

Generate the datasets A and B in  $\mathbb{R}^2$  with each of them consisting 2000 data points from normal distribution. The dataset A and B has been drawn from the  $N(\mu_1, \Sigma_1)$  and  $N(\mu_2, \Sigma_2)$ . Let us fix the  $\mu_1 = [-1, 1]$  and  $\mu_2 = [1, 1]$ .

- a. Find the optimal decision boundary for the classification of the dataset A and B using  $\Sigma_1 = \Sigma_2 = \begin{bmatrix} 0.6 & 0 \\ 0 & 0.6 \end{bmatrix}$ . Plot the dataset A and B with different colors and plot the obtained optimal decision boundary. Comment on the characteristics of obtained decision boundary.
- b. Find the optimal decision boundary for the classification of the dataset A and B using  $\Sigma_1 = \Sigma_2 = \begin{bmatrix} 0.7 & 0 \\ 0 & 0.3 \end{bmatrix}$ . Plot the dataset A and B with different colors and plot the obtained optimal decision boundary. Comment on the characteristics of obtained decision boundary.
- c. Find the optimal decision boundary for the classification of the dataset A and B using  $\Sigma_1 = \Sigma_2 = \begin{bmatrix} 0.6 & 0.25 \\ 0.25 & 0.4 \end{bmatrix}$ . Plot the dataset A and B with different colors and plot the obtained optimal decision boundary. Comment on the characteristics of obtained decision boundary.