# (Artificial) Neural Networks in TensorFlow

By Prof. Seungchul Lee Industrial Al Lab http://isystems.unist.ac.kr/ POSTECH

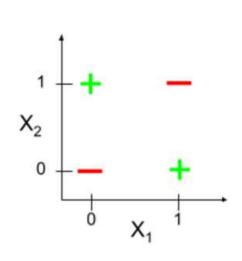
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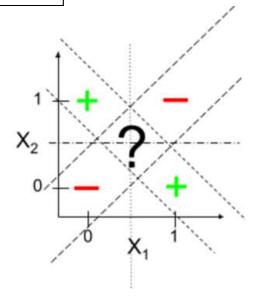
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## **XOR Problem**

- Minsky-Papert Controversy on XOR
  - not linearly separable
  - limitation of perceptron

$x_1$	$x_2$	$x_1$ XOR $x_2$
0	0	0
0	1	1
1	0	1
1	1	0



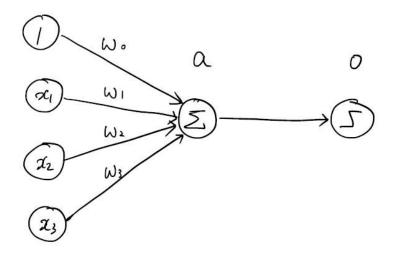


# 1. Artificial Neural Networks: Perceptron

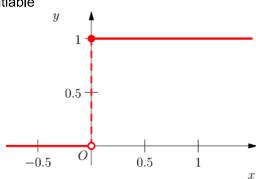
# 1.1. Perceptron for $h(\theta)$ or $h(\omega)$

- · Neurons compute the weighted sum of their inputs
- ullet A neuron is activated or fired when the sum a is positive

$$a=\omega_0+\omega_1x_1+\cdots \ o=\sigma(\omega_0+\omega_1x_1+\cdots)$$



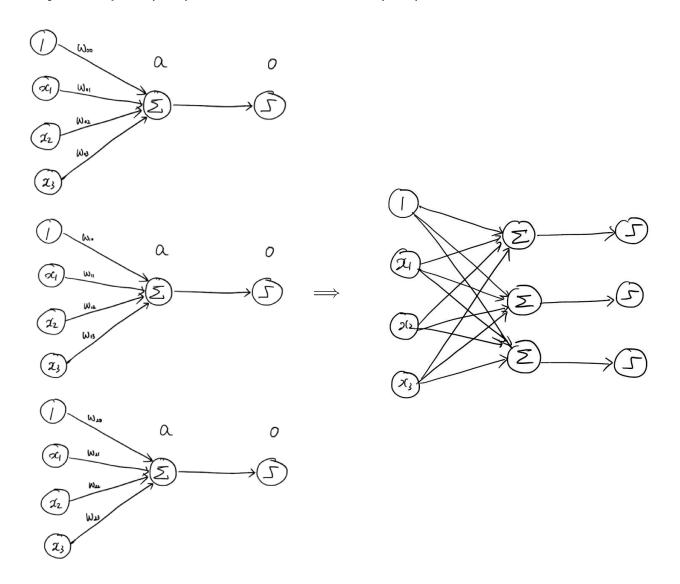
• A step function is not differentiable



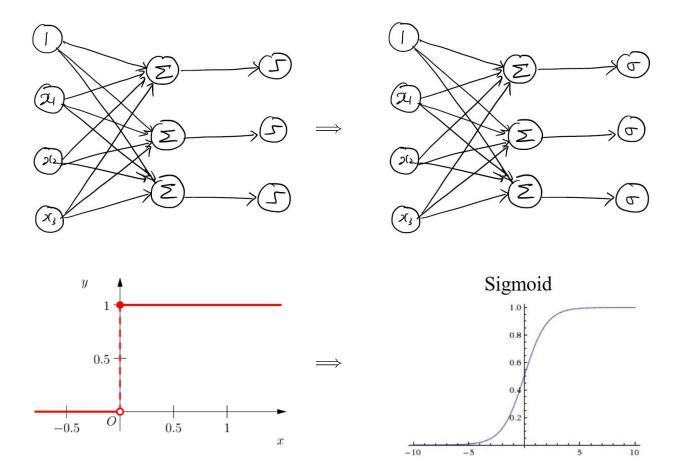
• One layer is often not enough

## 1.2. Artificial Neural Networks: MLP

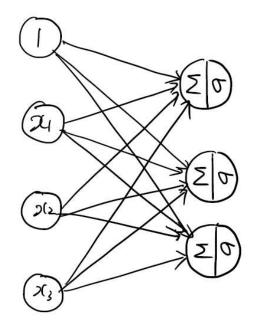
Multi-layer Perceptron (MLP) = Artificial Neural Networks (ANN) multi-neurons



