```
1: // $Id: powerint.cpp,v 1.14 2016-06-13 13:44:54-07 - - $
 2:
 3: //
 4: // NAME
 5: //
          powerint - power function raising a double to an int power
 6: //
 7: // SYNOPSIS
 8: //
          double powi (double base, int exponent);
9: //
10: // DESCRIPTION
11: //
          The powi() function computes the value of base raised to the
12: //
          power exponent.
13: //
14: // RETURN VALUES
15: //
          Upon successful completion, powi() returns the value of base
16: //
          raised to the power of exponent. If exponent is 0, 1.0 is
17: //
          returned regardless of the value of base (a number, 0, NaN,
18: //
          or +-Infinity). Otherwise multiplication and division are
19: //
          subject to the rules of IEEE-754 floating point arithmetic,
20: //
          for CPUs which support that.
21: //
22: // MATHEMATICS USED
23: //
24: //
          powi (x, -n)
                          \Rightarrow powi (1 / x, n)
25: //
          powi (x, 2 n)
                          => powi (x ** 2, n / 2)
26: //
          powi (x, n + 1) \Rightarrow x * powi (x, n)
27: //
28: //
          .EQ
29: //
                          = \{ (1 / x) \} \sup n
          x sup { - n }
30: //
                          = (x sup 2) sup {n / 2}
          x sup { 2 n }
31: //
          x \sup \{n+1\} = x (x \sup n)
32: //
          .EN
33: //
34: //
          $$
35: //
          x ^{n} \{ -n \}
                        = \{ (1 / x) \} ^n
          x^{(n)} = (x^{(n)} = (x^{(n)})
36: //
37: //
          x^{n} \{ n + 1 \} = x (x^{n})
38: //
          $$
39: //
40: //
41:
42: #include <cstdlib>
43: #include <iomanip>
44: #include <iostream>
45: #include <libgen.h>
46: #include <limits>
47: #include <sstream>
48: #include <string>
49: #include <typeinfo>
50: #include <vector>
51:
52: using namespace std;
54: const int DIGITS = numeric_limits<double>::digits10 + 6;
```

```
55:
 56: template <typename item_t>
 57: item_t from_string (const string& arg) {
        stringstream stream {arg};
 58:
 59:
        item_t result;
 60:
        stream >> result;
 61:
        return result;
 62: }
 63:
 64: void print_powi (double base, int exponent, double result) {
 65:
        cout << "powi: " << base << " ** " << exponent << " * "
 66:
             << result << endl;
 67: }
 68:
 69: double powi (double base, int exponent) {
 70:
        double result = 1.0;
 71:
        print_powi (base, exponent, result);
 72:
        if (exponent < 0) {</pre>
 73:
           base = 1.0 / base;
 74:
           exponent = - exponent;
 75:
           print_powi (base, exponent, result);
 76:
 77:
        while (exponent > 0) {
 78:
           if (exponent % 2 == 0) { /* is even */
 79:
              base *= base;
 80:
              exponent /= 2;
 81:
           }else {
 82:
              result *= base;
 83:
              --exponent;
 84:
           }
 85:
           print_powi (base, exponent, result);
 86:
 87:
        return result;
 88: }
 89:
 90: int main (int argc, char** argv) {
 91:
        vector<string> args (&argv[1], &argv[argc]);
 92:
        for (auto arg = args.cbegin(); arg != args.cend(); ++arg) {
 93:
           double base = from_string<double> (*arg);
           if (++arg == args.cend()) break;
 94:
 95:
           int exponent = from_string<int> (*arg);
 96:
           cout << endl << setprecision (DIGITS);</pre>
 97:
           double result = powi (base, exponent);
           cout << "ANSWER: " << base << " ** " << exponent
 98:
 99:
                << " == " << result << endl;
100:
101:
        return 0;
102: }
103:
104: /*
105: //TEST// valgrind --leak-check=full --show-reachable=yes \
106: //TEST//
                    --log-file=powerint.out.grind \
107: //TEST//
                    powerint 2 2 2 9 2 15 2 16 2 24 \
108: //TEST//
                    >powerint.out 2>&1
109: //TEST// mkpspdf powerint.ps powerint.cpp* powerint.out*
110: */
111:
```

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\$cmps109-wm/Assignments/asg1-dc-bigint/misc/powerint.cpp.log

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```
1:
 2: powi: 2 ** 2 * 1
 3: powi: 4 ** 1 * 1
 4: powi: 4 ** 0 * 4
 5: ANSWER: 2 ** 2 == 4
 6:
7: powi: 2 ** 9 * 1
 8: powi: 2 ** 8 * 2
 9: powi: 4 ** 4 * 2
10: powi: 16 ** 2 * 2
11: powi: 256 ** 1 * 2
12: powi: 256 ** 0 * 512
13: ANSWER: 2 ** 9 == 512
14:
15: powi: 2 ** 15 * 1
16: powi: 2 ** 14 * 2
17: powi: 4 ** 7 * 2
18: powi: 4 ** 6 * 8
19: powi: 16 ** 3 * 8
20: powi: 16 ** 2 * 128
21: powi: 256 ** 1 * 128
22: powi: 256 ** 0 * 32768
23: ANSWER: 2 ** 15 == 32768
24:
25: powi: 2 ** 16 * 1
26: powi: 4 ** 8 * 1
27: powi: 16 ** 4 * 1
28: powi: 256 ** 2 * 1
29: powi: 65536 ** 1 * 1
30: powi: 65536 ** 0 * 65536
31: ANSWER: 2 ** 16 == 65536
32:
33: powi: 2 ** 24 * 1
34: powi: 4 ** 12 * 1
35: powi: 16 ** 6 * 1
36: powi: 256 ** 3 * 1
37: powi: 256 ** 2 * 256
38: powi: 65536 ** 1 * 256
39: powi: 65536 ** 0 * 16777216
40: ANSWER: 2 ** 24 == 16777216
```

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\$cmps109-wm/Assignments/asg1-dc-bigint/misc/powerint.out.grind

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```
1: ==10852== Memcheck, a memory error detector
    2: ==10852== Copyright (C) 2002-2013, and GNU GPL'd, by Julian Seward et al
    3: ==10852== Using Valgrind-3.10.1 and LibVEX; rerun with -h for copyright
info
    4: ==10852== Command: powerint 2 2 2 9 2 15 2 16 2 24
    5: ==10852== Parent PID: 10851
    6: ==10852==
    7: ==10852==
    8: ==10852== HEAP SUMMARY:
    9: ==10852==
                     in use at exit: 0 bytes in 0 blocks
   10: ==10852==
                   total heap usage: 27 allocs, 27 frees, 907 bytes allocated
   11: ==10852==
   12: ==10852== All heap blocks were freed -- no leaks are possible
   13: ==10852==
   14: ==10852== For counts of detected and suppressed errors, rerun with: -v
   15: ==10852== ERROR SUMMARY: 0 errors from 0 contexts (suppressed: 1 from 1)
```