

Module FA

TopOpt?

Prof. J. Morlier

https://github.com/jomorlier/ALMcourse



History

- Homogenization of Microstructures was introduced by mathematics in the 1970s.
- First paper by Martin Bendsoe (Technical University of Denmark) and Noboru Kikuchi (University of Michigan) in 1000

A topology optimisation problem can be written in the general form of an optimization problem as

$$\min_{
ho} \; F = F(\mathbf{u}(
ho),
ho) = \int_{\Omega} f(\mathbf{u}(
ho),
ho) \mathrm{d}V$$

subject to

- $egin{align} oldsymbol{G}_0(
 ho) &= \int_\Omega
 ho(\mathbf{u}) \mathrm{d}V V_0 \leq 0 \ oldsymbol{G}_j(\mathbf{u}(
 ho),
 ho) \leq 0 ext{ with } j=1,\ldots,m \ \end{pmatrix}$

TopOpt

Je choisis un bloc de marbre et j'enlève tout ce dont je n' ai pas besoin.. Auguste Rodin (1840-1917)



Define the design space (marble block, fixed mesh)

Apply loads & BCs

Start optimization with hyper parameters

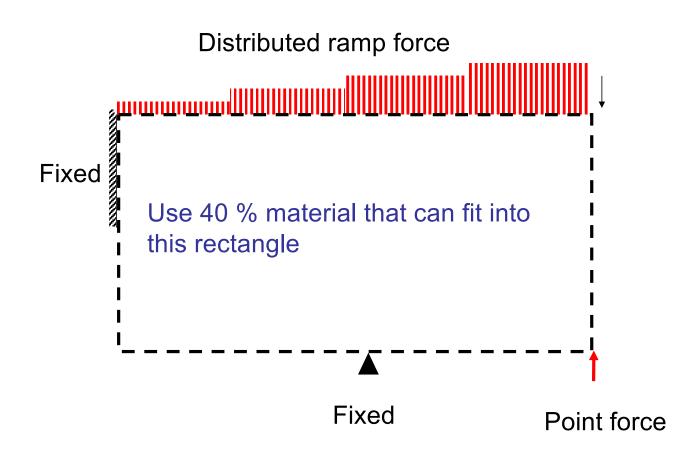
Interpreting the results

Optimal distribution of material (One can have an idea of the part to be reinforced, in addition to giving an excellent initial design ...)

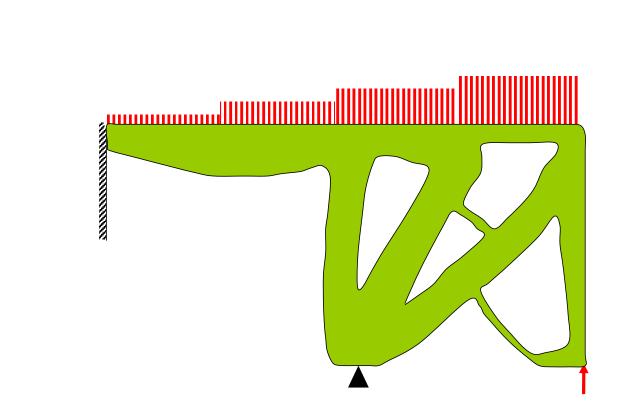
Why is it so powerful?

→There is a lot of possible redistribution of FORCES (internal)

Stiff structure for your specifications



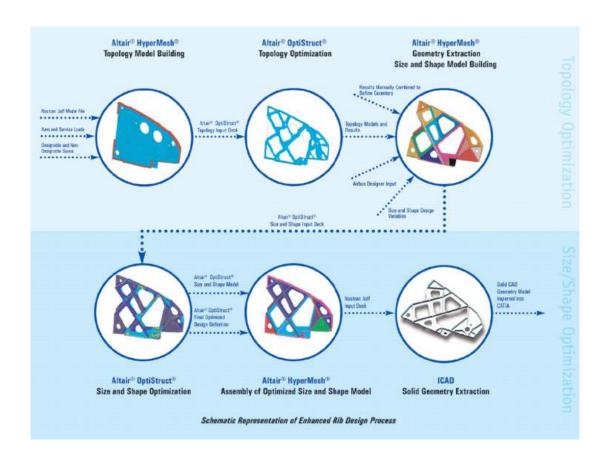
Stiff structure for your specifications



Well-Known example



Topology and shape optimization



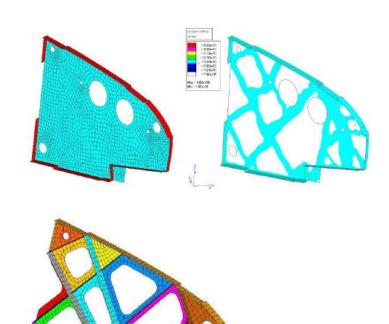


Airbus A380 example (cont.)

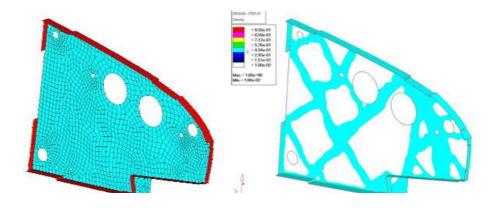
• Topology optimization:

• Sizing / shape optimization:





Finally...





Airbus A380 example (cont.)

Altair Engineering

HINGE RIB 4 -

Wing rib designs

The perforated plates were replaced by reinforced lattice structures (think of the path of preferential intern foces)

Is this really a discovery?



Supermarine Southampton, 1925



System approach automates the process!

Industrial probems

TopOpt: Preliminary phases of a project

The idea is to find the best path of stiffening in a given volume of matter.

The mass is only found where it is needed, which is a good starting point for optimization of shape or dimensioning.

Adapted formulation:

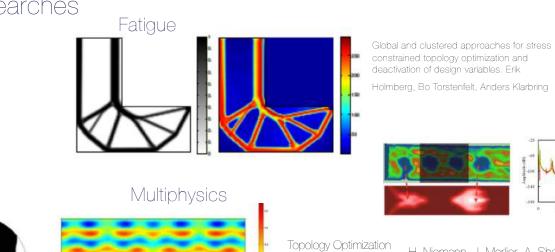
To find the structure with the best static behavior.

The paths of internal forces identified are those which help to rigidify the structure as well as possible

→ The structure will deform less, and stress levels will be possibly limited. But not only...

