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Algorithms

Examples

1. Demonstrate bubble sort to sort the list 3, 4, 2, 1.

Solution: On the first pass, we go $3421 \rightarrow 3241 \rightarrow 3214$, on the next pass we do $3214 \rightarrow 2314 \rightarrow 2134$ and on the third pass we do $2134 \rightarrow 1234$ and on the fourth pass, we make no changes which means the algorithm terminates.

2. Demonstrate the quick sort to sort the list 3, 6, 2, 5, 1, 4.

Solution: First we place the first number in the appropriate position and put the numbers smaller before it and the numbers larger after while preserving their relative order to get $362514 \rightarrow 213654$. Now we do the same on the smaller numbers and the larger to get $21 \rightarrow 12$ and $654 \rightarrow 546 \rightarrow 456$. This finally sorts the list as 123456.

3. Demonstrate the stable matching algorithm when men and women have the preferences $m_1: w_1 > w_2, m_2: w_1 > w_2$ and $w_1: m_1 > m_2, w_2: m_1 > m_2$.

Solution: Both men will propose to woman 1 and she will choose man number 1. Then man 2 will propose to his next option which is woman 2 and she will accept him. Thus, we get the final pairing $(m_1, w_1), (m_2, w_2)$.

Problems

- 4. **TRUE** False The stable matching algorithm with always produce a matching that is stable.
- 5. True **FALSE** There is only one stable matching.
- 6. Three women A, B, C are proposing to men E, F, G. Their preferences are as follows:

A	В	С	E	F	G
E > G > F	E > G > F	G > E > F	C > A > B	A > B > C	B > C > A

Show the stable matching algorithm with the women proposing to the men by clearly showing all rounds in a table.

Solution: E A, B A A, C C C F C C, B B B, A B	Solution:	Men	Rd 1	Rd 2	Rd 3	Rd 4	Rd 5
F <u>A</u>		Е	A, B	A	A, C	С	С
G C C, B B B, A B		F					A
		G	С	C, B	В	В, А	В

7. Sort the list 2, 1, 6, 4, 5, 3 using both bubble sort and quicksort.

Solution: Using bubble sort, we get

$$216453 \to 124536 \to 124356 \to 123456$$

Using quicksort using the last number as a pivot, we get

$$216453 \rightarrow 213645 \rightarrow (12)3(456)$$
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