# Complex networks exam

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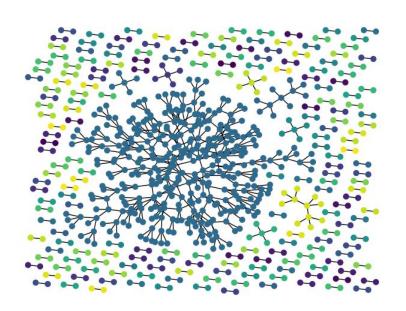
#### Problem 1 - Generation of instances of the random graph model

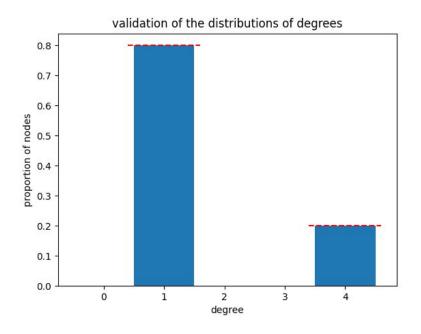
#### Code and algorithm

```
def gen rgm(N, pi):
    G = nx.Graph()
    for i in range(N):
        G.add node(i)
    n d1 = int(np.round(N*(1 - pi)/2)*2) # so that n d1 + 4*n d4 is pair
    n d4 = N - n d1
    stubs = []
    for i in range(n d1):
        stubs.append(i)
    for i in range(n dl, N):
        for j in range(4):
            stubs.append(i)
    while stubs:
        j = choose and pop from list(stubs)
        k = choose and pop from list(stubs)
       G.add edge(j, k)
        G.add edge(k, j)
    return G
```

```
def gen rgm biased(N, pi):
   G = nx.Graph()
   for i in range(N):
       G.add node(i)
   n dl = int(np.round(N*(1 - pi)/2)*2) # so that n dl + 4*n d4 is pair
   # use a dictionary of degrees
   degree = {}
    for i in range(N):
       degree[i] = 1 if i < n d1 else 4
   while len(degree) >= 2:
       unique stubs = list(degree.keys())
       # select a node and remove it from the temporary list of nodes to select from
       i = choose and pop from list(unique stubs)
       while True:
           # try to select another node and remove it from the temporary list
           k = choose and pop from list(unique stubs)
           # only add edge if there isn't already an edge
           if not G.has edge(j, k):
               G.add edge(i, k)
               G.add edge(k, j)
               # delete both index
               degree[j] -= 1
               # and if the degree is 0 remove the entry from the dict
               if degree[i] == 0:
                   del dearee[i]
               dearee[k] -= 1
               if degree[k] == 0:
                   del degree[k]
               break
           # if there is no more node to choose from:
           elif len(unique stubs) == 0:
               # delete the entry for j because we know that we weren't able to create an edge from j
               del degree[j]
               break
   return G
```

# Problem 1 - Generation of instances of the random graph model Validation





#### Problem 2: The giant component

#### Code and algorithm

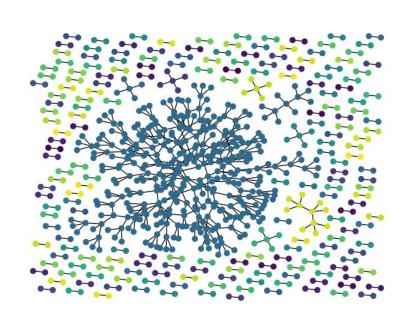
```
def get_connected_component(graph, node, visited=None):
    if visited is None:
        visited = []
    visited.append(node)

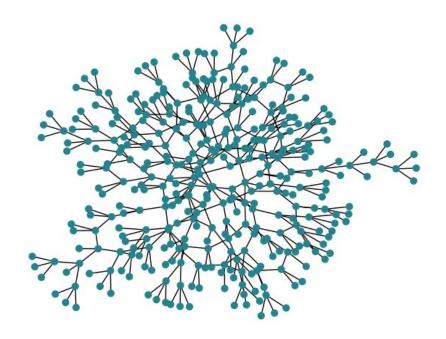
    for neighbor in graph.neighbors(node):
        if neighbor not in visited:
            connected = get_connected_component(graph, neighbor, visited)

        for connected_node in connected:
            if connected_node not in visited:
                 visited.append(connected_node)
    return visited
```

