(Artificial) Neural Networks in TensorFlow

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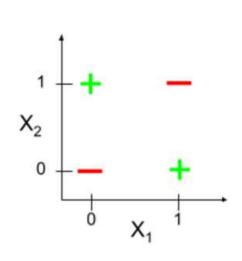
Table of Contents

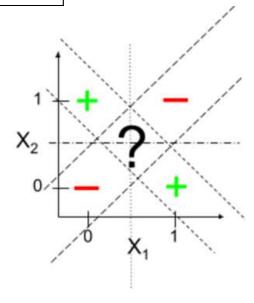
- I. 1. Artificial Neural Networks: Perceptron
 - I. 1.1. Perceptron for $h(\theta)$ or $h(\omega)$
 - II. 1.2. Artificial Neural Networks: MLP
- II. 2. Recall Supervised Learning Setup
- III. 3. Training Neural Networks
 - I. 3.1. Optimization
 - II. 3.2. Loss Function
 - III. 3.3. Learning
 - IV. 3.4. Deep Learning Libraries
- IV. 4. TensorFlow
 - I. 4.1. Import Library
 - II. 4.2. Load MNIST Data
 - III. 4.3. Build a Model
 - IV. 4.4. Define the ANN's Shape
 - V. 4.5. Define Weights, Biases and Network
 - VI. 4.6. Define Cost, Initializer and Optimizer
 - VII. 4.7. Summary of Model
 - VIII. 4.8. Define Configuration
 - IX. 4.9. Optimization
 - X. 4.10. Test

XOR Problem

- Minsky-Papert Controversy on XOR
 - not linearly separable
 - limitation of perceptron

x_1	x_2	x_1 XOR x_2
0	0	0
0	1	1
1	0	1
1	1	0



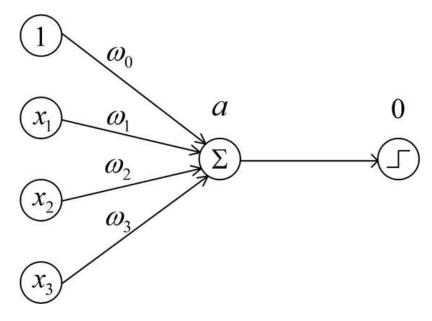


1. Artificial Neural Networks: Perceptron

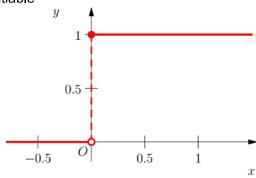
1.1. Perceptron for $h(\theta)$ or $h(\omega)$

- · Neurons compute the weighted sum of their inputs
- ullet A neuron is activated or fired when the sum a is positive

