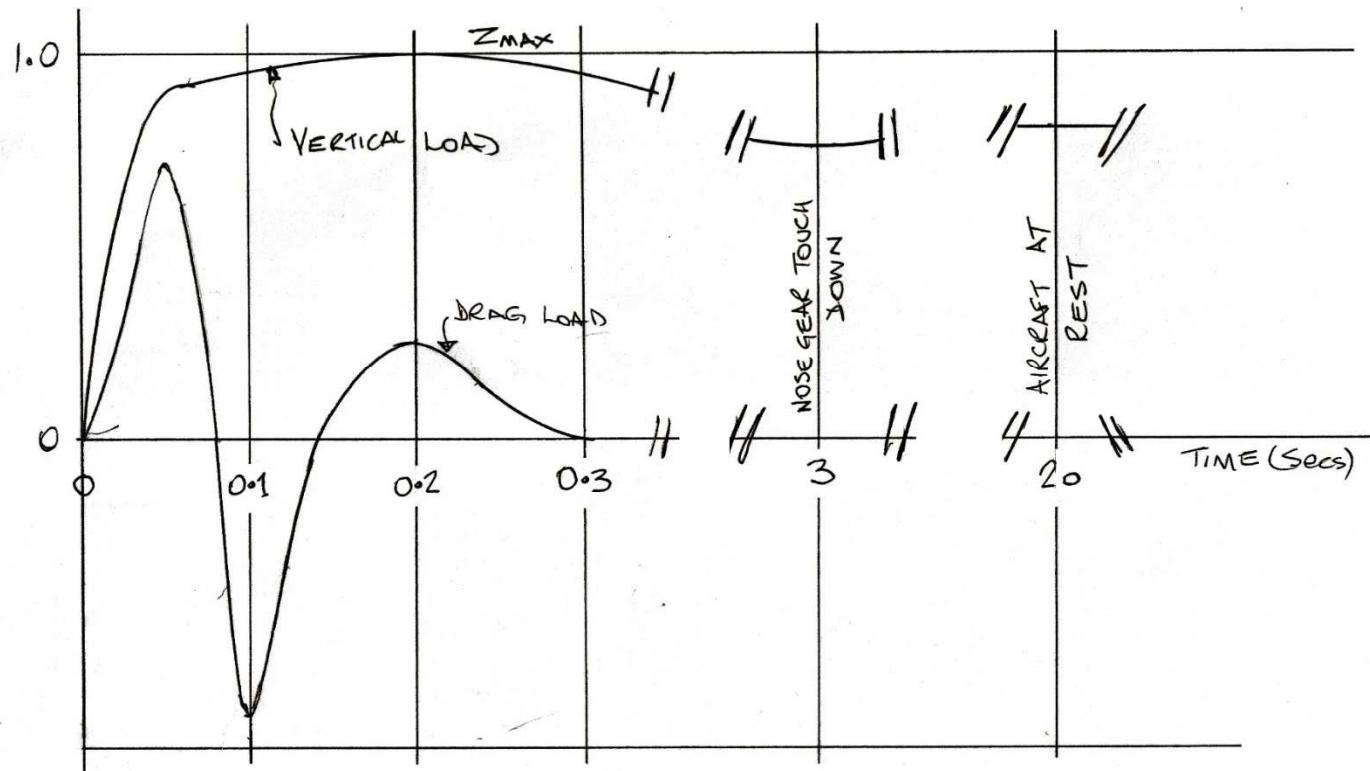


Landing Gear Load Sequence



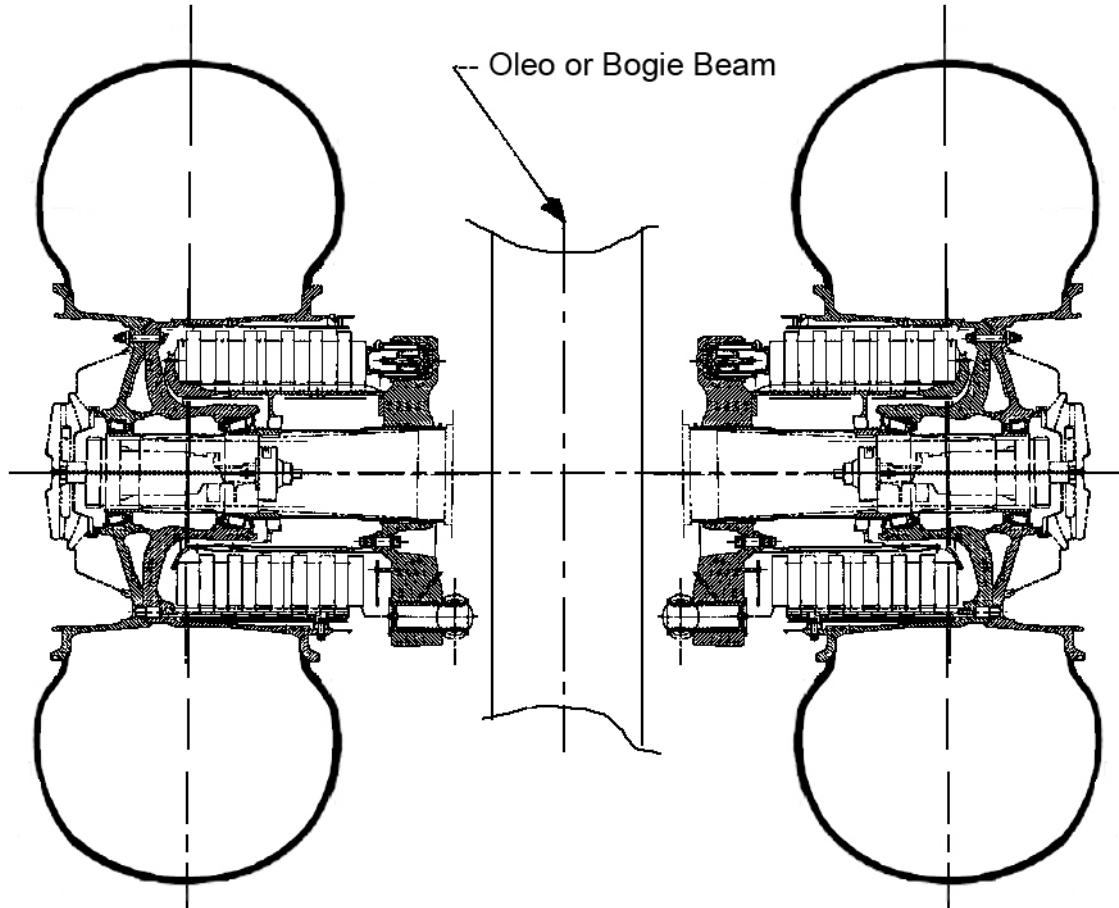
Landing Gear Time History

The Reaction Factor (λ) is the ratio of the Peak Vertical Load (Z_{max}) during the landing impact to the 1g Static Load at Maximum Landing Weight. For a light aircraft it can be as high as 3.0, for something like an A320 or larger, industry tends to use something like 1.25

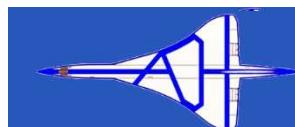


Wheel, Tyre and Brakes

Rim Dia = 20 inches
Energy/Wheel = 70 MJ
This is for a RTO at MTOW
Brakes on speed is typically
85 to 90 m/s



Lateral Spacing of Wheels is determined
by the ACN requirements and the need
to accommodate the brakes



Suggested Loads Cases that you should be aware of

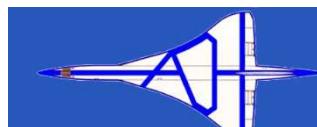
General

There are many other design cases that need to be considered for full certification (see figs 21, 22, and 23 of Airworthiness and Loads handout).

You should be aware that some of these cases can only be acted on when the design has progressed further.

At this stage you should certainly consider cabin pressurisation (the following values cover short range to long range aircraft). Values in mb

Max Nominal Operating Differential Pressure	556±7	to	605±7
Relief Valve Setting (actuating)	590±7	to	635±7
Max Relief valve overpressure (max flow)	621±7	to	665±7
Max Negative Differential Pressure	-70		
Stressing Values			
- Fatigue	556	to	605
- Static (relief valve setting)	597	to	642



Engine and Pod Loads (TurboFan)

The g and thrust values that are given in this section are applied to the combined mass of the Engine and Pod, at the combined CG.

Wing Mounted

Condition	Ult Factor	Fx	Fx	Fy	Fz
		Thrust	Mass	Mass	Mass
Flight	1.5	MCP or Zero		$\pm 3g$	1g
	1.5	MCP or Zero			$\pm 3g$
Landing	1.5	Idle or Zero			+3g
	1.5	Idle or Zero			-1g
Max Thrust	1.0	2 x Max TO			1.5g or Zero
	1.0	2 x Reverse			1.5g or Zero
Blade Loss	1.0				

Note: Should be aware of Wheels up Landing but not enough data available to derive

Rear Fuselage Mounted

Condition	Ult Factor	Fx	Fx	Fy	Fz
		Thrust	Mass	Mass	Mass
Flight	1.5	MCP or Zero		$\pm 3g$	1g
	1.5	MCP or Zero			+5g
Landing	1.5	MCP or Zero			-3g
	1.5	Idle or Zero			+4g
Max Thrust	1.0	2 x Max TO			1.5g or Zero
	1.0	2 x Reverse			1.5g or Zero
Blade Loss	1.0				
Ground	1.0		12g (30° Cone)		

Note: Take Reverse Thrust as 40% of Forward Thrust.

Blade Loss gives an out of balance rotating system (probably ignore at this stage)



Engine and Pod Loads (TurboProp)

The g and thrust values that are given in this section are applied to the combined mass of the Engine, Gearbox, Propeller and Nacelle, at the combined CG.

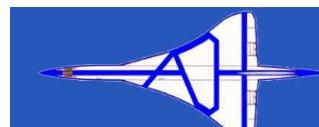
Wing Mounted

Condition	Ult Factor	Fx	Fx	Fy	Fz	Mx
		Thrust	Mass	Mass	Mass	Torque
Flight	1.5	MCP or Zero		$\pm 3g$	1g	
	1.5	MCP or Zero			$\pm 3g$	
Landing	1.5	Idle or Zero			$+3g$	
	1.5	Idle or Zero			-1g	
Max Thrust	1.0	2 x Max TO			1.5g or Zero	
	1.0	2 x Reverse			1.5g or Zero	
Torque	1.5				1g	2 x Mean Torque
"Failsafe"	1.0	0.5 x Max TO		$\pm 2g$	2g	Mean Torque
"Fatigue"	1.0				1g	Mean Torque

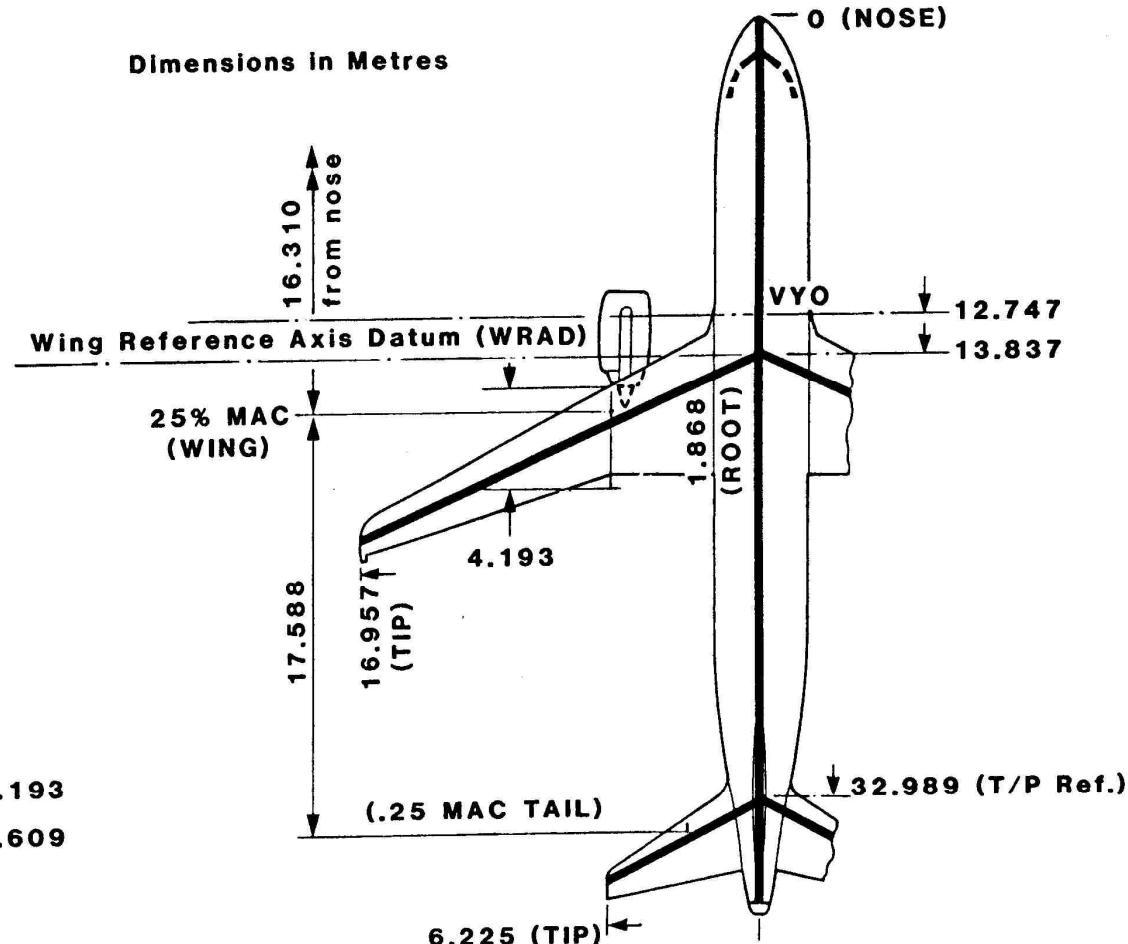
Note: Take Reverse Thrust as 40% of Forward Thrust.

The gearbox for the propeller is often supported by struts or rods from the gas generator. The failure of these rods has to be considered (take the failure of 1 or 2 rods depending on design).

Fatigue life to be taken as 20000 flights.



