

# Quantum information presentation

## Maximal Quantum cloning

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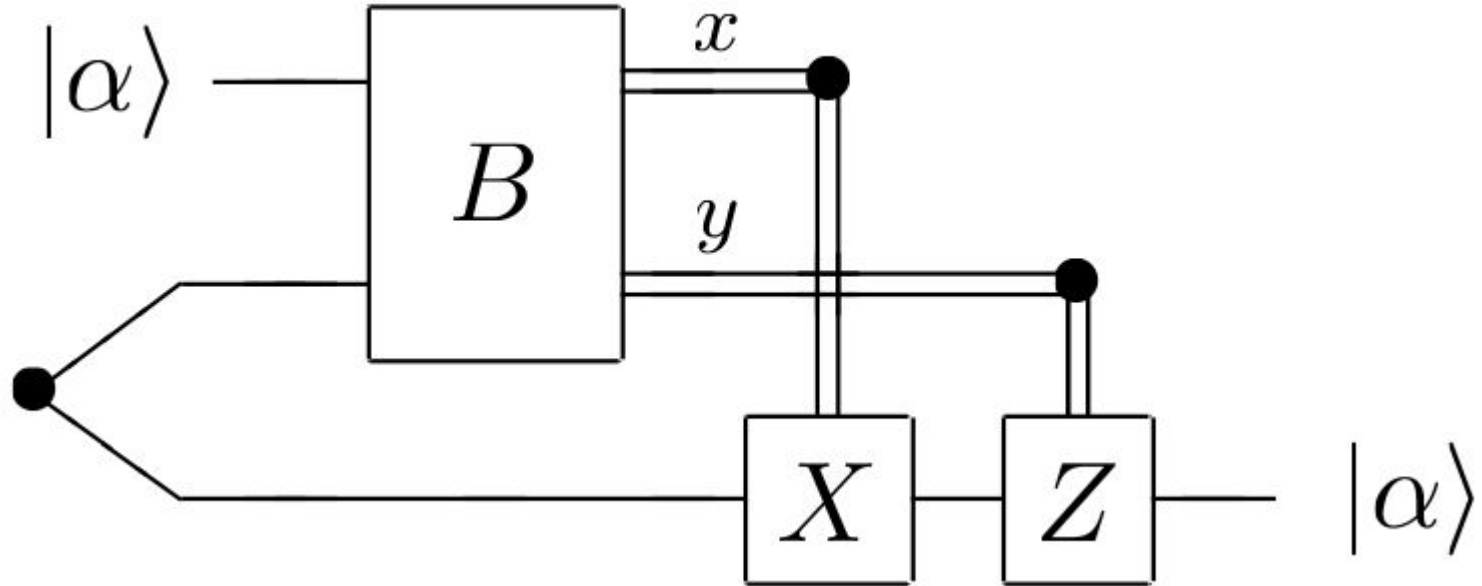
# What are we trying to do ?

Using quantum teleportation as a universal primitive to unitary quantum gates

Typical universal set of quantum gates: {CNOT, X, Y, Z, H}

# Quantum teleportation

## 1 - The teleportation setup



# Quantum teleportation

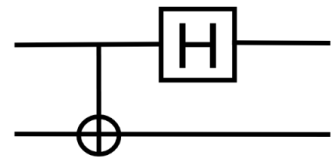
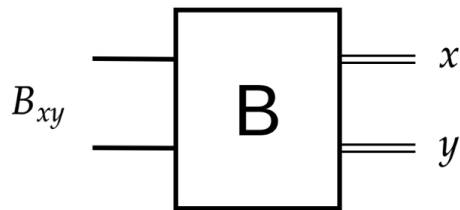
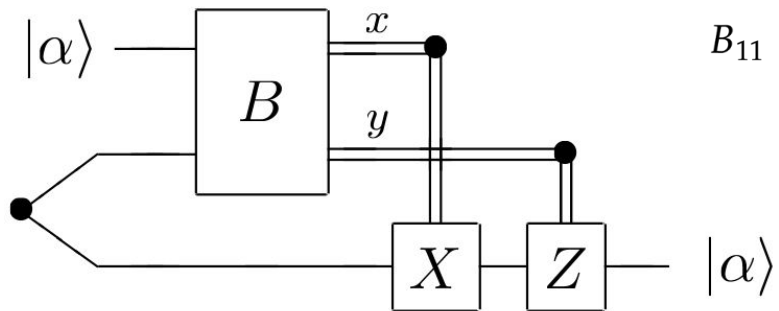
## 1 - The teleportation setup