$$a=\omega_0+\omega_1x_1+\cdots \ o=\sigma(\omega_0+\omega_1x_1+\cdots)$$



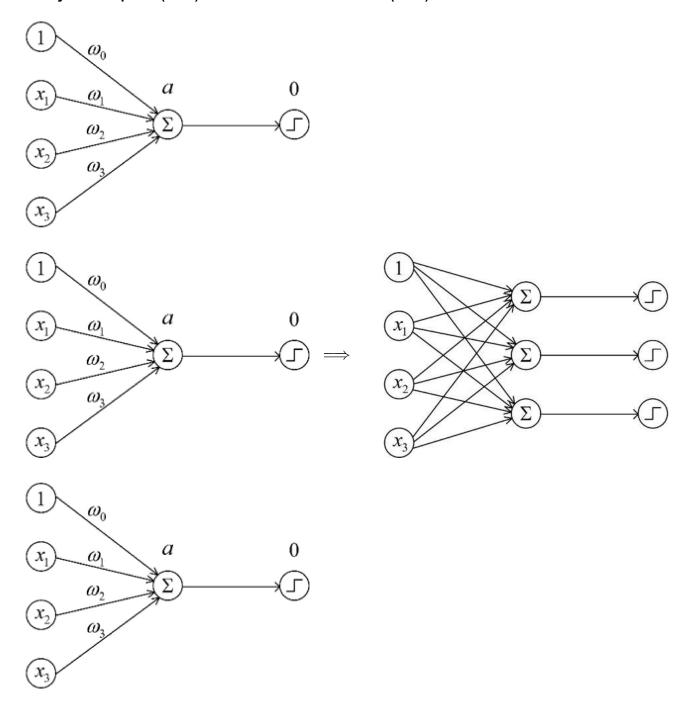
• A step function is not differentiable



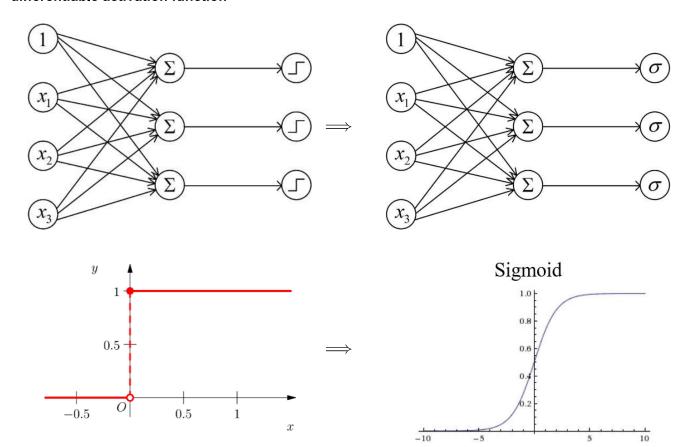
· One layer is often not enough

1.2. Artificial Neural Networks: MLP

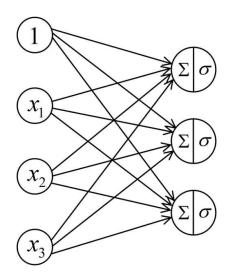
Multi-layer Perceptron (MLP) = Artificial Neural Networks (ANN) multi-neurons



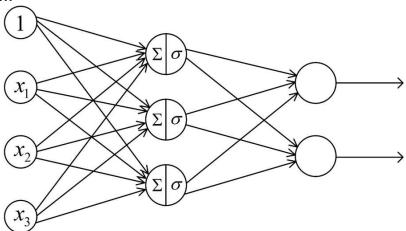
differentiable activation function



in a compact representation



multi-layer perceptron



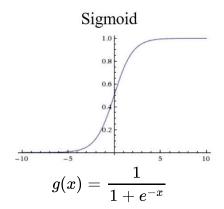
Transformation

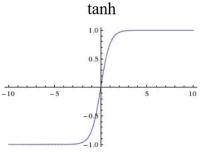
• Affine (or linear) transformation and nonlinear activation layer (notations are mixed:

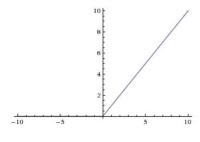
$$g=\sigma, \omega= heta, \omega_0=b$$
)

$$o(x) = g\left(heta^T x + b
ight)$$

• Nonlinear activation functions $(g=\sigma)$







Rectified Linear Unit

$$g(x) = \tanh(x)$$

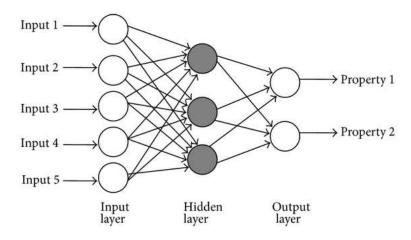
$$g(x) = \max(0, x)$$

Structure

A single layer is not enough to be able to represent complex relationship between input and output

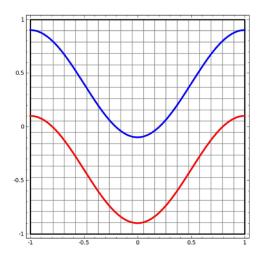
⇒ perceptrons with many layers and units

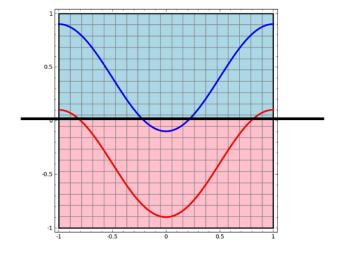
$$o_2 = \sigma_2 \left(heta_2^T o_1 + b_2
ight) = \sigma_2 \left(heta_2^T \sigma_1 \left(heta_1^T x + b_1
ight) + b_2
ight)$$