Aircraft Reference Axes



A320



Aircraft Reference Axes for Loads

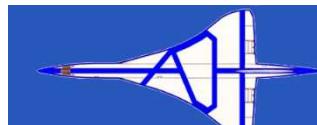
Fuselage Straight line through Horizontal Fuselage Datum

Wing Straight line in the Wing Plane (assume 'Flat' Wing)
through 40% Chord at Wing Root and
40% Chord at Wing Tip
(extrapolate to Aircraft Centre Line)

Tailplane Straight line in the Tailplane Plane
through 40% Chord at Root and Tip
(extrapolate to Aircraft Centre Line)

Fin Straight line in the Fin Plane
through 40% Chord at Root and Tip
(extrapolate to Horizontal Fuselage Datum)

These are suggestions, depending on the layout of the aircraft,
other values may be appropriate

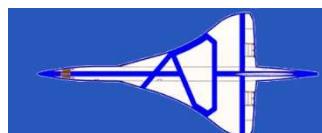
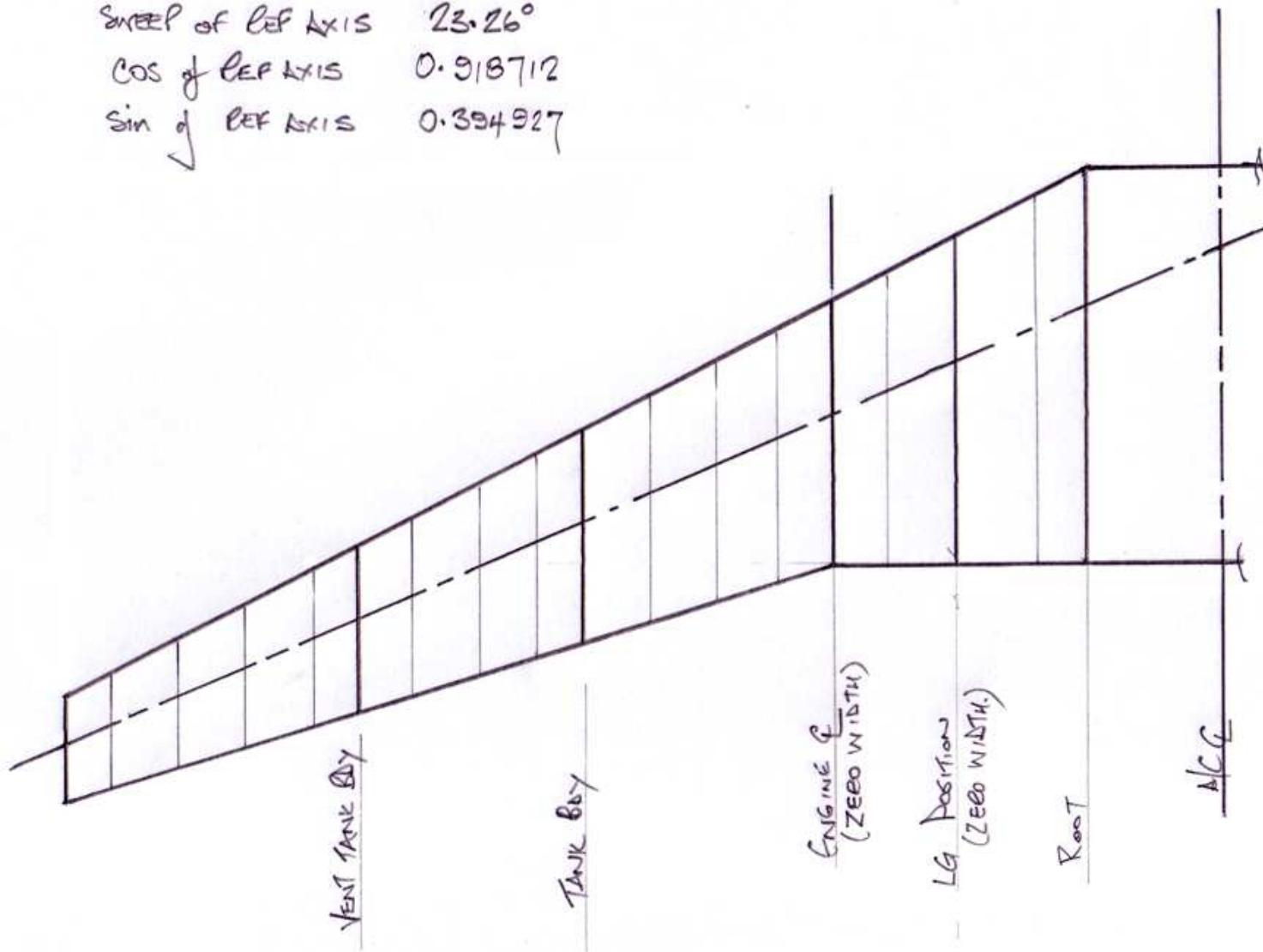


Wing Strip Layout

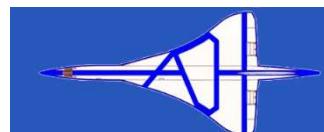
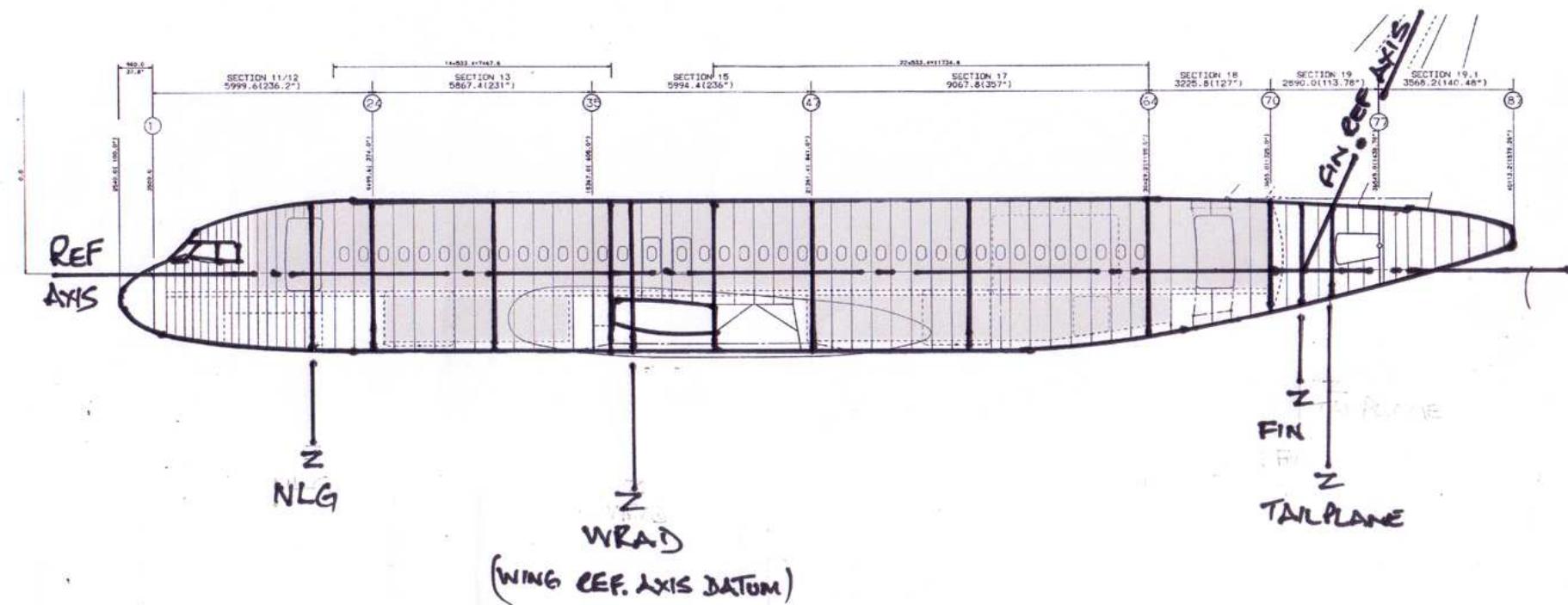
Sweep of ref axis 23.26°

Cos of ref axis 0.918712

Sin of ref axis 0.394927



Fuselage Strip Layout



Payload and Fuel information

Payload

The specification says that the pax weight is 100kg including a check-in baggage of approx 40lb (18kg).

We can assume that $100-18 = 82\text{kg/pax}$ is in the cabin either on seats or in the overhead lockers while the 18kg/pax is in the hold.

The 82kg/pax can be uniformly distributed over the cabin length for this exercise (that will include any galley/toilet areas).

The 18kg/pax will be uniformly distributed over the hold length (which will be less than the cabin length)

NOTE: For simplicity, it would be reasonable to distribute the 100kg/pax over the whole length of the cabin with effectively nothing in the holds.

Fuel

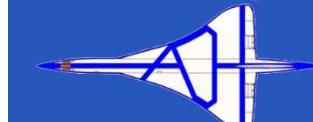
The fuel volume can be calculated using the GROSS volume of the tanks and then allowing for airspace and structure. Usually this is 10%. Hence NETT fuel volume is 90% of gross.

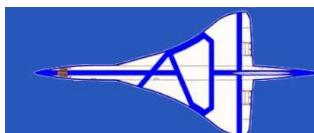
Experience suggests that fuel volume of an outer wing tank will be 85% of gross volume.

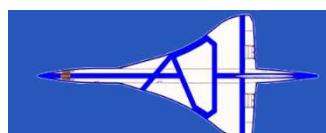
Inner wing tank 90% and the centre tank within the fuselage is 92%

Don't forget to apply the appropriate fuel density to derive the actual mass.

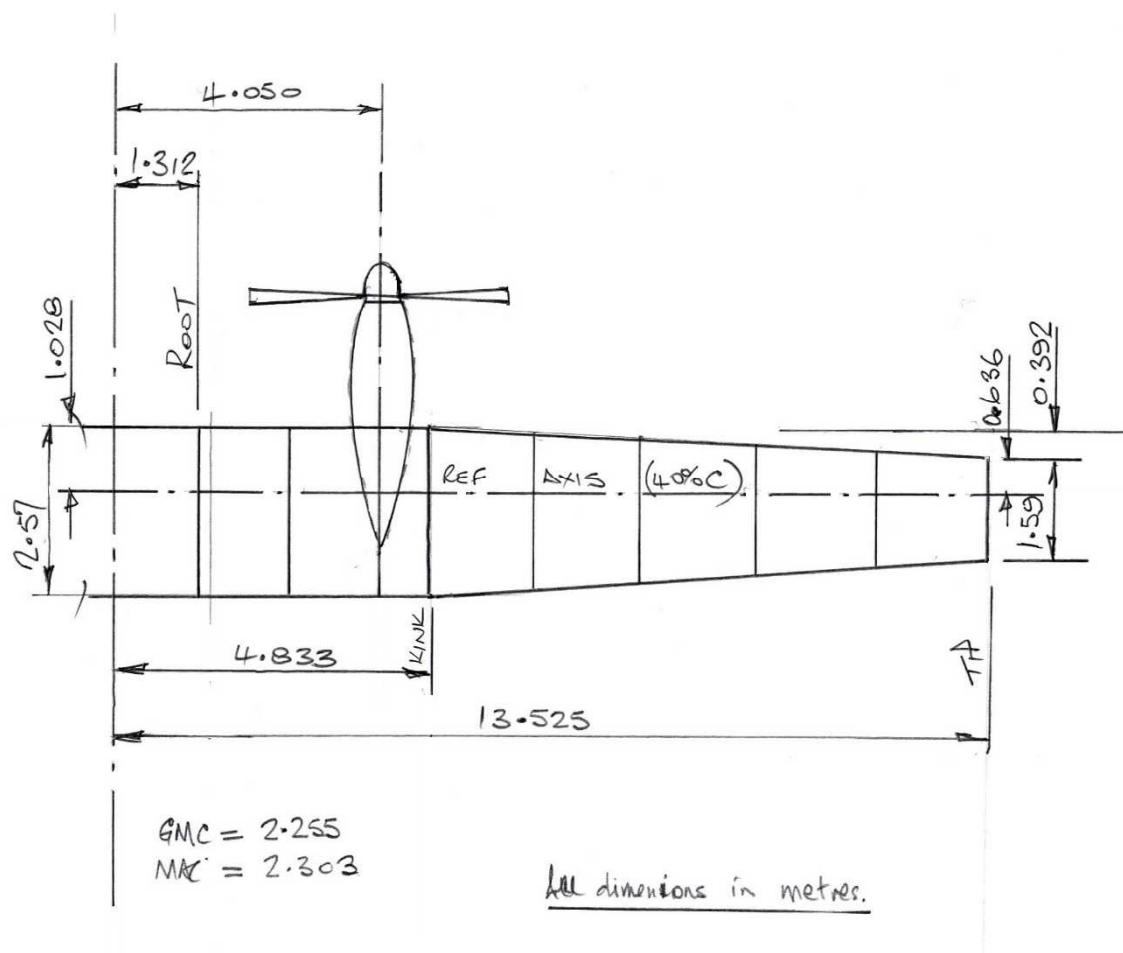
Fuel density can vary between 743 to 851 kg/m³. The nominal or typical value is 785 kg/m³ and this value should be used.



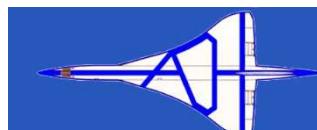




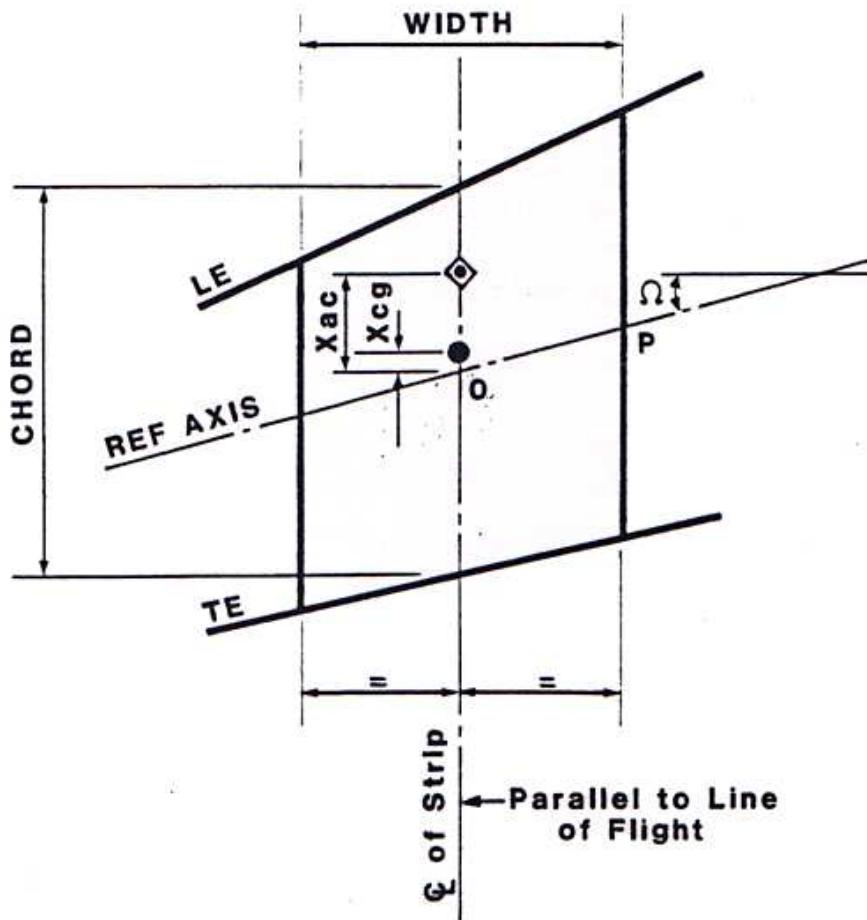
Wing Geometry



ATR 72



Strip Definition and Forces on Strip



TOTAL LOAD ON STRIP

$$F_s = -W_s \times n_s + (L_{so}/q_s) q_s + (L_s/L_{WPP}) L_{WPP}$$

MOMENT (PITCHING) ABOUT O (INTERSECTION OF STRIP C AND REF. AXIS)

$$M_{ps} = -W_s \times n_s \times x_{cg} + (L_{so}/q_s) q_s \times x_{ac} + (L_s/L_{WPP}) L_{WPP} \times x_{ac} + C_{Mo_L} \times \text{width} \times \text{chord}^2 \times q$$

FORCES AND MOMENTS AT P (INNER BOUNDARY OF STRIP)

$$S_A = F_s$$

$$M_R = F_s \times \text{width}/2 \quad \text{IN LINE OF FLIGHT OR A/C AXES}$$

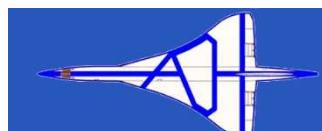
$$M_p = M_{ps} - F_s \cdot \frac{w}{2} \cdot \tan \alpha$$

TRANSFORM TO REFERENCE AXES

$$S_{ref} = S_A$$

$$M_{ref} = M_R / \cos \alpha - M_{ps} \sin \alpha$$

$$T_{ref} = M_{ps} \cos \alpha$$



Strip Definition and Forces on Strip

Assuming a flat wing (no dihedral) and tan, sin & cos refer to the sweep of the reference axis.

Taking the definitions of FS and MPS as given for the force and moment at the centre of the strip.

