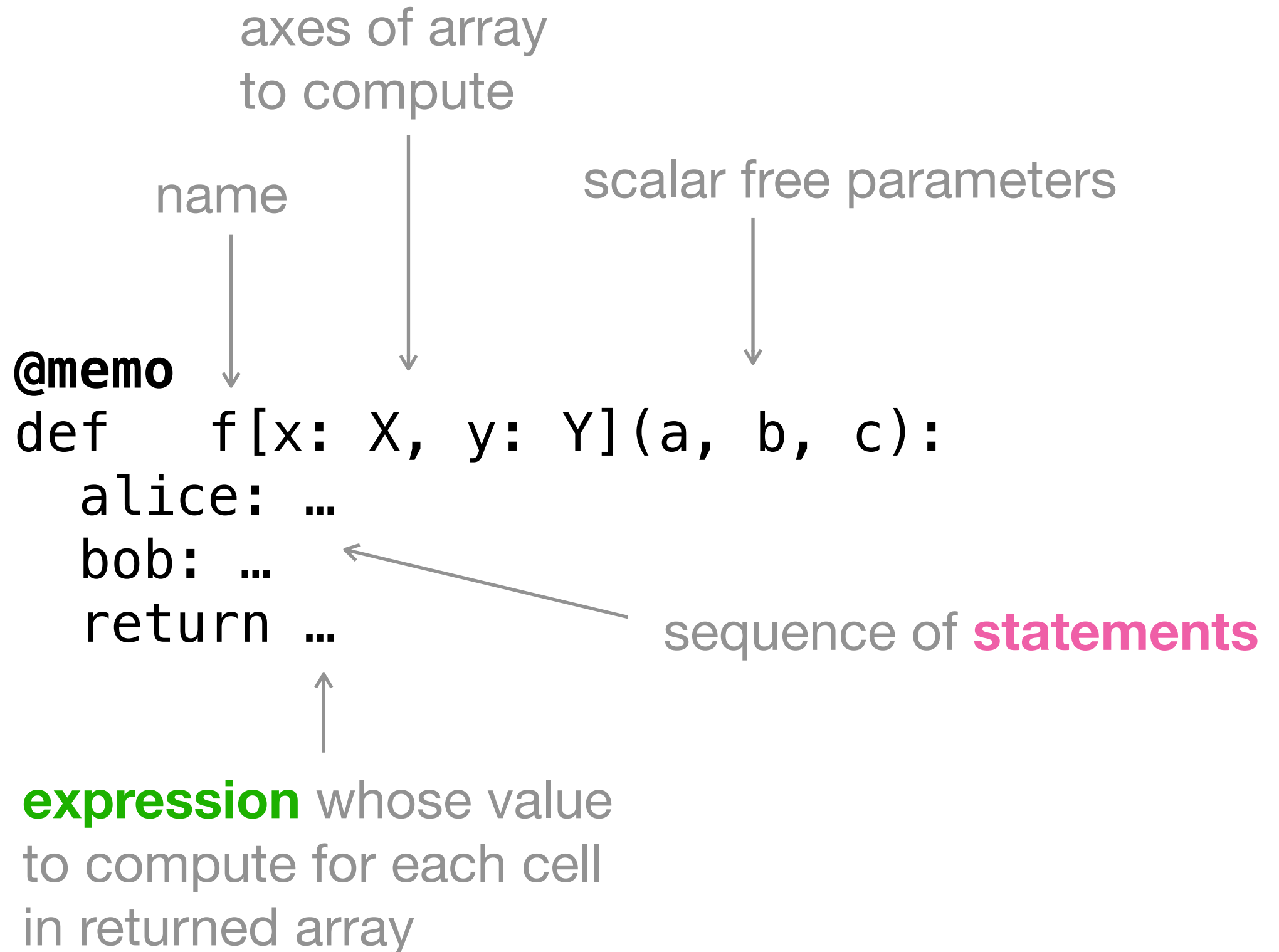


The memo handbook



Anatomy of a memo



Statements

chooses

Domain of choice (name of Python list/enum or JAX array)

Agent making choice

bob: chooses(a in Actions, wpp=exp(β *utility(a)))

Name of choice

"With probability proportional to"
For softmax, use wpp=exp(...)
For uniform choice, use wpp=1

Can make multiple choices simultaneously

bob: chooses(x in X, y in Y, wpp=joint(x, y))

more ways to choose

bob: **chooses**(a in Actions, **to_maximize**=utility(a))

↑
For argmax use to_maximize
For argmin use to_minimize

Aliases of "chooses" that don't imply agency/goal-orientation

↓
bob: **given**(r in Roles, wpp=1)
bob: **draws**(r in Roles, wpp=1)
bob: **assigned**(r in Roles, wpp=1)

thinks

Agent doing the thinking



```
bob: thinks[  
    alice: chooses(...),  
    charlie: chooses(...),  
    ...  
]
```