Linear Classifier

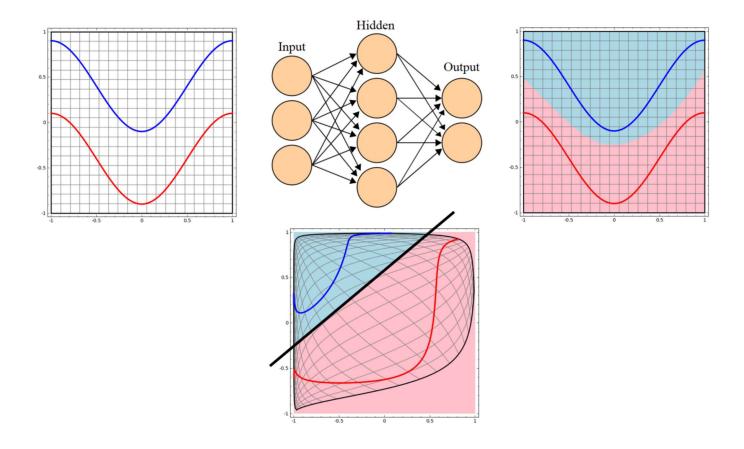
• Perceptron tries to separate the two classes of data by dividing them with a line





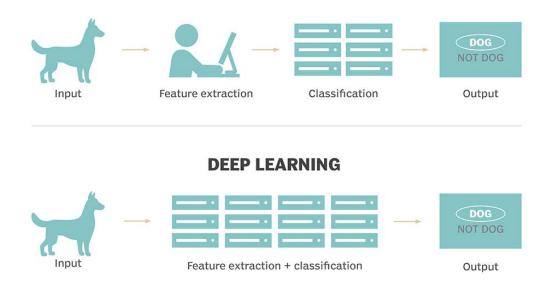
Neural Networks

• The hidden layer learns a representation so that the data is linearly separable



2. Recall Supervised Learning Setup

TRADITIONAL MACHINE LEARNING



3. Training Neural Networks

= Learning or estimating weights and biases of multi-layer perceptron from training data

3.1. Optimization

3 key components

- 1. objective function $f(\cdot)$
- 2. decision variable or unknown heta
- 3. constraints $g(\cdot)$

In mathematical expression

$$egin{array}{ll} \min_{ heta} & f(heta) \ & ext{subject to} & g_i(heta) \leq 0, \qquad i=1,\cdots,m \end{array}$$

3.2. Loss Function

· Measures error between target values and predictions

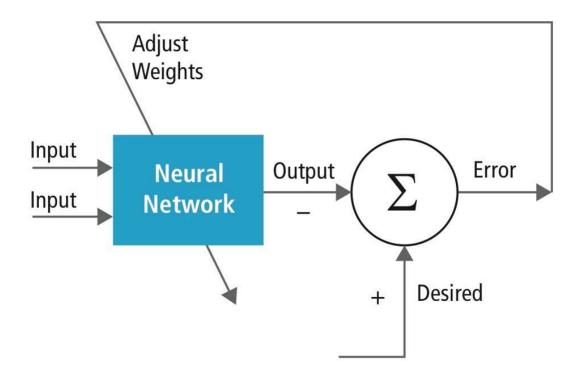
$$\min_{ heta} \sum_{i=1}^{m} \ell\left(h_{ heta}\left(x^{(i)}
ight), y^{(i)}
ight)$$

- Example
 - Squared loss (for regression):

$$rac{1}{N}\sum_{i=1}^{N}\left(h_{ heta}\left(x^{(i)}
ight)-y^{(i)}
ight)^{2}$$

Cross entropy (for classification):

$$-rac{1}{N}\sum_{i=1}^{N}y^{(i)}\log\Bigl(h_{ heta}\left(x^{(i)}
ight)\Bigr)+\Bigl(1-y^{(i)}\Bigr)\log\Bigl(1-h_{ heta}\left(x^{(i)}
ight)\Bigr)$$