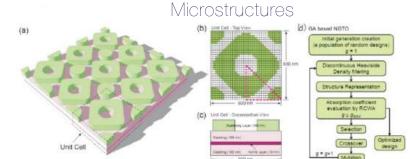
→ Lots of Actuall Researches

Optimal shape



Topology Optimization of silver nano-particles in thin film solar cells Soohwan Byun,
Jeonghoon Yoo

H. Niemann, J. Morlier, A. Shahdin and Y. Gourinat. Damage Localization using Experimental Modal Parameters and Topology Optimization. Mechanical Systems and Signal Processing. 24(3)636-652. 2010



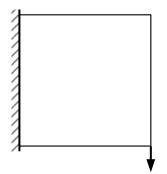
Electric field

Topology Optimization for Highly-efficient Light-trapping Structure in Solar Cell Shuangcheng Yu, Chen Wang, Cheng Sun, Wei Chen*

Discrete Material Optimization:

Prof. Pierre DUYSINX Université de Liège LTAS - Automotive Engineering

Maximum stiffness in the plane of a plate by selecting the best orientations of fibers



| 13 | 14 | 15 | 1 |
|----|----|----|---------|
| 9 | 10 | 11 | -6 1 |
| 5 | 6 | 7 | 8 |
| 1 | 2 | 3 | 4 |

Loads and boundary conditions

Design model with 4* 4 patches

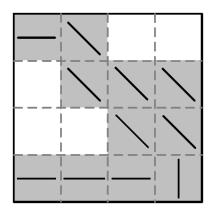
| Table 4 Material properties | | | | | |
|-----------------------------|-----------|----------|----------|--|--|
| E_x | E_{ν} | G_{xy} | v_{xy} | | |
| 146.86GPa | 10.62GPa | 5.45GPa | 0.33 | | |

| Table 3 Orientations | | | | |
|-------------------------------|--|---|--|--|
| Number of material phases (m) | Number of design variables for each region (m_v) | Discrete orientation angle (°) | | |
| 4 | 2 | 90/45/0/-45 | | |
| 9 | 4 | 80/60/40/20/0/-20/-40/-60/-80 | | |
| 12 | 4 | 90/75/60/45/30/15/0/-15/-30/-45/-60/-75 | | |

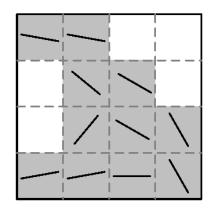
Discrete Material Optimization: exemple

Topological optimization: vacuum + composite laminate

Volume constraints: V < 11/16



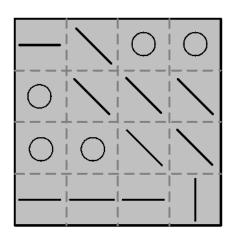
4 orientations 90/45/0/-45



18 orientations 90/80/70/60/50/40/30/20/10/0 / -10/-20/-30/-40/-50/-60/-70/-80

Discrete Material Optimization: exemple

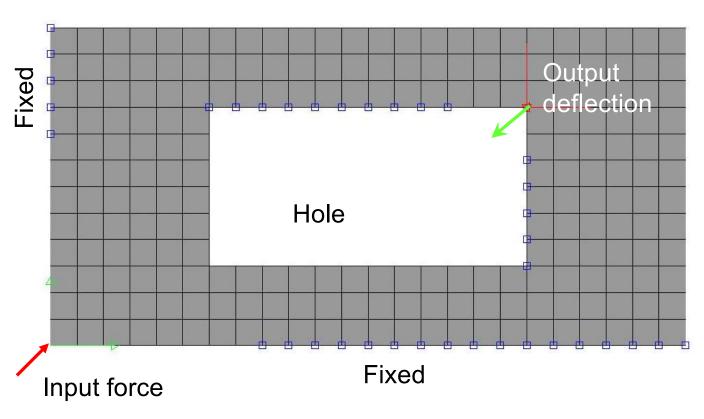
Use of both glass fibers and foam Limitation of the number of domains occupied by the fiber of glass



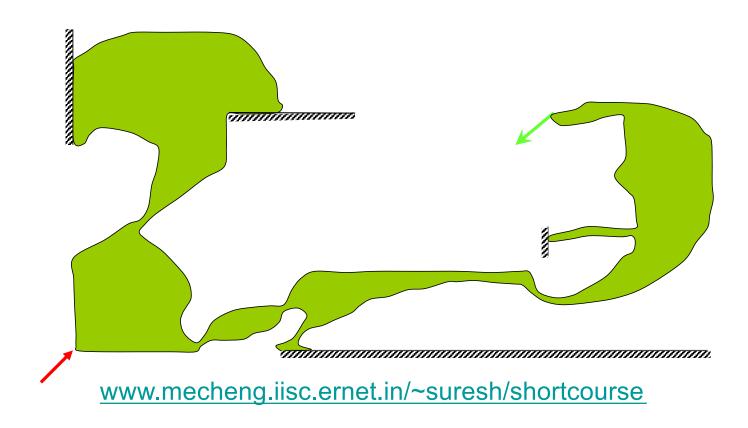
Optimization result of the square plate under vertical force with volume constraint
Glass-epoxy with 4 orientations
(90/45/0/-45) and polymer-foam

Compliant mechanism to your specifications

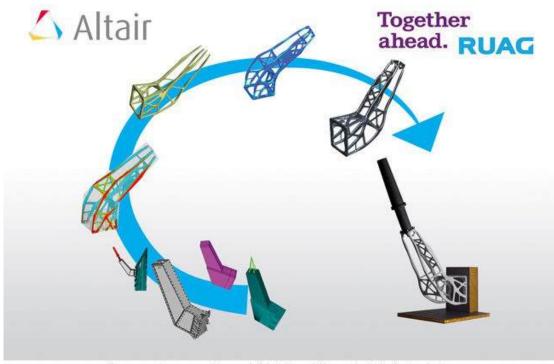




Compliant mechanism to your specifications



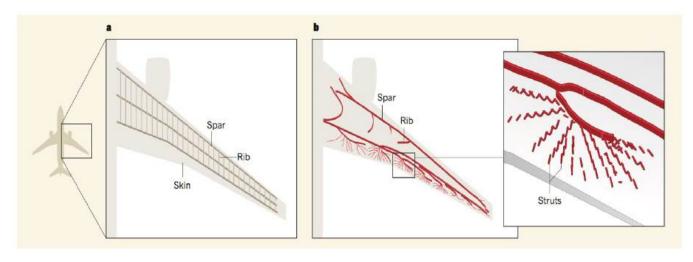
ALM



Processus de re-conception pour la fabrication additive par l'optimisation topologique

http://bcove.me/yg7pqkak

HPC



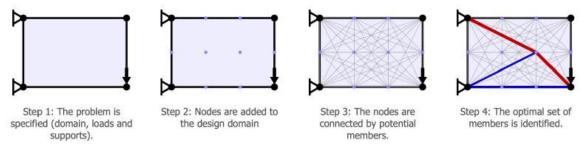
https://www.nature.com/articles/nature23911

More recently

https://www.layopt.com/truss/ https://www.youtube.com/watch?v=8OuU5K4iwSM

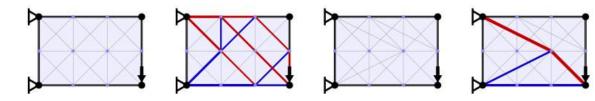
Layout Optimization

It was realized in the 1960s that minimum volume structures could be identified computationally. The steps in the numerical layout optimization procedure used by LayOpt are shown in the image below. First, the design domain (the region within which the structure is permitted to lie) is populated with nodes. Each pair of nodes is then connected with a potential structural member to create a "fully connected ground structure". Finally, a mathematical optimization problem is solved to identify the minimum volume subset of members and their sizes.

