

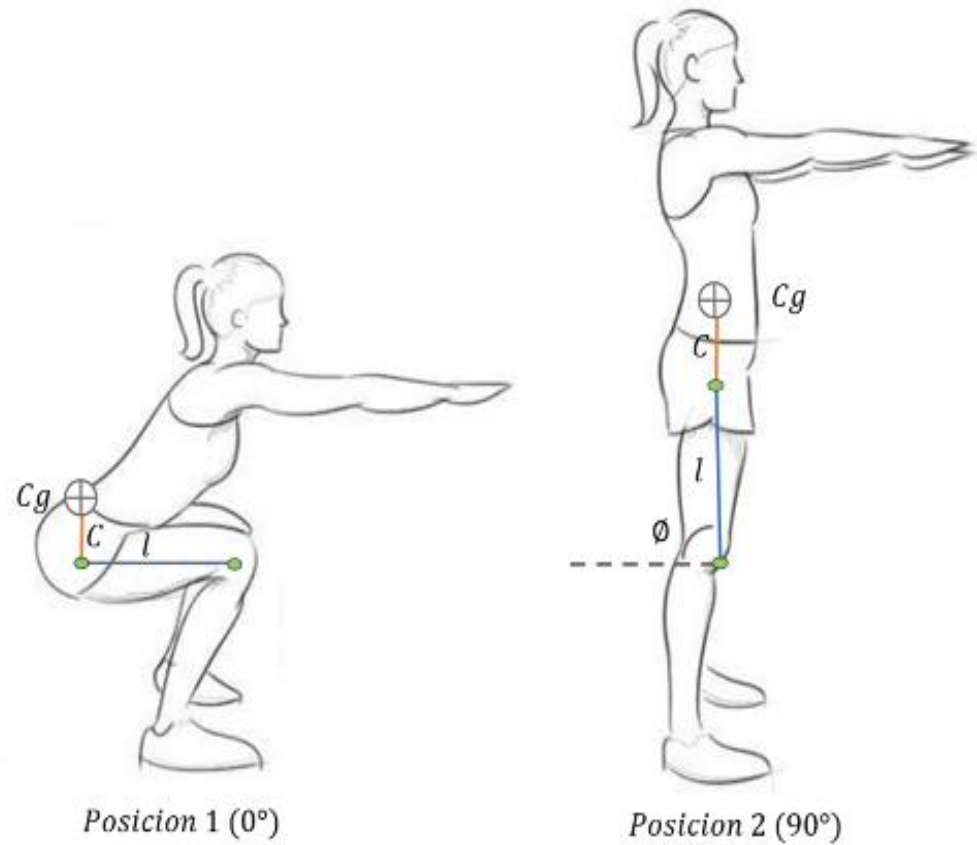
# Design of the Compliant Mechanism of a Biomechanical Assistive Device for the Knee

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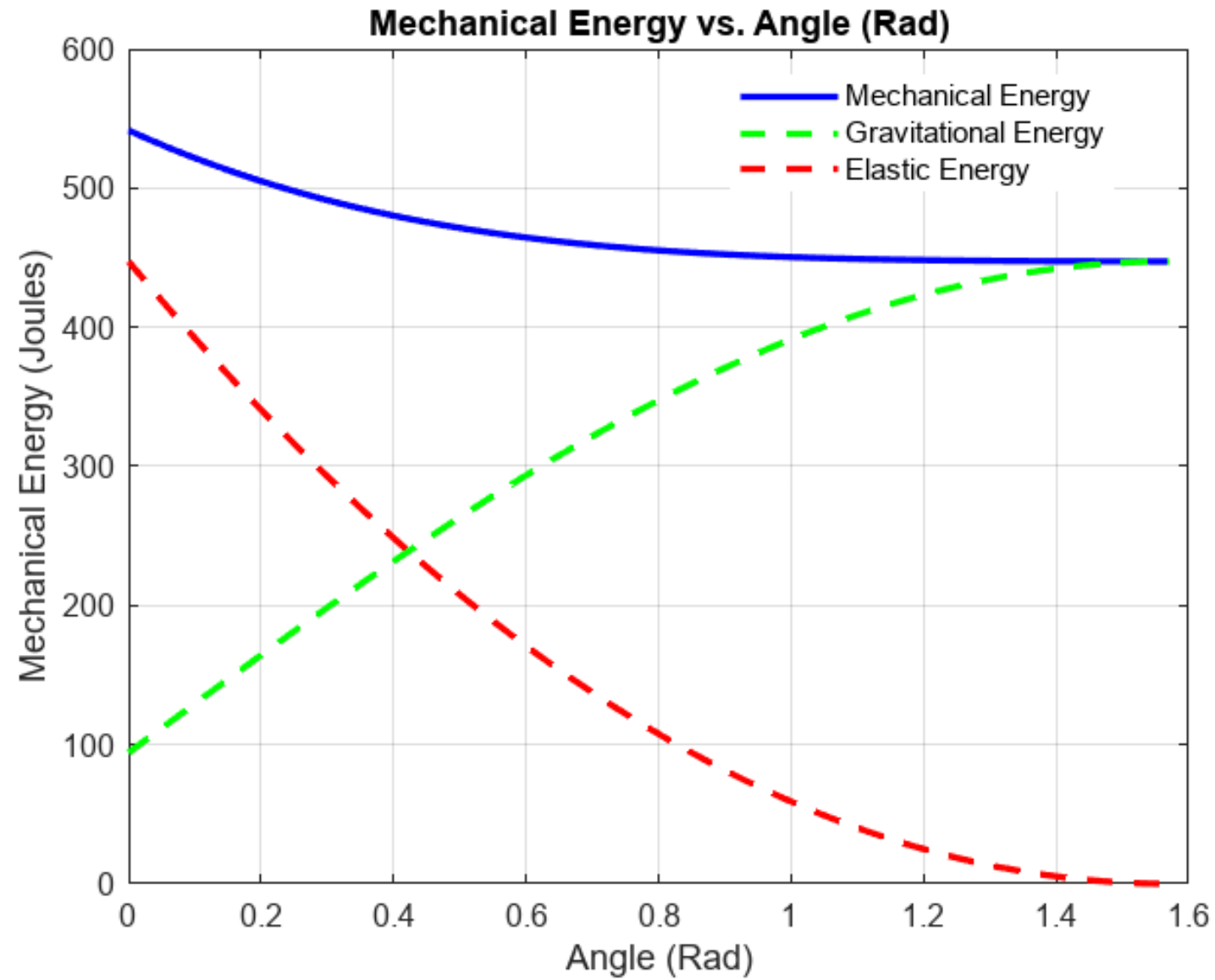
**PUCP**



Supplemental Fig. 1. Study conditions for the energy balance.

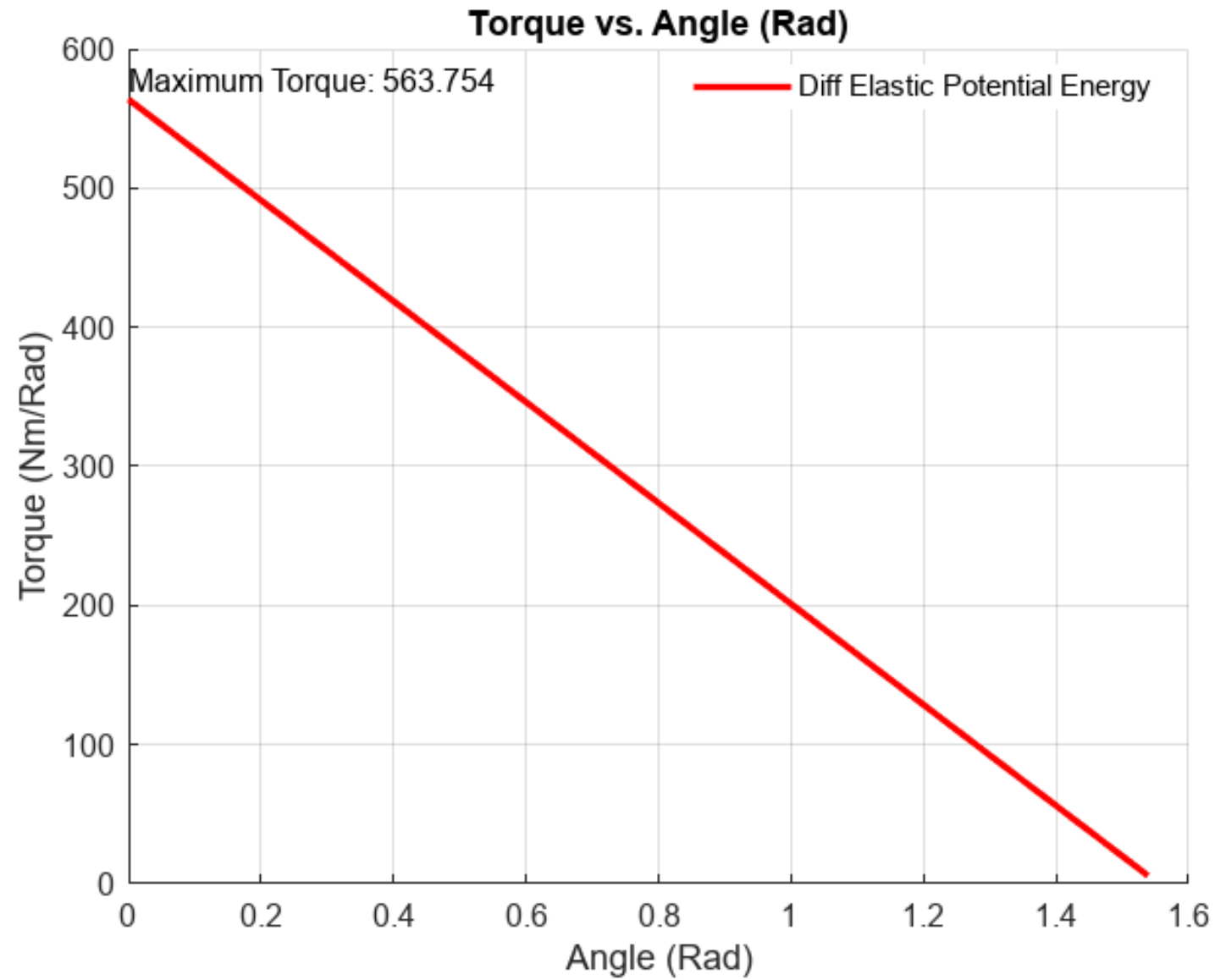
*Adapted from:*

<https://i.pinimg.com/originals/51/90/f4/5190f41ff6c399ce0f657b9c7adee82a.jpg>



Supplemental Fig. 2. Behavior of mechanical energy as a function of angle.

*Source: Matlab*



Supplemental Fig. 3. Torque vs position relationship.