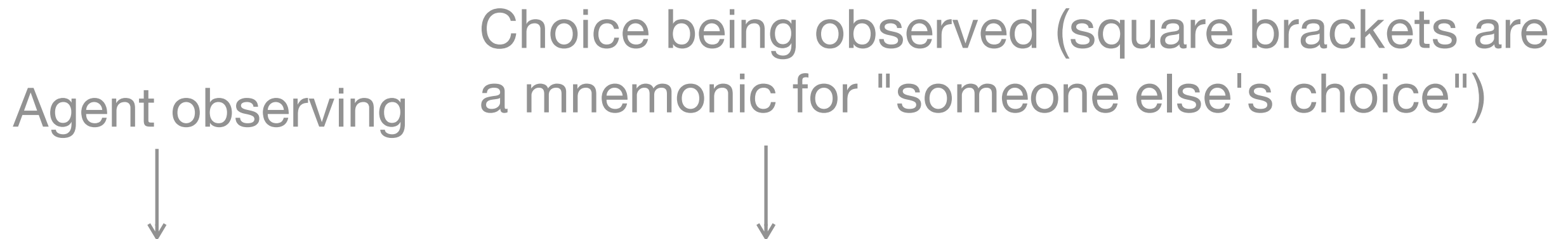


What that agent thinks
(notice the commas!)

observes

Agent observing

Choice being observed (square brackets are a mnemonic for "someone else's choice")



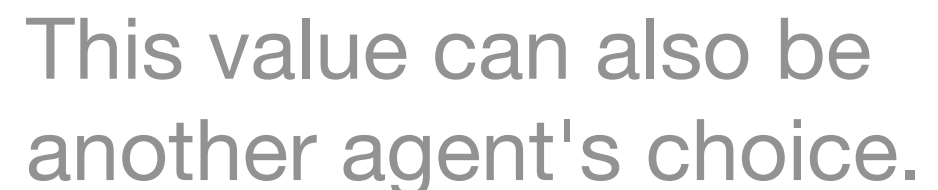
bob: observes [alice.x] is y

What the choice is observed to actually be.
Can create false beliefs this way!