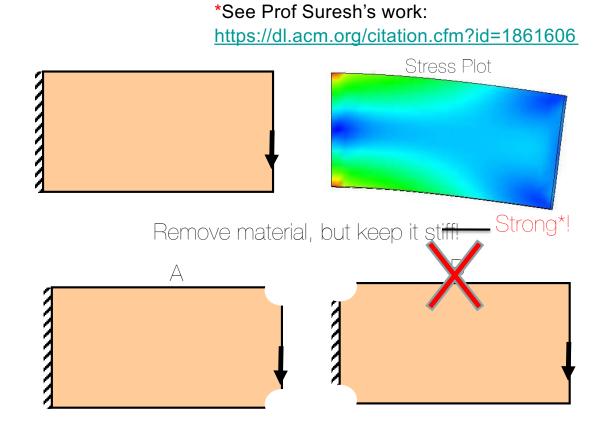


In LayOpt, nodes are located at the intersections of grid lines, and at locations where the grid lines cross the edges of the design domain. The coarseness of the grid can be adjusted using the slider. When a very fine nodal grid is employed a very close approximation of the true minimum volume is obtained. However, increasing the number of nodes also increases the computational resources required, and usually the complexity of the resulting structure.

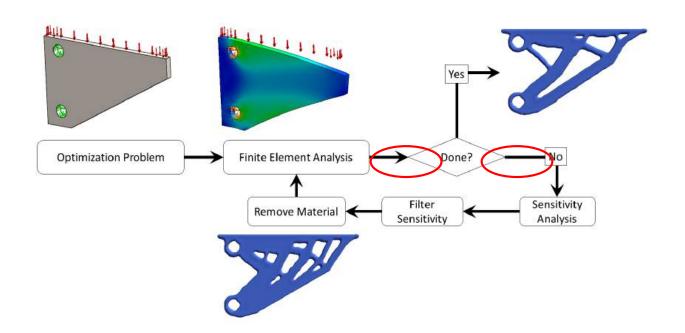
To increase the computational efficiency LayOpt makes use of the adaptive member adding method proposed by Gilbert and Tyas (2003). This only requires a subset of the possible connections to be considered initially (here only adjacent nodes are initially connected). Once this problem is solved, each initially neglected potential member is checked to see if it is likely to reduce the calculated volume. If so, then is considered for addition to the problem in the next iteration. This process continues until no potential members can be found that have the potential to reduce the volume of the structure. At this point the volume of the structure will be identical to the solution of the corresponding problem which included all potential member connections from the outset. LayOpt shows the result of each member adding iteration as it is calculated, allowing you to see how the optimal design is being identified.



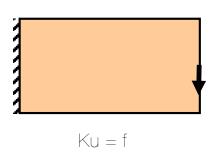
Intuition ...



TopOpt relies on FEA Online computation: http://www.cloudtopopt.com



TopOpt



- 1. Objective?
- 2. Constraints?
- 3. Method?

Compliance $J = f^Tu$

Compliance = 1/Stiffness

Minimize Compliance

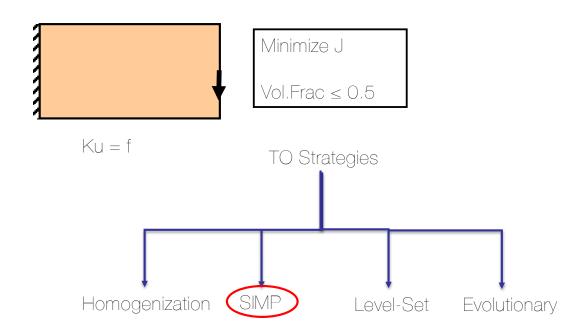
Volume Constraint

Minimize J

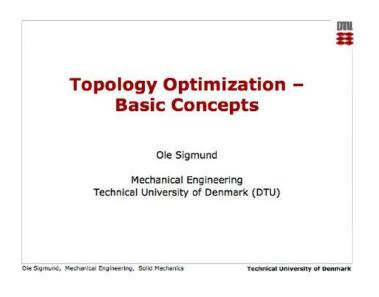
 $Vol.Frac \le 0.5$

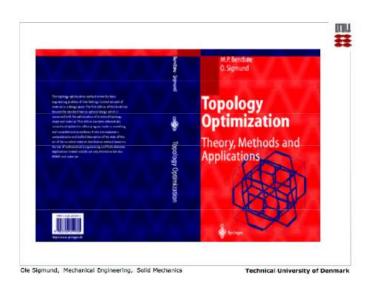
Method: Gradient based: Need sensitivities...

Current TO Strategies



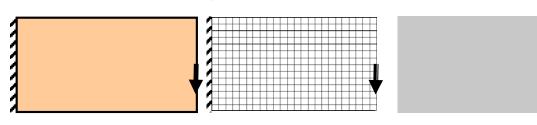
One pioneer, SIMP (Solid Isotropic Material with Penalization)





SIMP

SIMP: Solid Isotropic Material with Penalization



Min Compliance

$$v = 0.5v_0$$

Where do we add holes?

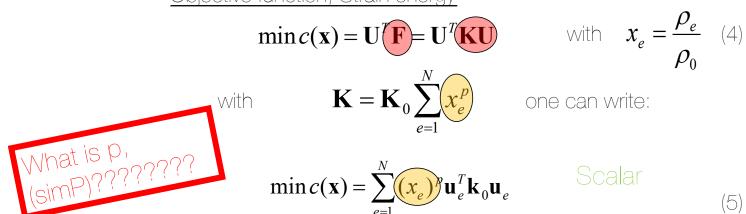
 $0<\rho_{\epsilon}\leq 1$: 'Pseudo Density'

 $Min_{\rho_{\epsilon}}$ Compliance

$$\sum \rho_{e} v_{e} = 0.5 v_{0}$$

Intuitive Problem? Quadratic Form

Objective function; Strain energy



Contraints: mass target

$$\frac{V(\mathbf{x})}{V_0} = f = \underbrace{const} \iff \sum_{e=1}^{N} V_{e} \underbrace{x_e} V_0 f = 0 = h(\mathbf{x})^{\text{Scalar}}$$
$$0 < \rho_{\min} \le \rho_e \le 1$$