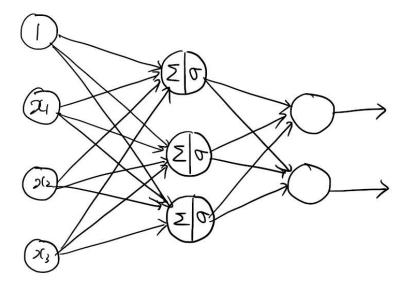
## differentiable activation function



## in a compact representation



### multi-layer perceptron



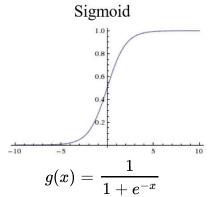
#### **Transformation**

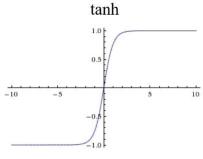
• Affine (or linear) transformation and nonlinear activation layer (notations are mixed:

$$g=\sigma, \omega= heta, \omega_0=b$$
 )

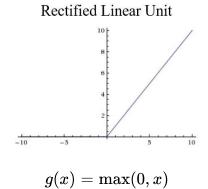
$$o(x) = g\left( heta^T x + b
ight)$$

• Nonlinear activation functions ( $g=\sigma$ )





 $g(x) = \tanh(x)$ 

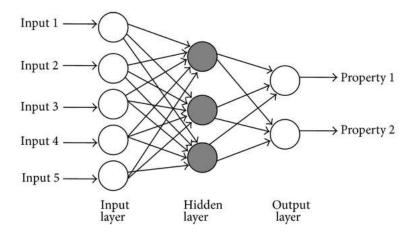


#### Structure

A single layer is not enough to be able to represent complex relationship between input and output

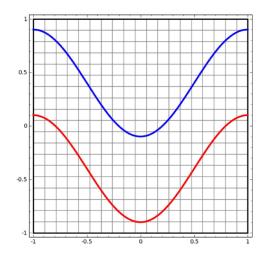
⇒ perceptrons with many layers and units

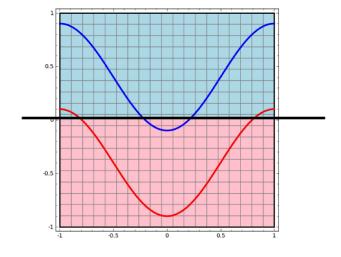
$$o_2 = \sigma_2 \left( heta_2^T o_1 + b_2
ight) = \sigma_2 \left( heta_2^T \sigma_1 \left( heta_1^T x + b_1
ight) + b_2
ight)$$



#### **Linear Classifier**

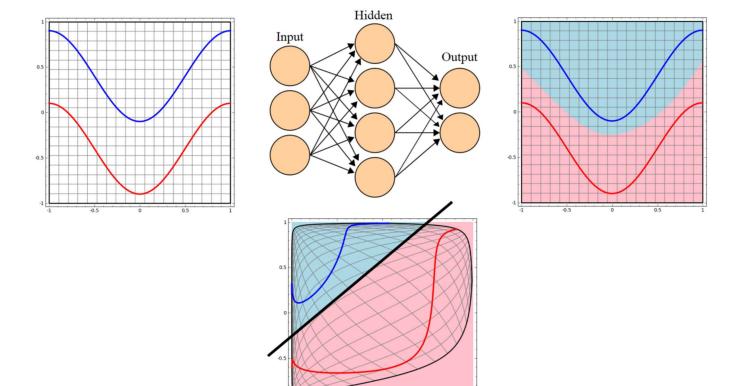
• Perceptron tries to separate the two classes of data by dividing them with a line





