

selection sort

| # | Random | Ascending | Descending |
|--------|----------|-----------|------------|
| 50000 | 2928250 | 2530596 | 2731627 |
| 60000 | 4217830 | 3634821 | 3935534 |
| 70000 | 5743746 | 4956010 | 5359250 |
| 80000 | 7497989 | 6485603 | 6997772 |
| 90000 | 9484922 | 8199756 | 8835713 |
| 100000 | 11726152 | 10111550 | 10921941 |
| 110000 | 13829590 | 11956606 | 12883294 |

Bubble Sort

| # | Random | Ascending | Descending |
|---------|----------|-----------|------------|
| 50000 | 4419667 | 191 | 3806293 |
| 60000 | 6379496 | 251 | 5486297 |
| 70000 | 8441816 | 294 | 7254168 |
| 80000 | 11367136 | 321 | 9761513 |
| 90000 | 14031026 | 383 | 11976432 |
| 100000 | 17812095 | 420 | 15177394 |
| 110000 | 20967007 | 485 | 17855939 |
| 500000 | | 1927 | |
| 700000 | | 2867 | |
| 1200000 | | 4707 | |

Insertion

| # | Random | Ascending | Descending |
|---------|---------|-----------|------------|
| 50000 | 1552793 | 268 | 3099826 |
| 60000 | 2202957 | 336 | 4470570 |
| 70000 | 2986246 | 360 | 4940399 |
| 80000 | 3870987 | 416 | 7936005 |
| 90000 | 4901478 | 463 | 9770110 |
| 100000 | 6073772 | 590 | 12499492 |
| 110000 | 7316057 | 2079 | 14568512 |
| 500000 | | 3623 | |
| 700000 | | 4460 | |
| 1200000 | | 7054 | |

Merge

| # | Random | Ascending | Descending |
|---------|--------|-----------|------------|
| 50000 | 7569 | 4252 | 4053 |
| 60000 | 9239 | 5076 | 4982 |
| 80000 | 13045 | 6819 | 6840 |
| 100000 | 16232 | 9055 | 8843 |
| 300000 | 52189 | 28484 | 28461 |
| 500000 | 89298 | 47968 | 49096 |
| 700000 | 127941 | 69842 | 69070 |
| 1200000 | 230116 | 122134 | 120290 |

Quick 1

| # | Random | Ascending | Descending |
|---------|--------|-----------|------------|
| 50000 | 7579 | 3840 | 5603 |
| 60000 | 8955 | 4597 | 7204 |
| 80000 | 12112 | 6326 | 9443 |
| 100000 | 15469 | 8646 | 11984 |
| 300000 | 51471 | 25688 | 37675 |
| 500000 | 96842 | 43280 | 66812 |
| 700000 | 123619 | 64530 | 95930 |
| 1200000 | 218267 | 109615 | 171158 |

Quick 2

| # | Random | Ascending | Descending |
|---------|--------|-----------|------------|
| 50000 | 7574 | 3513 | 4630 |
| 60000 | 9369 | 4212 | 5548 |
| 80000 | 11845 | 5671 | 7093 |
| 100000 | 15471 | 7401 | 9679 |
| 300000 | 51059 | 24393 | 30610 |
| 500000 | 85434 | 40517 | 52003 |
| 700000 | 123365 | 61175 | 76062 |
| 1200000 | 223048 | 107148 | 133532 |

Answer Question:

1. **-Random:** the selection sort, Bubble sort and insertion sort are quadratic growth rate, because I can observe that the curves of them are not linear from the graphs, and time increase while the problem size increases, their complexity is $O(n^2)$ and the curves of them are above the merge, quick1 and quick2 sorts. Moreover, the merge sort, quick 1 and quick 2 sorts in the random condition are almost like $N \cdot \log N$, because the curves of them are below the selection sort, bubble and insertion sort, the time they (merge, quick1, quick2) used are smaller than others when the problem size is same. $O(N \cdot \log N) < O(N^2)$

Ascending: the selection will cost more time when the problem size is same, and its curve is quadratic growth rate, because the selection sort curve is above others a lot., and its curve is also quadratic growth rate, problem size increases then time increases. On the other hand, the curve of bubble case in ascending is linear $O(n)$. The insertion sort is linear $O(n)$ in ascending condition. because when the problem size increases from N to $2N$, the time also increases to $2T$ (previous time). Merge, quick 1 and quick2 sort are $N \cdot \log N$ curve, because when the problem size is same, the time that these three sort used is larger than bubble and insertion, but lower than selection in ascending condition, then I can conclude that its complexity must be between $O(N)$ and $O(N^2)$, so it is $O(N \cdot \log N)$.

Descending: the curves of selection, bubble, insertion sorts in descending are quadratic growth rate, $O(n^2)$. because when problem size increase from N to $2N$, the time increase to 4 times of previous time.

Merge, and quick 1 are $n \cdot \log N$ curve, their curves are below the bubble and insertion when the problem size is same. And the quick 2 is also $O(N \log N)$, because its curve is similar to quick 1.

2. $N = 10,000,000$;

Selection sort: Random: $n=50000$, $t = 2928250$

$$N=10,000,000, T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 11.6 \cdot 10^{10}$$

Ascending: $n = 50000$, $t = 2530596$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 10.12 \cdot 10^{10}$$

Descending: $n = 50000$, $t = 2731627$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 10.92 \cdot 10^{10}$$

Bubble sort: Random: $n=50000$, $t = 4419667$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 17.6 \cdot 10^{10}$$

Ascending: $n=50000$, $t = 191$

$$T = 10,000,000/50000 \cdot t = 200 \cdot t \approx 38200$$

Descending: $n=50000$, $t = 3806293$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 15.2 \cdot 10^{10}$$

Insertion Sort: : Random: $n=50000$, $t = 1552793$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 6.2 \cdot 10^{10}$$

Ascending: $n=50000$, $t = 268$

$$T = 10,000,000/50000 \cdot t = 200 \cdot t \approx 53600$$

Descending: $n=50000$, $t = 3099826$

$$T = (10,000,000/50000)^2 \cdot t = 40000 \cdot t \approx 12.36 \cdot 10^{10}$$

Merge Sort: : Random: $n=50000$, $t = 7569$, $N = 10000000$, $T/t = N \log N / n \log n$

$O(N \log N)$ $T \approx 2107833$

Ascending: $n=50000$, $t = 4252$, $N = 10000000$, $T/t = N \log N / n \log n$

$$T \approx 1131936$$

Descending: $n=50000$, $t = 4053$, $T/t = N \log N / n \log n$

$$T = 1123475$$

Quick1 Sort: : Random: $n=50000$, $t = 7579$, $T/t = N \log N / n \log n$

$O(N \log N)$ $T \approx 1985671$

Ascending: $n=50000$, $t = 3840$, $T/t = N \log N / n \log n$

$$T \approx 1029164$$

Descending: $n=50000$, $t = 5603$,

$$T = 1578350$$

Quick2 Sort: : Random: $n=50000$, $t = 7574$

$$T \approx 2018556$$

Ascending: $n=50000$, $t = 3513$

$$T \approx 982299$$

Descending: $n=50000$, $t = 4630$

$$T \approx 1204447$$