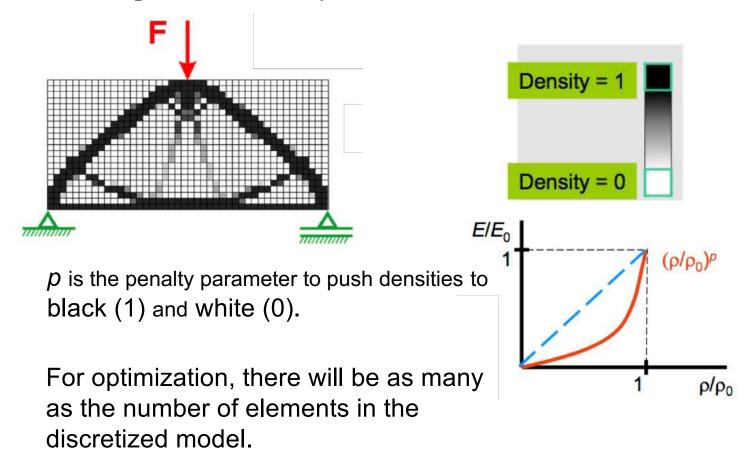
Quadratic Form

X ∈ R MXI, AI ∈ R MXM

Quadratic form: XTAIX

 $X^TA|X$ is a scalar value. $(1\times m)\times (m\times m)\times (m\times 1) \rightarrow 1\times 1$

Penalization for altering stiffness localy



Rozvany, G.I.N., Zhou, M., and Gollub, M. (1989). Continuum Type Optimality Criteria Methods for Large Finite Element Systems with a Displacement Connstraint, Part 1. *Structural Optimization* 1:47-72.

Penalty parameter in the SIMP method: some justification

Hashin-Shtrikman bounds

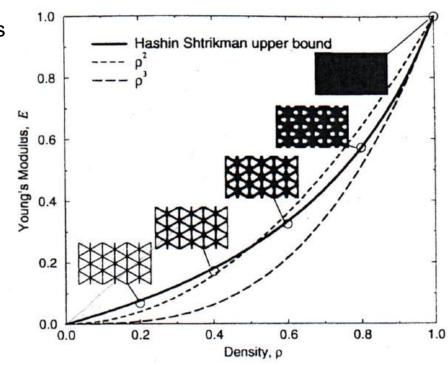
$$0 \le E \le \frac{\rho E^0}{3 - 2\rho}$$

Therefore,

$$\rho^{p}E^{0} \leq \frac{\rho E^{0}}{3 - 2\rho}$$

$$\Rightarrow p \geq 3$$

$$\Rightarrow p \ge 3$$



Bendsøe, M.P. and Sigmund, O., "Material Interpolation Schemes in Topology Optimization," Archives in Applied Mechanics, Vol. 69, (9-10), 1999, pp. 635-654.

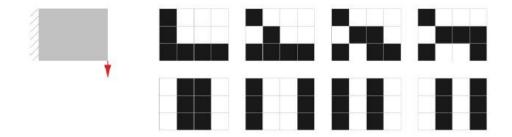
Pixels?





Pixels

- Finding a solution by checking all the possible combinations IS impossible since the number of topologies nT increases exponentially with the number of finite elements n
- $nT = 2^n$



The legal (top) and some illegal (bottom) topologies with 4 by 3 elements

Division into elements (pixels or voxels) and binary decision for each or example 10,000 elements --> 210,000 possible configurations!

Nice idea!

- 1. Transform discrete variables continuously (TO USE gradient-based algorithms)
- 2. Find an objective function with "cheap" derivatives (we will see this later)

Others formulations

$$\min_{\boldsymbol{\mu}} \max_{l=1,\dots,nc} C_l = \mathbf{F}_l^T \mathbf{q}_l$$

$$\sum_{i} \mu_i V_i \leq \overline{V}$$

$$0 < \underline{\mu}_i \leq \mu_i \leq 1$$

$$\min_{\boldsymbol{\mu}} \sum_{i} \mu_{i} V_{i}$$

$$q_{j} \leq \overline{q}_{j} \qquad j = 1, ..., m$$

$$0 < \underline{\mu}_{i} \leq \mu_{i} \leq 1$$

- If several load cases no
- → we can minimize the maximal compliance
- → with all obtained by solving Klial=Fl
- Prescribed displacement
- → we can minimize the volume (mass)
- → wrt amplitude at node j inferior to a certain displacement

Others formulations

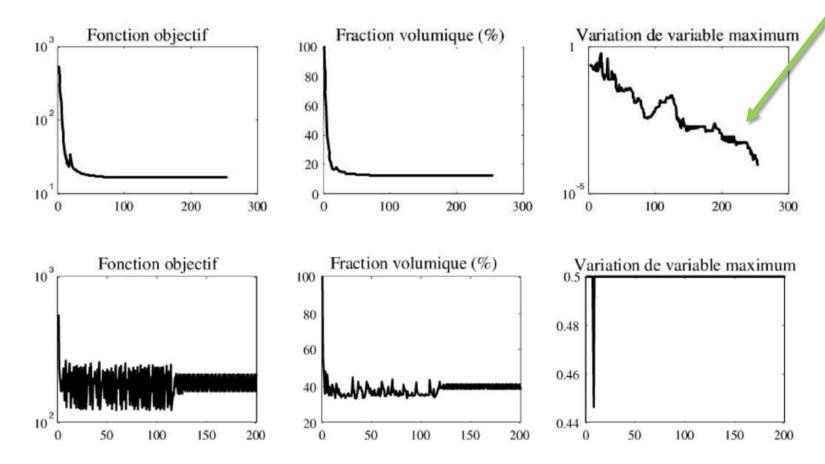
$$\max_{\mu} \min_{k=1,nf} \omega_{k}$$

$$\sum_{i} \mu_{i} V_{i} \leq \overline{V}$$

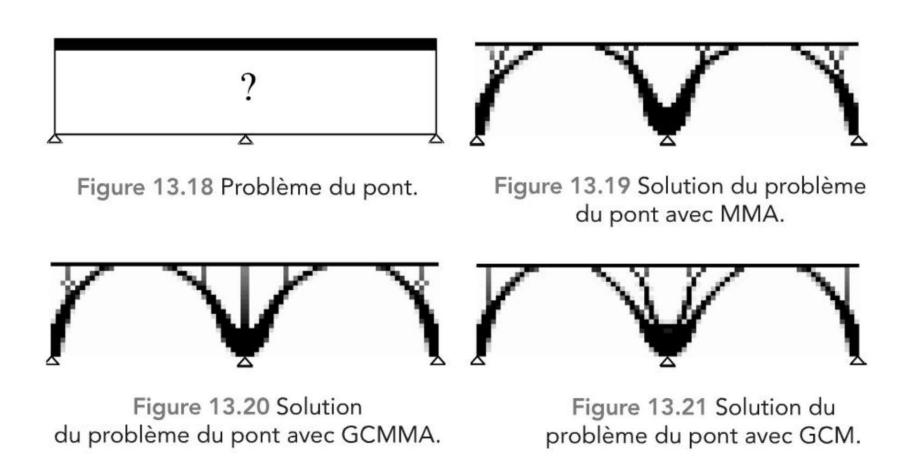
$$0 < \underline{\mu}_{i} \leq \mu_{i} \leq 1$$

