

A Mathematical Exploration of the Hover Slam Manuever

A Mathematical Exploration



Contents

1 Introduction

On December 21st, 2015. SpaceX, the privately owned space company, successfully landed the booster stage (Also referred to as the first stage) of the *Falcon 9* back at their launch site in Cape Canaveral, Florida. This is considered by some to be the next major advancement towards making humans an interplanetary species. Elon Musk, the founder and CEO of the company intends to achieve "plane-like" levels of rapid reusability of rockets, in hopes that this will help propel humans towards Mars.

SpaceX has since then, successfully landed their first stage rocket boosters a total of **XX** times, both at land and on a barrage in the ocean.

I still vividly remember the moment my heart skipped a beat as the rocket landed, and my previous passion for spaceflight was reignited.

With my passion at it's peak I began playing the video game "Kerbal Space Program", a game described as a "Spaceflight sandbox". In the game, you design your own rockets and control their maneuvering as you like. After watching the Falcon 9 land I started recreating the rocket in the game. I then quickly realized how complicated it was to preform a propulsive landing of its first stage. The complexity of the landing intrigued me. And as I eventually learned how to adjust the timing and thrust of the engines I figured it would be easier to create a script that will do this for me, much like this is done in real life. One of the hardships I encountered was to figure out how to determine when I was going to fire my engines to perform this so-called "hover slam" maneuver (also called the "suicide burn").

I therefore decided to dedicated my Mathematics IA to exploring this topic and figuring out how to achieve a perfect and autonomous landing.

2 Background theory

2.1 The maneuver

Before one can begin to explore the mathematics behind the maneuver, it is important to understand what a hover slam is. The Maneuver can be broken down into **3** phases:

Step 1: The Pre-Entry Phase

This is the phase before the spacecraft enters the denser part of the atmosphere. What happens in this phase is the orientation, boost-back burn, and the entry-burn. The purpose of this stage is to prepare the booster for immense mechanical stress of entering the atmosphere at high speeds, and to align its ballistic trajectory towards its desired landing location. In most cases, this requires a "boost-back" burn, where the rocket could either turn its trajectory 180° *back to the launch site*.

See illustration 1 for a visual representation.

Step 2: The Entry Phase

Step 3: The Landing Phase The hover slam is a term for a Manuever in which the spacecraft awaits the retro-grade firing to slow it self down so that a landing with an intact spacecraft can take place of its

The more slang-like term of the hover slam: the "suicide burn" explains the consequence that occurs if the manuever was not completed successfully,