

1 Antiderivatives

1. Solve the initial-value problem (i.e., find an equation for y).

$$\frac{dy}{dt} = \sqrt{t} + \frac{2}{\sqrt{t}}, \quad t > 0, \quad y(1) = 5.$$

2. Find f .

(a) $f''(x) = 6x + 12x^2$.

(b) $f''(x) = \sin \theta + \cos \theta, \quad f(0) = 3, \quad f'(0) = 4$.

3. A particle moves along a straight line with velocity function $v(t) = \sqrt{x}(6 + 5x)$. It's displacement at $t = 1$ is 10 m. Find its position function $s(t)$.

2 Integrals

1. Recall the following definition.

The area A of the region S that lies under the graph of the continuous function f is the limit of the sum of the areas of approximating rectangles:

$$A = \lim_{n \rightarrow \infty} R_n = \lim_{n \rightarrow \infty} [f(x_1)\Delta x + \dots + f(x_n)\Delta x] = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i)\Delta x.$$

Use this definition to find an expression for the area under the graph of f as a limit. Do not evaluate the limit.

$$f(x) = \frac{2x}{x^2 + 1}, \quad 1 \leq x \leq \pi/3.$$

2. A table of values of an increasing function f is shown. Use the table to find lower and upper estimates for $\int_{14}^{26} f(x) dx$.

x	14	18	22	26
$f(x)$	-6	-2	1	3

3. Evaluate the integral by interpreting it in terms of areas.

(a) $\int_{-1}^2 |x| dx$.

(b) $\int_{-3}^0 (1 + \sqrt{9 - x^2}) dx$.