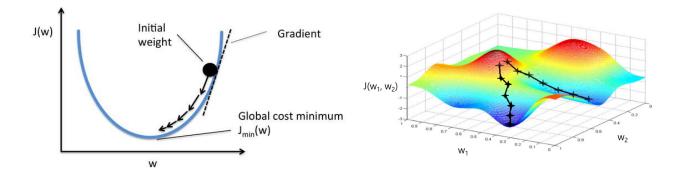


3.3. Learning

(Stochastic) Gradient Descent

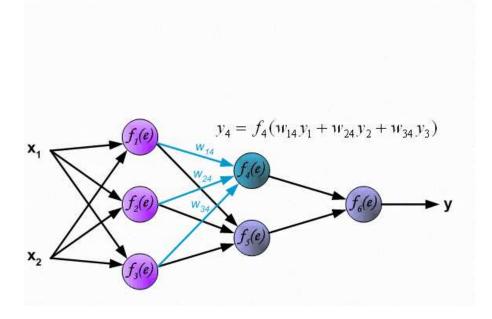
- Negative gradients points directly downhill of the cost function
- We can decrease the cost by moving in the direction of the negative gradient (lpha is a learning rate)

$$heta:= heta-lpha
abla_{ heta}\left(h_{ heta}\left(x^{(i)}
ight),y^{(i)}
ight)$$



Backpropagation

- Forward propagation
 - the initial information propagates up to the hidden units at each layer and finally produces output
- Backpropagation
 - allows the information from the cost to flow backwards through the network in order to compute the gradients



- Chain Rule
 - Computing the derivative of the composition of functions

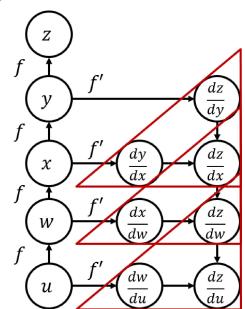
$$\circ f(g(x))' = f'(g(x))g'(x)$$

$$\bullet$$
 $\frac{dz}{dx} = \frac{dz}{du} \bullet \frac{dy}{dx}$

$$\bullet$$
 $\frac{dz}{dw} = \left(\frac{dz}{du} \bullet \frac{dy}{dx}\right) \bullet \frac{dx}{dw}$

o
$$f(g(x))' = f'(g(x))g'(x)$$
o $\frac{dz}{dx} = \frac{dz}{dy} \bullet \frac{dy}{dx}$
o $\frac{dz}{dw} = (\frac{dz}{dy} \bullet \frac{dy}{dx}) \bullet \frac{dx}{dw}$
o $\frac{dz}{du} = (\frac{dz}{dy} \bullet \frac{dy}{dx} \bullet \frac{dx}{dw}) \bullet \frac{dw}{du}$

- Backpropagation
 - Update weights recursively



Optimization procedure

Start at a random point

Repeat

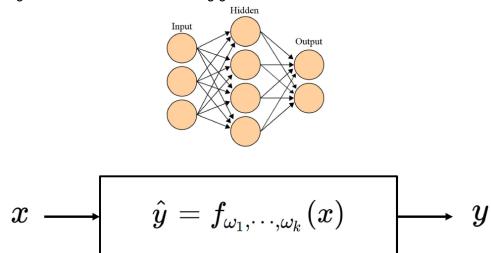
Determine a descent direction
Choose a step size
Update

Until stopping criterion is satisfied

- It is not easy to numerically compute gradients in network in general.
 - The good news: people have already done all the "hardwork" of developing numerical solvers (or libraries)
 - There are a wide range of tools

Summary

· Learning weights and biases from data using gradient descent



3.4. Deep Learning Libraries

Caffe



• Platform: Linux, Mac OS, Windows

• Written in: C++

• Interface: Python, MATLAB

Theano

theano

• Platform: Cross-platform

Written in: PythonInterface: Python

Tensorflow



• Platform: Linux, Mac OS, Windows

• Written in: C++, Python

• Interface: Python, C/C++, Java, Go, R

4. TensorFlow

• Tensor Flow (https://www.tensorflow.org) is an open-source software library for deep learning.

Computational Graph

- tf.constant
- tf.Variable
- tf.placeholder

In [1]:

```
import tensorflow as tf
a = tf.constant([1, 2, 3])
b = tf.constant([4, 5, 6])
A = a + b
B = a * b
```