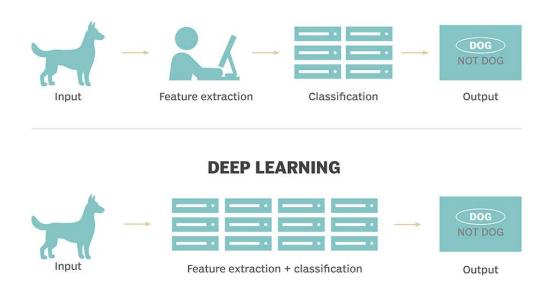
### **Neural Networks**

• The hidden layer learns a representation so that the data is linearly separable



# 2. Recall Supervised Learning Setup

#### TRADITIONAL MACHINE LEARNING



## 3. Training Neural Networks

= Learning or estimating weights and biases of multi-layer perceptron from training data

## 3.1. Optimization

#### 3 key components

- 1. objective function  $f(\cdot)$
- 2. decision variable or unknown heta
- 3. constraints  $g(\cdot)$

#### In mathematical expression

$$egin{array}{ll} \min & f( heta) \ & ext{subject to} & g_i( heta) \leq 0, \qquad i=1,\cdots,m \end{array}$$

## 3.2. Loss Function

· Measures error between target values and predictions

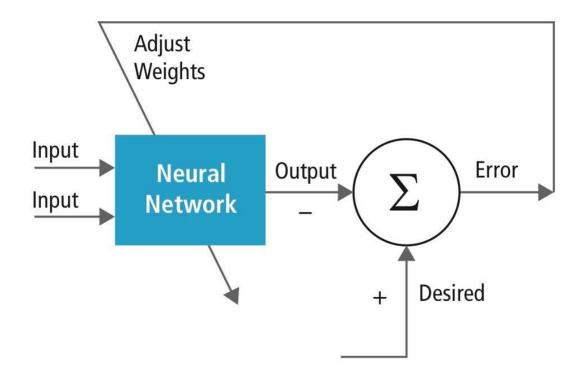
$$\min_{ heta} \sum_{i=1}^{m} \ell\left(h_{ heta}\left(x^{(i)}
ight), y^{(i)}
ight)$$

- Example
  - Squared loss (for regression):

$$rac{1}{N}\sum_{i=1}^{N}\left(h_{ heta}\left(x^{(i)}
ight)-y^{(i)}
ight)^{2}$$

Cross entropy (for classification):

$$-rac{1}{N}\sum_{i=1}^{N}y^{(i)}\log\Bigl(h_{ heta}\left(x^{(i)}
ight)\Bigr)+\Bigl(1-y^{(i)}\Bigr)\log\Bigl(1-h_{ heta}\left(x^{(i)}
ight)\Bigr)$$

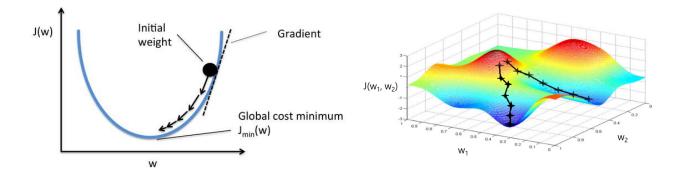


## 3.3. Learning

### (Stochastic) Gradient Descent

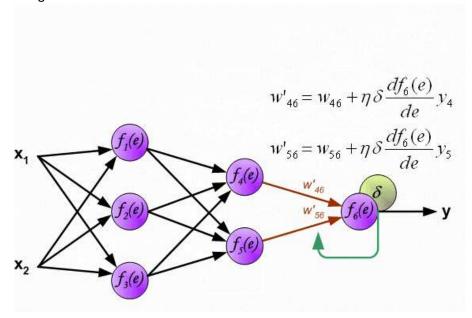
- · Negative gradients points directly downhill of the cost function
- We can decrease the cost by moving in the direction of the negative gradient (lpha is a learning rate)

$$heta:= heta-lpha
abla_{ heta}\left(h_{ heta}\left(x^{(i)}
ight),y^{(i)}
ight)$$



#### **Backpropagation**

- · Forward propagation
  - the initial information propagates up to the hidden units at each layer and finally produces output
- Backpropagation
  - allows the information from the cost to flow backwards through the network in order to compute the gradients