- Eigensolver to obtain the stiffest structure at a certain volfrac
- → wrt a vibration ccriteria

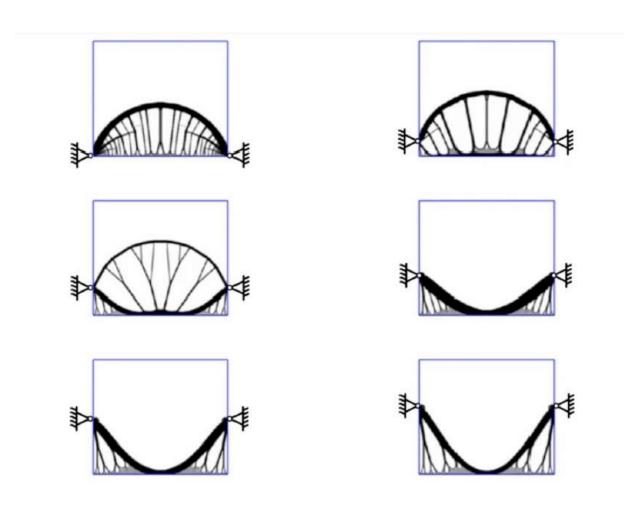
Which is the best optimizer? why?



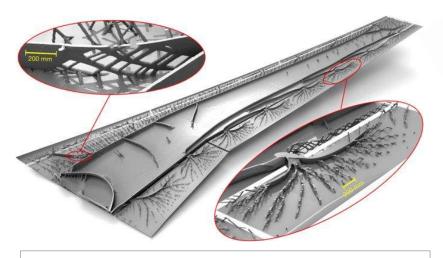
Can you comment this? Compliance are re



Small changes in BCs ...

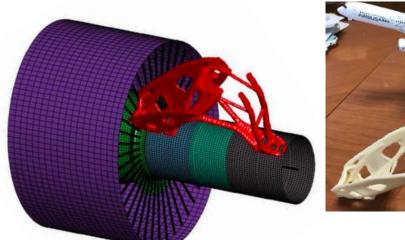


Interested in research?



Niels Aage, Erik Andreassen, Boyan S Lazarov, and Ole Sigmund. Giga-voxel computational morphogenesis for structural design. Nature, 550(7674):84, 2017.

Coniglio, S., Gogu, C., Amargier, R., & Morlier, J. (2019, May). Application of geometric feature based topology optimization to engine pylon architecture design including engine performance criteria. In 13th Wolrd Congress on Structural and Multidisciplinary Optimization.





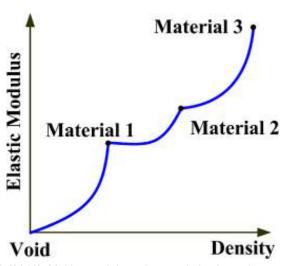
Coniglio, S., Gogu, C., Amargier, R., & Morlier, J. (2019). Engine pylon topology optimization framework based on performance and stress criteria. AIAA Journal, 57(12), 5514-5526.



MULTIMATERIAL

• Solid Isotropic Material with Penalization (SIMP)

•
$$E_e(\rho_e) = A_E * \rho_e^p + B_E$$
,
 $\rho_e \in [\rho_i, \rho_{i+1}]$, $A_E = \frac{E_i - E_{i+1}}{\rho_i^p - \rho_{i+1}^p}$, $B_E = E_i - A_E * \rho_i^p$



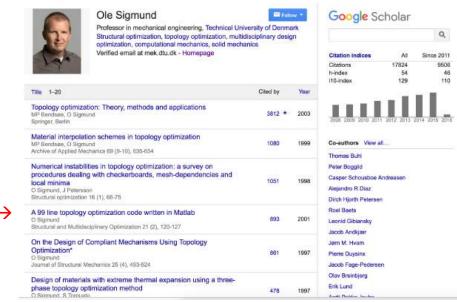
Zuo, W., & Saitou, K. (2016). Multi-material topology optimization using ordered SIMP interpolation. *Structural and Multidisciplinary Optimization*, *55*(2), 477-491. doi:10.1007/s00158-016-1513-3

BUT ...IN PRACTICE?

Educational article:

O. Sigmund, A 99 line topology optimization code written in Matlab Struct Multidisc Optim 21, 120-127 Springer-Verlag 2001

Heuristic formulation (intuitive method of optimisation, but with no convergency proofs) to update xe by bi-section algorithm



History (1988, Bendsoe)

A topology optimization problem based on the powerlaw approach, where the objective is to minimize compliance can be written as

$$\min_{\mathbf{x}} : \quad c(\mathbf{x}) = \mathbf{U}^T \mathbf{K} \mathbf{U} = \sum_{e=1}^{N} (x_e)^p \ \mathbf{u}_e^T \ \mathbf{k}_0 \ \mathbf{u}_e$$
subject to:
$$\frac{V(\mathbf{x})}{V_0} = f$$

$$: \quad \mathbf{K} \mathbf{U} = \mathbf{F}$$

$$: \quad \mathbf{0} < \mathbf{x}_{\min} \le \mathbf{x} \le \mathbf{1}$$
(1)

where **U** and **F** are the global displacement and force vectors, respectively, **K** is the global stiffness matrix, \mathbf{u}_e and \mathbf{k}_e are the element displacement vector and stiffness matrix, respectively, **x** is the vector of design variables, \mathbf{x}_{\min} is a vector of minimum relative densities (non-zero to avoid singularity), $N = (\mathbf{nelx} \times \mathbf{nely})$ is the number of elements used to discretize the design domain, p is the penalization power (typically p = 3), $V(\mathbf{x})$ and V_0 is the material volume and design domain volume, respectively and f (volfrac) is the prescribed volume fraction.

Compliance minimization self adjoint

Compliance is the opposite of stiffness

$$C = \mathbf{f}^T \mathbf{u} = \mathbf{u}^T K \mathbf{u}$$

Inexpensive derivatives (use chain rule)

$$\frac{dC}{dx} = 2\mathbf{u}^T K \frac{d\mathbf{u}}{dx} + \mathbf{u}^T \frac{dK}{dx} \mathbf{u}$$

But since $K\mathbf{u} = \mathbf{f}$ if \mathbf{f} does not depend on \mathbf{x}

$$K\frac{d\mathbf{u}}{dx} = -\frac{dK}{dx}\mathbf{u}$$

$$\frac{dC}{dx} = -\mathbf{u}^T \frac{dK}{dx} \mathbf{u}$$

Knowing displacements you also know gradients

Need a DEMO?

• Recall
$$\frac{dC}{dx} = -\mathbf{u}^T \frac{dK}{dx} \mathbf{u}$$

For density variables

$$\frac{dC}{d\rho^e} \propto -\mathbf{u}^T \rho^{p-1} K^e \mathbf{u}$$

- Want to increase density of elements with high strain energy and vice versa
- To minimize compliance for given weight can use an optimality criterion method.