Values at the INNER boundary in line of flight will be

$$\begin{aligned} S_A &= F_S \\ M_R &= F_S * (w/2) \\ M_P &= M_{PS} - F_S * (w/2) * \tan \end{aligned}$$

Convert to reference axis, the values at the INNER boundary will be

$$\begin{aligned} S_{REF} &= S_A \\ M_{REF} &= M_R * \cos - M_P * \sin \\ T_{REF} &= M_R * \sin + M_P * \cos \end{aligned}$$

Substituting for M_R and M_P

$$\begin{aligned} M_{REF} &= F_S * (w/2) * \cos - M_{PS} * \sin + F_S * (w/2) * \tan * \sin \\ T_{REF} &= F_S * (w/2) * \sin + M_{PS} * \cos - F_S * (w/2) * \tan * \cos \end{aligned}$$

Re-arranging the equations

$$\begin{aligned} M_{REF} &= F_S * (w/2) * (\cos + \sin * \sin / \cos) - M_{PS} * \sin \\ (\cos + \sin * \sin / \cos) &= 1 / \cos \end{aligned}$$

$$\begin{aligned} T_{REF} &= F_S * (w/2) * (\sin - \sin * \cos / \cos) + M_{PS} * \cos \\ (\sin - \sin * \cos / \cos) &= 0 \end{aligned}$$

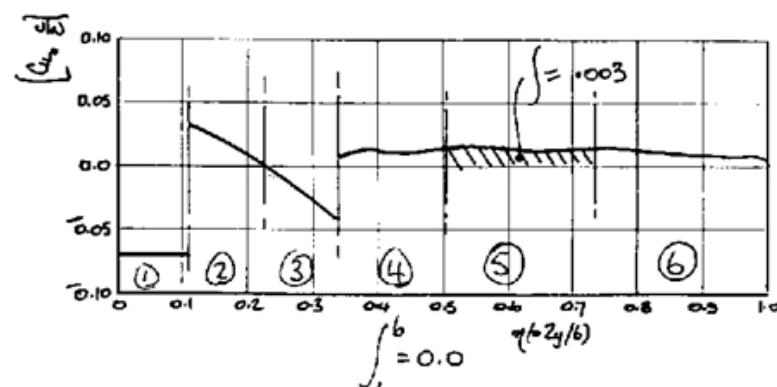
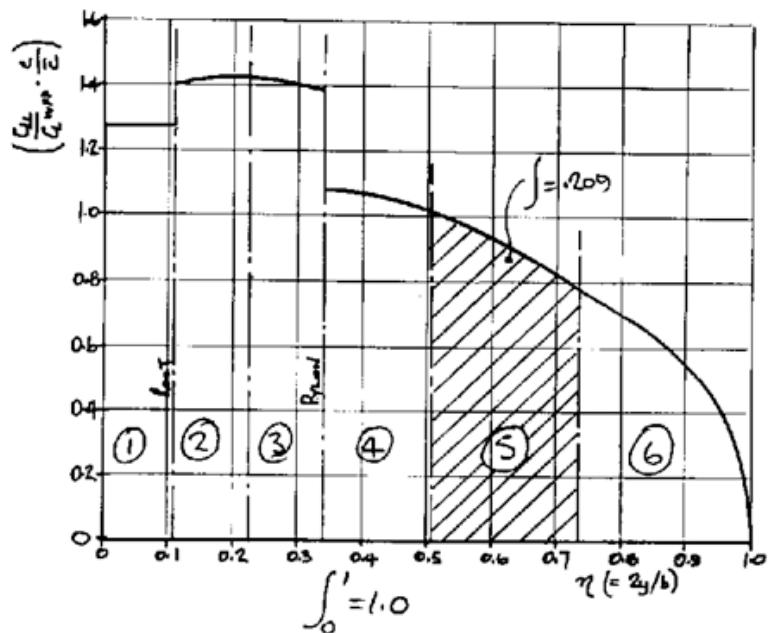
Which gives the final equations

$$\begin{aligned} S_{REF} &= S_A \\ M_{REF} &= M_R / \cos - M_{PS} * \sin \\ T_{REF} &= M_{PS} * \cos \end{aligned}$$

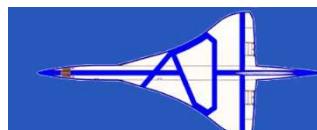
These values at the INNER boundary of the strip have to be added to the values from the OUTER boundary (or from the previous strip)



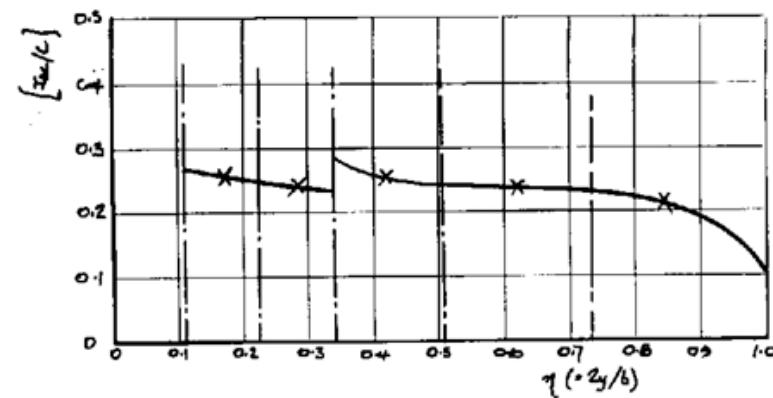
Aerodynamic Data - Wing



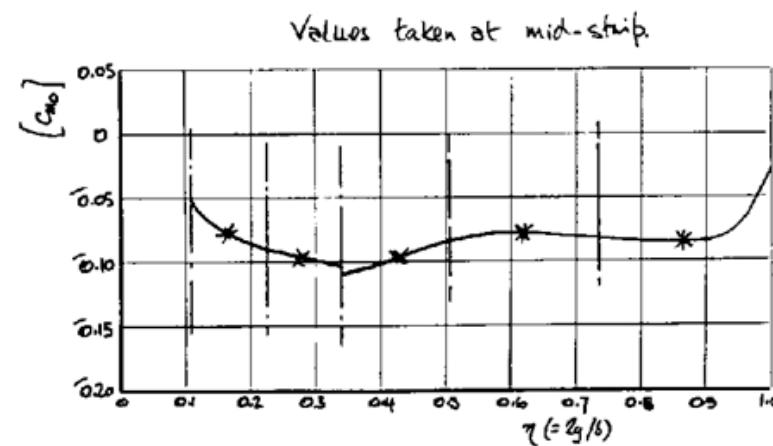
A320



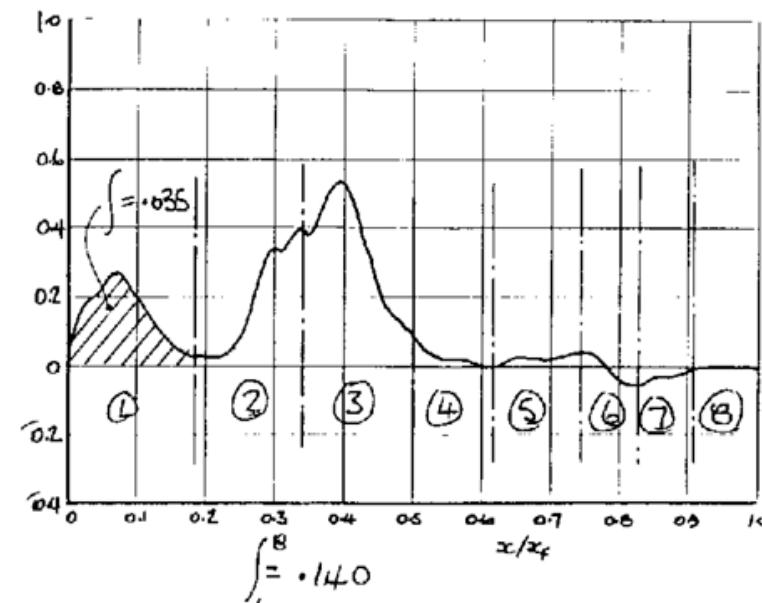
Values taken at mid-strib.



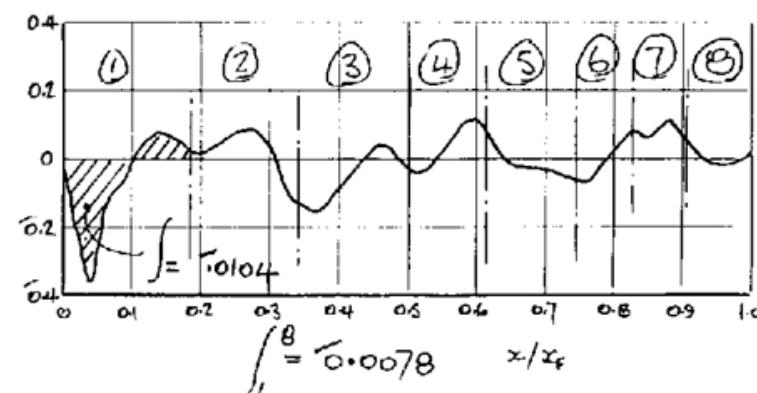
WING AERODYNAMIC DATA (UB90)



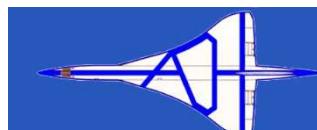
Aerodynamic Data - Fuselage



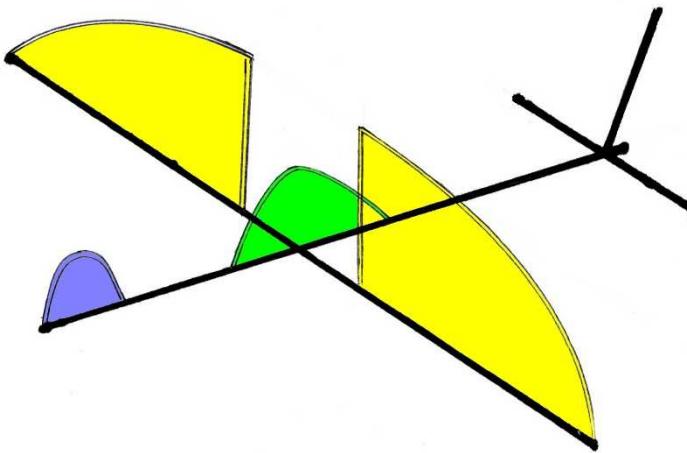
FUSELAGE AERODYNAMIC DATA (UB90)



A320



Aero Lift Distribution



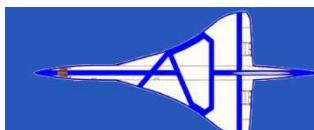
Wing + Fuselage lift = 100 ($L_w + L_f = 100$)

Typically $L_w = 86$ & $L_f = 14$

Lift on Fuselage is in 2 parts (Wing Carry over
and Nose contribution)

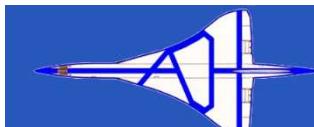
$L_{f(nose)} = 4$ and acts over approx 1.5 fus diameters.

$L_{f(carry\ over)} = 10$ and acts over 1.5 Wing Root chords
centred on 1/4 Chord (Root)

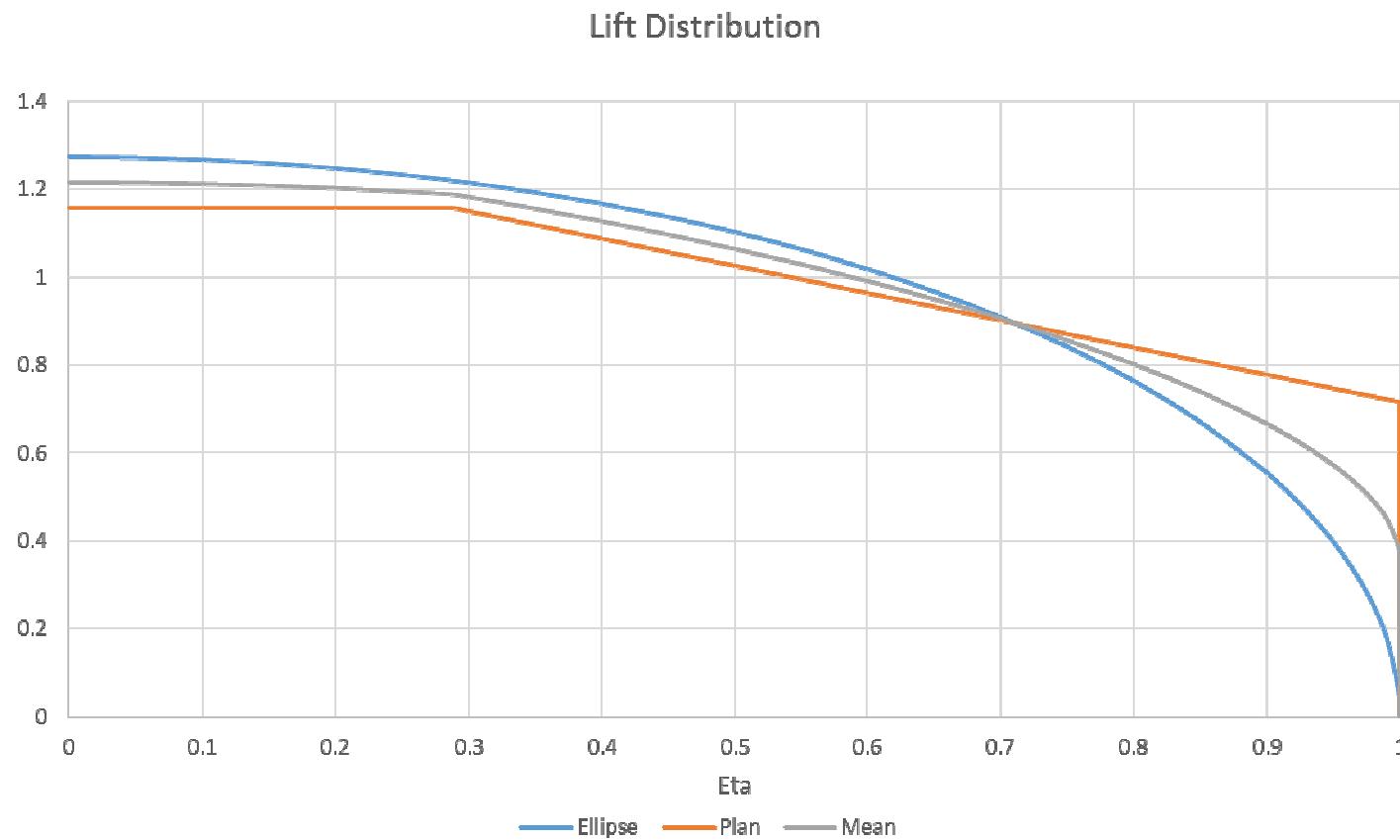


Schrenk's Method

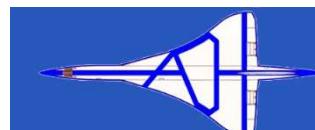
- O. Schrenk, (1940), A Simple Approximation Method for Obtaining the Spanwise Lift Distribution, NACA TM 948. Available online at the URL:
<http://naca.central.cranfield.ac.uk/reports/1940/naca-tm-948.pdf>
- The method is valid for wings whose lift distribution is close to be elliptical
- The method is based on the following steps:
 1. Consider ellipse whose semi-axis is equal to the wing-span and whose area is equivalent to the wing area
 2. Consider the chord distribution associated with a quarter of the ellipse
 3. Take the average between the quarter-ellipse chord distribution and the actual one
 4. The aforementioned average represents the local product of the actual chord times the sectional lift coefficient
 5. Divide the average by the local chord in order to get the local lift coefficient for a global lift coefficient of 1