*Source: Matlab*



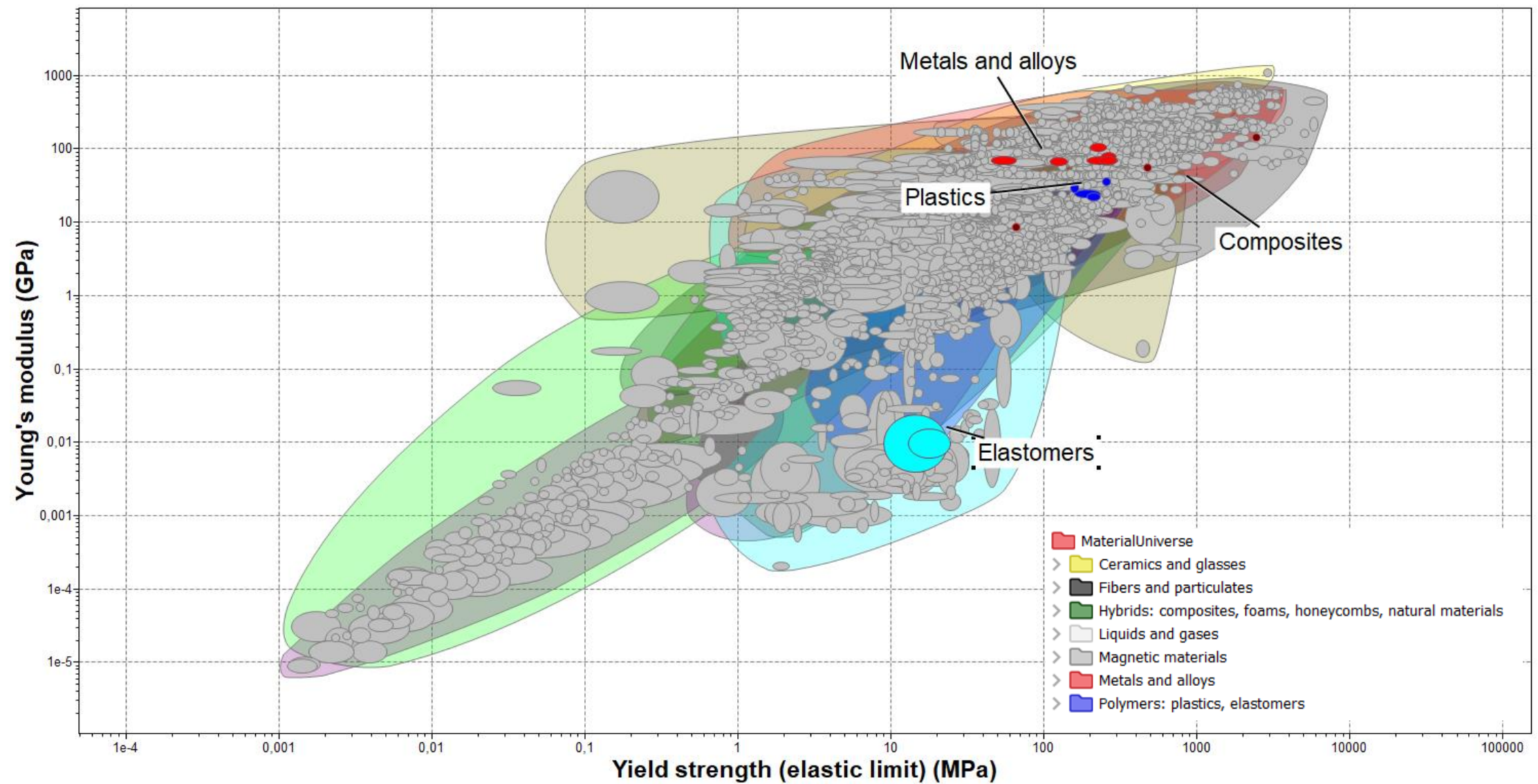
Supplemental Fig. 4. 3D model of the patient's left leg.

# SUPPLEMENTAL TABLE I

## SELECTION CRITERIA

Units	Attribute	Constant
<i>N/A</i>	Materials group	Biomaterials
<i>Kg/m<sup>3</sup></i>	Density,	$1e3 < x < 5e4$
<i>GPa</i>	Young's modulus	$< 1e4$
<i>MPa</i>	Yield strength	$< 1e4$
<i>MPa</i>	Tensile Strength	$< 1e4$
<i>N/A</i>	Magnetic type	Non-magnetic
<i>N/A</i>	Medical grades? (USP Class VI, ISO 10993)	Yes
<i>N/A</i>	Sterilizability (steam autoclave)	Yes
<i>N/A</i>	Guidance for MRI Safety	Good, Excellent
<i>N/A</i>	RoHS 2 (EU) compliant grades?	Low Risk for Potential Interaction
<i>N/A</i>	SIN List indicator (0-1, 1 = high risk)	$> 0$
<i>N/A</i>	Contains $> 5\text{wt}\%$ critical elements?	No
<i>N/A</i>	Water (salt)	Limited use, Acceptable, Excellent
<i>N/A</i>	Weak acids	Limited use, Acceptable, Excellent
<i>N/A</i>	Strong acids	Unacceptable, Limited use, Acceptable, Excellent
<i>N/A</i>	Weak alkalis	Limited use, Acceptable, Excellent
<i>N/A</i>	Strong alkalis	Limited use, Acceptable, Excellent
<i>N/A</i>	Organic solvents	Limited use, Acceptable, Excellent
<i>N/A</i>	UV radiation (sunlight)	Fair, Good, Excellent
<i>N/A</i>	Flammability	Slow burning, Self-extinguishing, Non-flammable

*Source: Granta Edupack*



Supplemental Fig. 5. Young's Modulus (E) Vs Yield Stress ( $\sigma_y$ ).

Source: Granta Edupack

# SUPPLEMENTAL TABLE II

## COMPARISON OF MATERIALS

Units	Atribut	Peek (30% carbon fiber)	Peek (40% carbon fiber)
<i>Kg/m<sup>3</sup></i>	Density,	1430	1450
<i>GPa</i>	Young's modulus	22.5	36.55
<i>MPa</i>	Yield strength	208	255
<i>MPa</i>	Tensile Strength	208	276
<i>N/A</i>	Magnetic type	Non-magnetic	Non-magnetic
<i>N/A</i>	Medical grades? (USP Class VI, ISO 10993)	Yes	Yes
<i>N/A</i>	Sterilizability (steam autoclave)	Excellent	Excellent
<i>N/A</i>	Guidance for MRI Safety	Good, Excellent	Good, Excellent
<i>N/A</i>	RoHS 2 (EU) compliant grades?	Low risk	Low risk
<i>N/A</i>	SIN List indicator (0-1, 1 = high risk)	0	0
<i>N/A</i>	Contains >5wt% critical elements?	No	No
<i>N/A</i>	Water (salt)	Excellent	Excellent
<i>N/A</i>	Weak acids	Excellent	Excellent
<i>N/A</i>	Strong acids	Unacceptable	Unacceptable
<i>N/A</i>	Weak alkalis	Excellent	Excellent
<i>N/A</i>	Strong alkalis	Excellent	Excellent
<i>N/A</i>	Organic solvents	Excellent	Excellent
<i>N/A</i>	UV radiation (sunlight)	Excellent	Excellent
<i>N/A</i>	Flammability	Self-Extinguishing	Self-Extinguishing

*Source: Granta Edupack*



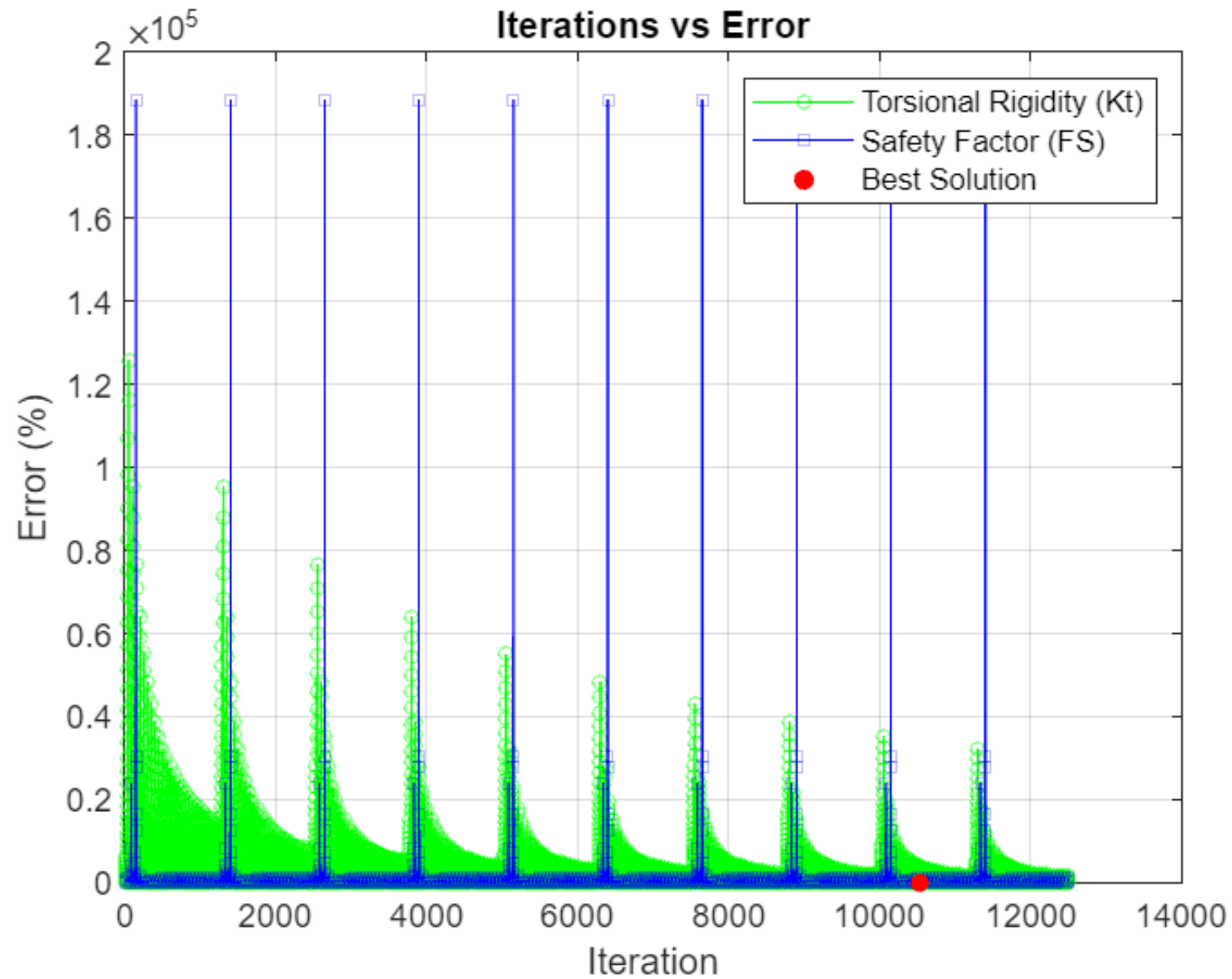
	PEEK (30% carbon fiber)	PEEK (40% carbon fiber)	PEEK/IM carbon fiber, UD prepreg, UD lay-up, 90°	Gold, Jeneric Pentron Rx C, quenched (dental alloy)	Silver, commercial purity, fine, cold worked, hard	Silver, commercial purity, Grade 99.9, cast (cold worked), hard, bar	Gold, Jeneric Pentron Special Inlay Gold (dental alloy)
General information							
Biomaterials - All	✓	✓	✓	✓	✓	✓	✓
Physical properties							
Density (kg/m <sup>3</sup> )	1430	1450	1560	15500	10500	10500	15400
Mechanical properties							
Young's modulus (GPa)	22,7	36,5	8,8	81,4	71	72	108
Yield strength (elastic limit) (MPa)	208	255	65	261	239	260	224
Tensile strength (MPa)	208	276	65	530	294	296	423
Magnetic properties							
Magnetic type	Non-magnetic	Non-magnetic	Non-magnetic	Non-magnetic	Non-magnetic	Non-magnetic	Non-magnetic
Healthcare & food							
Medical grades? (USP Class VI, ISO 10993)	✓	✓	✓	✓	✓	✓	✓
Sterilizability (steam autoclave)	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
Guidance for MRI Safety	Low Risk for Potential Interaction	Low Risk for Potential Interaction	Low Risk for Potential Interaction	Low Risk for Potential Interaction	Low Risk for Potential Interaction	Low Risk for Potential Interaction	Low Risk for Potential Interaction
Restricted substances risk indicators							
RoHS 2 (EU) compliant grades?	✓	✓	✓	✓	✓	✓	✓
SIN List indicator (0-1, 1 = high risk)	0	0	0	0	0	0	0
Critical materials risk							
Contains >5wt% critical elements?	No	No	No	No	No	No	No
Durability							
Water (salt)	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
Weak acids	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
Strong acids	Unacceptable	Unacceptable	Limited use	Excellent	Limited use	Limited use	Excellent
Weak alkalis	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
Strong alkalis	Excellent	Excellent	Acceptable	Excellent	Acceptable	Acceptable	Excellent
Organic solvents	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
UV radiation (sunlight)	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent	Excellent
Flammability	Self-extinguishing	Self-extinguishing	Self-extinguishing	Non-flammable	Non-flammable	Non-flammable	Non-flammable
Enlaces							

Supplemental Fig. 6. Comparison of materials.