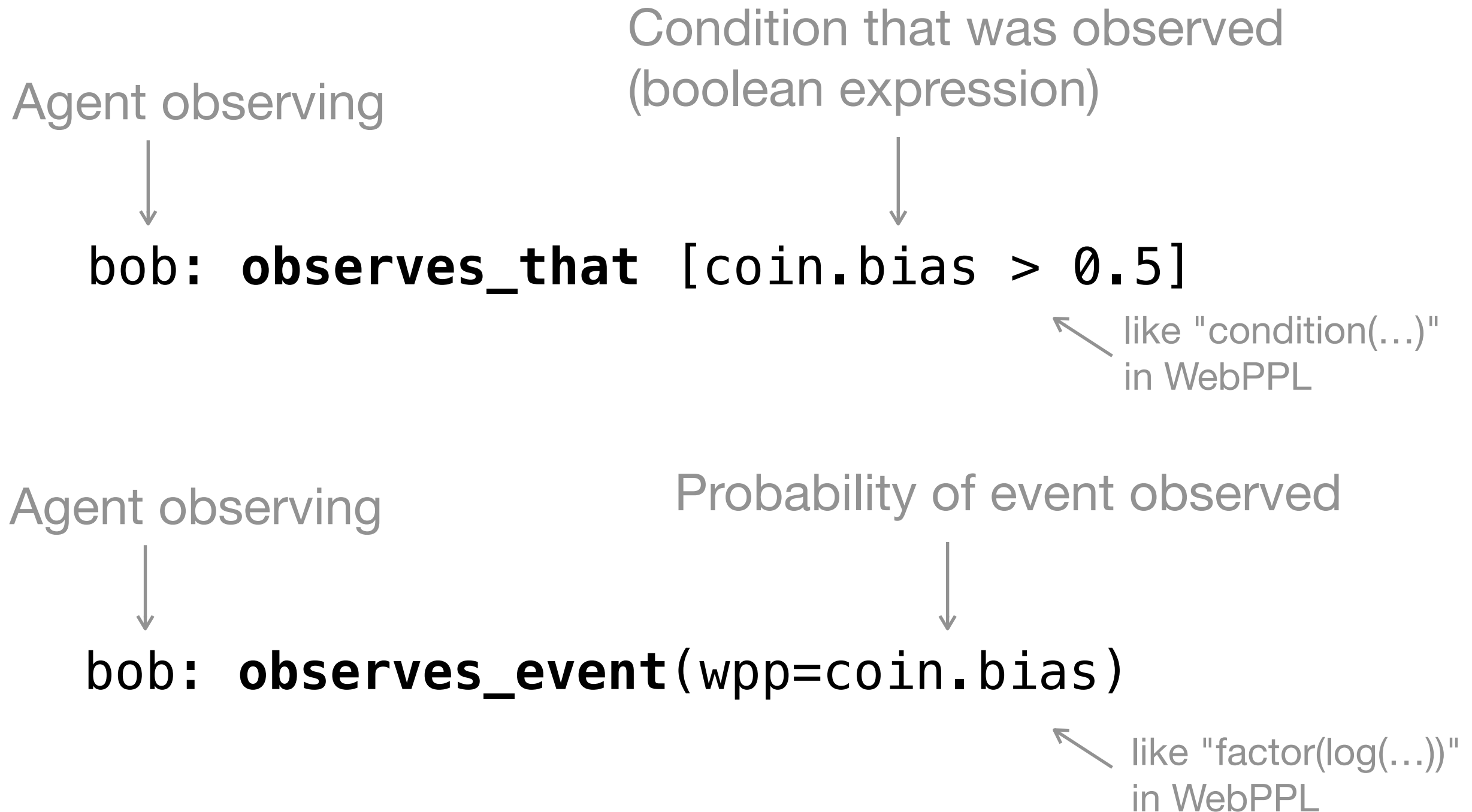


bob: observes [alice.x] is charlie.y

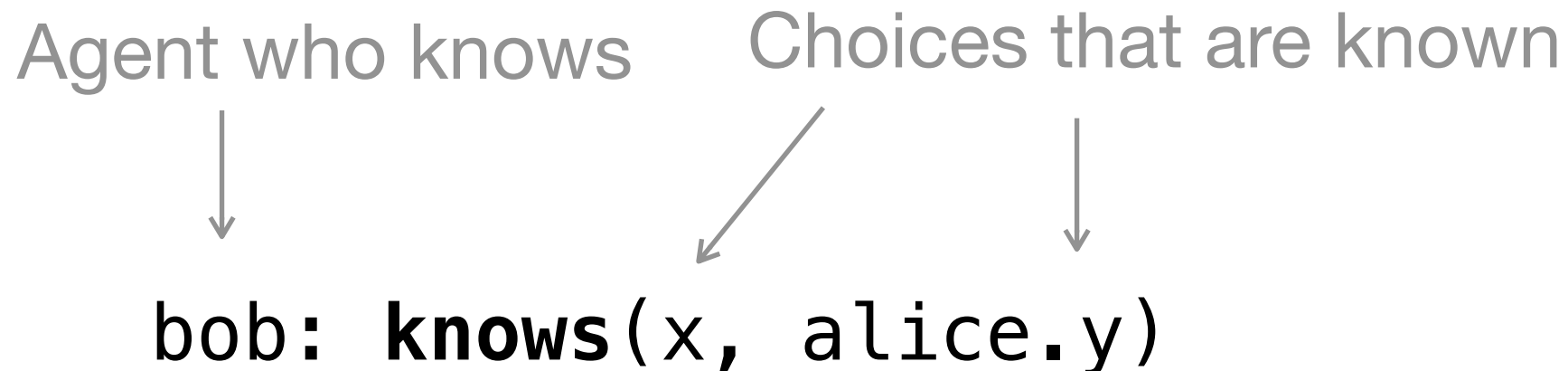
This value can also be
another agent's choice.



more ways to observe



knows



This utility is useful for the common case of "pushing" a variable into an agent's frame of mind. Roughly shorthand for this:

↓

```
bob: thinks[ alice: chooses(y in Y, wpp=...) ]  
bob: observes [alice.y] is alice.y
```

snapshots_self_as

Agents can remember "snapshots" of their past selves.
Useful for counterfactuals and hypotheticals, especially
when used with "imagine" expressions (see below...).

Agent who snapshots "aliases" of snapshots
↓ ↓
alice: **snapshots_self_as**(past_alice, ...)

```
alice: observes [bob.x] is x  
return alice[ past_alice[ E[bob.x] ] ]
```

not affected by "observe" statement

Expressions

literals

floating-point numbers only



3.14

also references to declared free parameters



a, b, c, ...

operators

memo supports most Python unary/binary ops

↓
`1 + 1`

also some free bonus functions

↓
`exp(...), log(...), abs(...)`

can also call any function tagged with `@jax.jit`

↓
`@jax.jit`
`def f(x):`

`return np.cos(x)`

useful for calling deep learning, etc.
JAX is a big ecosystem

← note: can only take scalar inputs
and can only return one scalar output

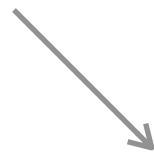
choices

```
alice: chooses(x in X, wpp=1)  
alice: chooses(y in Y, wpp=f(x, y))
```



you can refer to an agent's own
choice as if it were simply a variable

or refer to other agents' choices with "dot" notation



```
alice.x + alice.y
```

probabilistic operators

expectation



E[alice.x + bob.z]