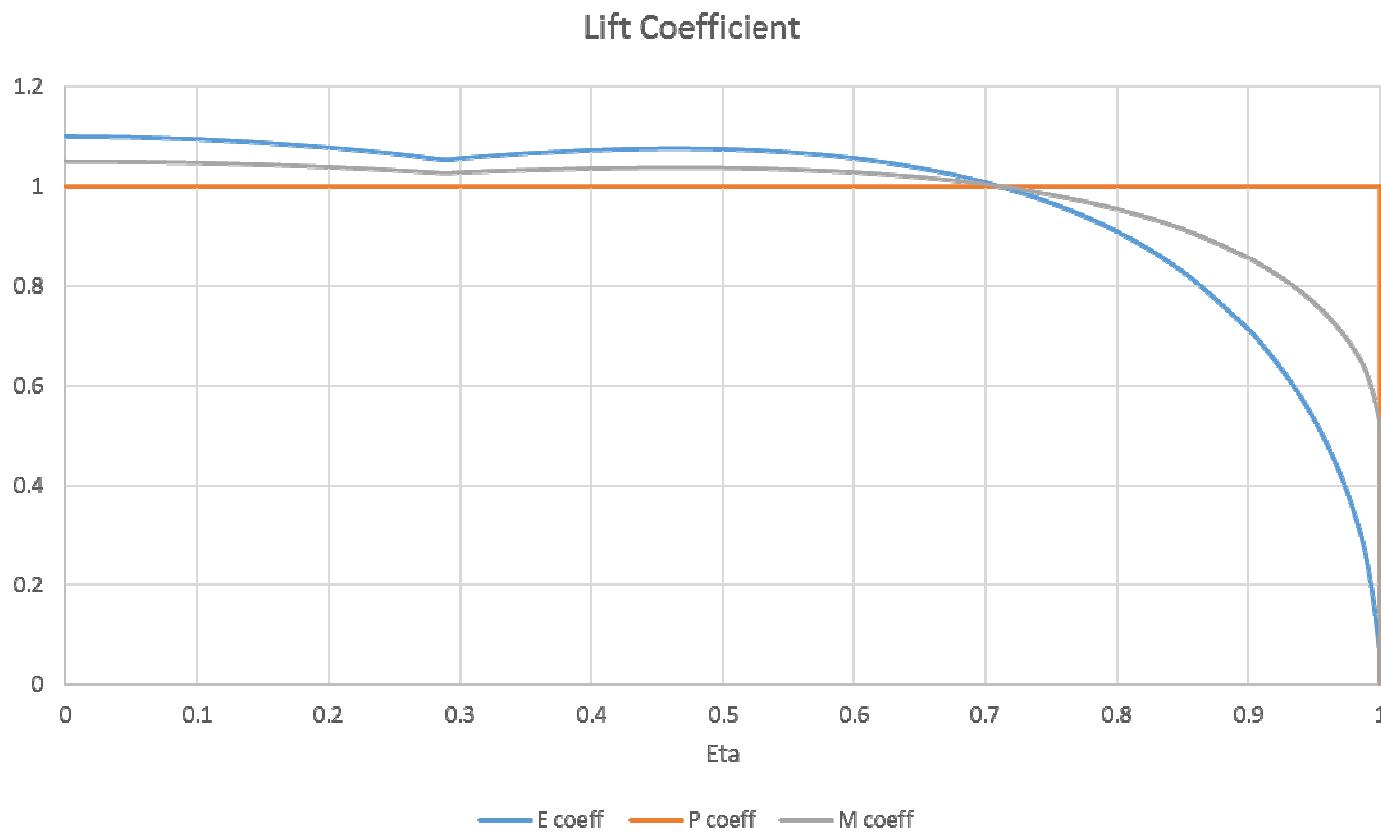
Schrenk's Method



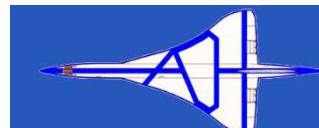
ATR 72



Schrenk's Method



ATR 72



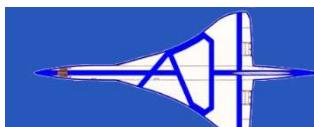
Schrenk Method – Lift Distribution

- Let us consider a condition at V_C and at an altitude depending on the aircraft in question (ATR72 probably at sea level while the A320 will be at a higher altitude)
- The lift distribution is normally derived non-dimensionally and is then scaled to the appropriate total lift which will depend on the load factor n .
- Assume that the lift generated by the horizontal tail is negative and equal to the lift on the fuselage. This means that the lift on the exposed wing (outbd of the root) is equal to the aircraft weight times the load factor n . – *this is an overestimation suitable only for early design iterations*
- Thus $L = nW = (L_W + L_F) + L_T$

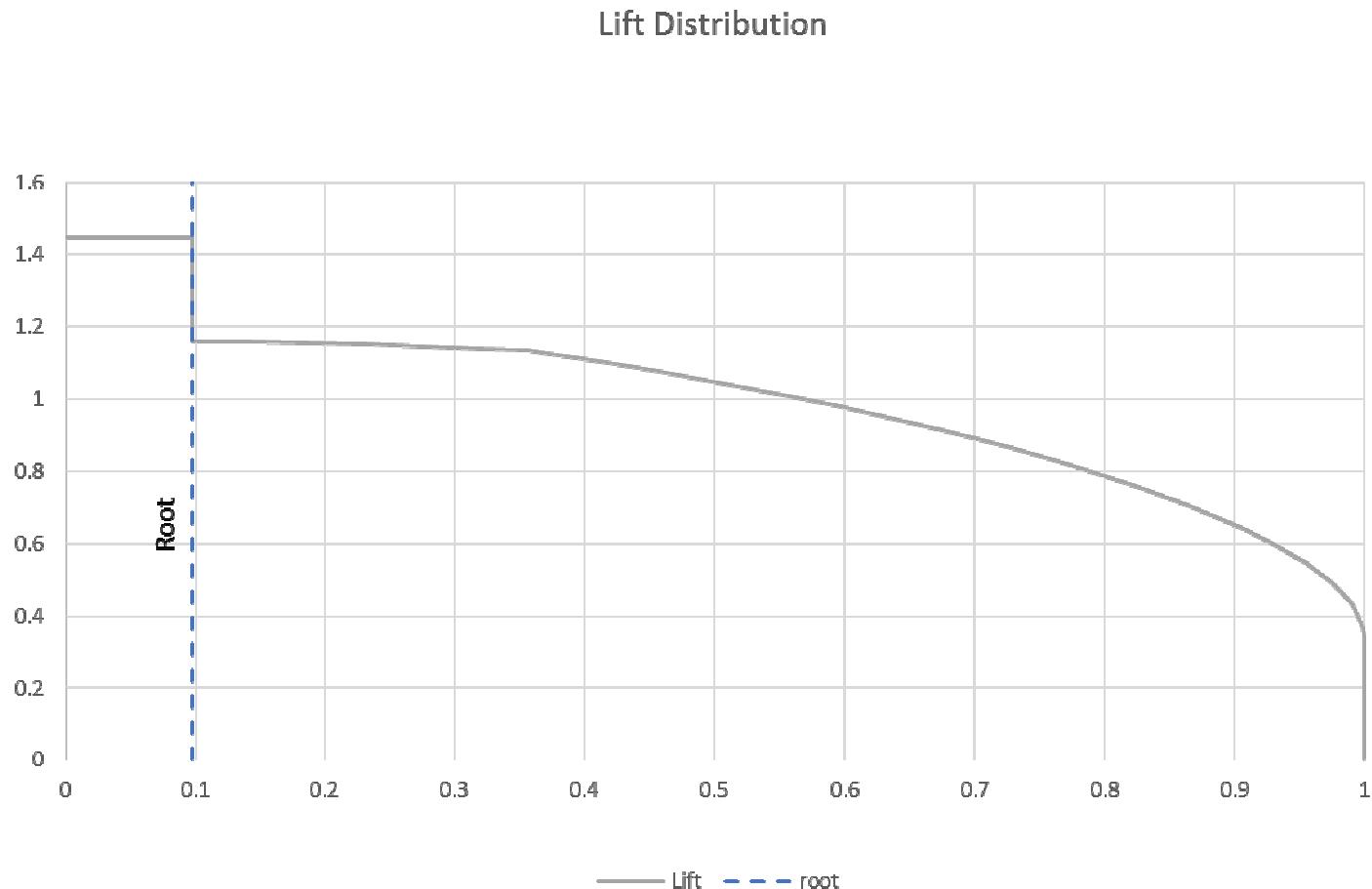
If $L_W + L_F = 100$, typically, the breakdown between wing and fuselage is

$$L_W = 86 \text{ and } L_F = 14$$

Thus $(L_W + L_F)$ needs to be scaled to give $L_W = L$



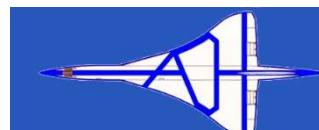
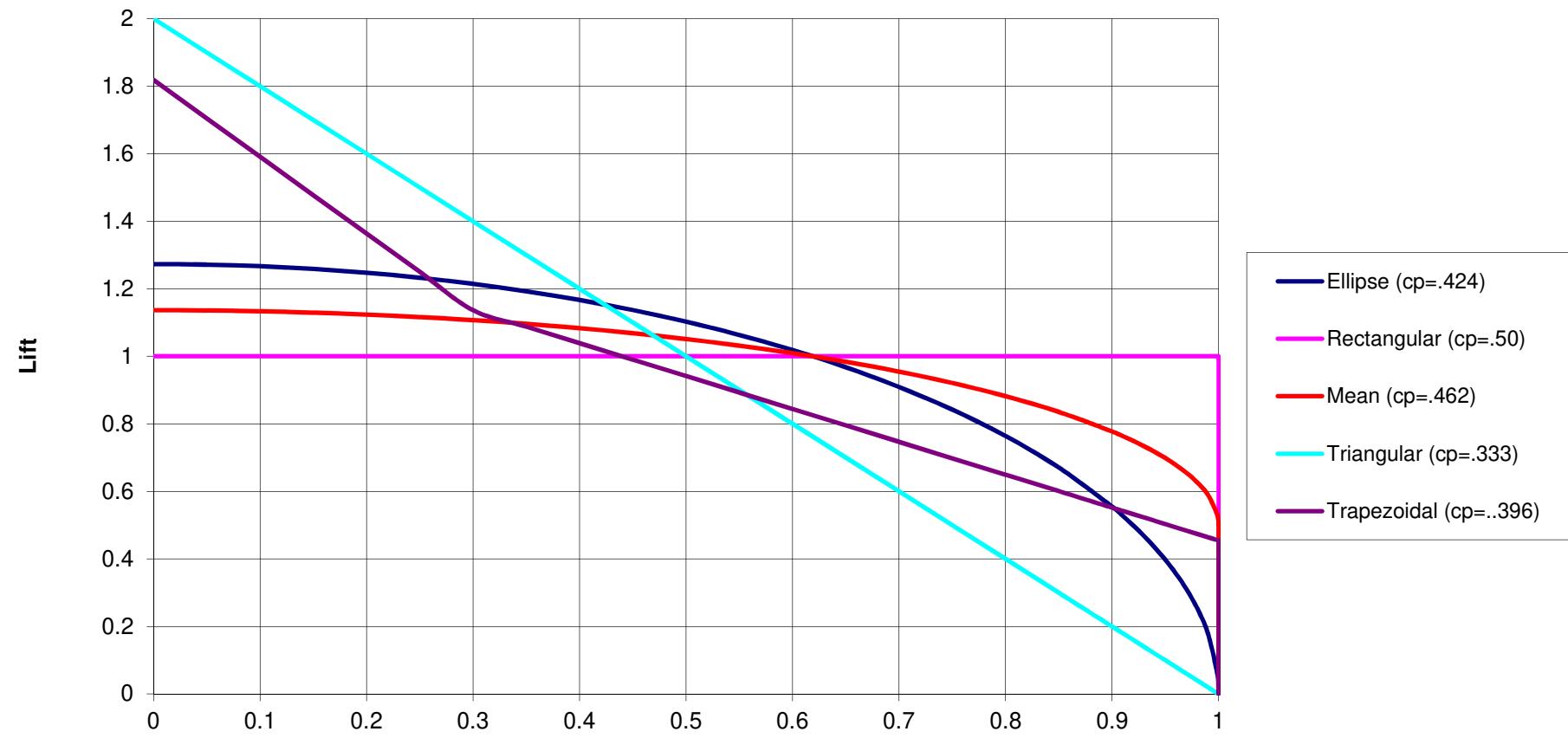
Schrenk's Method – Lift Distribution



ATR 72



Spanwise Lift Distributions



Wing Weight Estimation

- A typical figure for civil transport aircraft:

$$W_W = 10 \text{ to } 15\% \text{ of } W_T$$

- A semi-empirical formula given in Torenbeek (p280) is

$$W_W = 0.0017 W_T \left(\frac{b}{\cos \Lambda_{1/2}} \right)^{\frac{3}{4}} \left[1 + \sqrt{\frac{6.25}{b} \cos \Lambda_{1/2}} \right] (n_{ult})^{\frac{11}{20}} \left(\frac{b S_W}{t_r W_T \cos \Lambda_{1/2}} \right)^{\frac{3}{10}}$$

- Dimensions in feet (areas in ft²); weight in pounds;
- The following is advised but should be used with care
 - For 2 wing mounted engines reduce weight by 5% (4 engines; -10%)
 - If the landing gear is mounted on the fuselage, reduce weight by 5%.

Other formulae are given in Shevell, Standford University, Raymer and Roskam



Structural Weight

- We have an estimation of the total weight of the wing (structure and systems = $2468+394 = 2862\text{kg}$). But how is it distributed? It can depend on the size and type of aircraft.
- Let us assume that it is constant in the center wing box (i.e. between the intersections with the fuselage) and triangular for the outer wing. But why?
- Note that the joints are a key component, both in terms of structural function and contribution to the overall weight of the wing assembly

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Structural Weight

- A general “geometrical” method for estimating the structural weight distribution in a wing:
Savelyev, V.V., (1946), Distribution of Structural Weight of Wing Along the Span, NACA TM-1086
- According to the reference above a uniform weight distribution is suitable for the center wing and a triangular distribution is adequate for the outer wing

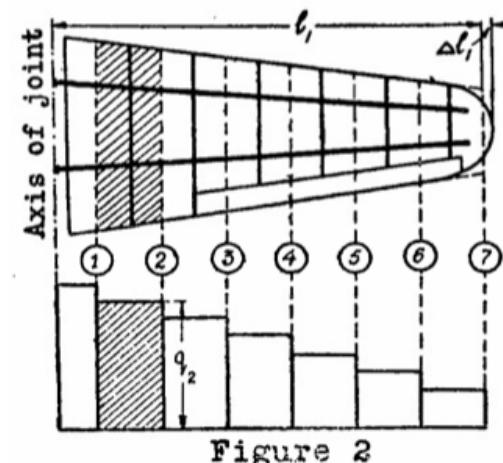
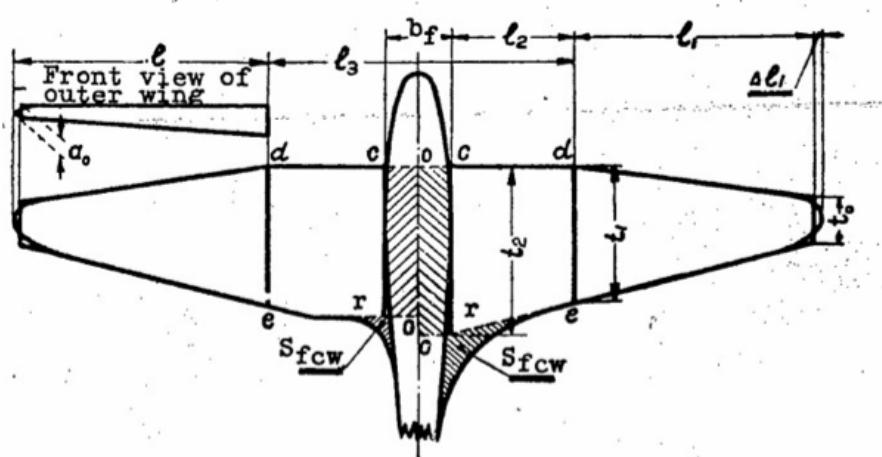
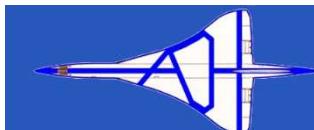


Figure 2



Wing Spanwise Mass Distribution

This can depend on the size of the aircraft and the layout of the wing and we are looking mainly what happens outboard of the root.

Light aircraft tend to be uniformly distributed e.g. kg/m is constant

The next is a triangular distribution which seems to work best for almost straight wings (little or no sweep).