Source: Granta Edupack

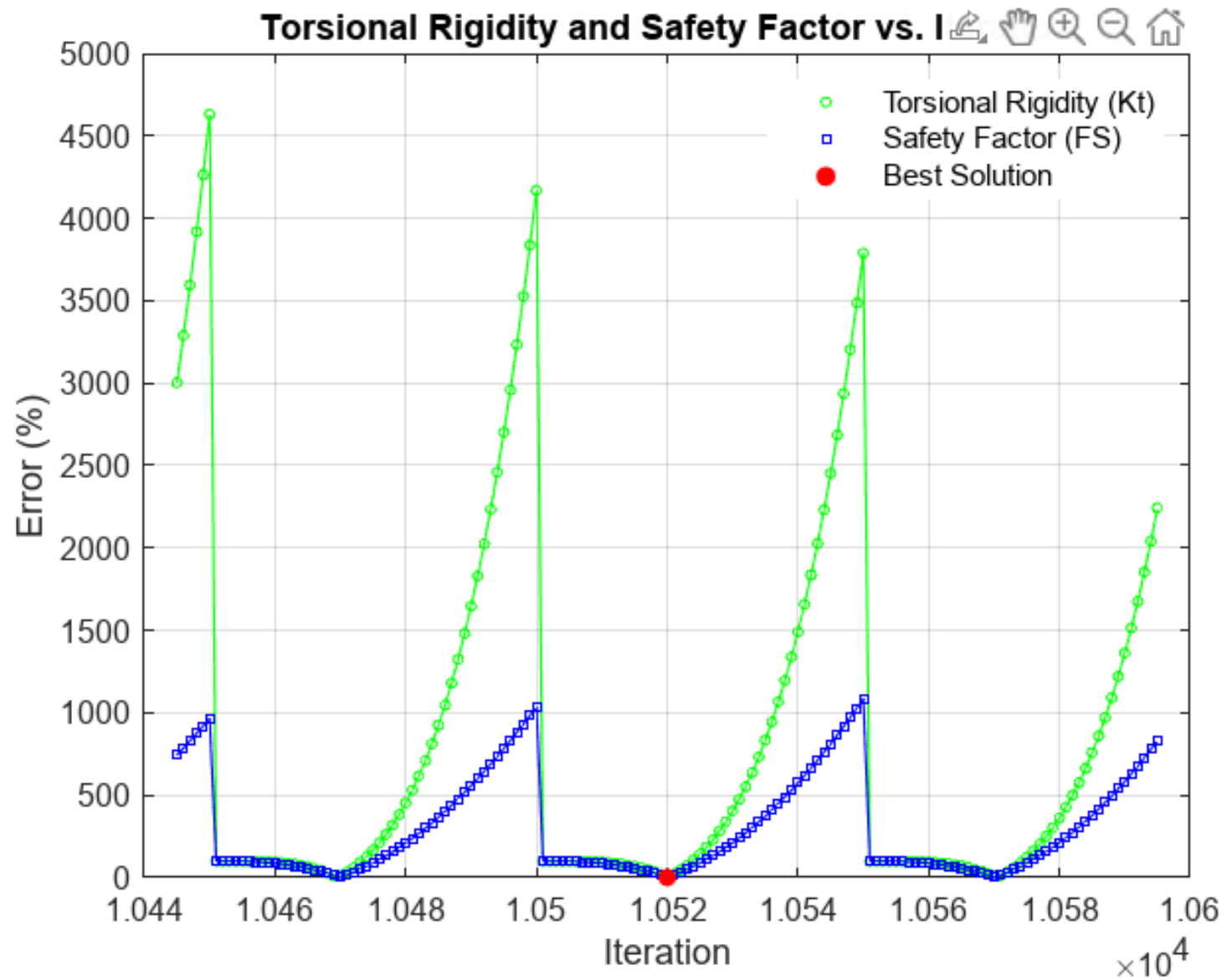
SUPPLEMENTAL TABLE III  
TECHNICAL REQUIREMENTS MATRIX

TECHNICAL REQUIREMENT	DESCRIPTION	METRIC	UNIT	RELEVANCE (1- 10)
Stability and Support	Ability to provide support to the knee.	Maximum load capacity	Newton (N)	9
Controlled Movement	Ability to allow controlled movements.	Degree of limitation	Degrees (°)	8
Comfort	Level of comfort when using the orthosis.	Subjective evaluation	Scale of 1- 10	5
Durability	Resistance to wear and device lifespan.	Test cycles	Cycles	8
Ease of Use	Ease of putting on and taking off the orthosis.	Placement time	Seconds (s)	7
Ventilation	Ability to keep the skin dry.	Subjective evaluation	Scale of 1- 10	6
Weight	Weight of the device.	Total weight	Grams (g)	7
Aesthetic Appearance	Visual appearance of the device.	Subjective evaluation	Scale of 1- 10	5
Safety	Assurance of user safety.	Compliance with regulations	Yes/No	10
Fit	Ability to customize the fit.	Adjustment degrees	Degrees (°)	8



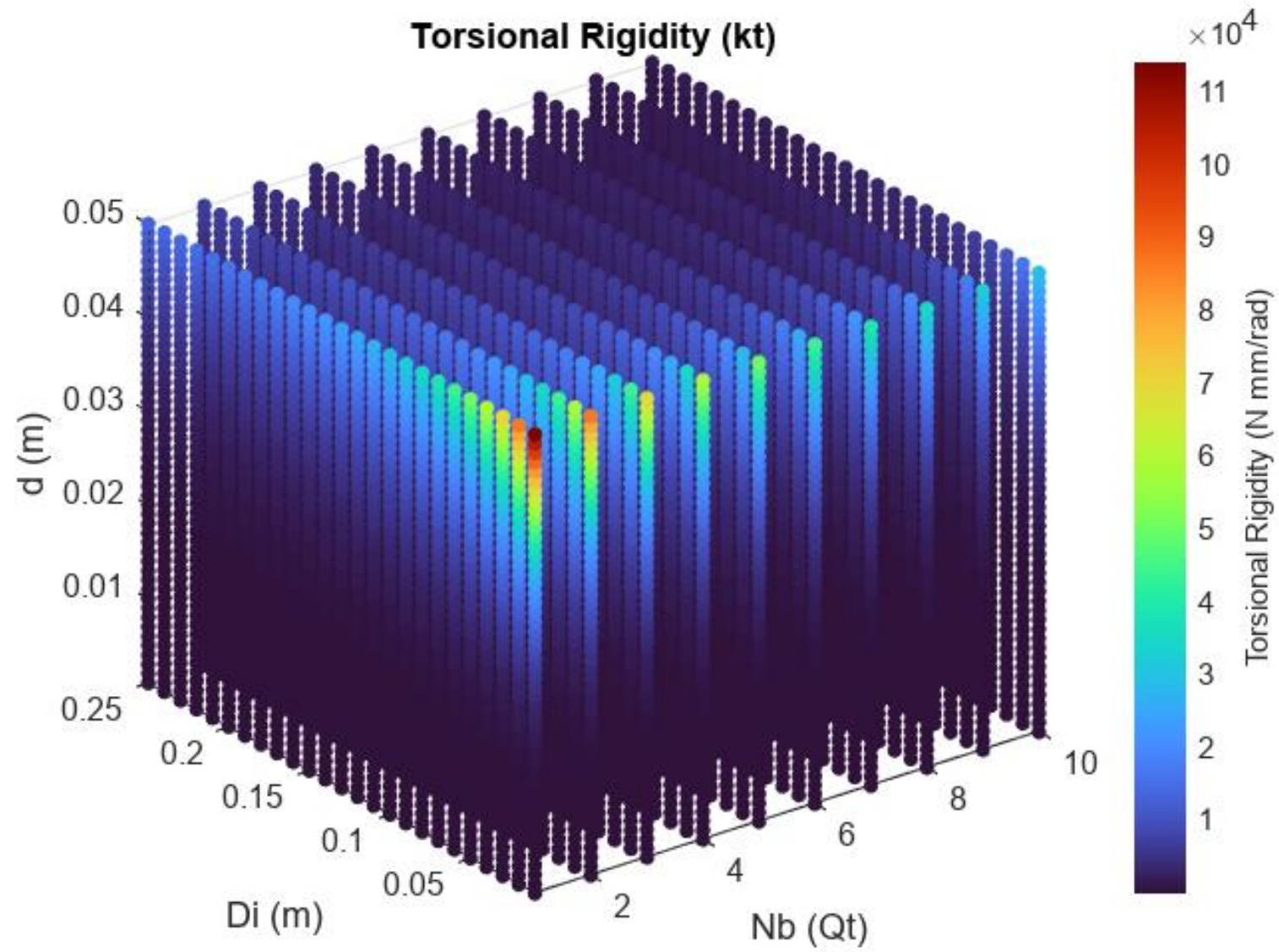
Supplemental Fig. 7. Torsional Rigidity Error and Safety Factor Error vs. Total iterator.