In [2]:

```
A Out[2]:
```

<tf.Tensor 'add:0' shape=(3,) dtype=int32>

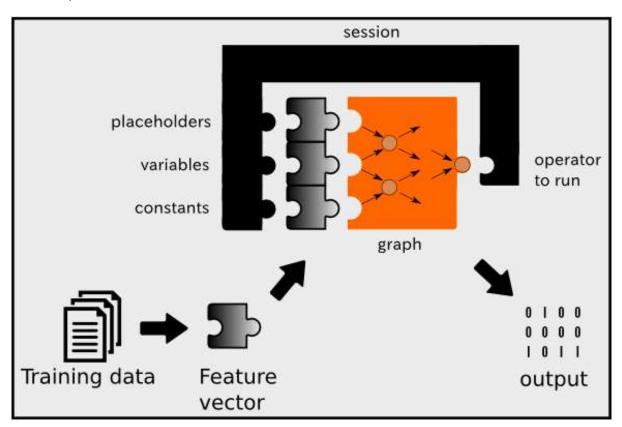
In [3]:

Out[3]:

В

<tf.Tensor 'mul:0' shape=(3,) dtype=int32>

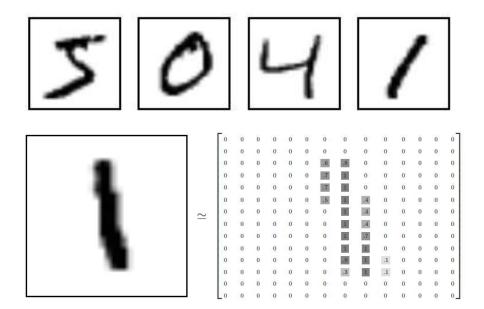
To run any of the three defined operations, we need to create a session for that graph. The session will also allocate memory to store the current value of the variable.



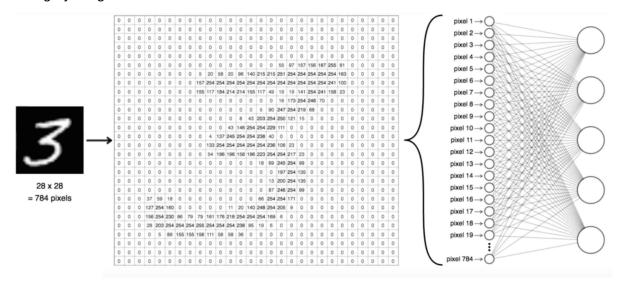
```
In [4]:
sess = tf.Session()
sess.run(A)
Out [4]:
array([5, 7, 9], dtype=int32)
In [5]:
sess.run(B)
Out[5]:
array([ 4, 10, 18], dtype=int32)
tf. Var iable is regarded as the decision variable in optimization. We should initialize variables to use
tf.Variable.
In [6]:
w = tf.Variable([1, 1])
In [7]:
init = tf.global_variables_initializer()
sess.run(init)
In [8]:
sess.run(w)
Out[8]:
array([1, 1], dtype=int32)
The value of tf.placeholder must be fed using the feed_dict optional argument to Session.run().
In [9]:
x = tf.placeholder(tf.float32, [2, 2])
In [10]:
sess.run(x, feed_dict=\{x : [[1,2],[3,4]]\})
Out[10]:
array([[ 1., 2.],
       [ 3., 4.]], dtype=float32)
```

ANN with TensorFlow

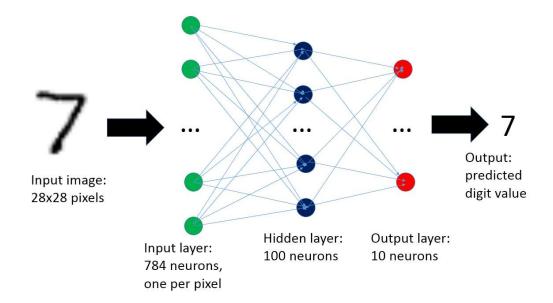
- MNIST (Mixed National Institute of Standards and Technology database) database
 - Handwritten digit database
 - 28×28 gray scaled image
 - ullet Flattened matrix into a vector of 28 imes 28 = 784

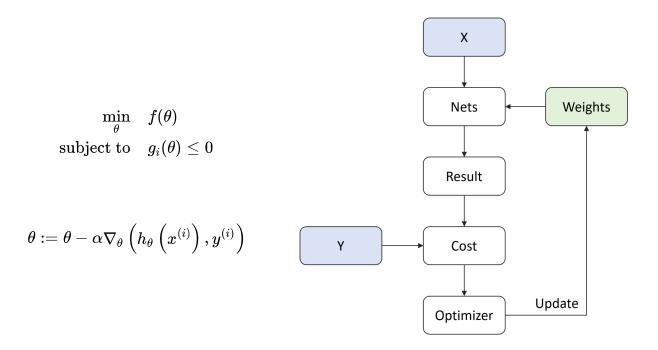


feed a gray image to ANN



· our network model





4.1. Import Library

In [11]:

Import Library
import numpy as np
import matplotlib.pyplot as plt
import tensorflow as tf

4.2. Load MNIST Data

• Download MNIST data from tensorflow tutorial example

In [12]:

```
from tensorflow.examples.tutorials.mnist import input_data
mnist = input_data.read_data_sets("MNIST_data/", one_hot=True)
```

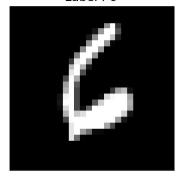
```
Extracting MNIST_data/train-images-idx3-ubyte.gz
Extracting MNIST_data/train-labels-idx1-ubyte.gz
Extracting MNIST_data/t10k-images-idx3-ubyte.gz
Extracting MNIST_data/t10k-labels-idx1-ubyte.gz
```

In [13]:

```
train_x, train_y = mnist.train.next_batch(10)
img = train_x[3,:].reshape(28,28)

plt.figure(figsize=(5,3))
plt.imshow(img, 'gray')
plt.title("Label : {}".format(np.argmax(train_y[3])))
plt.xticks([])
plt.yticks([])
plt.show()
```

Label: 6



One hot encoding

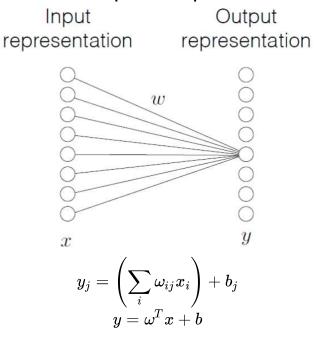
In [14]:

```
print ('Train labels : {}'.format(train_y[3, :]))
```

Train labels: [0. 0. 0. 0. 0. 1. 0. 0. 0.]

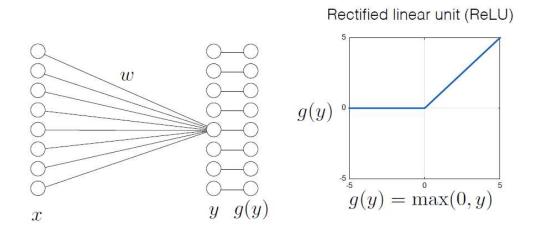
4.3. Build a Model

First, the layer performs several matrix multiplication to produce a set of linear activations



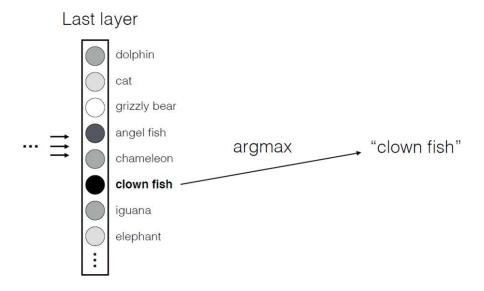
hidden1 = tf.matmul(x, weights['hidden1']) + biases['hidden1']
hidden1 = tf.add(tf.matmul(x, weights['hidden1']), biases['hidden1'])

Second, each linear activation is running through a nonlinear activation function



hidden1 = tf.nn.relu(hidden1)

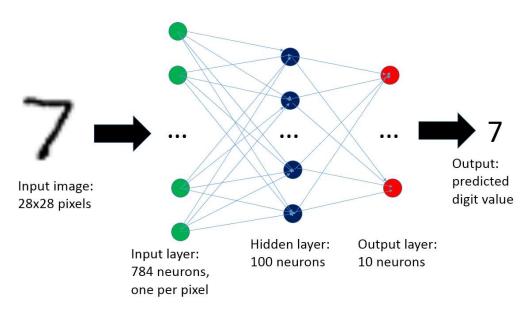
Third, predict values with an affine transformation



output = tf.matmul(hidden1, weights['output']) + biases['output']
output = tf.add(tf.matmul(hidden1, weights['output']), biases['output'])