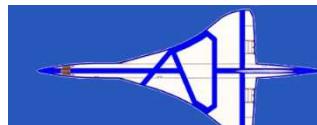
The final distribution is effectively a function of thickness v chord ratio.
It can be linear (2 slopes) or (t/c) times c to the power of 3/2

$$W = K \int_{Root}^{Tip} \left(\frac{t}{c}\right) c^n \ dy$$

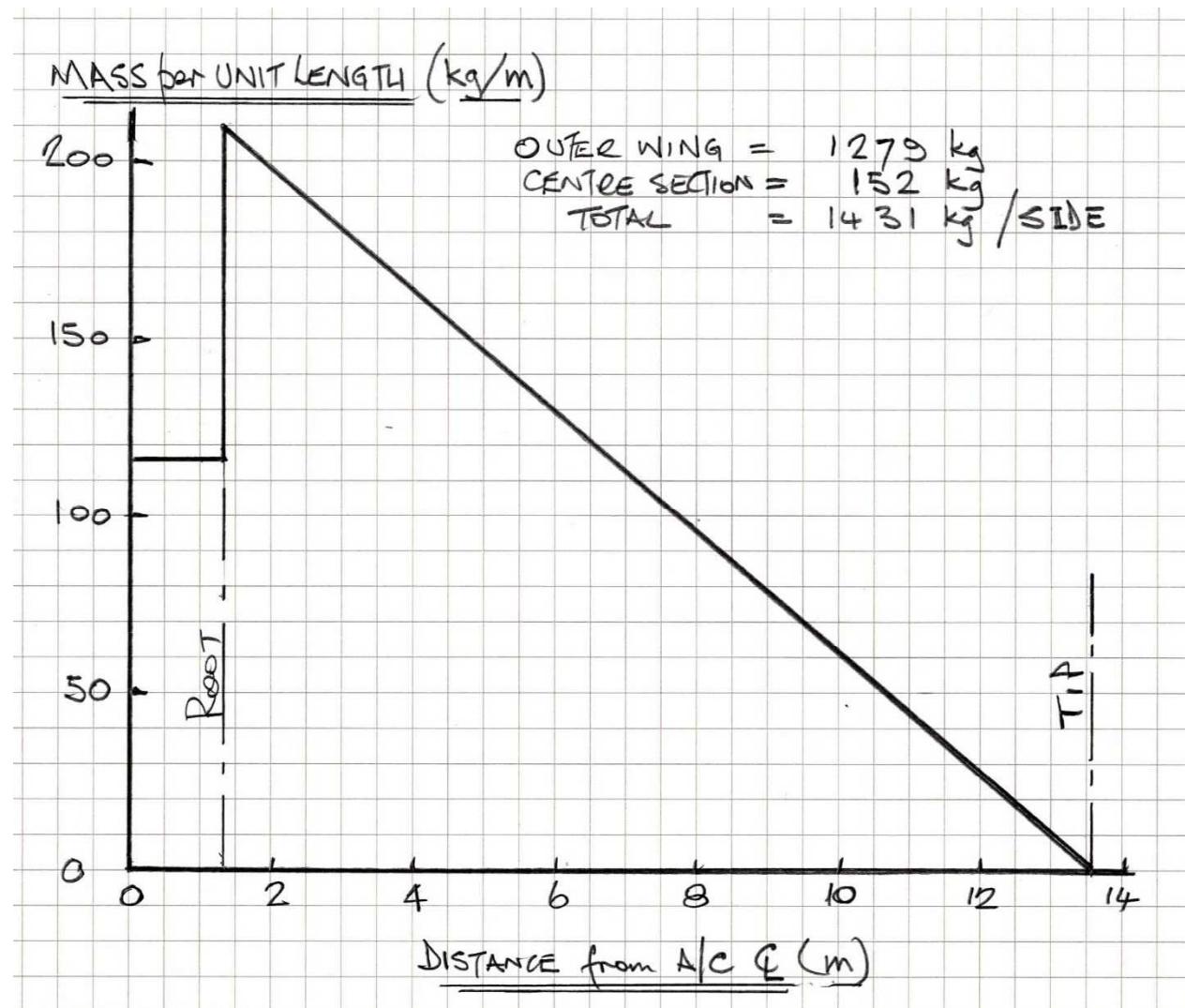
$$W = 9356 / 2 \text{ kg per side (from sheet 24)}$$

$$n = 3/2 \quad \text{----- simple geometry suggests } n=2$$

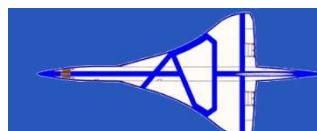
$$w(y) = K \left[\left(\frac{t}{c}\right) c^n \right] (y)$$

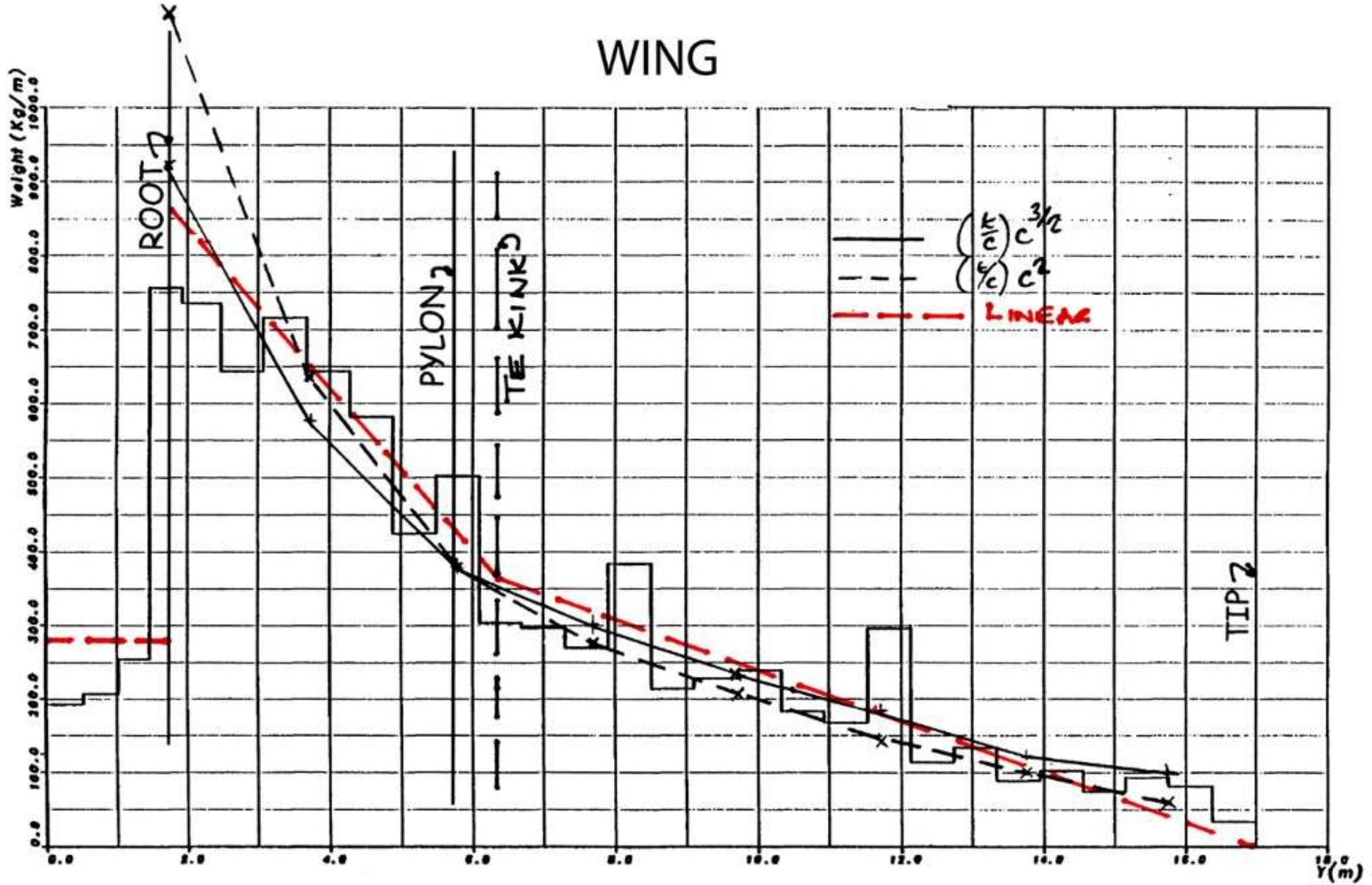


Wing Mass Distribution

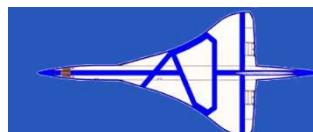


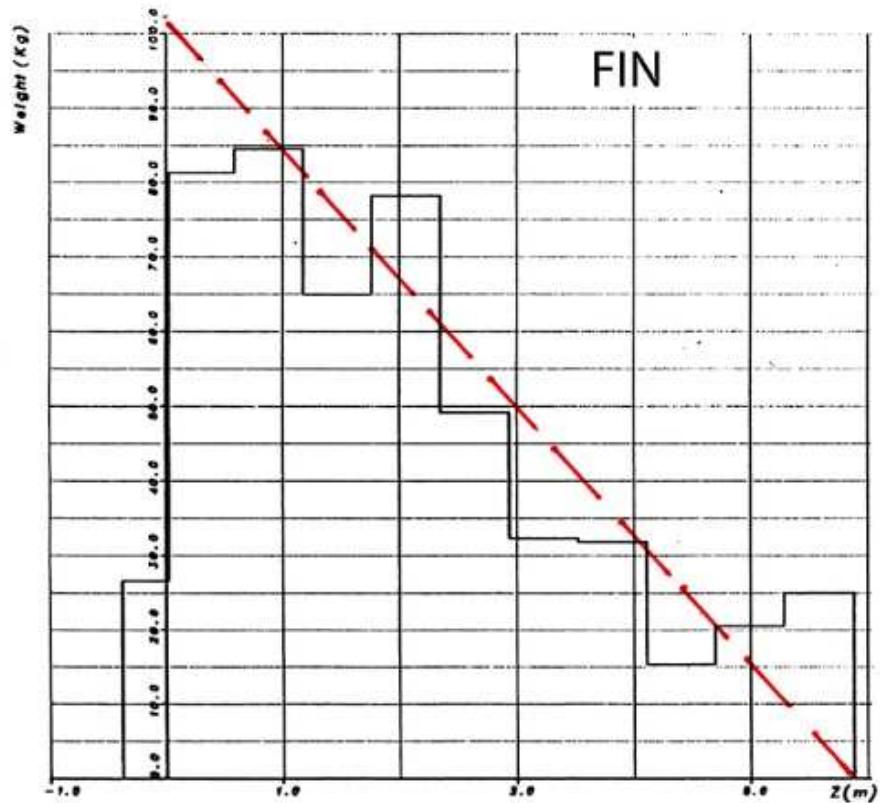
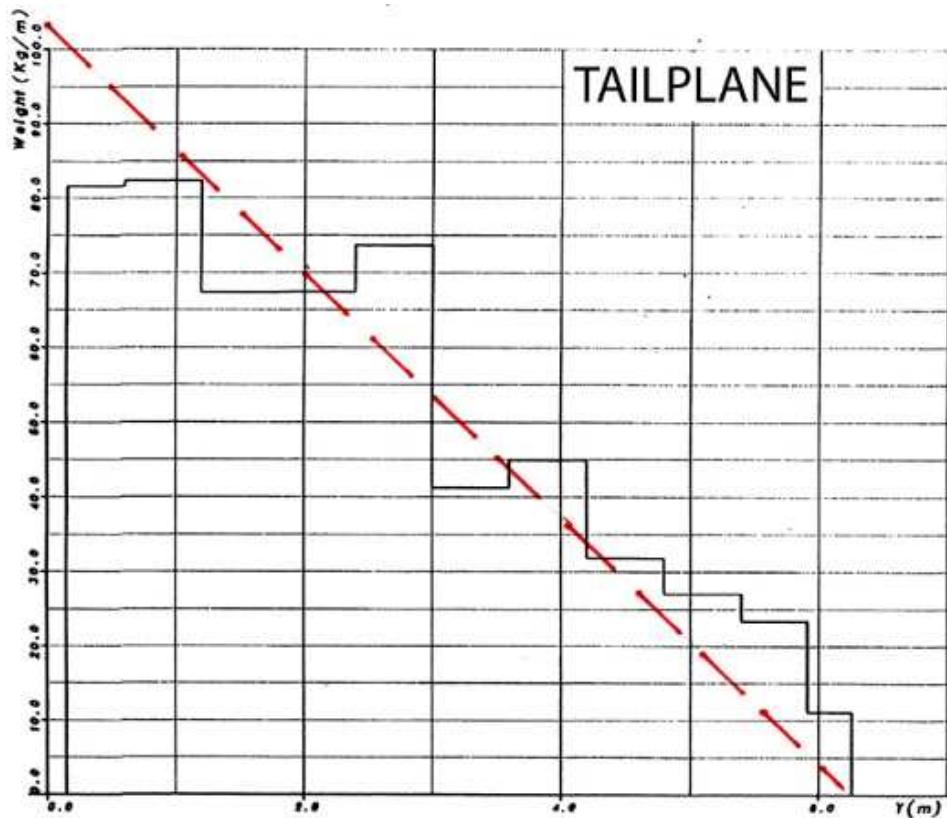
ATR 72



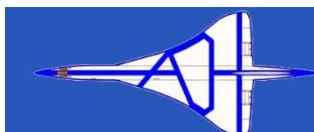


A320





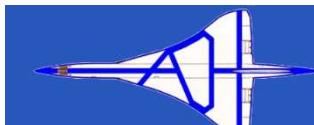
A320



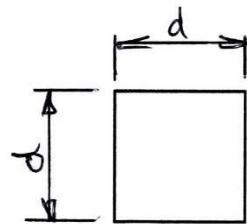
Fuel Weight

- The maximum stipulated fuel capacity is 5000 kg, corresponding to 6.37 m³ (Nett Volume for Fuel Density of 785 kg/m³). This is the aircraft value.
- The fuel is stored in the outer wing, from the root rib to 60% of the semi-span.
- Gross fuel volume is that corresponding to the outer geometry of the wing box. This is the outer skin line and front and rear spar datums.
- Nett fuel volume is 90% of Gross volume. This takes into account the structure and airspace required in the tank.

ATR 72



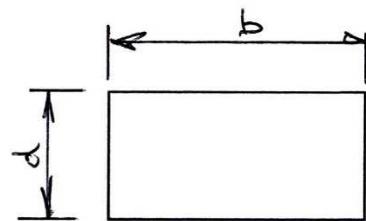
Area Info



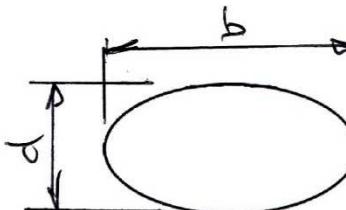
$$\text{AREA} = d^2$$



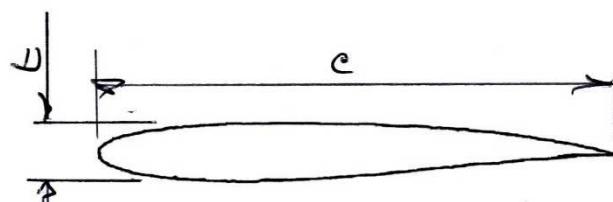
$$\text{AREA} = \frac{\pi}{4} d^2 = 0.7854 d^2$$