*Source: Matlab*



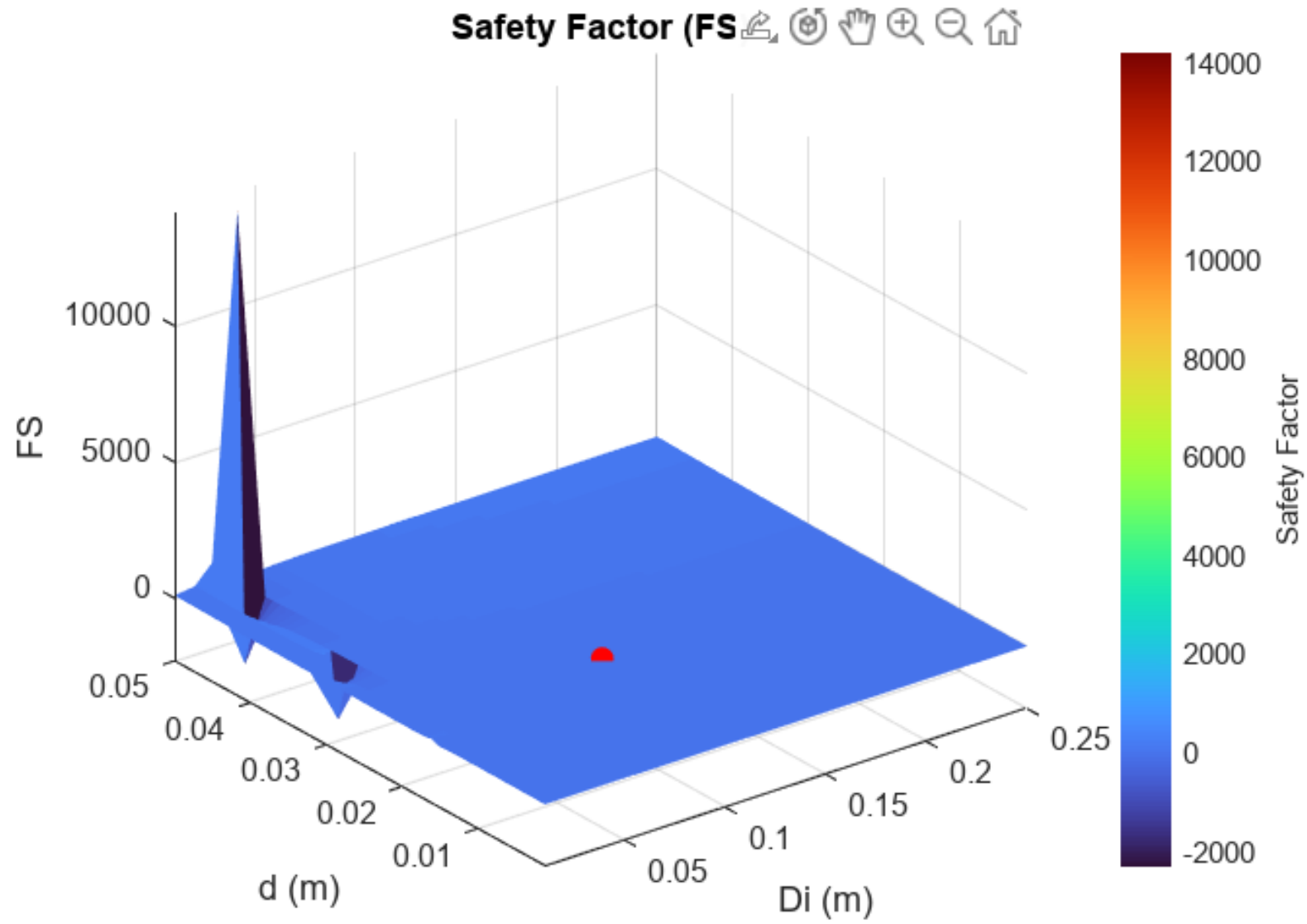
Supplemental Fig. 8. Torsional Rigidity Error and Safety Factor Error vs. Partial iterator.

Source: Matlab



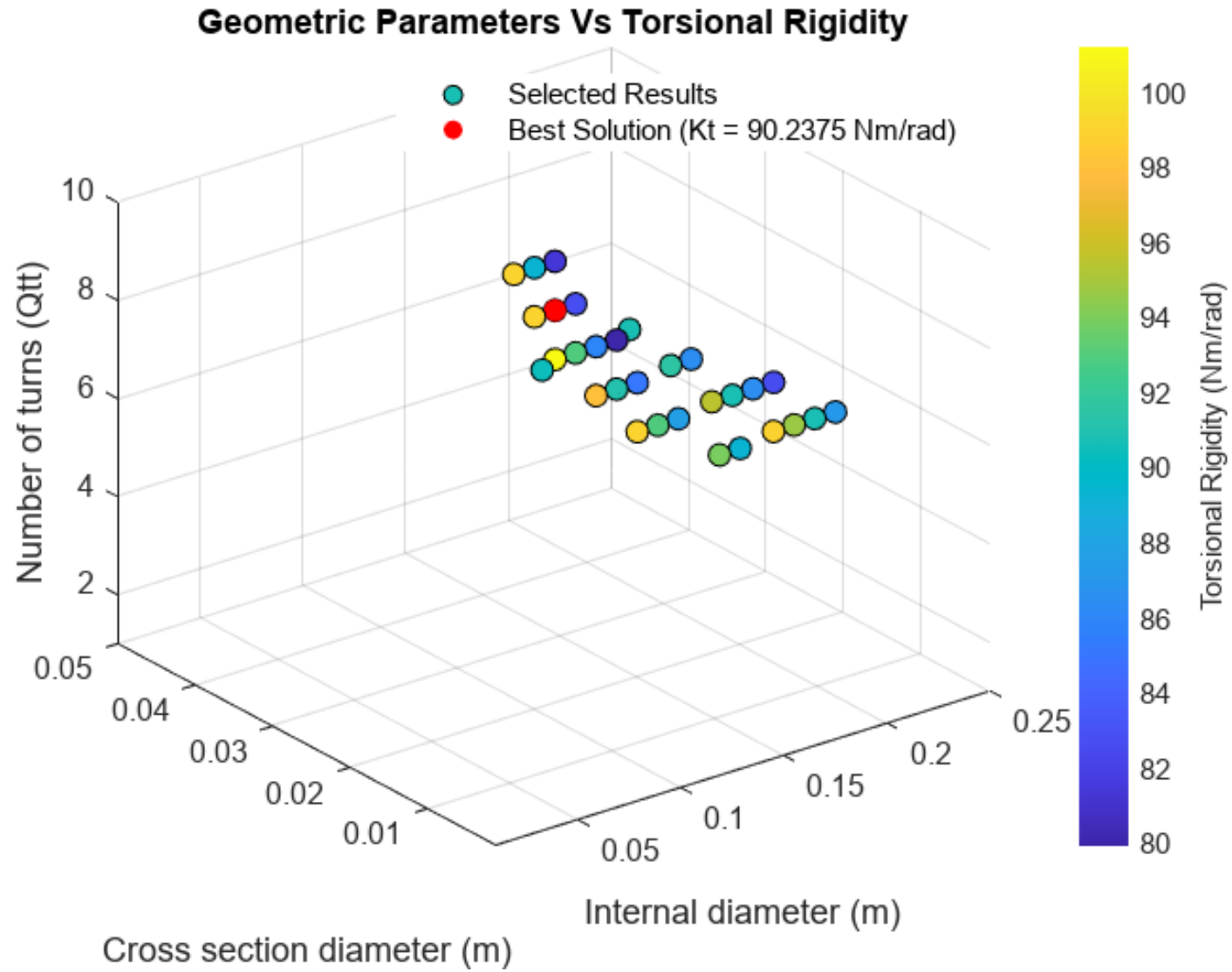
Supplemental Fig. 9. Torsional Rigidity (kt) Map.

*Source: Matlab*



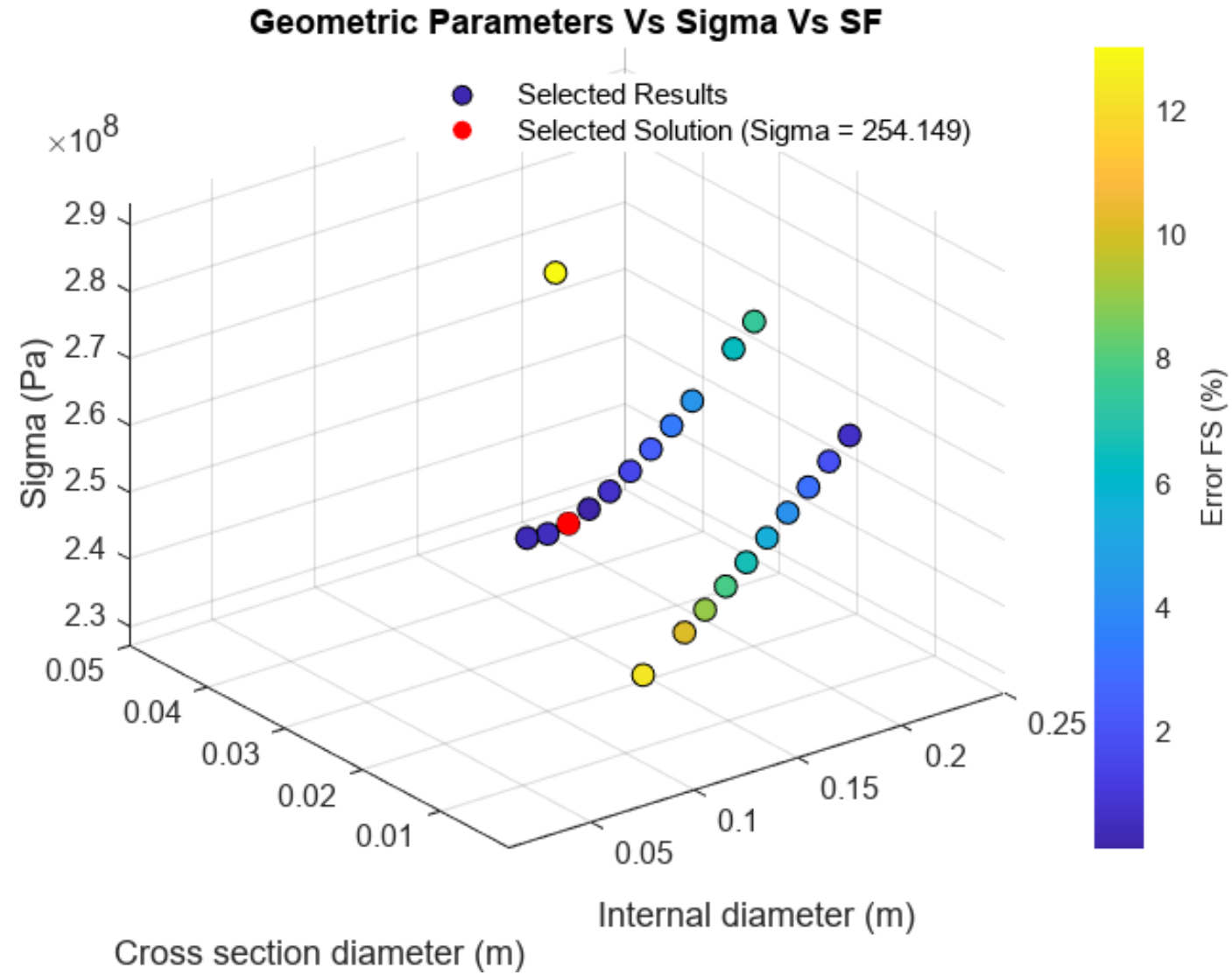
Supplemental Fig. 10. Safety Factor (FS) Map.

*Source: Matlab*



Supplemental Fig. 11. Geometric parameters Vs. Torsional Rigidity. Top 30 results.