- · Chain Rule
  - Computing the derivative of the composition of functions

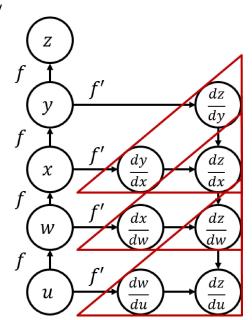
$$ullet f(g(x))' = f'(g(x))g'(x)$$

$$\bullet$$
  $\frac{dz}{dx} = \frac{dz}{du} \bullet \frac{dy}{dx}$ 

$$\bullet \quad \frac{dz}{dw} = \left(\frac{dz}{du} \bullet \frac{dy}{dx}\right) \bullet \frac{dx}{dw}$$

or full give derivative of the correction 
$$f(g(x))' = f'(g(x))g'(x)$$
or  $\frac{dz}{dx} = \frac{dz}{dy} \bullet \frac{dy}{dx}$ 
or  $\frac{dz}{dw} = (\frac{dz}{dy} \bullet \frac{dy}{dx}) \bullet \frac{dx}{dw}$ 
or  $\frac{dz}{du} = (\frac{dz}{dy} \bullet \frac{dy}{dx} \bullet \frac{dx}{dw}) \bullet \frac{dw}{du}$ 

- Backpropagation
  - Update weights recursively

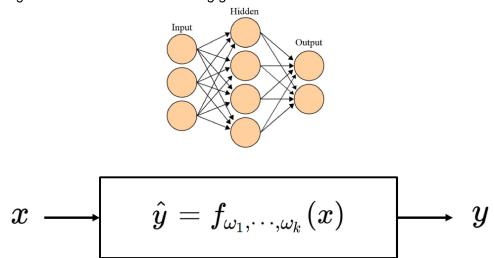


#### **Optimization procedure**

- It is not easy to numerically compute gradients in network in general.
  - The good news: people have already done all the "hardwork" of developing numerical solvers (or libraries)
  - There are a wide range of tools

#### **Summary**

· Learning weights and biases from data using gradient descent



## 3.4. Deep Learning Libraries

#### Caffe



• Platform: Linux, Mac OS, Windows

• Written in: C++

• Interface: Python, MATLAB

#### **Theano**

theano

• Platform: Cross-platform

Written in: PythonInterface: Python

#### **Tensorflow**



• Platform: Linux, Mac OS, Windows

• Written in: C++, Python

• Interface: Python, C/C++, Java, Go, R

## 4. TensorFlow

• TensorFlow (https://www.tensorflow.org) is an open-source software library for deep learning.

#### **Computational Graph**

- tf.constant
- tf.Variable
- tf.placeholder

#### In [1]:

```
import tensorflow as tf

a = tf.constant([1, 2, 3])
b = tf.constant([4, 5, 6])

A = a + b
B = a * b

In [2]:

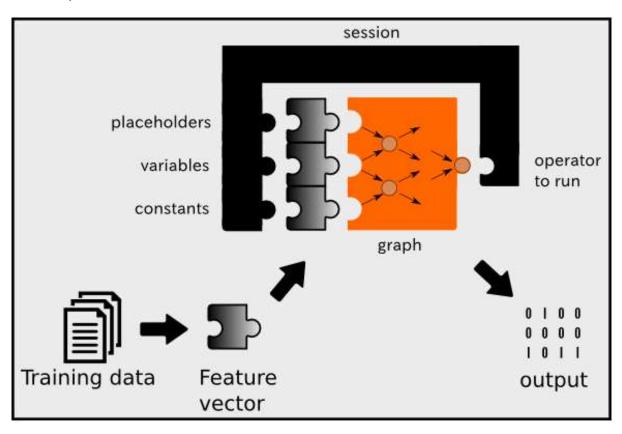
A
Out[2]:
<tf.Tensor 'add:0' shape=(3,) dtype=int32>
```

In [3]:

В

Out[3]:
<tf.Tensor 'mul:0' shape=(3,) dtype=int32>

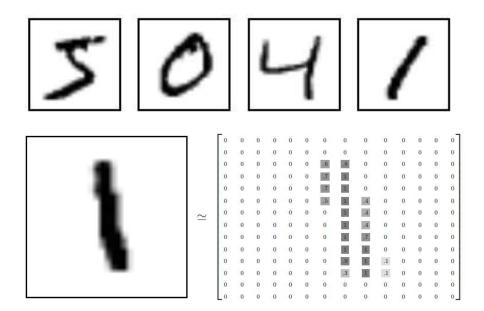
To run any of the three defined operations, we need to create a session for that graph. The session will also allocate memory to store the current value of the variable.