$$\text{AREA} = bd$$



$$\text{AREA} = \frac{\pi}{4} bd = 0.7854 bd$$

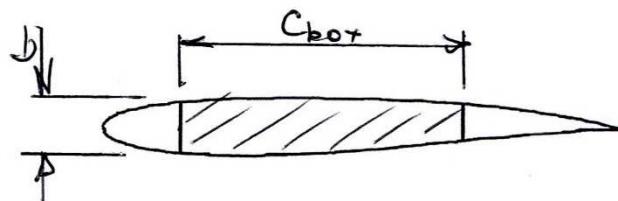


NACA SECTION

$$\text{AREA} = 0.684 tc$$

SUPER CRITICAL

$$\text{AREA} = 0.693 tc$$



SPACES at 20 ± 60

$$\text{AREA} = 0.938 tc_{box}$$

SPACES at 10 ± 60

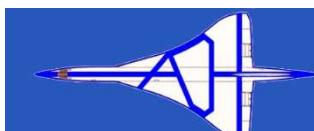
$$\text{AREA} = 0.927 tc_{box}$$

SPACES at 15 ± 65

$$\text{AREA} = 0.918 tc_{box}$$

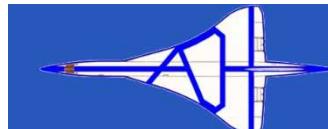
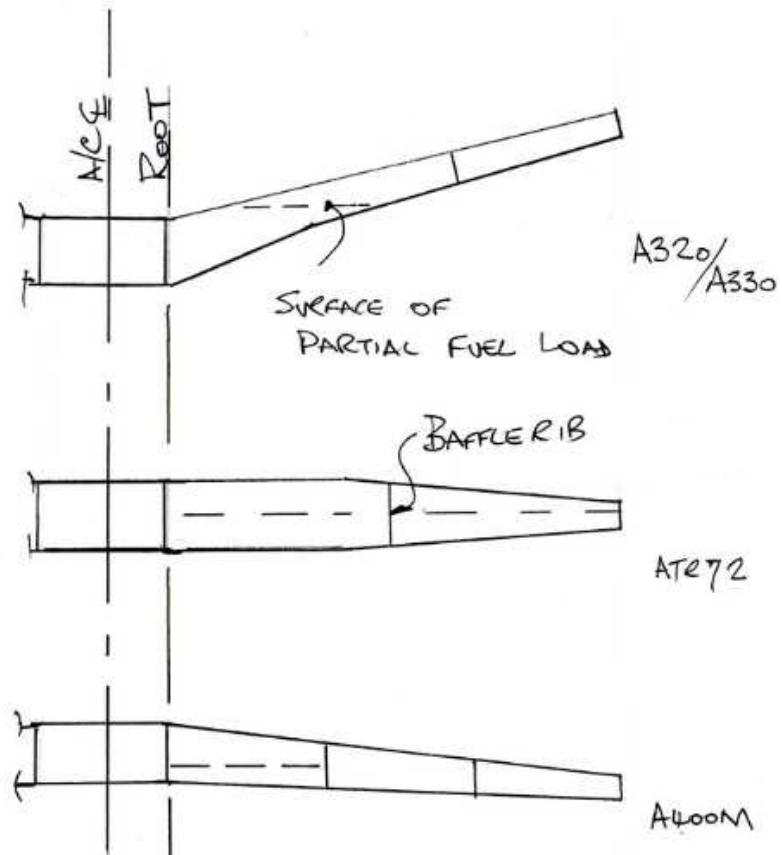
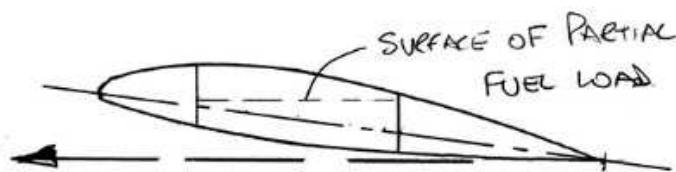
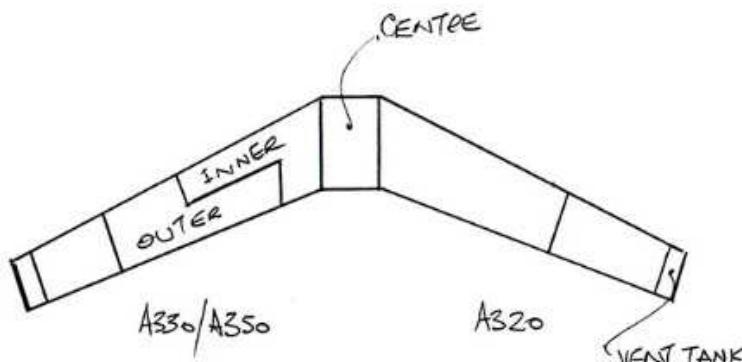
SPACES at 15 ± 60

$$\text{AREA} = 0.937 tc_{box}$$



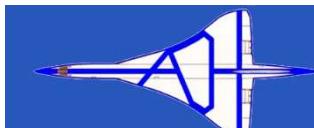
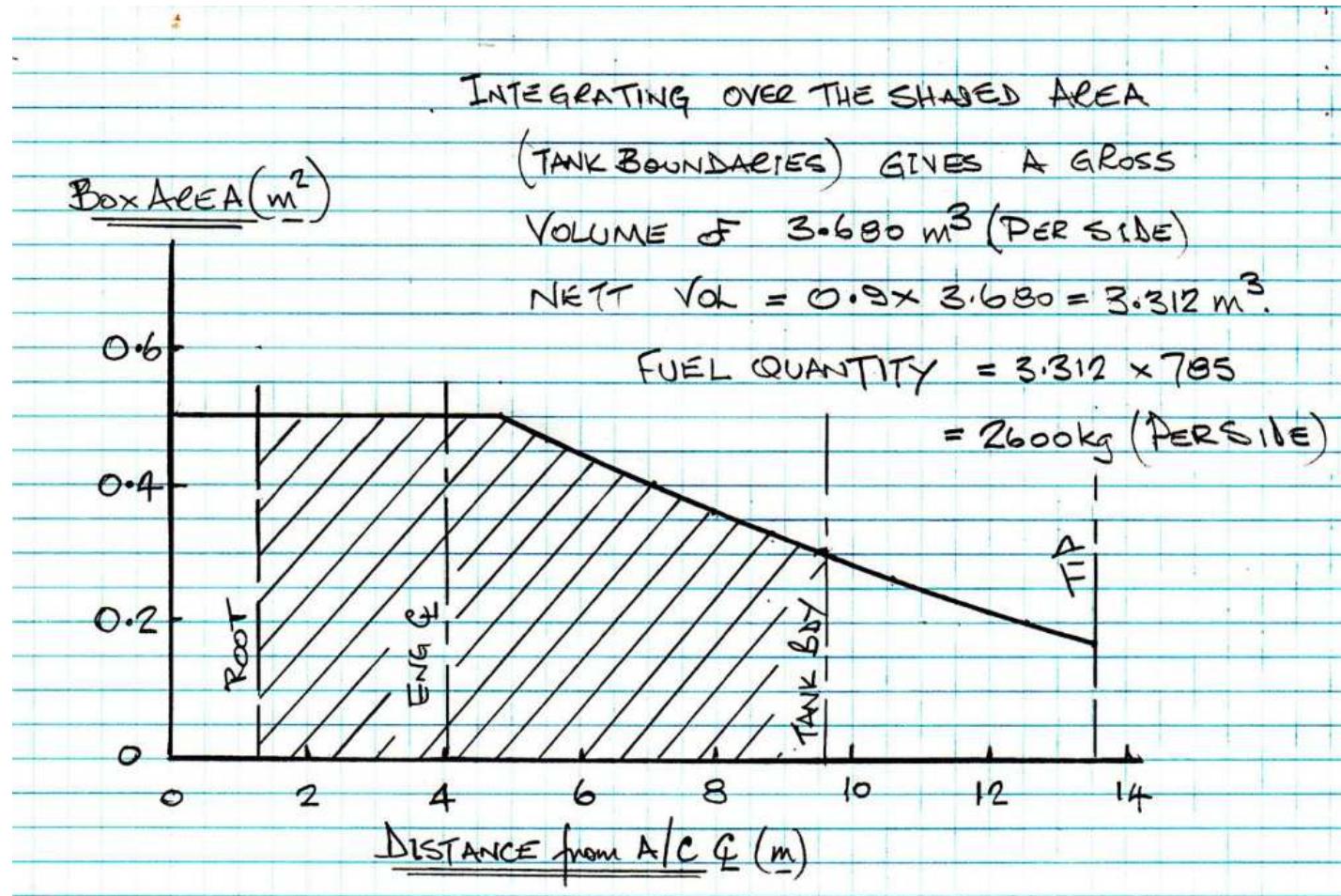
Some Information about Fuel Tanks

For Design Projects, it is suggested that full Fuel Tanks are assumed.
Calculating Volumes and CG positions could be very involved



Box Area & Fuel Mass

- The fuel mass is distributed using wing box area



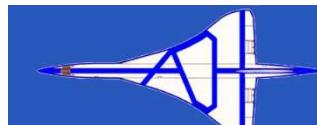
Chordwise CG position at OWE

Wing	Aircraft CL	0.45 c
	Root	0.45 c
	Inner Engine	0.43 c
	Outer Engine	0.43 c
	Tip	0.43 c
Tailplane	CL	0.45 c
	Tip	0.45 c
Fin	CL	0.45 c
	Tip	0.45 c

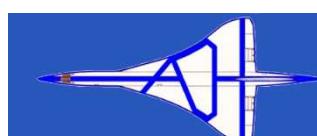
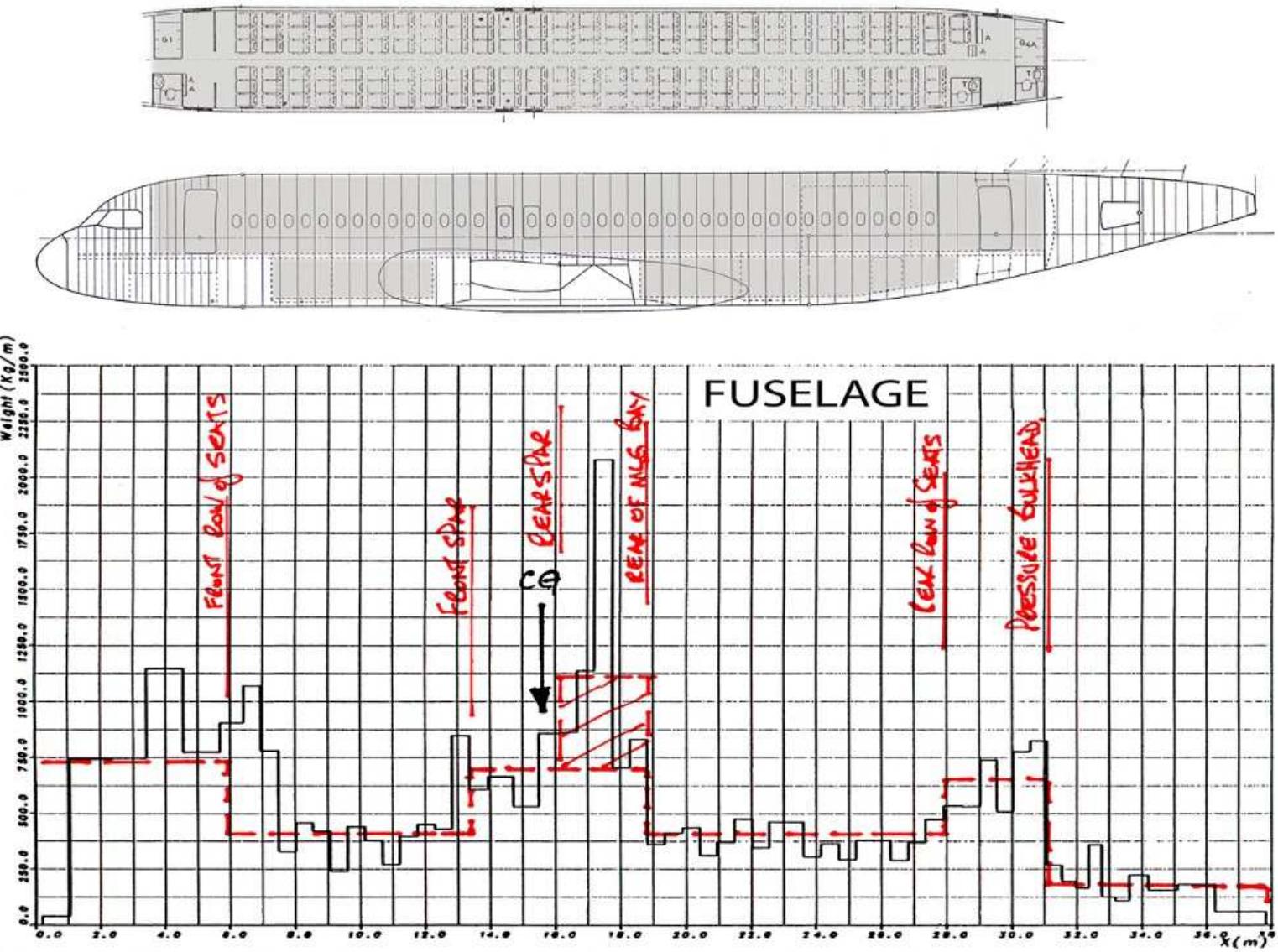
Fuel in the Wing is assumed to have a chordwise CG midway between the spars

These are suggestions, depending on the layout of the aircraft,
other values may be appropriate.

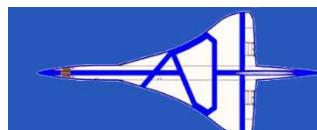
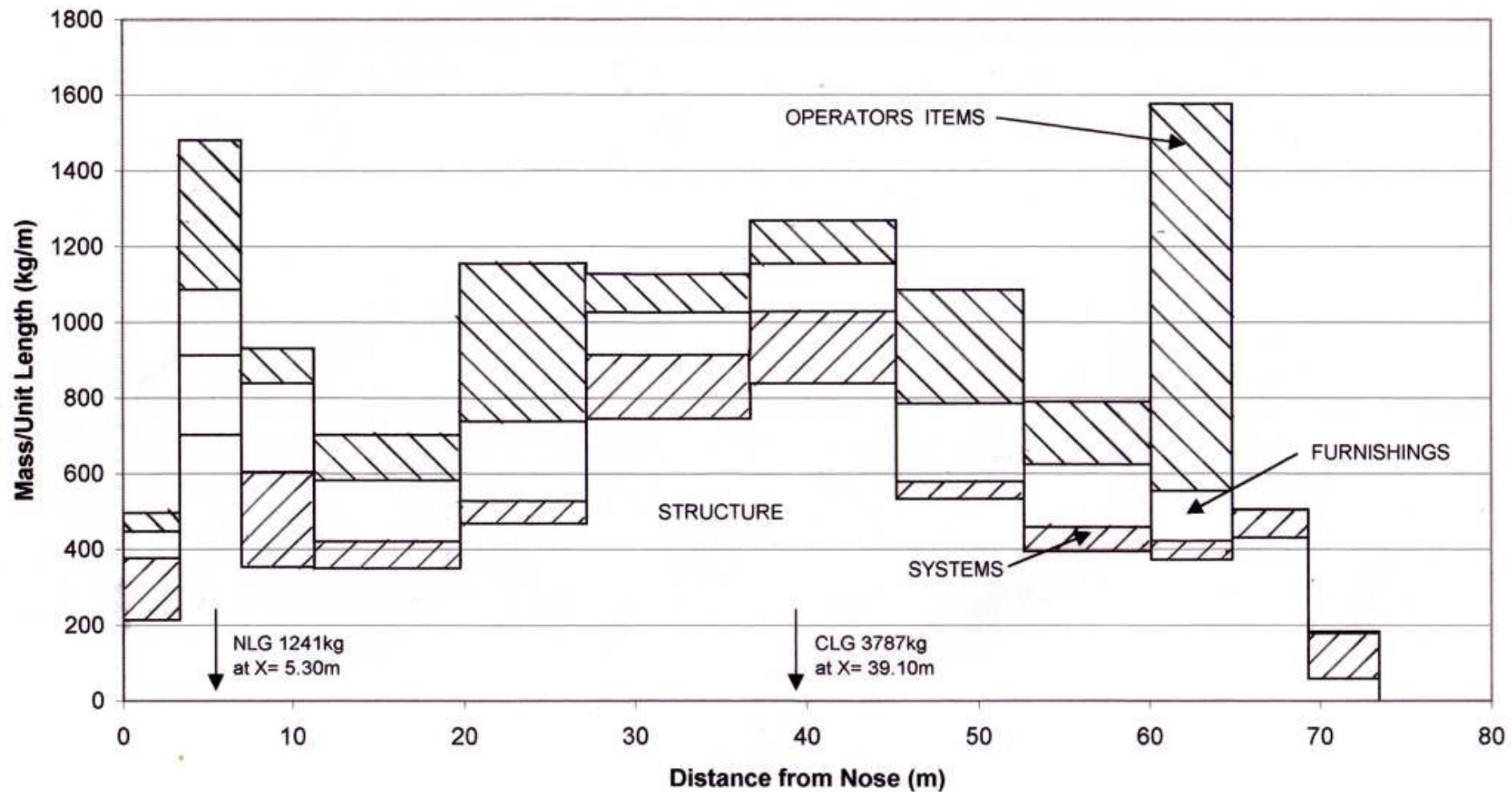
For example, small light aircraft, 0.40 c might be more appropriate.