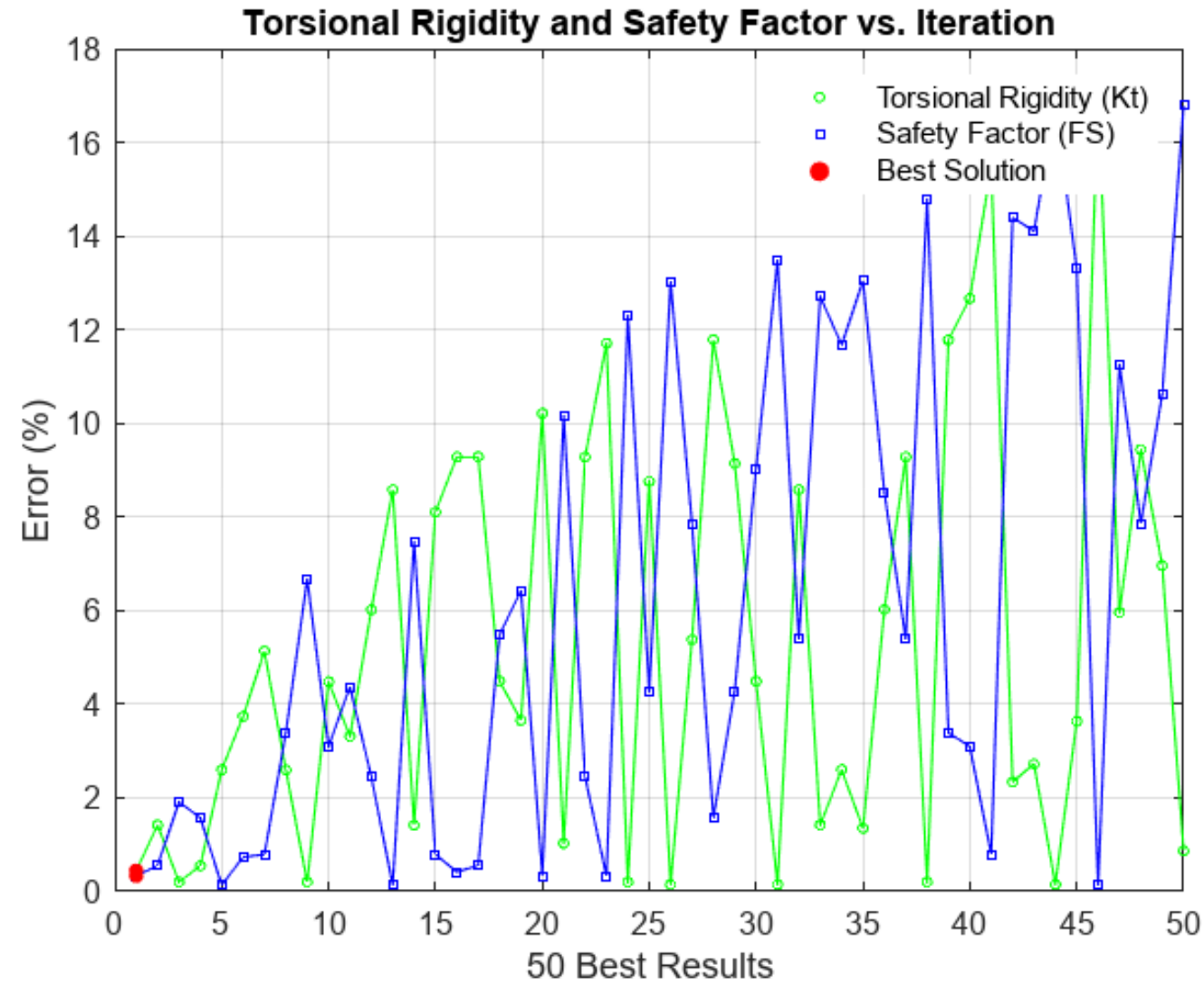
*Source: Matlab*



Supplemental Fig. 12. Geometric Parameters Vs Sigma Vs Safety Factor.

*Source: Matlab*



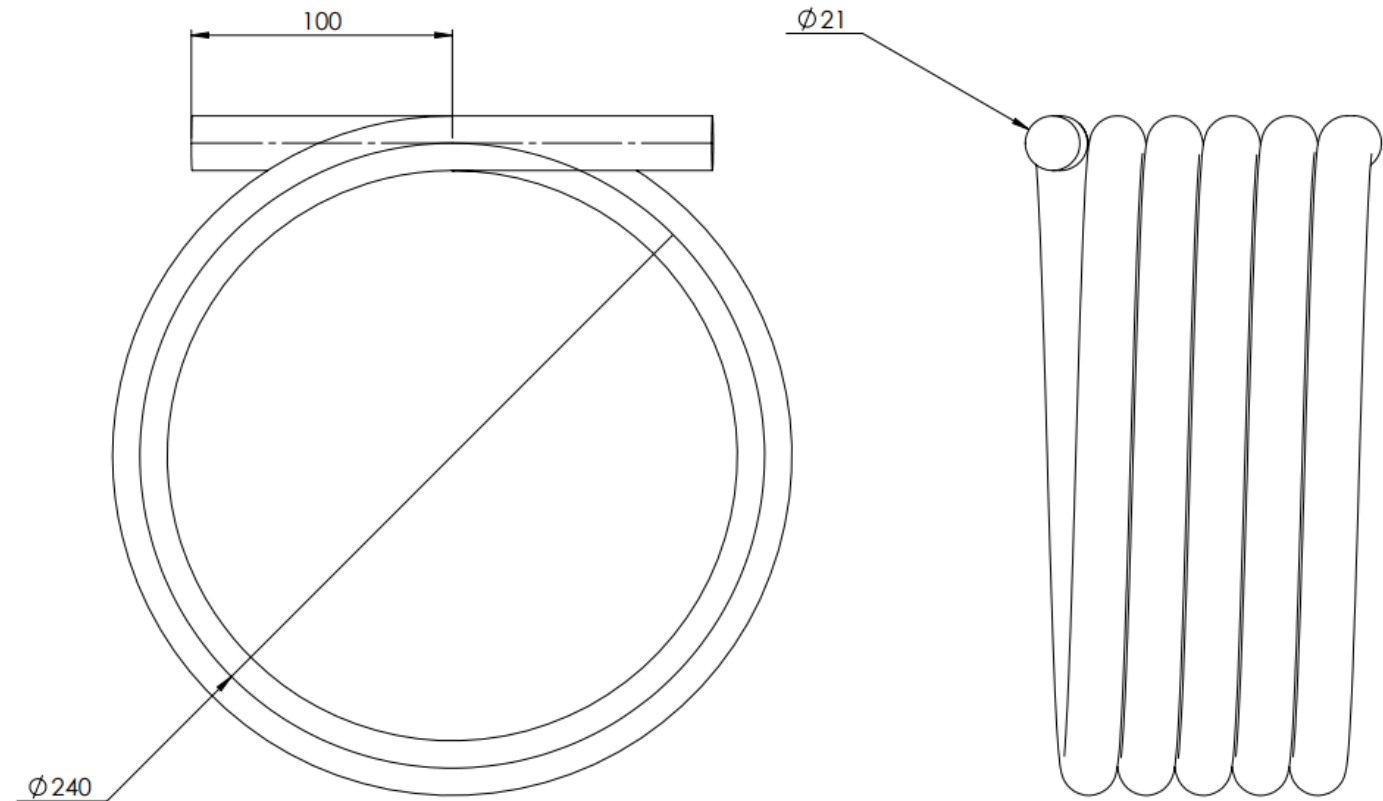


Supplemental Fig. 13. Torsional Rigidity and Safety Factor vs. Iteration.

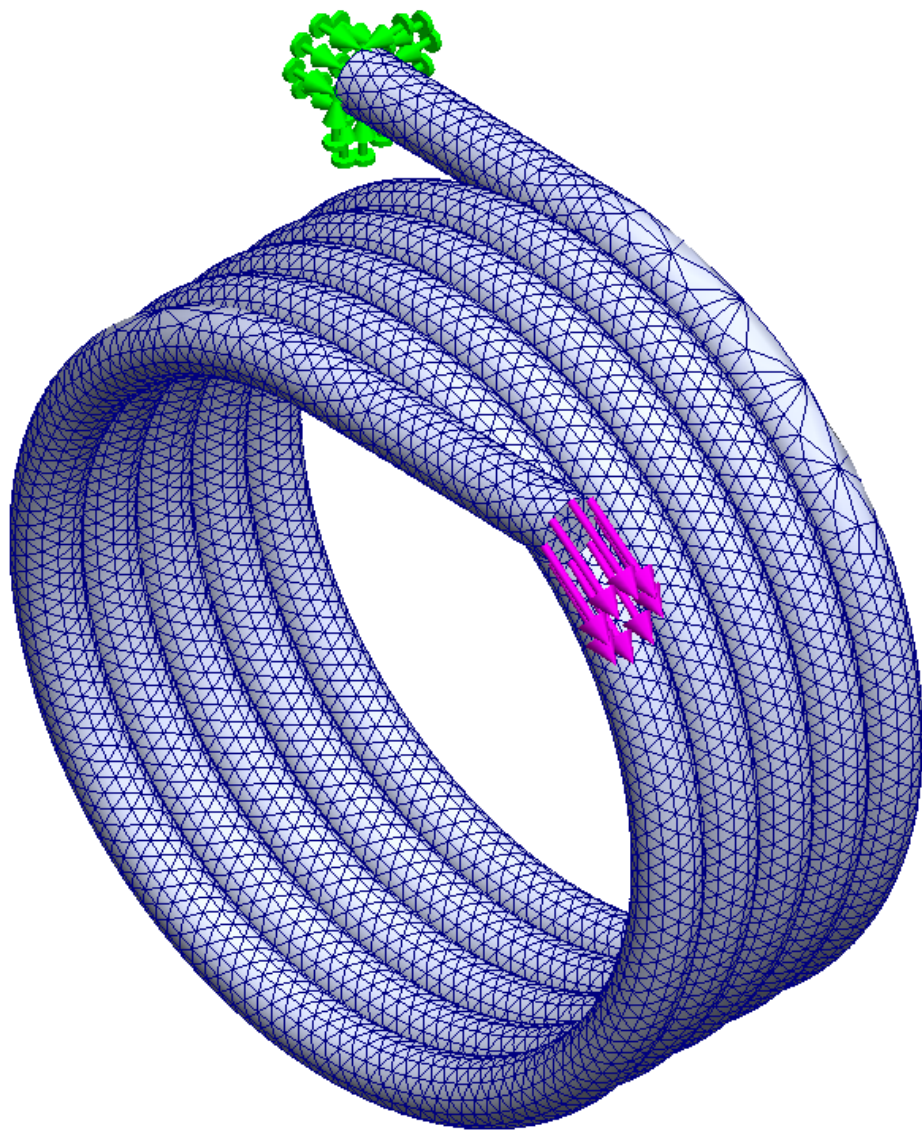
*Source: Matlab*

COMPARISON OF RESULTS BASED ON GEOMETRIC PARAMETERS									
SUPPLEMENTAL TABLE IV									
Iteration	Nb	Di	d	Sigma	FS	KtCal	ErrorFS	ErrorKt	
10520	9	0.11	0.02	2.5415e+08	1.0033	90.237	0.33486	0.44409	
11720	10	0.1	0.02	2.5359e+08	1.0056	89.354	0.55638	1.419	
6171	5	0.24	0.021	2.5022e+08	1.0191	90.823	1.9103	0.20192	
8170	7	0.14	0.02	2.5908e+08	0.98426	91.139	1.5741	0.55025	
9320	8	0.12	0.02	2.5535e+08	0.99861	92.996	0.13898	2.5997	
6221	5	0.25	0.021	2.5314e+08	1.0073	87.251	0.73399	3.7393	
9370	8	0.13	0.02	2.5704e+08	0.99208	85.986	0.79223	5.1347	
7020	6	0.16	0.02	2.6394e+08	0.96612	92.996	3.3879	2.5997	
7221	6	0.2	0.021	2.3904e+08	1.0668	90.823	6.6771	0.20192	
6121	5	0.23	0.021	2.4734e+08	1.031	94.7	3.0963	4.4796	
7070	6	0.17	0.02	2.6666e+08	0.95626	87.638	4.3738	3.3125	
8220	7	0.15	0.02	2.614e+08	0.97552	85.183	2.4481	6.0203	
10570	9	0.12	0.02	2.5535e+08	0.99861	82.863	0.13898	8.5805	
5970	5	0.2	0.02	2.7561e+08	0.92523	89.354	7.477	1.419	
8120	7	0.13	0.02	2.5704e+08	0.99208	97.99	0.79223	8.1086	
11670	10	0.09	0.02	2.5394e+08	1.0042	99.053	0.41764	9.2822	
10470	9	0.1	0.02	2.5359e+08	1.0056	99.053	0.55638	9.2822	
7271	6	0.21	0.021	2.4174e+08	1.0548	86.57	5.4841	4.4906	
5920	5	0.19	0.02	2.7252e+08	0.93572	93.954	6.4283	3.6561	