And for other responses?

$$O = f(x, U)$$

$$\frac{\partial O}{\partial x} = \frac{\partial f^{T}}{\partial U} \frac{\partial U}{\partial x}$$

$$KU = F$$

$$\frac{\partial K}{\partial x}U + K\frac{\partial U}{\partial x} = 0$$

$$\frac{\partial O}{\partial x} = \frac{\partial f}{\partial U}^T \frac{\partial U}{\partial x} = -\frac{\partial f}{\partial U}^T K^{-1} \frac{\partial K}{\partial x} U = -\frac{\partial f}{\partial U}^T \delta$$

$$K\lambda = \frac{\partial f}{\partial U}$$
 Adjoint Method

$$K\delta = \frac{\partial K}{\partial x}U$$
 Direct Method

response
Either one solution per
Either one solution per
design variables
That's why
Compliance!

Matlab Code

```
x(1:nely, 1:nelx) = volfrac;
                                                       % INITIALIZE
loop = 0; change = 1.;
while change > 0.01
                                                        % START ITERATION While Xk+1>>Xk
              loop = loop + 1;
              xold = x;
              [U]=FE(nelx,nely,x,penal); % FE-ANALYSIS
              [KE] = Ik;
              C = 0.;
for ely = 1:nely
 for elx = 1: nelx
   n1 = (nely+1)*(elx-1)+ely;
   n2 = (nely+1)^* elx + ely;
   Ue = U([2*n1-1;2*n1;2*n2-1;2*n2;2*n2+1;2*n2+2;2*n1+1;2*n1+2],1);
   c = c + x(ely, elx) \wedge penal*Ue'*KE*Ue;
                                                     % OBJECTIVE FUNCTION
   dc(ely,elx) = -penal*x(ely,elx)^(penal-1)*Ue'*KE*Ue; % SENSITIVITY ANALYSIS
```

Sensitivity

$$\frac{\partial c}{\partial x_e} = -p(x_e)^{p-1} \ \mathbf{u}_e^T \ \mathbf{k}_0 \ \mathbf{u}_e$$

Update rule

 OPTIMALITY CRITERIA METHOD

$$\begin{cases} \max(x_{\min}, x_e - m) \\ \text{if } x_e B_e^{\eta} \leq \max(x_{\min}, x_e - m), \\ x_e B_e^{\eta} \\ \text{if } \max(x_{\min}, x_e - m) < x_e B_e^{\eta} < \min(1, x_e + m) \end{cases} \qquad B_e = \frac{-\frac{\partial c}{\partial x_e}}{\lambda \frac{\partial V}{\partial x_e}}$$

$$\min(1, x_e + m)$$

$$\text{if } \min(1, x_e + m) \leq x_e B_e^{\eta},$$

Element Stiffness Matrix

function [KE]=Ik

%Element Stiffness Matrix

FEM Analysis (2D mesh is invariant wrt to homotheties)

```
function [U]=FE(nelx,nely,x,penal)
[KE] = Ik;
K = \text{sparse}(2^*(\text{nelx}+1)^*(\text{nely}+1), 2^*(\text{nelx}+1)^*(\text{nely}+1));
F = \text{sparse}(2^*(\text{nely}+1)^*(\text{nelx}+1), 1); U = \text{zeros}(2^*(\text{nely}+1)^*(\text{nelx}+1), 1);
for elx = 1: nelx
for ely = 1: nely
 n1 = (nely+1)*(elx-1)+ely;
 n2 = (nely+1)^* elx + ely;
 edof = [2*n1-1; 2*n1; 2*n2-1; 2*n2; 2*n2+1; 2*n2+2; 2*n1+1; 2*n1+2];
 K(edof, edof) = K(edof, edof) + x(ely, elx)^penal*KE;
end
end
F(2*(nelx+1)*(nely+1), 1)=-1;
fixeddofs=union([1,2],[2*nely+1:2*(nely+1)]);
alldofs = [1:2*(nely+1)*(nelx+1)];
freedofs = setdiff(alldofs, fixeddofs);
% SOLVING
U(freedofs,:) = K(freedofs, freedofs) \ F(freedofs,:);
U(fixeddofs,:)=0;
```

TO HAVE REAL DISPLACEMENT

- 1) Choose consistent units N, mm, MPa for example (Remember Nastran Course)
- 2) Put the real Young's modulus $E=210^{\circ}3$ MPa for example;
- 3) Multiply the unit load by true amplitude F for example 54*1°3 N;
- 4) Multiply the elementary stiffness matrix by the thickness (mm)
- 5) 2D mesh is invariant wrt to homotheties; Need to check that nelx and nely are related to the true value for example 140 and 50 mm
- 6) Apply the BCs

The compliance unit is mJ.

OPTIMALITY CRITERIA

```
function [xnew]=OC(nelx,nely,x,volfrac,dc)
|1 = 0; |2 = 100000; move = 0.2;
while (12-11 > 1e-4)
Imid = 0.5*(12+11);
xnew = max(0.001, max(x-move, min(1., min(x+move, x.*sqrt(-dc./lmid)))));
 if sum(sum(xnew)) - volfrac*nelx*nely > 0;
                                                                             Imid: 50.0000
                                                                                           11: 0.0000
                                                                                                       12: 50.0000
 11 = Imid;
                                                                             Imid: 25.0000
                                                                                            11: 0.0000
                                                                                                       12: 25.0000
                                                                             lmid: 12.5000
                                                                                           11: 0.0000
                                                                                                       12: 12.5000
 else
                                                                             Imid: 6.2500
                                                                                           11: 6.2500
                                                                                                       12: 12.5000
  12 = \text{Imid};
                                                                             lmid: 9.3750
                                                                                           11: 6.2500
                                                                                                       12: 9.3750
                                                                             Imid: 7.8125
                                                                                           11: 6.2500
                                                                                                       12: 7.8125
 end
                                                                              Imid: 7.0313
                                                                                           11: 7.0313
                                                                                                       12: 7.8125
                                                                              Imid: 7.4219
                                                                                           11: 7.0313
                                                                                                       12: 7.4219
end
                                                                             Imid: 7.2266
                                                                                           11: 7.2266
                                                                                                       12: 7.4219
                                                                              Imid: 7.3242
                                                                                           11: 7.3242
                                                                                                       12: 7.4219
                                                                             Imid: 7.3730
                                                                                           11: 7.3242
                                                                                                       12: 7.3730
                                                                             Imid: 7.3486
                                                                                           11: 7.3242
                                                                                                       12: 7.3486
                                                                             Imid: 7.3364
                                                                                           11: 7.3364
                                                                                                       12: 7.3486
                                                                             Imid: 7.3425
                                                                                           11: 7.3425
                                                                                                       12: 7.3486
                                                                             Imid: 7.3456
                                                                                           11: 7.3425
                                                                                                       12: 7.3456
                                                                             lmid: 7.3441
                                                                                           11: 7.3441
                                                                                                       12: 7.3456
                                                                             Imid: 7.3448
                                                                                           11: 7.3448
                                                                                                       12: 7.3456
                                                                             lmid: 7.3452
                                                                                           11: 7.3448
                                                                                                       12: 7.3452
                                                                             Imid: 7.3450
                                                                                           11: 7.3450
                                                                                                       12: 7.3452
                                                                             12: 7.3451
```

Can also use:

- fmincon
- MMA...