Fuselage Mass Distribution



Fuselage Mass Distribution



Engine Weight

- Pratt and Whitney PW127 W
- 2750 SHP rating
- Bare weight: 522 kg (propeller NOT included)
- Mounted at 4.05m from fuselage centerline



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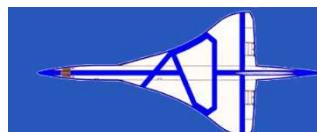
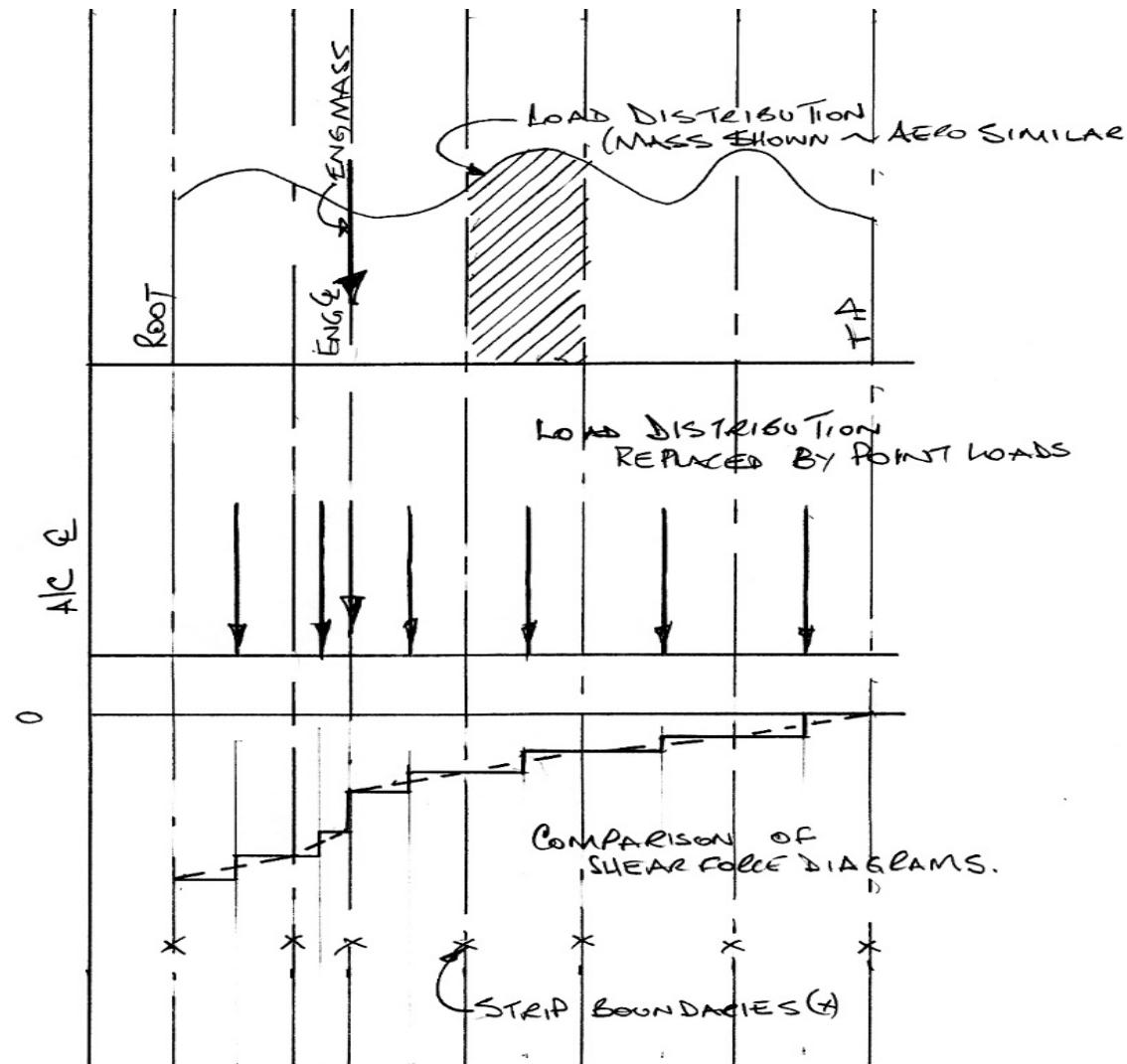
Engine + Nacelle Mass

	Mass(kg)	CG(m fwd of LE)
Engine	1044	0.9
Nacelle	228	0.0
Propeller	400	2.0
Fuel System	12	0.0
Systems	140	0.0
Operator Items	30	0.0
Total	1854	0.938

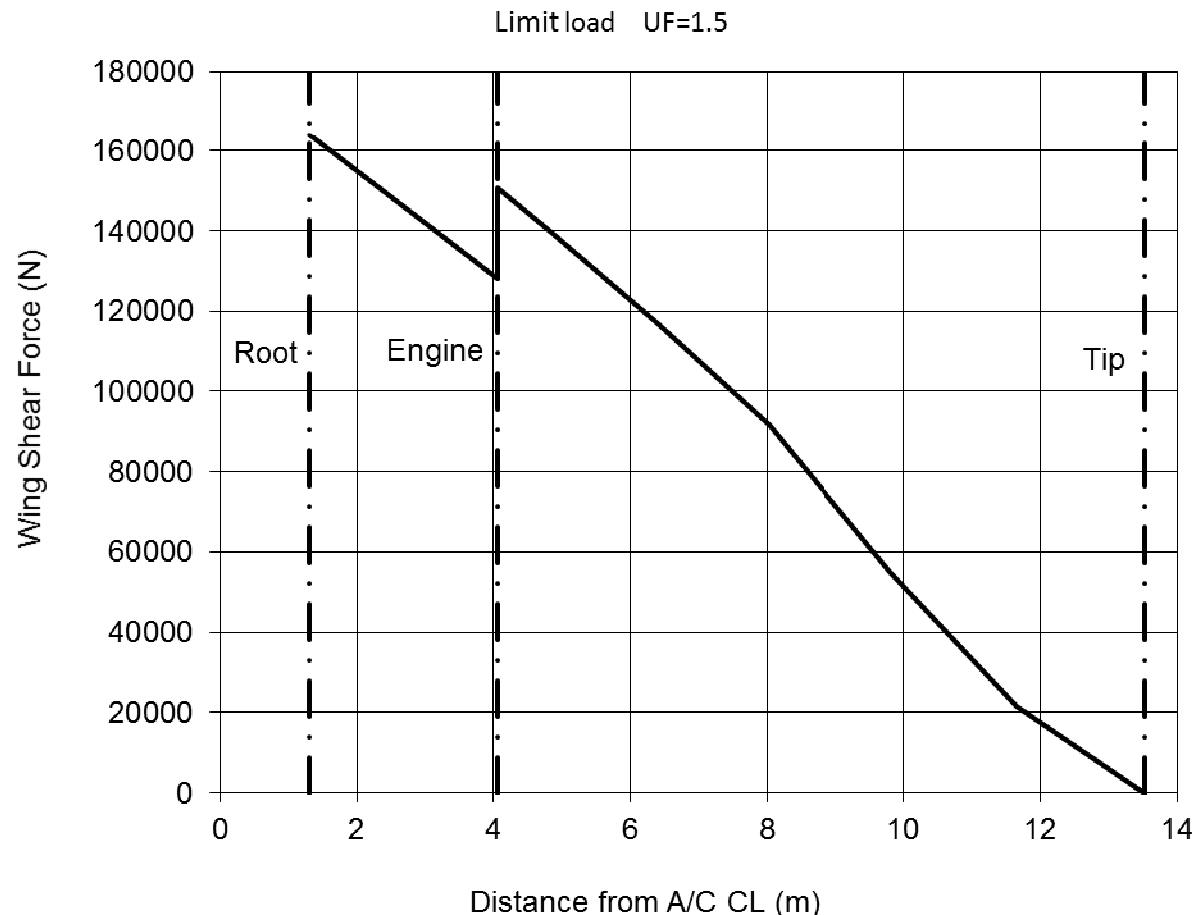
Use 927kg at 2.0m fwd of Ref Axis (per side)



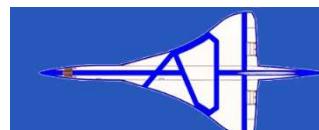
Distributed Load to Point Load



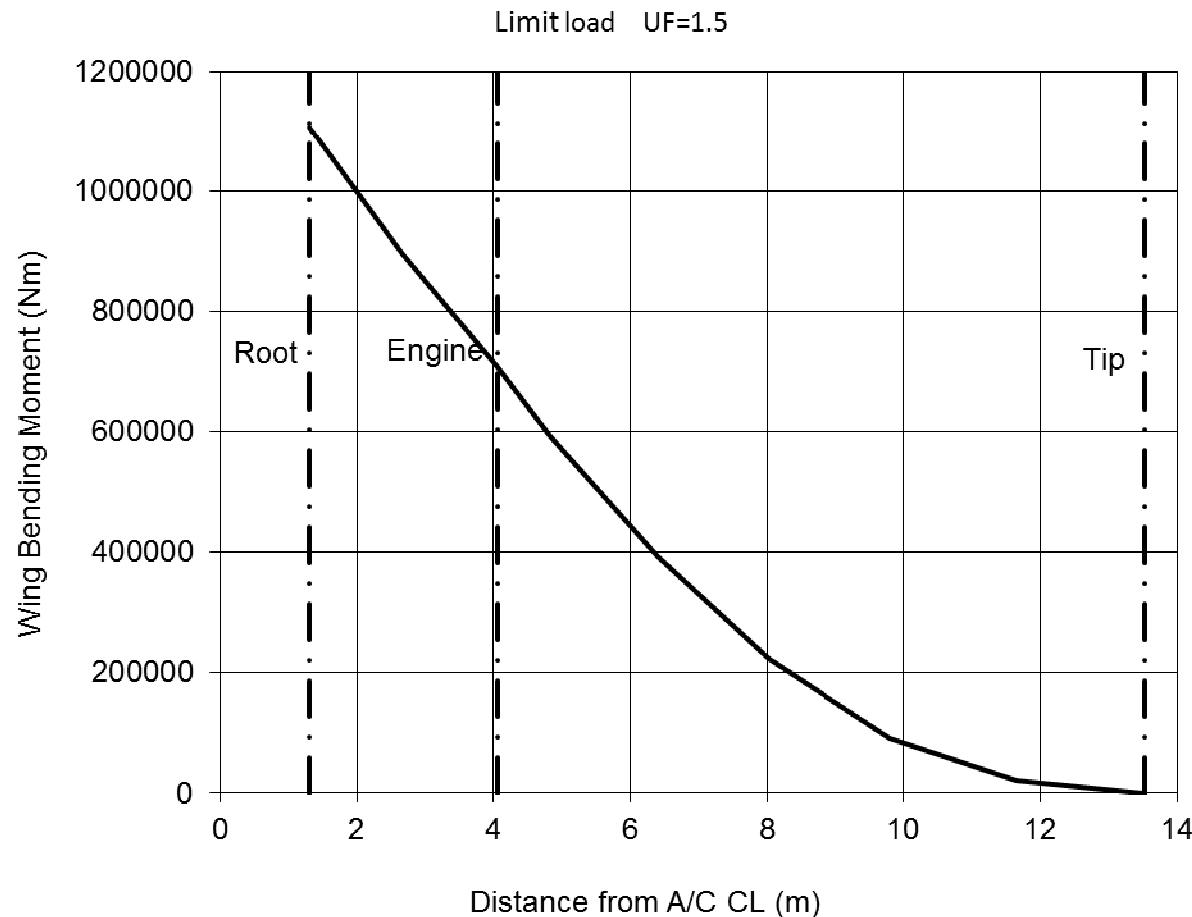
Wing Shear Force (2.5g)



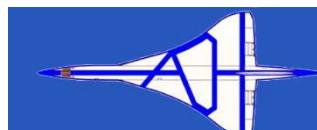
ATR 72

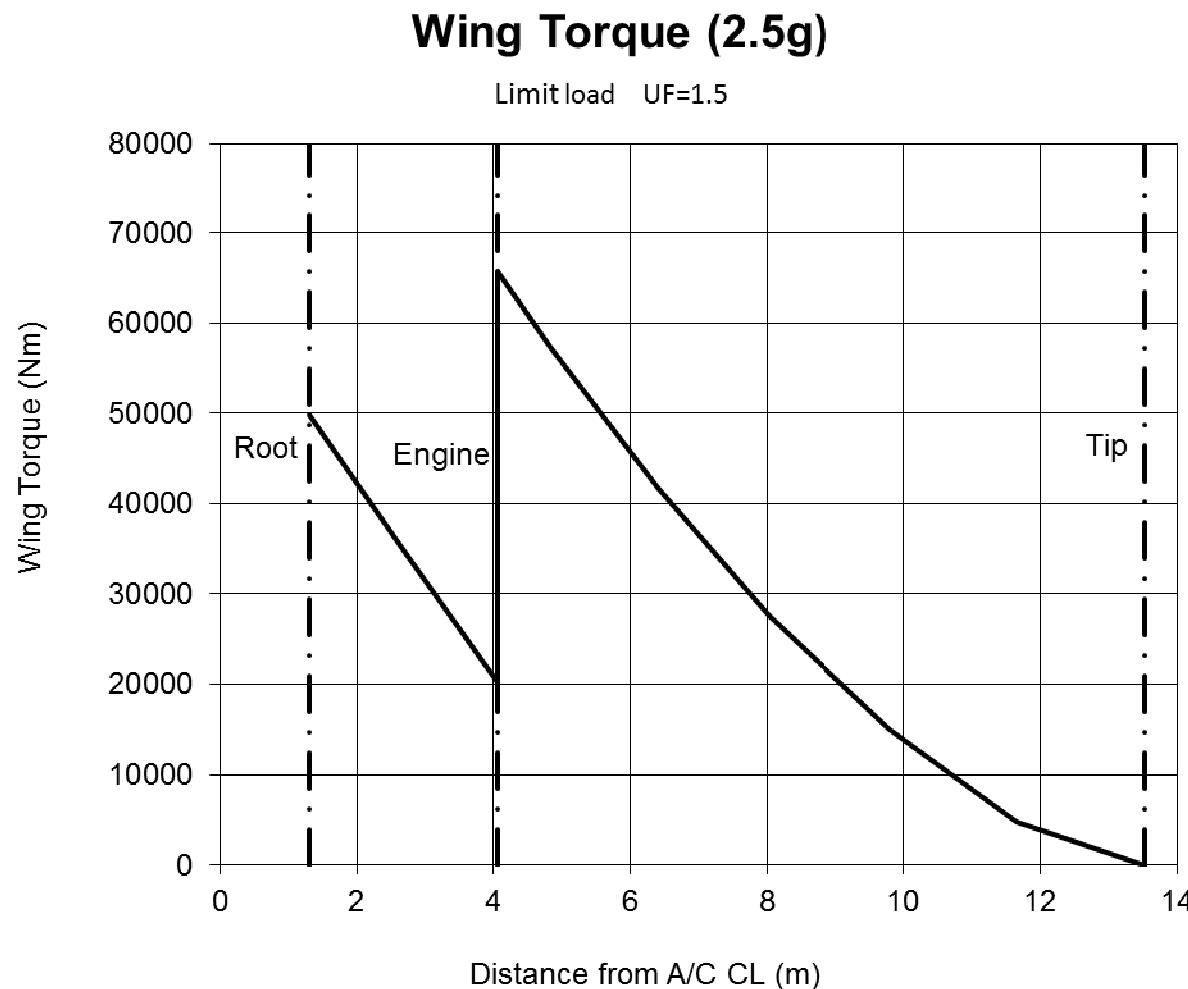


Wing Bending Moment (2.5g)