Helical Torsional Spring  
Material: Peek (40% Carbon fiber)  
Step: 22 mm  
Number of turns (Nb): 5 Qtt  
Internal diameter (Di): 240 mm  
Cross section diameter (d): 21 mm



Supplemental Fig. 12. Torsional Rigidity and Safety Factor vs. Iteration.  
*Source: SolidWorks*



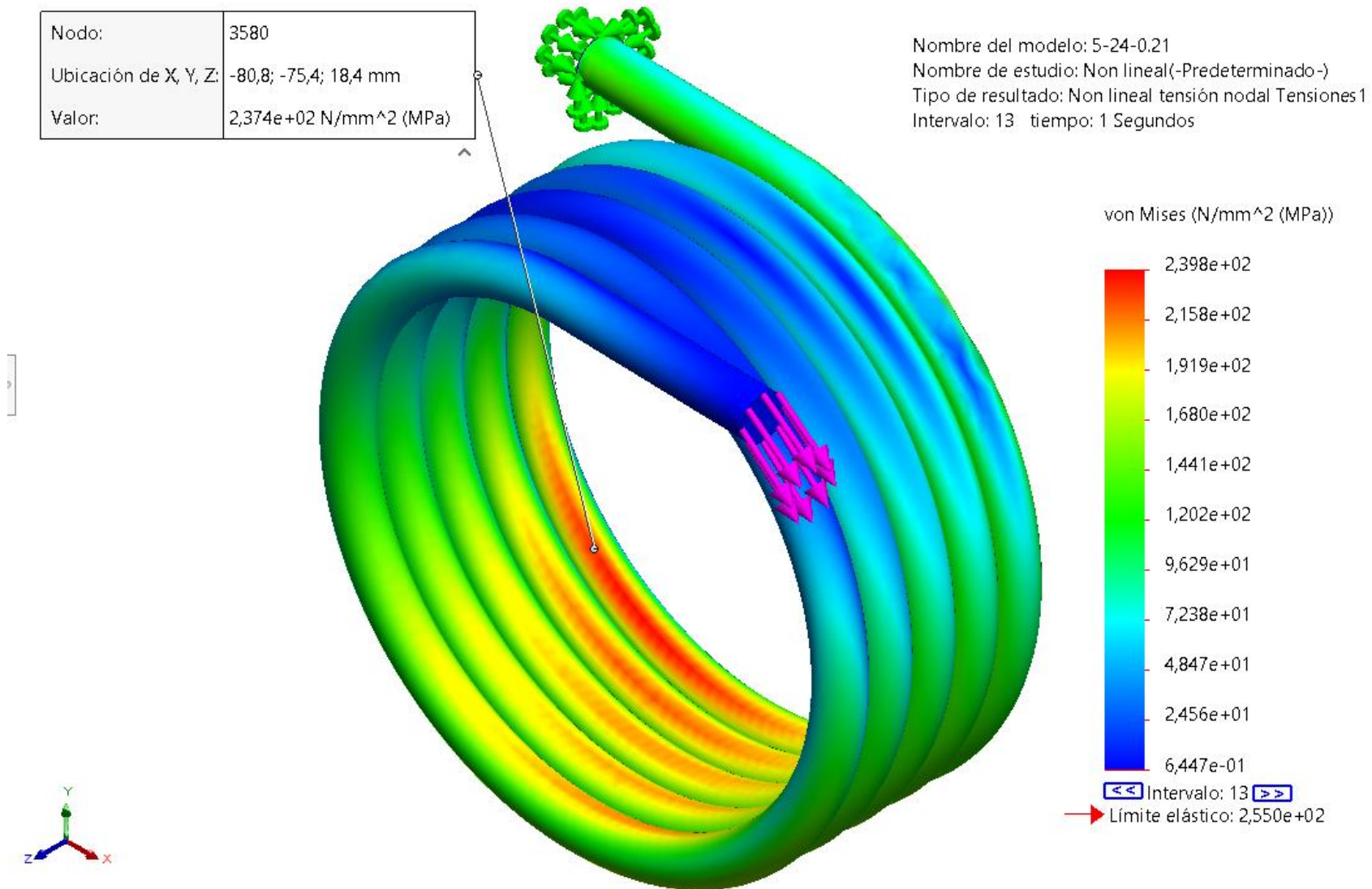
Supplemental Fig. 13. Border conditions.  
*Source: SolidWorks*

#### Estudio Detalles

Nombre de estudio	Non lineal* (-Predeterminado-)
Tipo de análisis	Non lineal - Análisis estático
Tipo de malla	Malla sólida
Hora de inicio	0
Hora de finalización	1
Incremento de tiempo	Paso automático
Formulación de grandes desplazamientos	Activar
Actualizar la dirección de la carga con la deformada	Desactivar
Formulación de grandes deformaciones unitarias	Desactivar
Guardar datos para reiniciar el análisis	Desactivar
Efecto térmico	Incluir cargas térmicas
Temperatura a tensión cero	298
Unidades	Kelvin
Tipo de solver	Automático
Opciones de unión rígida incompatibles	Simplificada
Técnica de control	Fuerza
Técnica iterativa	NR(Newton-Raphson)
Método de integración	Newmark

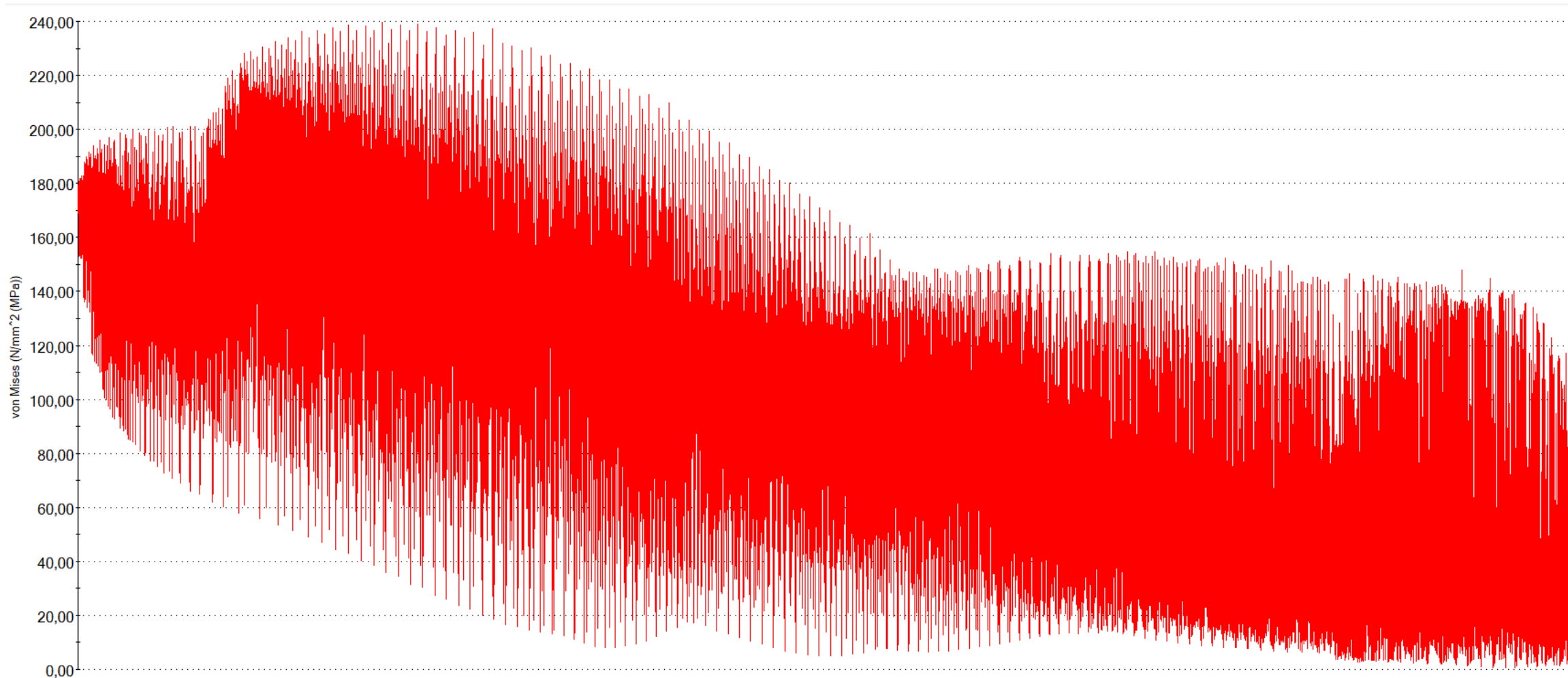
#### Malla Detalles

Nombre de estudio	Non lineal* (-Predeterminado-)
DetallesTipo de malla	Malla sólida
Mallador utilizado	Malla basada en curvatura de combinado
Puntos jacobianos para malla de alta calidad	16 puntos
Tamaño máx. de elemento	5,49633 mm
Tamaño mín. de elemento	1,83209 mm
Calidad de malla	Elementos cuadráticos de alto orden
Número total de nodos	107711
Número total de elementos	65357
Cociente máximo de aspecto	5,4567
Porcentaje de elementos con cociente de aspecto < 3	99,9
Porcentaje de elementos con cociente de aspecto > 10	0
Porcentaje de elementos distorsionados	0
Número de elementos distorsionados	0
Tiempo para completar la malla (hh:mm:ss)	00:01:13
Nombre de computadora	