The MMA approach, which was initially proposed by Svanberg (see Mini Project) is based on the first-order Taylor series expansion of the objective and constraint functions.

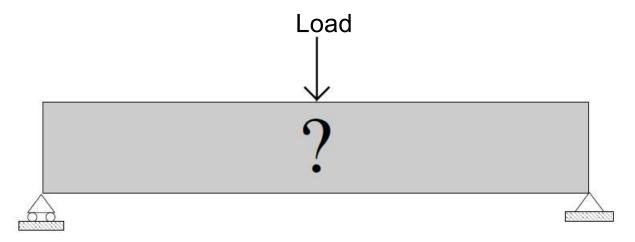
With this method, an explicit convex subproblem is generated to approximate the implicit nonlinear problem.

Matlab code command

top(nelx, nely, volfrac, penal, rmin)

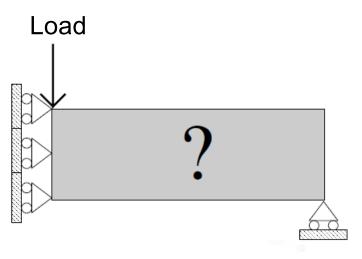
- nelx and nely: number of elements in the horizontal and vertical directions,
- volfrac: volume fraction,
- penal: penalization power,
- rmin: filter size (divided by element size).

Default boundary conditions: MMB Beam



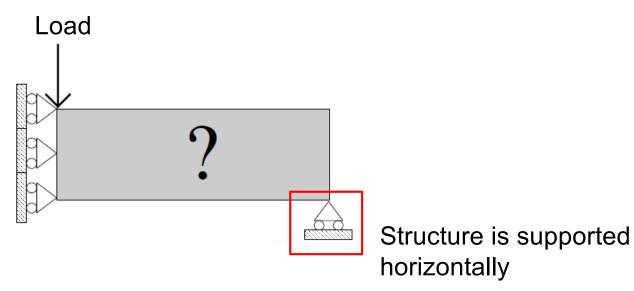
Full domain

• Default boundary conditions: MMB Beam



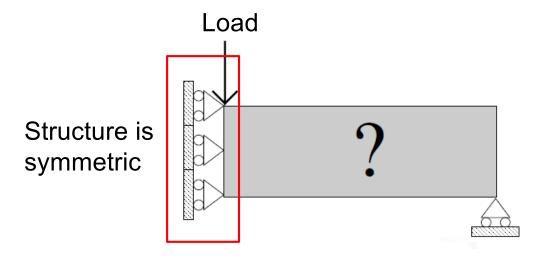
Half design domain

• Default boundary conditions: MMB Beam



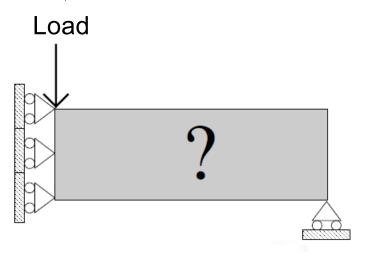
Half design domain

• Default boundary conditions: MMB Beam



Half design domain

How can we measure compliance?



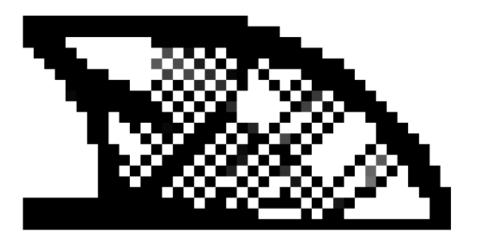
Compute static equilibrium: KU = F

Measure Energy of the System: $\mathbf{U}^T \mathbf{K} \mathbf{U}$

Example 1

Numerical instability

top(40, 20, 0.5, 3, 1.0)



effect→ Checkerboard Pattern

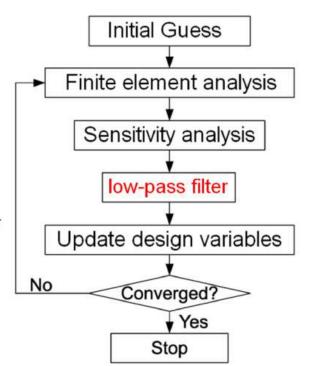
Example 1 -- Checkerboard Pattern Problem

→ Solution: LOW PASS Filter

$$\frac{\widehat{\partial c}}{\partial x_e} = \frac{1}{x_e \sum_{f=1}^{N} \hat{H}_f} \sum_{f=1}^{N} \hat{H}_f x_f \frac{\partial c}{\partial x_f}.$$

$$\hat{H}_f = r_{\min} - \operatorname{dist}(e, f)$$
,

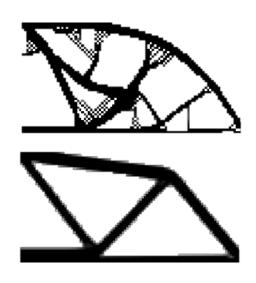
$$\{f \in N \mid \operatorname{dist}(e, f) \leq r_{\min}\}, \quad e = 1, \dots, N$$