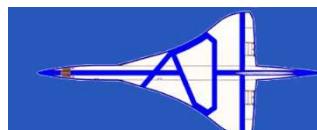


ATR 72



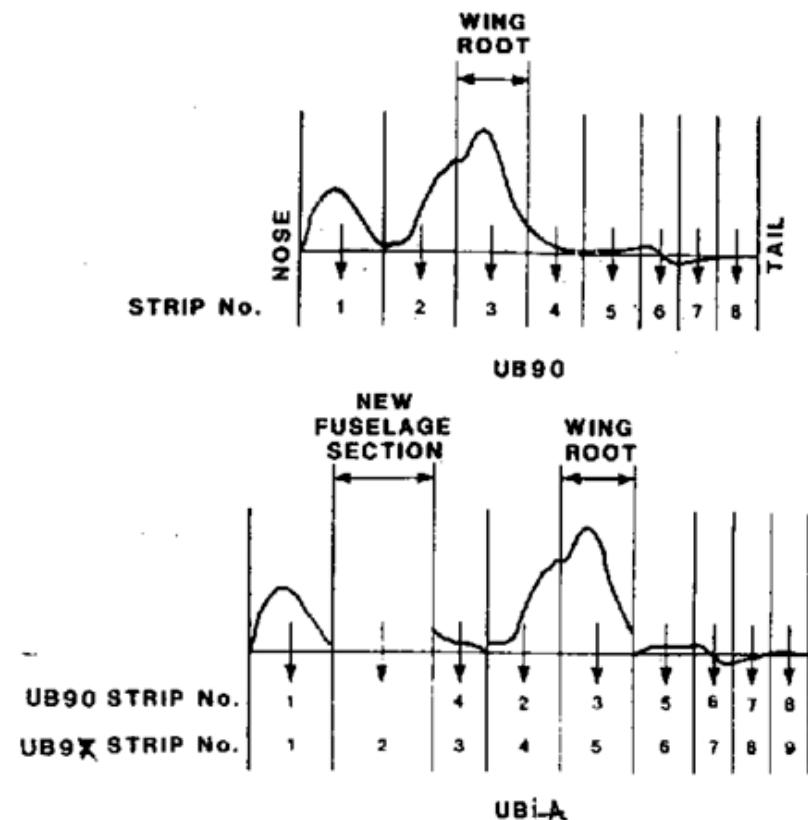


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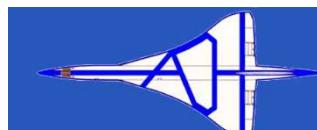
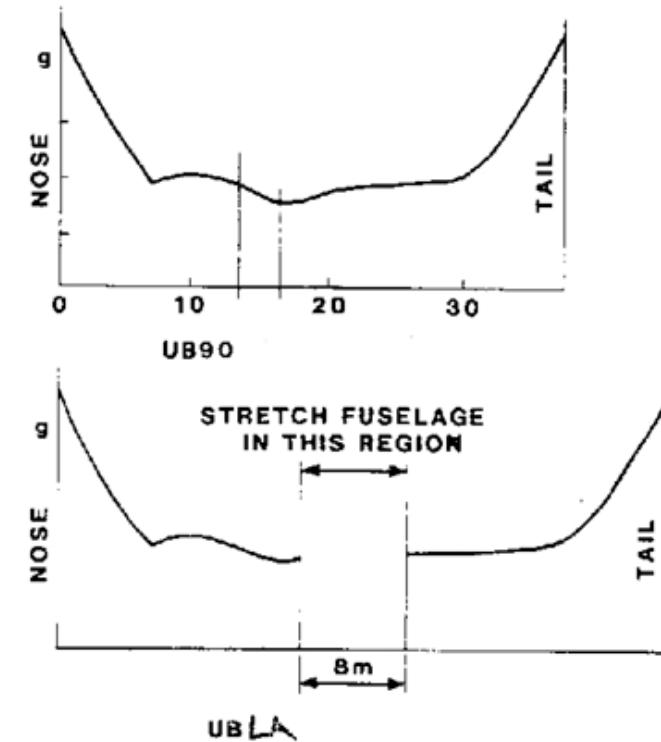


Suggestions when Changing Fuselage Length

Fuselage Aerodynamic Distribution



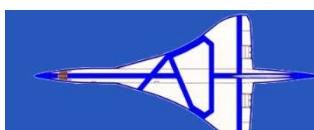
Fuselage Vertical Inertia Factor (Flexible Landing)



Wing Geom

	given	calc	calc	given			
			wing geom				
strip	bdy	width	CL	chord	wc^2	Ref Axis	LE
	(m)	(m)	(m)	(m)	(m^3)	(m)	aft Datum
cl		0					0
Root	1		2	1	6.000	72.0000	1.670
	2		2	3	5.481	60.0722	2.530
	4						0.5195
LG	3		0	4	4.961	0.0000	2.960
	4		1.85	4.925	4.481	37.1389	3.357
	5.85						1.5195
Pod	5		0	5.85	4.000	0.0000	3.755
	5.85						2.0000
	6		3.75	7.725	3.610	48.8809	4.561
Tank Bdy	9.6						2.9740
	7		3.4	11.3	2.868	27.9573	6.098
Vent T Bdy	13						4.8312
	8		4.4	15.2	2.057	18.6201	7.774
Tip	17.4						6.8571

A320



Wing Mass

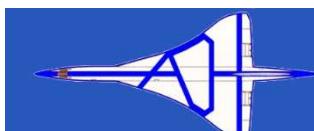
A320



Wing Aero

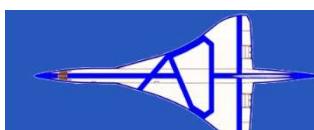
	S(kN)	M(kNm)	T(kNm)		Lwfp=	1886799	qS=	2352830	Values are per side							
	437	3860	-153	Values at ROOT												
strip	Ls/Lwfp	xac/c	xac(RA)	Lso/qS	Crnol	Ls	Lso	Fs	SF	mean SF	dMR	MR	Mol	Fs*xac	MPs	MP
1	0	0	0	0	0	0	0	0	820783	6782788.4	0	0	0	97598		
2	0.1656	0.2842	0.4528	0.00227	-0.0927	156211	2673	158884	820783	1641565.6	5141222.7	-103021	71947	-31074	97598	
3	0.0000	0.0000	0.0000	0.00000	0.0000	0	0	0	661899	741341	1482681.8	3658540.9	0	0	0	128672
4	0.1524	0.2632	0.6587	-0.00186	-0.1153	143777	-2194	141584	661899	591107	1093548.3	3658540.9	-79247	93262	14016	128672
5	0.0000	0.0000	0.0000	0.00000	0.0000	0	0	0	520315	520315	0	2564992.6	0	0	0	114656
6	0.2300	0.2759	0.5908	0.00253	-0.1136	216994	2982	219976	520315	410328	1538728.7	-102728	129956	27228		114656
7	0.1749	0.2537	0.5391	0.00261	-0.0768	165048	3065	168113	300340	216284	735364.04	1026263.9	-39717	90630	50913	87428
8	0.1374	0.2064	0.4925	0.00225	-0.0830	129577	2650	132227	132227	66114	290899.85	290899.85	-28607	65122	36515	36515
									0			0			0	

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Wing Results

A320



Fuselage Geom

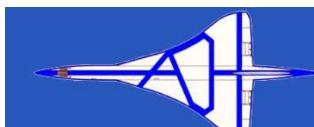
	strip	bdy	width	CL	chord
	given	calc	calc	given	
	strip	strip	strip	Fuse	
	strip	bdy	width	CL	width
		(m)	(m)	(m)	(m)
Nose		0			
	1		5.08	2.54	4.058
		5.08			
NLG	2		0	5.08	4.058
		5.08			
	3		1.88	6.02	4.058
F24		6.96			
	4		3.2	8.56	4.058
F30		10.16			
	5		3.2	11.76	4.058
FS		13.36			
	6		0.48	13.6	4.058
		13.84			
WRAD	7		0	13.84	4.058
		13.84			
	8		2.28	14.98	4.058
RS		16.12			
	9		2.7	17.47	4.058
F47		18.82			
	10		4.26	20.95	4.058
F55		23.08			
	11		4.82	25.49	4.058
F64		27.9			
	12		3.22	29.51	4.058
P Bulkhead		31.12			
	13		0.88	31.56	4.058
		32			
Fin	14		0	32	4.058
		32			
	16		1	32.5	4.058
		33			
Tailplane	17		0	33	4.058
		33			
	18		4.58	35.29	4.058
Tail		37.58			

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Fuselage Mass

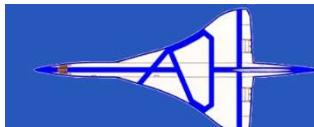
A320



Fuselage Aero

				Lwfp=	1886799	qS=	2352830	Values are per side		
strip	Ls/Lwfp	Lso/qS	Ls	Lso	Fs	SF	mean SF	dM	M	
1	0.030	-0.023	56839	-54970	1869	0	935	4747	0	
2	0.000	0.000	0	0	0	1869	1869	0	4747	
3	0.003	0.004	6124	9408	15532	17401	9635	18114	22861	
4	0.005	0.005	10097	12840	22936	40337	28869	92382	115244	
5	0.036	-0.003	67944	-6202	61742	102079	71208	227867	343111	
6	0.008	-0.003	15124	-6153	8971	111050	106565	51151	394262	
7	0.000	0.000				61614			-733591	
8	0.037	-0.004	69035	-9879	59156	2459	32037	73043	-806634	
9	0.014	0.001	27080	3153	30233	-27774	-12658	-34176	-772458	
10	0.004	0.008	7201	18449	25649	-53423	-40599	-172950	-599509	
11	0.005	-0.003	9606	-6111	3496	-56919	-55171	-265924	-333585	
12	-0.001	0.000	-1523	1018	-505	-56414	-56666	-182465	-151120	
13	-0.001	0.002	-1290	4682	3393	-59806	-58110	-51137	-99984	
14	0.000	0.000	0	0	0	-59806		0	-99984	
16	-0.001	0.004	-1545	9333	7788	-67594	-63700	-63700	-36284	
17	0.000	0.000	0	0	-72569	4976	-31309	-47678	11394	
18	-0.001	0.003	-1104	6080	4976	0	2488	11394	0	
Tailplane A										
Fs= -72569 N at 33.657 m from nose										
dM= -47678 Nm										

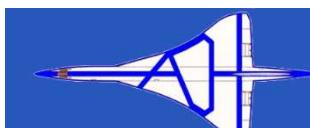
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Fuselage Results

strip	SF (mass)	SF (aero)	SF (total)	M (mass)	M (aero)	M (total)		S (N)	M (Nm)	Defn	strip	bdy (m)
1	0	0	0	0	0	0		0	0	Nose	1	0
2	-91788	1869	-89919	-233141	4747	-228394		-89919	-228394	NLG	2	5.08
3	-91788	1869	-89919	-233141	4747	-228394		-89919	-228394		3	5.08
4	-133008	17401	-115606	-444449	22861	-421587		-115606	-421587	F24	4	6.96
5	-227741	40337	-187404	-1021647	115244	-906404		-187404	-906404	F30	5	10.16
6	-323783	102079	-221704	-1904087	343111	-1560976		-221704	-1560976	FS	6	13.36
7	-338260	111050	-227210	-2107880	394262	-1713618		-227210	-1713618	WRAD	7	13.84
8	-525356	61614	-463741	-4453507	-733591	-5187098		-463741	-5187098		8	13.84
9	-455229	2459	-452770	-3335641	-806634	-4142275		-452770	-4142275	RS	9	16.12
10	-342965	-27774	-370739	-2258080	-772458	-3030538		-370739	-3030538	F47	10	18.82
11	-221896	-53423	-275320	-1054924	-599509	-1654433		-275320	-1654433	F55	11	23.08
12	-88556	-56919	-145474	-306734	-333585	-640319		-145474	-640319	F64	12	27.9
13	-37105	-56414	-93519	-104420	-151120	-255541		-93519	-255541	P Bulkhead	13	31.12
14	-32300	-59806	-92106	-73882	-99984	-173866		-92106	-173866	Fin	14	32
16	-27299	-59806	-87105	-65595	-99984	-165578		-87105	-165578		16	32
17	-20871	-67594	-88465	-41510	-36284	-77793		-88465	-77793	Tailplane	17	33
18	-14458	4976	-9482	-33108	11394	-21714		-9482	-21714		18	33
	0	0	0	0	0	0		0	0	Tail		37.58

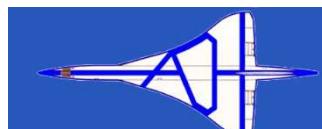
A320



Short Range vs Long Range OR Small vs Large

The following values are for a mainly metal structure

	Short Range OR Small	Long Range OR Large
Wing Stringer Pitch Upper cover Lower cover	165 mm 165mm	205mm 180mm
Rib Pitch	650mm	820mm
Design Service Goal	60000 Flight Cycles 100000 Flight Hours	19000 Flight Cycles 140000 Flight Hours
Mission	Short Range	17% Short Range 59% Medium Range 24% Long Range
Fuselage Frame Pitch	21inches(533mm)	533 or 600mm
Fuselage Stringer Pitch	180mm	180mm

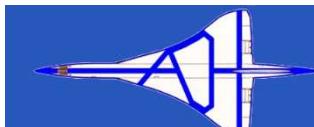


Summary of Objectives for Design Project

- ▶ This is NOT to demonstrate that you can carry out a skin/stringer compression panel analysis or similar detailed design exercise, but will assess you on understanding of the structural components, their positioning, their functions and their classification.
- ▶ You will need to demonstrate attention to:
 - **Loads**

Know what load cases drive which types of structure, and what kind of loads

- Load cases (via n-v diagram and prescribed cases, also via weight-cg and mission profile)
- Derive SMT loading and running loads for wings, SF, BM, torque diagrams for wing and fuselage for all identified cases
- Ground loads, identify cases
- Load alleviation – can you make structure lighter by active or passive load alleviation
- Spanwise CP position – ib = good for structures bad for aero, where do you put it?
- Internal pressure loads – what are the cases? (NB Airbus may be able to provide an envelope acceleration plot)
- Brazier loads, use "classical" methods to derive the loads
- Thermal loads if dis-similar materials are used anywhere, if differential thermal effects take place can we design the structure to avoid picking up the loads?



Summary of Objectives for Design Project

- **Geometry –**
- **wing**
 - Structure positioning, front spar, rear spar,
 - Key rib positions,
 - rib pitches and orientation,
 - stringer pitches and orientation,
 - Gear, flap track and engines
 - Systems, vents, pumps etc
 - Manholes
- **fuselage**
 - Cross section geometry
 - Frame geometry and stringer positions
 - Floor beams
 - Doors – cargo and pax
 - Main structural item positons,
 - ▶ Gear
 - ▶ Engines (if applicable)
 - ▶ Empenage
 - ▶ APU
 - ▶ Wingbox



Summary of Objectives for Design Project

– **Integration**

Understand the influence of each of these with respect to the wingbox

- LE devices (slats etc, if applicable)
- MLG (if applicable)
- Engine (if applicable)
- Flaps
- failsafe and crashworthiness issues

– **Wing fuel tank layouts**

Basic fuel systems integration, engine feed, venting, refueling pipe and pump locations, tank boundaries, lightning strike requirements, dry bay requirements

– **Principal structural design drivers**

- Damage tolerance
- Fatigue
- Stability
- Static Strength
- Max and min thickness drivers

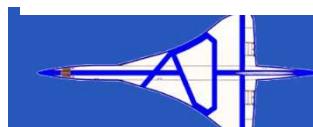
– **Material selection**

Weight savings for composite structures should be considered carefully, a clean wing will enable much larger weight savings than one with many local load inputs.

- Composite
 - Manufacturing processes, build procedures, tolerances, section join-ups
 - Laminate design (stacking rules, ply orientations etc)
- Metallic
 - Manufacturing processes
 - Alloy choices

– **Weights**

- Bottom up calc – this will be difficult at this stage of the design but spot checks would be useful



Summary of Objectives for Design Project

– **Integration**

Understand the influence of each of these with respect to the wingbox

- LE devices (slats etc, if applicable)
- MLG (if applicable) – what support structure will this need?
- Engine (if applicable)
- Flaps
- failsafe and crashworthiness issues

– **Wing fuel tank layouts**

Basic fuel systems integration,

- engine feed routing,
- venting,
- refuel/defuel piping,
- pump locations,
- tank boundaries (considering unconstrained rotor burst failure),
- lightning strike zone requirements,
- dry bay requirements



Summary of Objectives for Design Project

- ▶ In your section you should ALWAYS include:
 - a 3-view GA
 - Wing planform showing
 - high lift surfaces and types (eg slats, krugers, droop nose, single or double slotted flaps)
 - control surfaces ailerons and spoilers
 - structural datums for spars, ribs etc
 - tank geometry,
 - fuel systems basic architecture,
 - gear position, ie footprint and support positions
 - a/c CG position,
 - Wing Aerodynamic Centre position
 - Fuselage layout, showing;
 - Nose gear position
 - Pressure bulkheads
 - Wing centre box
 - Gear positions (if applicable)
 - Engine positions (if applicable)
 - Diagrams of engine attachment, gear attachment showing load cases applied
 - Show how the structures can assist in the low cost carrier design goal, investigate the compromises along the design path.