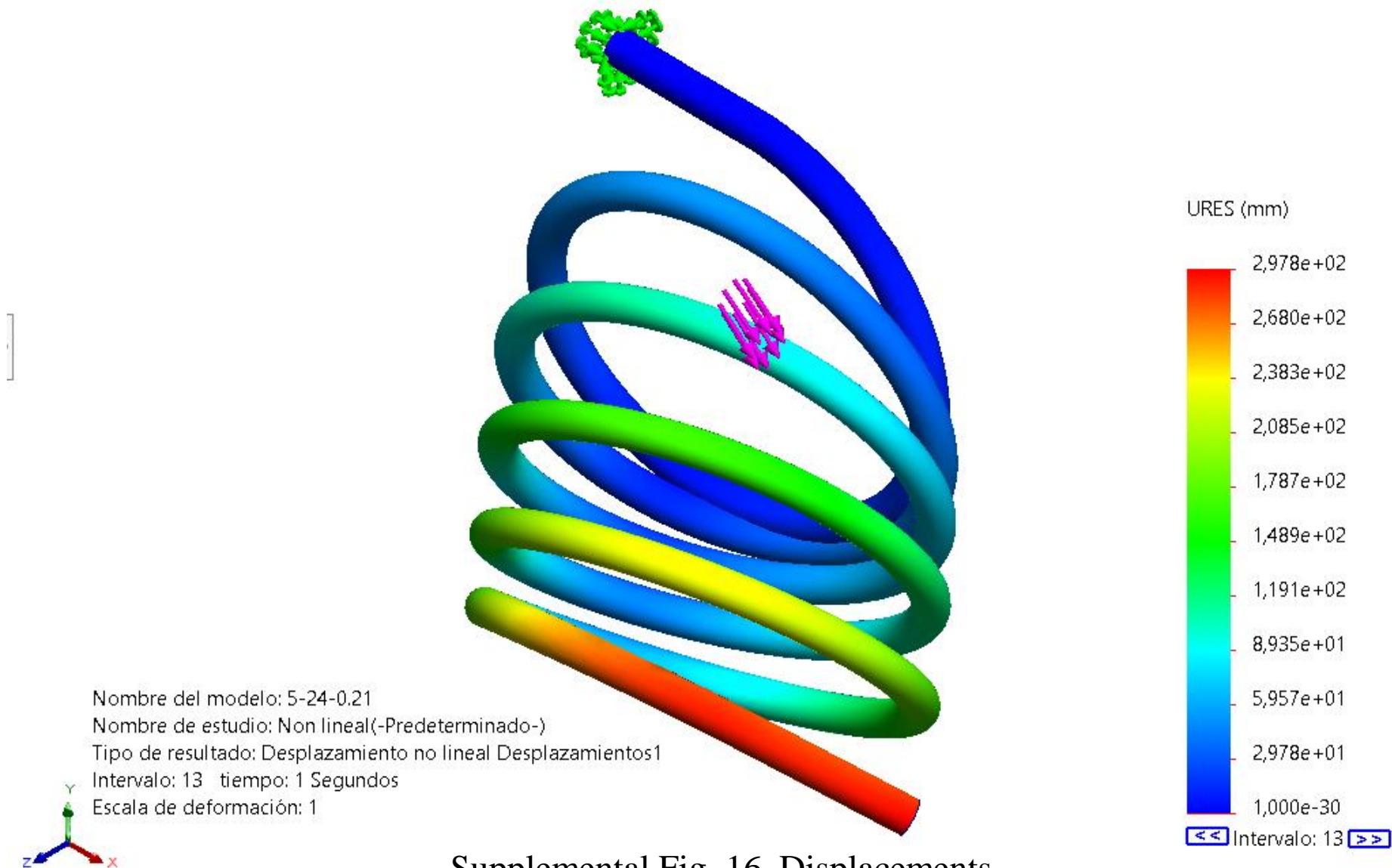
Supplemental Fig. 14. Von Mises.  
*Source: SolidWorks*

Nombre de estudio: Non lineal(-Predeterminado-)  
Tipo de resultado: Non lineal tensión nodal Tensiones1  
Intervalo: 13 tiempo: 1 Segundos



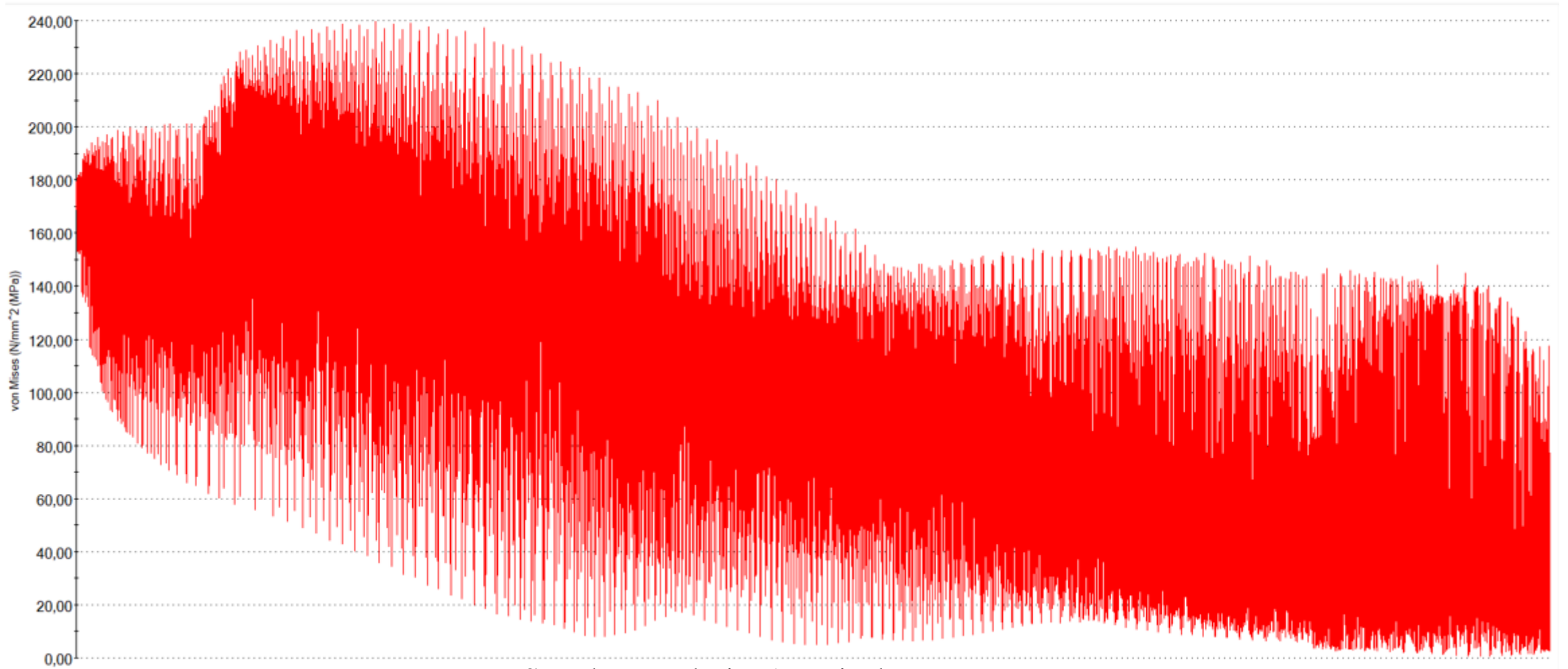
Supplemental Fig. 15. Von Mises Graphical Distribution axes Y.  
*Source: SolidWorks*





Supplemental Fig. 16. Displacements.  
*Source: SolidWorks*

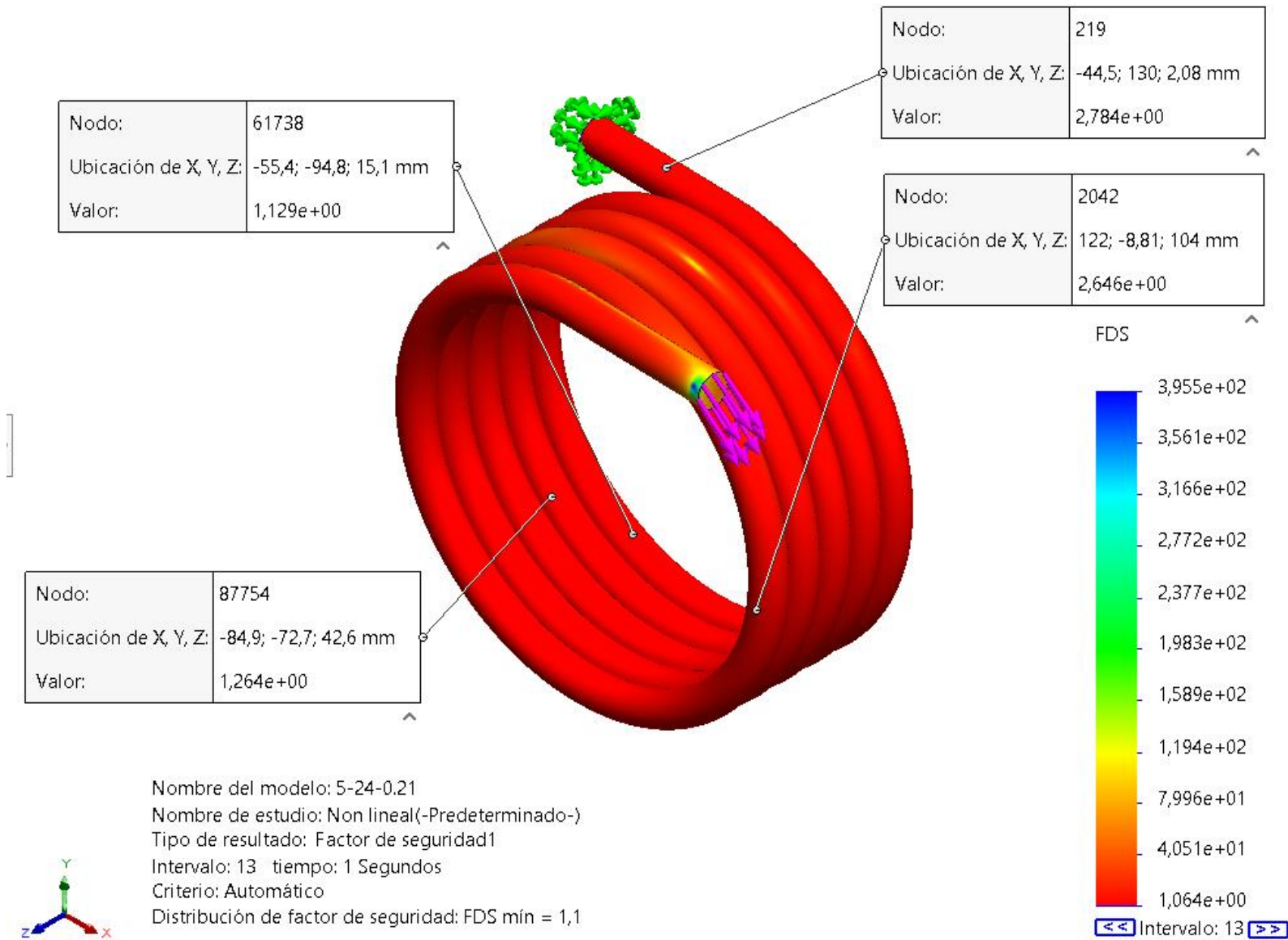
Nombre de estudio: Non lineal(-Predeterminado-)  
Tipo de resultado: Non lineal tensión nodal Tensiones1  
Intervalo: 13 tiempo: 1 Segundos



Supplemental Fig. 17. Displacements Y.