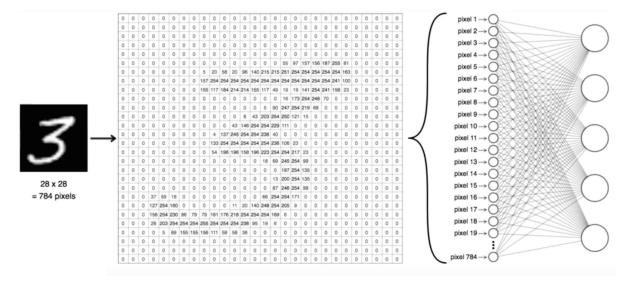
```
In [4]:
sess = tf.Session()
sess.run(A)
Out[4]:
array([5, 7, 9], dtype=int32)
In [5]:
sess.run(B)
Out[5]:
array([ 4, 10, 18], dtype=int32)
tf. Variable is regarded as the decision variable in optimization. We should initialize variables to use
tf.Variable.
In [6]:
w = tf.Variable([1, 1])
In [7]:
init = tf.global_variables_initializer()
sess.run(init)
In [8]:
sess.run(w)
Out[8]:
array([1, 1], dtype=int32)
The value of tf.placeholder must be fed using the feed_dict optional argument to Session.run().
In [9]:
x = tf.placeholder(tf.float32, [2, 2])
In [10]:
sess.run(x, feed_dict=\{x : [[1,2],[3,4]]\})
Out[10]:
array([[ 1., 2.],
       [ 3., 4.]], dtype=float32)
```

#### **ANN with TensorFlow**

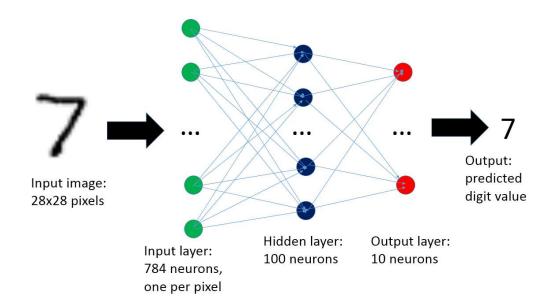
- MNIST (Mixed National Institute of Standards and Technology database) database
  - Handwritten digit database
  - $28 \times 28$  gray scaled image
  - Flattened matrix into a vector of  $28 \times 28 = 784$

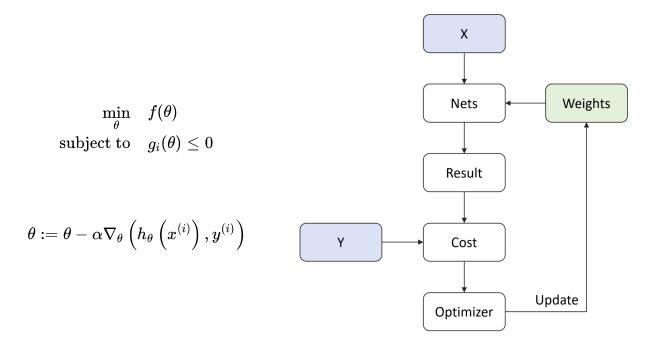


· feed a gray image to ANN



#### · our network model





# 4.1. Import Library

```
In [11]:
```

```
# Import Library
import numpy as np
import matplotlib.pyplot as plt
import tensorflow as tf
```

#### 4.2. Load MNIST Data

• Download MNIST data from tensorflow tutorial example

#### In [12]:

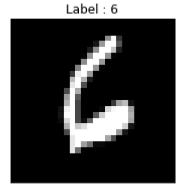
```
from tensorflow.examples.tutorials.mnist import input_data
mnist = input_data.read_data_sets("MNIST_data/", one_hot=True)
```

```
Extracting MNIST_data/train-images-idx3-ubyte.gz
Extracting MNIST_data/train-labels-idx1-ubyte.gz
Extracting MNIST_data/t10k-images-idx3-ubyte.gz
Extracting MNIST_data/t10k-labels-idx1-ubyte.gz
```

#### In [13]:

```
train_x, train_y = mnist.train.next_batch(10)
img = train_x[3,:].reshape(28,28)

plt.figure(figsize=(5,3))
plt.imshow(img,'gray')
plt.title("Label : {}".format(np.argmax(train_y[3])))
plt.xticks([])
plt.yticks([])
plt.show()
```