(mutual) entropy between choices



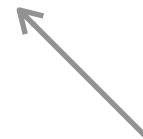
H[alice.x, bob.y, ...]

probability



Pr[alice.y >= 0]
Pr[a.x > 0, b.y < 2]

can use both
commas and
"and" for joint



variance



Var[alice.y * 2]

queries

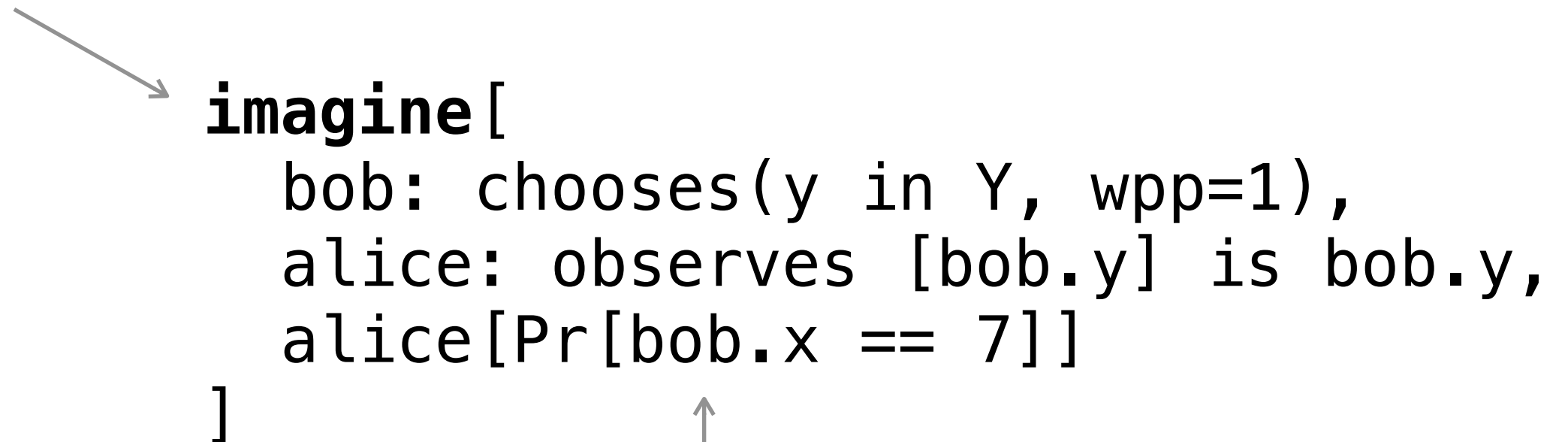
```
Var[alice[abs(x) * 2]]  
alice[bob.y == 7]
```



can "query" another agent for the value
of an expression using square brackets

hypotheticals

set up hypothetical world by
running statements



The diagram illustrates the process of setting up a hypothetical world. It features a code block for the `imagine` function. An arrow points from the text 'set up hypothetical world by running statements' to the opening bracket of the `imagine` function. Another arrow points from the text 'last line = expression to evaluate in that world' to the final expression inside the function, `alice[Pr[bob.x == 7]]`.

```
imagine[  
    bob: chooses(y in Y, wpp=1),  
    alice: observes [bob.y] is bob.y,  
    alice[Pr[bob.x == 7]]  
]
```

last line = expression to
evaluate in that world

memo calls

```
@memo  
def f[x: X](a): ...
```

```
@memo  
def g():  
  alice: chooses(x in X, wpp=f[x](3.14))
```



can reference one memo from another,
syntax evokes array indexing.
need to pass parameters, too!

cost reflection

```
@memo def f[...](a, b, c): ...
```

```
cost @ f(3, 4, 5)
```



get number of FLOPs needed
to evaluate f
(note: no axes, params only!)

reference to Python variable

```
class Action(IntEnum): WAIT = 0; ...
```

```
@memo def f[...](...):  
    return {Action.WAIT}
```



use braces for inline reference
to a global Python variable

Things to do with a memo

Running a memo

call it like a function with params
(returns an array with prescribed axes)



`f(a, b)`

pretty-print table of results



`f(a, b, print_table=True)`

`f(a, b, return_pandas=True)`

`f(a, b, return_xarray=True)`

get outputs in other formats

save "comic book" visualization of model via graphviz



`f(a, b, save_comic="file")`

Automatic differentiation (useful for fitting by gradient descent)

```
@memo  
def f[...](a, b): ...
```

returns tuple of value + gradient wrt params a & b



```
jax.value_and_grad(f)(a, b)
```