$$\underbrace{|\Psi\rangle}_{\text{epr}} = B_{00} = |\Phi^+\rangle = \frac{|00\rangle + |11\rangle}{\sqrt{2}}$$

$$B_{10} = |\Phi^-\rangle = \frac{|00\rangle - |11\rangle}{\sqrt{2}}$$

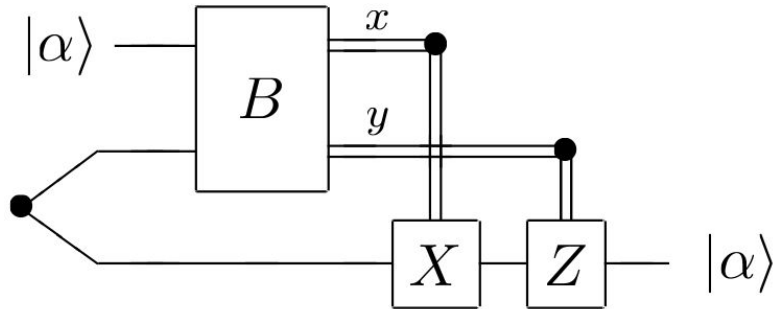
$$B_{01} = |\Psi^+\rangle = \frac{|01\rangle + |10\rangle}{\sqrt{2}}$$

$$B_{11} = |\Psi^-\rangle = \frac{|01\rangle - |10\rangle}{\sqrt{2}}$$



# Quantum teleportation

## 1 - The teleportation setup



$$\begin{aligned} |\alpha\rangle \otimes |\Psi\rangle = & \frac{1}{2} (B_{00} \otimes |\alpha\rangle \\ & + B_{10} \otimes X |\alpha\rangle \\ & + B_{01} \otimes Z |\alpha\rangle \\ & + B_{11} \otimes XZ |\alpha\rangle) \end{aligned}$$

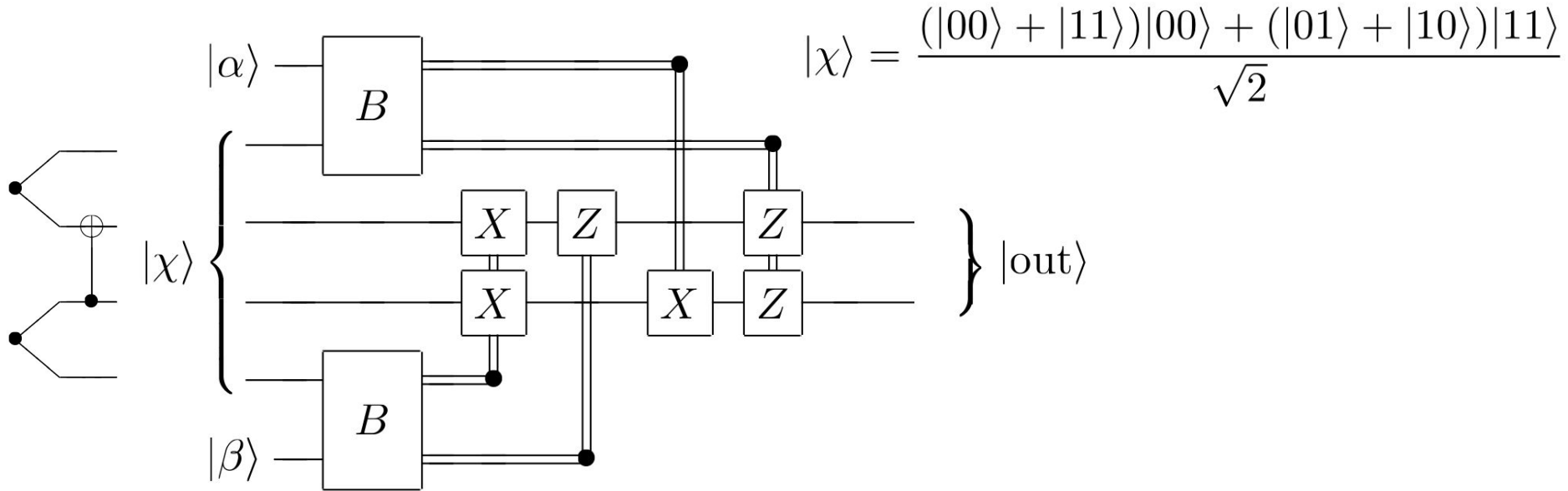
# Quantum teleportation

## 2 - Why use quantum teleportation ?

- Use different types of qubit for computation and storage
- Long range qubit transportation