#### One hot encoding

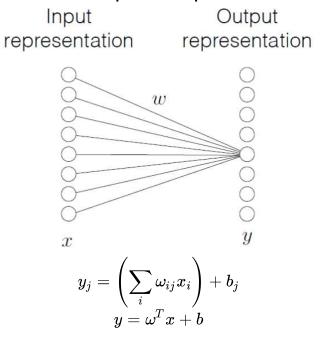
#### In [14]:

```
print ('Train labels : {}'.format(train_y[3, :]))
```

```
Train labels : [ 0. 0. 0. 0. 0. 1. 0. 0. 0.]
```

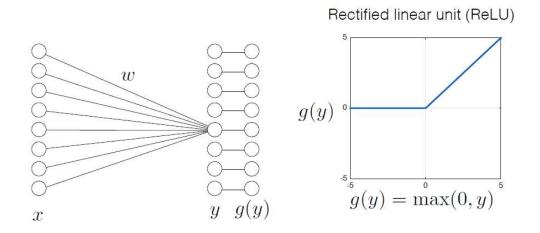
## 4.3. Build a Model

First, the layer performs several matrix multiplication to produce a set of linear activations



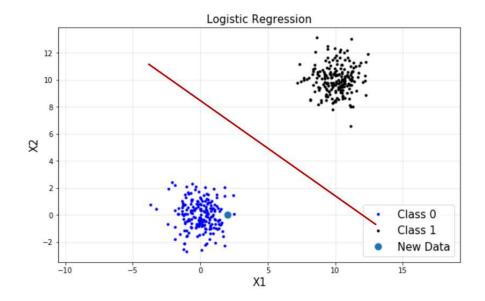
# hidden1 = tf.matmul(x, weights['hidden1']) + biases['hidden1']
hidden1 = tf.add(tf.matmul(x, weights['hidden1']), biases['hidden1'])

#### Second, each linear activation is running through a nonlinear activation function



hidden1 = tf.nn.relu(hidden1)

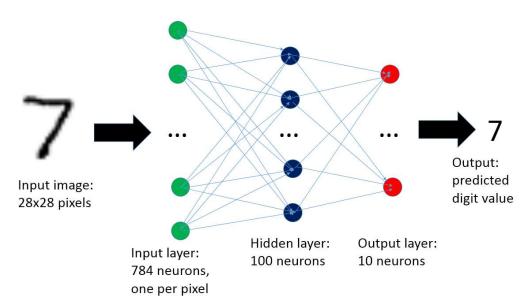
#### Third, predict values with an affine transformation



# output = tf.matmul(hidden1, weights['output']) + biases['output']
output = tf.add(tf.matmul(hidden1, weights['output']), biases['output'])

## 4.4. Define the ANN's Shape

- Input size
- · Hidden layer size
- The number of classes



```
In [15]:
```

```
n_input = 28*28
n_hidden1 = 100
n_output = 10
```

## 4.5. Define Weights, Biases and Network

- · Define parameters based on predefined layer size
- Initialize with normal distribution with  $\mu=0$  and  $\sigma=0.1$

#### In [16]:

```
weights = {
    'hidden1' : tf.Variable(tf.random_normal([n_input, n_hidden1], stddev = 0.1)),
    'output' : tf.Variable(tf.random_normal([n_hidden1, n_output], stddev = 0.1)),
}
biases = {
    'hidden1' : tf.Variable(tf.random_normal([n_hidden1], stddev = 0.1)),
    'output' : tf.Variable(tf.random_normal([n_output], stddev = 0.1)),
}
x = tf.placeholder(tf.float32, [None, n_input])
y = tf.placeholder(tf.float32, [None, n_output])
```

#### In [17]:

```
# Define Network
def build_model(x, weights, biases):
    # first hidden Layer
    hidden1 = tf.add(tf.matmul(x, weights['hidden1']), biases['hidden1'])
    # non Linear activate function
    hidden1 = tf.nn.relu(hidden1)

# Output Layer with Linear activation
    output = tf.add(tf.matmul(hidden1, weights['output']), biases['output'])
    return output
```

## 4.6. Define Cost, Initializer and Optimizer

#### Loss

- Classification: Cross entropy
  - Equivalent to apply logistic regression

$$-rac{1}{N} \sum_{i=1}^{N} y^{(i)} \log(h_{ heta}\left(x^{(i)}
ight)) + (1-y^{(i)}) \log(1-h_{ heta}\left(x^{(i)}
ight))$$