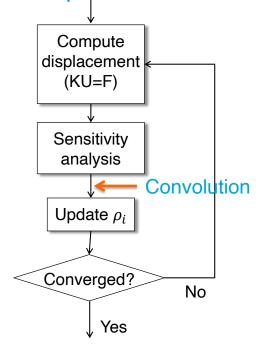


[dc] = check(nelx, nely, rmin, x, dc); % FILTERING OF SENSITIVITIES

Filtering

Sensitivity Filtering by a Convolution Operation

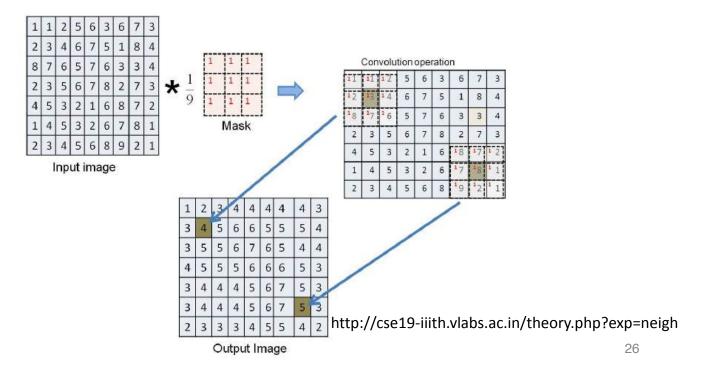




25

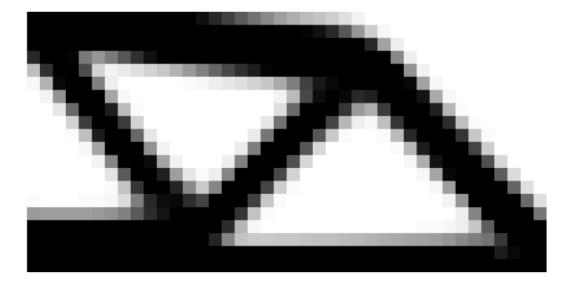
Filtering

Convolution Operation



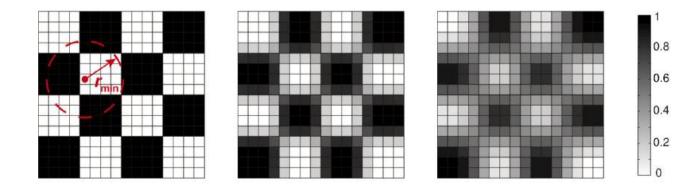
Example 2

• top(40, 20, 0.5, 3, 1.5)



• top(40, 20, 0.5, 3, 3) effect?

Filter

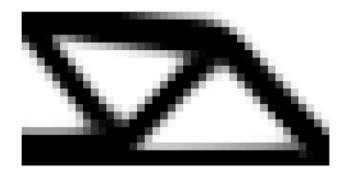


A checkerboard field and filtered fields $(r_{\min} = 1.5l_e \text{ and } 3l_e)$

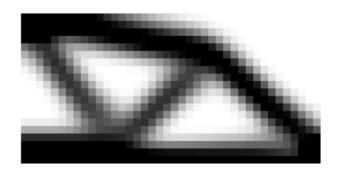
Example 3

rmin=1.5Obj=82.7562;

→ Size of the filter makes it possible to obtain a more physical representation (Unblur?)



rmin=3Obj=99.1929;



Example 3: Change mesh!

top(60, 30, 0.5, 3, 1.0)Obj: 83.0834

top(40, 20, 0.5, 3, 1.0)Obj: 80.4086;





Example 4: mixing

• top(60, 30, 0.5, 3, 1.5) Obj: 81.3491

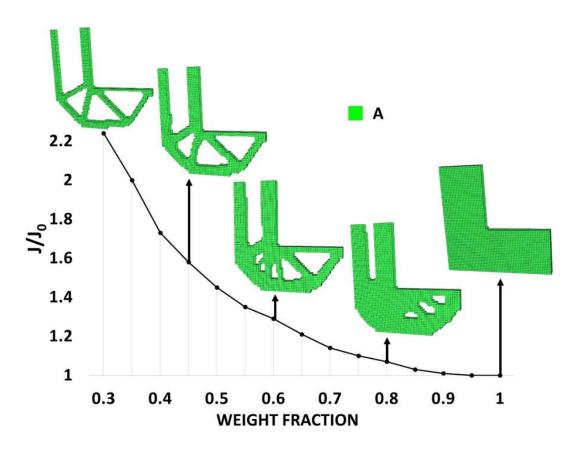
Filter size

• top(60, 30, 0.5, 3, 2.25) Obj: 83.5963

top(40, 20, 0.5, 3, 1.5) Obj=82.7562;

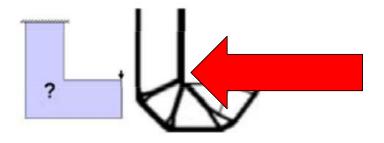


The engineer's way: Pareto



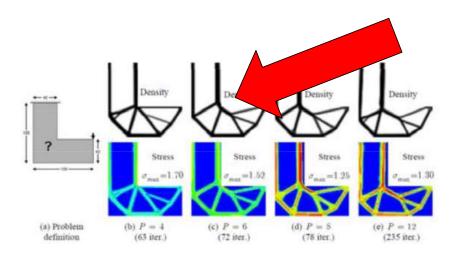
https://github.com/jomorlier/ALMcourse/blob/master/teaching/BE_Topopt_eleve.pdf

At this time the structure is rigid... but feasible?



Check the stress?

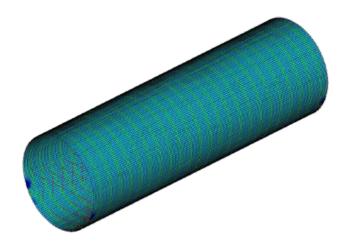
Results

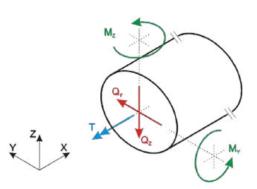


Le et al., SMO (2010)

Its it better?

Topopt on barrel (Fuselage) using Optistruct





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Structural topology optimization for multiple load cases using a dynamic aggregation technique

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(Received 1 December 2008; final version received 16 March 2009)

A series of techniques is presented for overcoming some of the numerical invashifities associated with SIMP materials. These techniques are combined to create a robust tepology optimization algorithm designed to be able to excenmentate a large sain of profestors as to mee elsely resemble those fraud in industry applications. A variant of the Krosselmeirs-Seinhauser (KS) function in which the aggregation parameter is dynamically increased over the course of the continuation is used to handle multi-load professes. Results from this method are compared with those obtained using the board formulation. It is shown that the KS aggregation method perdicase results superior to those of the board formulation, which can be highly susceptible to local minima. Adaptive metho-efficient in presented as a means of addressing the method perdicase results accessive method-fritement sycles can generate assorth, well-defined structures, and when used in combination with nine-node elements, virtually eliminate checkerboarding and flexural lingues.

Keywords: topology optimization; Kreisielmeier-Steinhauser function; adaptive mesh refinement; multiple load cases

1. Introduction

Since the its inception more than two decades ago (Bendsee and Kikuchi 1988), topology optimization has undergone significant growth both in terms of its number of practitioners as well as the types of problems to which it is applied. Researchers from a wide range of disciplines and industries have adopted the method due to its ability to produce highly efficient, light-weight structures. A salient example of this trend is the Airbus A380 aircraft (Krog et al. 2004), in which topology optimization was used in the preliminary structural layout design of the leading edge and wingbox ribs. Examples such as this highlight the need for increased robustness in topology optimization algorithms. The desire to generate optimized topologies for feasible real-world structures demands that these frameworks come equipped with features and capabilities that take into account factors such as multiple load cases, material failure constraints, and bockling effects.

These considerations often give rise to optimization constraints that are difficult to implement due to numerical instabilities inherent in most topology optimization procedures. This article

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Topology Optimisation —Altair Optistruct



Conclusion

"The art of structure is where to put the holes"

Robert Le Ricolais French-American engineer and philosopher (1894-1977)