# Using quantum teleportation to build quantum gates

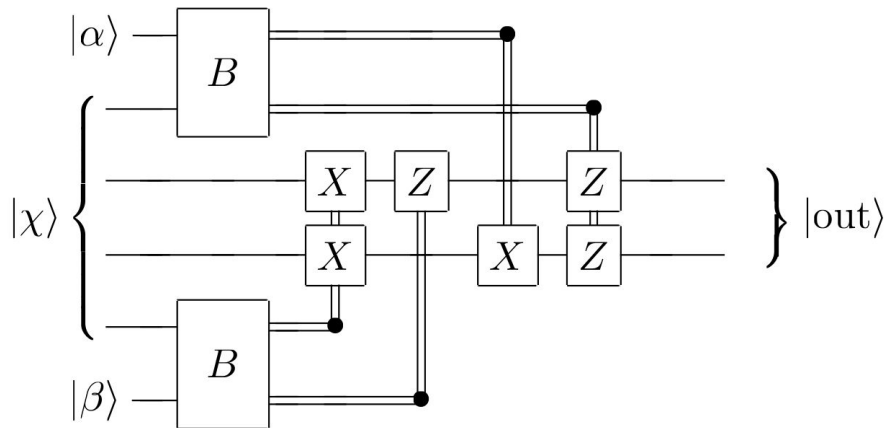
3 - From a quantum teleporter to the CNOT gate:



# Using quantum teleportation to build quantum gates

3 - From a quantum teleporter to the CNOT gate:

Using the CNOT gate we have built, and single-qubit gates we have a universal set of quantum gates !



*Circuit functionality is proven later on*



# Fault tolerant quantum gates

## 4 - introducing fault tolerance

Redondance block to correct faults

- > Avoid operations within blocks to avoid error propagation
- > Prefere transversal operations

# Fault tolerant quantum gates

4 - introducing fault tolerance: building gates from the C3 group

$$C_1 = \{X, Y, Z\} \quad (\text{Pauli gates})$$

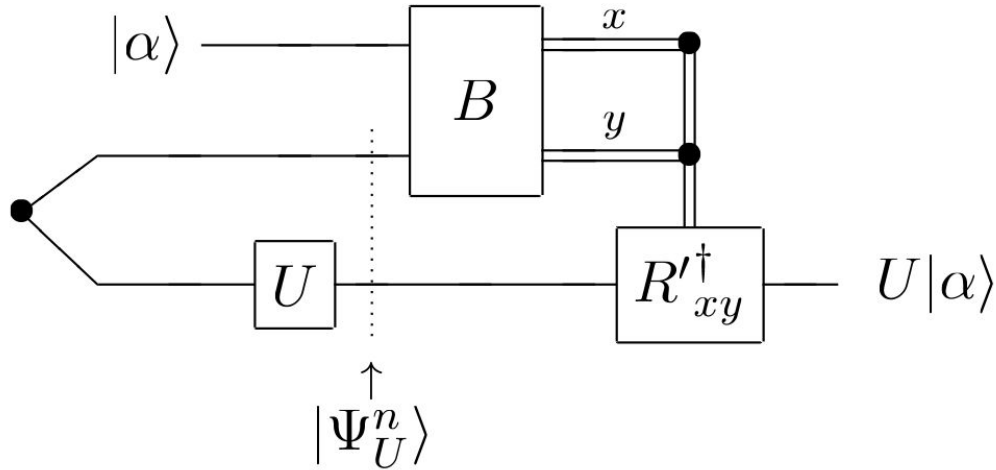
$$C_2 = \{U | UC_1U^\dagger \subseteq C_1\} = \{S, H, CNOT \dots\} \quad (\text{Clifford gates})$$

$$C_3 = \{U | UC_1U^\dagger \subseteq C_2\}$$

C1 and C2 gates can be applied transversely, while C3 gates cannot in general.