#### Initializer

· Initialize all the empty variables

#### **Optimizer**

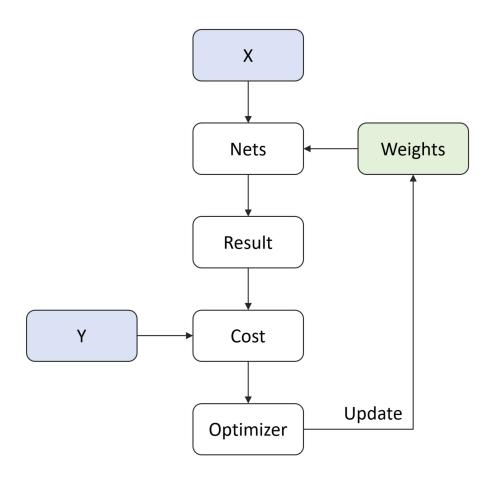
· AdamOptimizer: the most popular optimizer

#### In [18]:

```
# Define Cost
pred = build_model(x, weights, biases)
loss = tf.nn.softmax_cross_entropy_with_logits(logits=pred, labels=y)
loss = tf.reduce_mean(loss)

# optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
LR = 0.0001
optm = tf.train.AdamOptimizer(LR).minimize(loss)
init = tf.global_variables_initializer()
```

## 4.7. Summary of Model



## 4.8. Define Configuration

- · Define parameters for training ANN
  - n\_batch: batch size for stochastic gradient descent
  - n\_iter: the number of learning steps
  - n\_prt: check loss for every n\_prt iteration

```
In [19]:
```

```
n_batch = 50  # Batch Size
n_iter = 2500  # Learning Iteration
n_prt = 250  # Print Cycle
```

## 4.9. Optimization

#### In [20]:

```
# Run initialize
# config = tf.ConfigProto(allow_soft_placement=True) # GPU Allocating policy
# sess = tf.Session(config=config)
sess = tf.Session()
sess.run(init)

# Training cycle
for epoch in range(n_iter):
    train_x, train_y = mnist.train.next_batch(n_batch)
    sess.run(optm, feed_dict={x: train_x, y: train_y})

if epoch % n_prt == 0:
    c = sess.run(loss, feed_dict={x : train_x, y : train_y})
    print ("Iter : {}".format(epoch))
    print ("Cost : {}".format(c))
```

Iter: 0

Cost: 2.49772047996521

Iter: 250

Cost: 1.4581751823425293

Iter: 500

Cost: 0.7719646692276001

Iter : 750

Cost: 0.5604625344276428

Iter : 1000

Cost: 0.4211314022541046

Iter: 1250

Cost: 0.5066109299659729

Iter: 1500

Cost: 0.32460322976112366

Iter : 1750

Cost: 0.412553608417511

Iter : 2000

Cost: 0.26275649666786194

Iter: 2250

Cost: 0.481355220079422

### 4.10. Test

#### In [21]:

```
test_x, test_y = mnist.test.next_batch(100)

my_pred = sess.run(pred, feed_dict={x : test_x})
my_pred = np.argmax(my_pred, axis=1)

labels = np.argmax(test_y, axis=1)

accr = np.mean(np.equal(my_pred, labels))
print("Accuracy : {}%".format(accr*100))
```

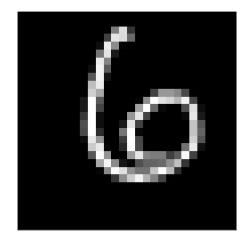
Accuracy: 96.0%

#### In [22]:

```
test_x, test_y = mnist.test.next_batch(1)
logits = sess.run(tf.nn.softmax(pred), feed_dict={x : test_x})
predict = np.argmax(logits)

plt.imshow(test_x.reshape(28,28), 'gray')
plt.xticks([])
plt.yticks([])
plt.yticks([])
plt.show()

print('Prediction : {}'.format(predict))
np.set_printoptions(precision=2, suppress=True)
print('Probability : {}'.format(logits.ravel()))
```



```
Prediction : 6
Probability : [ 0.01 0.01 0.07 0. 0.01 0.01 0.89 0. 0.01 0.
]
```

#### In [23]:

```
%%javascript
$.getScript('https://kmahelona.github.io/ipython_notebook_goodies/ipython_notebook_toc.
js')
```