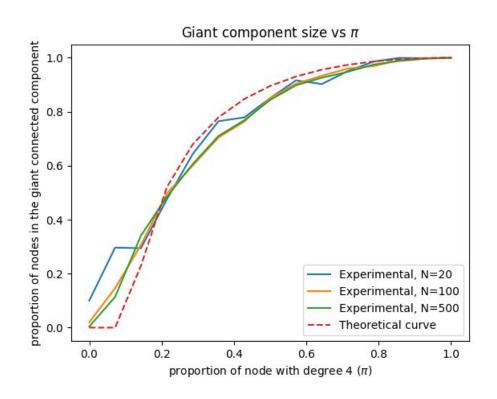
### Problem 2: The giant component

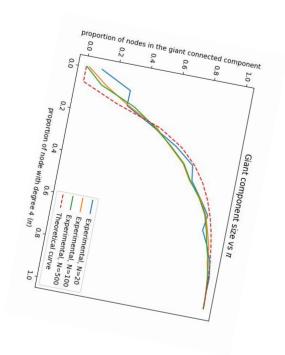
Validation





#### Problem 2: The giant component





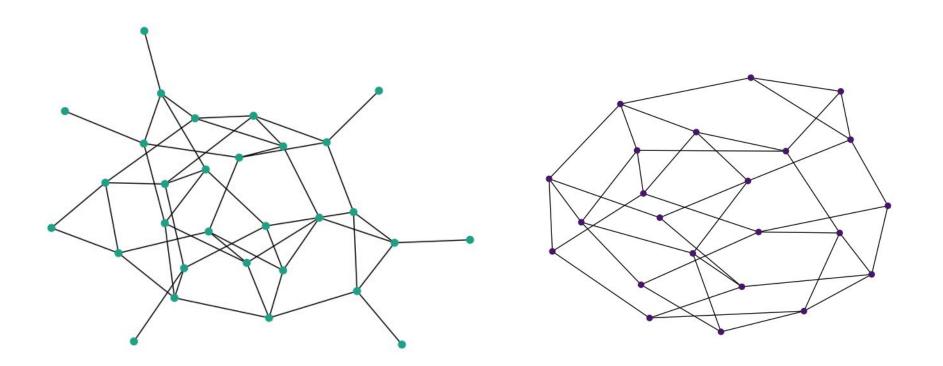
#### Problem 3: Emergence of the 3-core

Code and algorithm

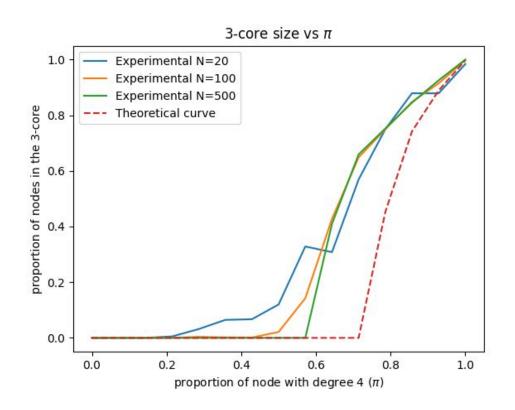
```
# we use the prunning algorithm we saw in class:
def find k core(graph, k):
    G = copy.deepcopy(graph)
    while True:
        to remove=[]
        for node in G.nodes:
            if G.degree[node] < k:</pre>
                to remove.append(node)
        if len(to remove) == 0:
            if len(G.nodes) == 0:
                return
            # the k-core still has to be a single connected graph
            k core = find largest connected component(G)
            return k core
        for node in to remove:
            G.remove node(node)
```

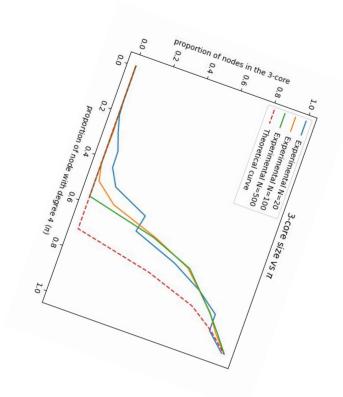
### Problem 3: Emergence of the 3-core

Validation



#### Problem 3: Emergence of the 3-core

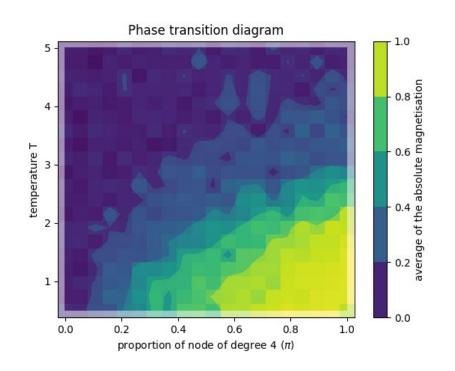


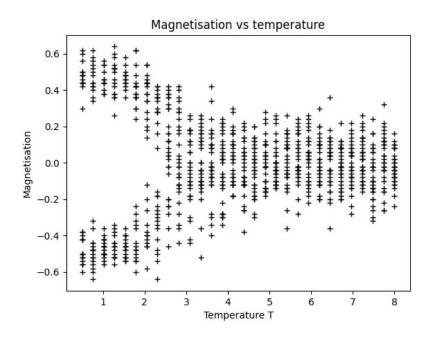


## Problem 4: The ferromagnetic Ising model

```
def monte carlo simulate(graph, state, T, N it per node):
    n nodes = graph.number of nodes()
    for i in range(n nodes*N it per node):
        node = np.random.randint(0, n nodes)
        total surounding spin = 0
        for neighbor in graph.neighbors(node):
            total surounding spin += state[neighbor]
        delta E = 2*state[node]*total surounding spin
        if delta E < 0:
            state[node] = -state[node]
        else:
            P flip = np.exp(-delta E/T)
            if np.random.rand() < P flip:</pre>
                state[node] = -state[node]
    return state
```

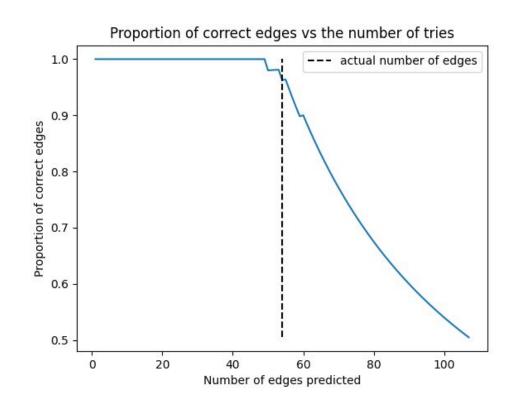
#### Problem 4: The ferromagnetic Ising model





#### Problem 5: Inverse Ising model

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### Conclusion and questions

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