# Fault tolerant quantum gates

4 - introducing fault tolerance: building gates from the C3 group

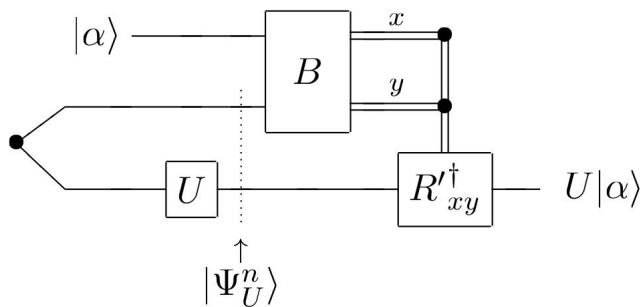
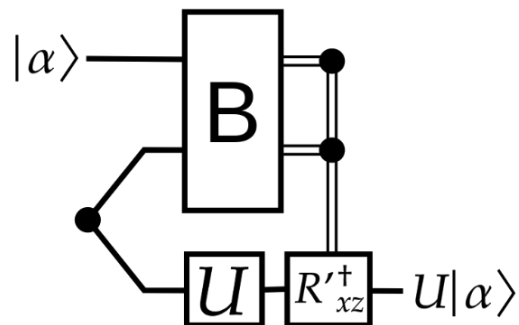
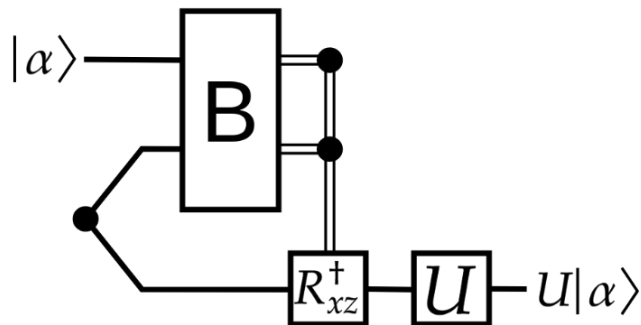
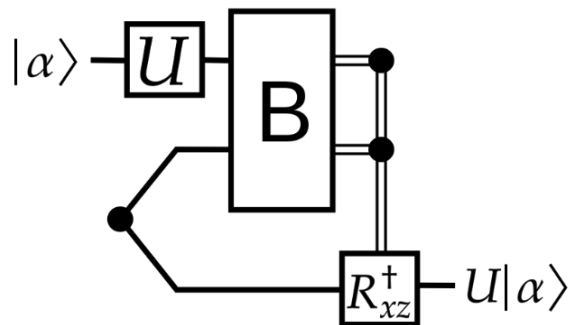


$$|\Psi_U^n\rangle = (I \otimes U)|\Psi^n\rangle$$

$$|\psi_{out}\rangle = UR_{xz}|\psi\rangle = R'_{xz}U|\psi\rangle$$

# Fault tolerant quantum gates

## 4 - introducing fault tolerance: building gates from the C3 group



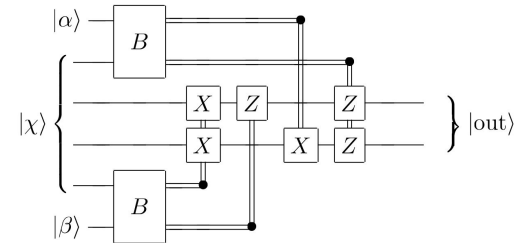
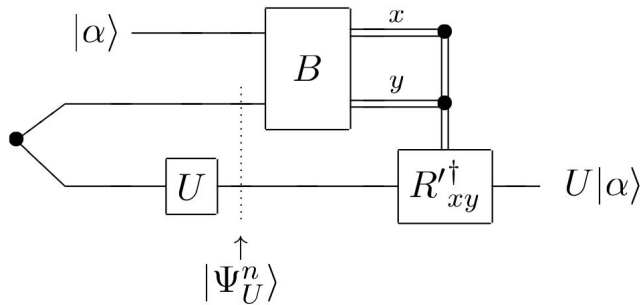
$$|\psi_{out}\rangle = UR_{xz}|\psi\rangle = R_{xz}'U|\psi\rangle$$

# Fault tolerant quantum gates

## 4 - introducing fault tolerance: building gates from the C3 group

We can build gates from the C3 group ( $C_n$ ) only by applying gates from the C2 group ( $C_{n-1}$ ) to the actual Qubits !

*Can also be used to prove the CNOT gate circuit*



# Conclusion

Advantages of this method:

- Typical advantages of quantum teleportation:
  - Apply gates on “volatile qubit”, while storing “stable qubit”
- Use already existing quantum teleportation device
- Apply “complex” gates (for fault tolerant comp.) using “simpler” gates