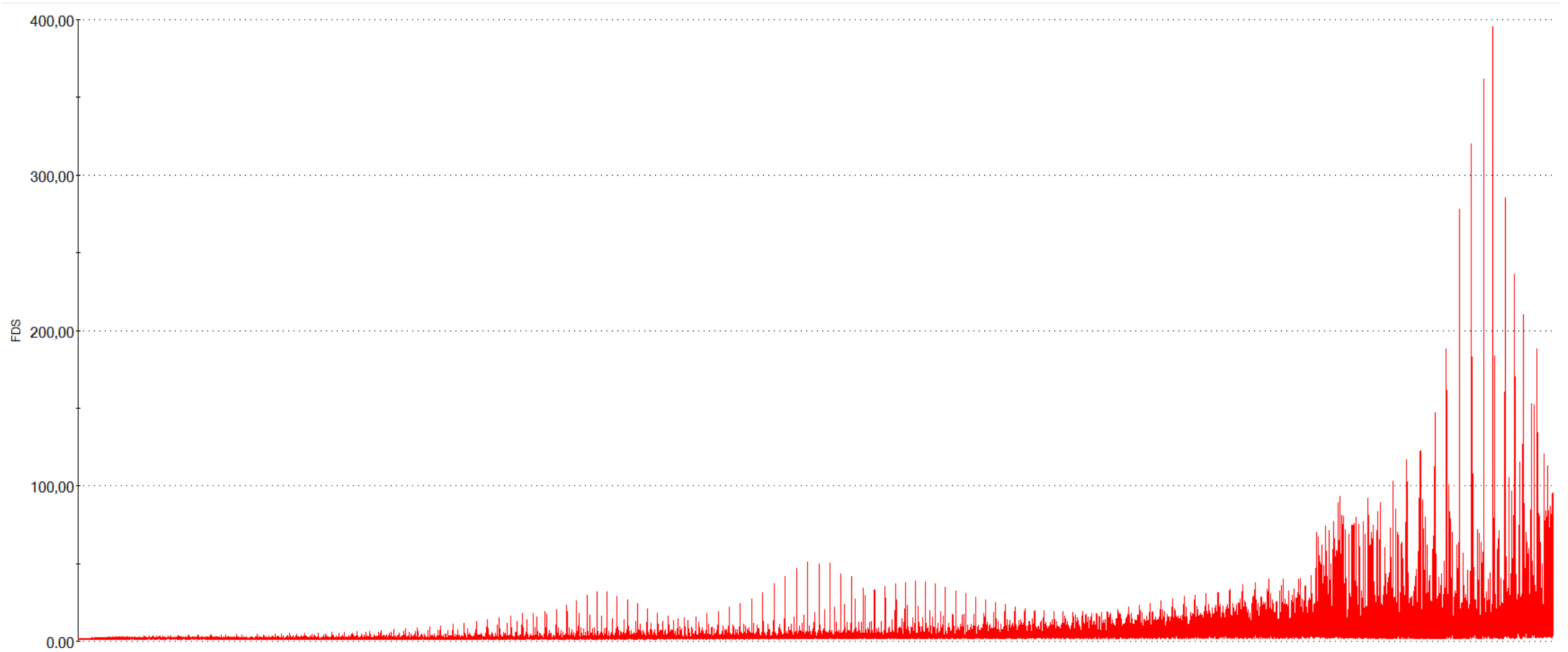
*Source: SolidWorks*





Supplemental Fig. 18. Safety Factor.  
 Source: SolidWorks

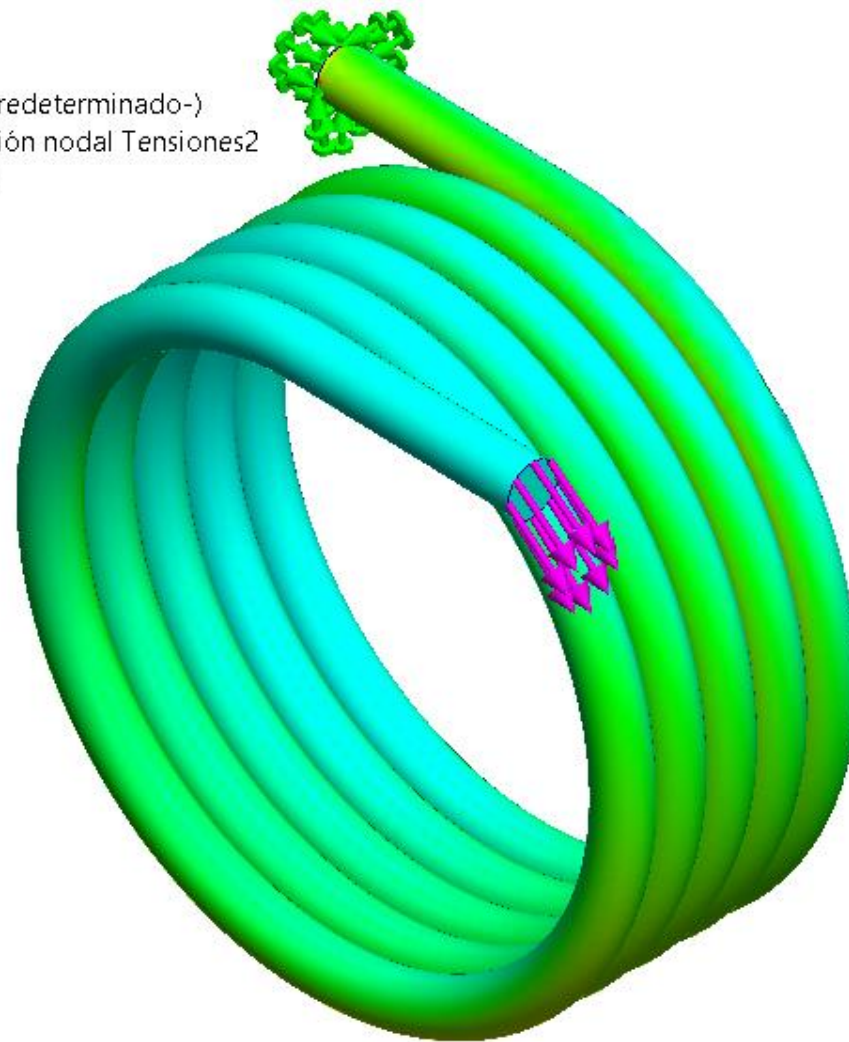
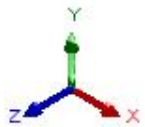
Nombre de estudio: Non lineal(-Predeterminado-)  
Tipo de resultado: Factor de seguridad1  
Intervalo: 13 tiempo: 1 Segundos  
Criterio: Automático



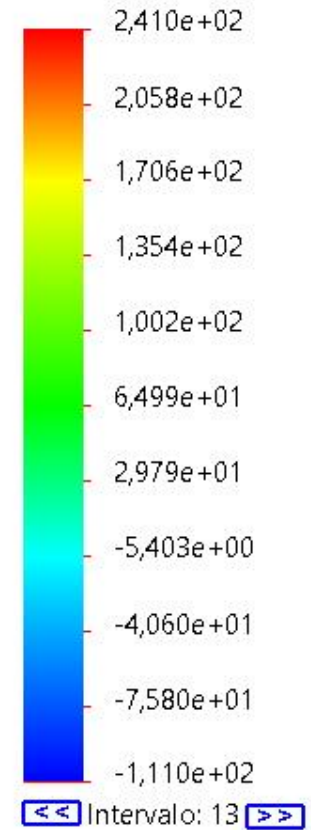
Supplemental Fig. 19. Safety Factor Distribution axes Y.

*Source: SolidWorks*

Nombre del modelo: 5-24-0.21  
Nombre de estudio: Non lineal(-Predeterminado-)  
Tipo de resultado: Non lineal tensión nodal Tensiones2  
Intervalo: 13 tiempo: 1 Segundos

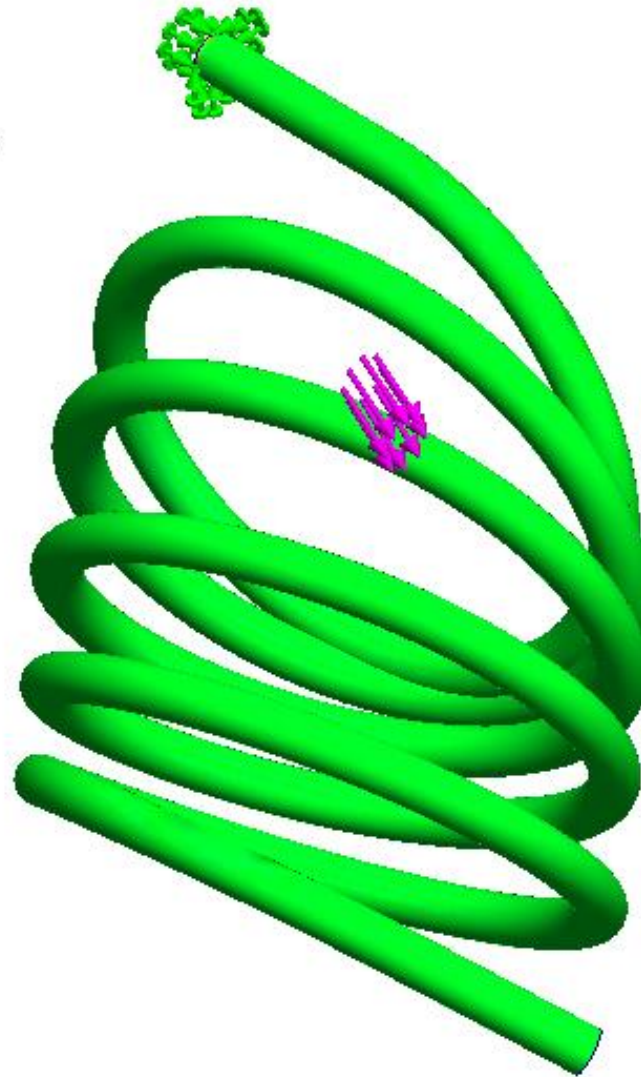
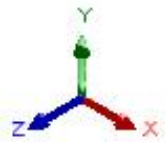


P1 (N/mm<sup>2</sup> (MPa))

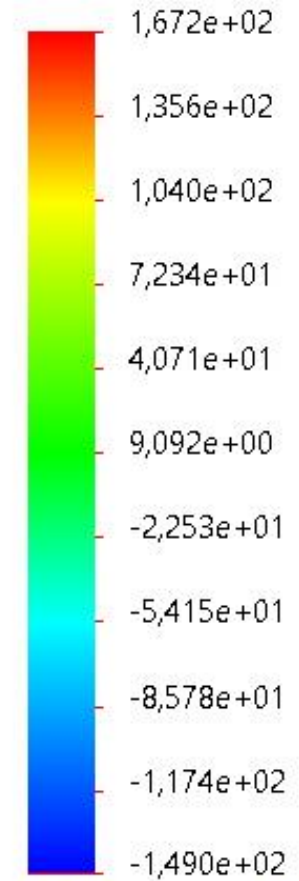


Supplemental Fig. 20. Principal Stress (P1).  
*Source: SolidWorks*

Nombre del modelo: 5-24-0.21  
Nombre de estudio: Non lineal (-Predeterminado-)  
Tipo de resultado: Non lineal tensión nodal Tensiones3  
Intervalo: 13 tiempo: 1 Segundos  
Escala de deformación: 1



P2 (N/mm<sup>2</sup> (MPa))



<< Intervalo: 13 >>

Supplemental Fig. 20. Principal Stress (P2).  
*Source: SolidWorks*

SUPPLEMENTAL TABLE V  
RESULTS COMPARISON

Ref	Units	Analytic	Simulation	Error % Simulation	Analytic Vs Simulation Error %
$\sigma_{VM}$	MPa	250.22	239.8	4.16 %	4.34 %
$FS$	N/A	1.02	1.1	7.84 %	7.27 %
$\Theta$	mm	280	297.8	6.35 %	5.97 %
$Kt$	N*m/Rad	90.82	85.71	5.62 %	5.96 %

In the simulation, an elasticity coefficient of 85.71 *Nm/rad* was obtained compared to the required 90.65 *Nm/rad* to keep the system in equilibrium, suggesting that the device will provide 94.55% assistance during knee flexion.