4.4. Define the ANN's Shape

- · Input size
- · Hidden layer size
- The number of classes



In [15]:

```
n_input = 28*28
n_hidden1 = 100
n_output = 10
```

4.5. Define Weights, Biases and Network

- · Define parameters based on predefined layer size
- Initialize with normal distribution with $\mu=0$ and $\sigma=0.1$

In [16]:

```
weights = {
    'hidden1' : tf.Variable(tf.random_normal([n_input, n_hidden1], stddev = 0.1)),
    'output' : tf.Variable(tf.random_normal([n_hidden1, n_output], stddev = 0.1)),
}
biases = {
    'hidden1' : tf.Variable(tf.random_normal([n_hidden1], stddev = 0.1)),
    'output' : tf.Variable(tf.random_normal([n_output], stddev = 0.1)),
}

x = tf.placeholder(tf.float32, [None, n_input])
y = tf.placeholder(tf.float32, [None, n_output])
```

In [17]:

```
# Define Network
def build_model(x, weights, biases):
    # first hidden layer
    hidden1 = tf.add(tf.matmul(x, weights['hidden1']), biases['hidden1'])
    # non linear activate function
    hidden1 = tf.nn.relu(hidden1)

# Output layer with linear activation
    output = tf.add(tf.matmul(hidden1, weights['output']), biases['output'])
    return output
```

4.6. Define Cost, Initializer and Optimizer

Loss

- Classification: Cross entropy
 - Equivalent to apply logistic regression

$$-rac{1}{N} \sum_{i=1}^{N} y^{(i)} \log(h_{ heta}\left(x^{(i)}
ight)) + (1-y^{(i)}) \log(1-h_{ heta}\left(x^{(i)}
ight))$$

Initializer

· Initialize all the empty variables

Optimizer

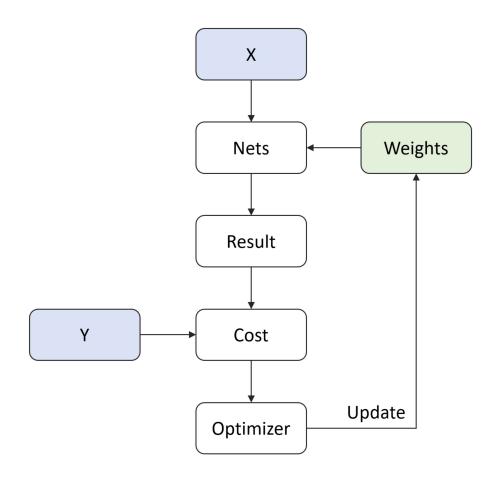
· AdamOptimizer: the most popular optimizer

In [18]:

```
# Define Cost
pred = build_model(x, weights, biases)
loss = tf.nn.softmax_cross_entropy_with_logits(logits=pred, labels=y)
loss = tf.reduce_mean(loss)

# optimizer = tf.train.GradientDescentOptimizer(learning_rate).minimize(cost)
LR = 0.0001
optm = tf.train.AdamOptimizer(LR).minimize(loss)
init = tf.global_variables_initializer()
```

4.7. Summary of Model



4.8. Define Configuration

- Define parameters for training ANN
 - n_batch: batch size for stochastic gradient descent
 - n_i ter: the number of learning steps
 - n_prt: check loss for every n_prt iteration

```
In [19]:
```

```
n_batch = 50  # Batch Size

n_iter = 2500  # Learning Iteration

n_prt = 250  # Print Cycle
```

4.9. Optimization

In [20]:

```
# Run initialize
# config = tf.ConfigProto(allow_soft_placement=True) # GPU Allocating policy
# sess = tf.Session(config=config)
sess.run(init)

# Training cycle
for epoch in range(n_iter):
    train_x, train_y = mnist.train.next_batch(n_batch)
    sess.run(optm, feed_dict={x: train_x, y: train_y})

if epoch % n_prt == 0:
    c = sess.run(loss, feed_dict={x : train_x, y : train_y})
    print ("Iter : {}".format(epoch))
    print ("Cost : {}".format(c))
```

Iter: 0

Cost : 2.49772047996521

Iter: 250

Cost: 1.4581751823425293

Iter: 500

Cost : 0.7719646692276001

Iter: 750

Cost : 0.5604625344276428

Iter: 1000

Cost : 0.4211314022541046

Iter: 1250

Cost : 0.5066109299659729

Iter: 1500

Cost: 0.32460322976112366

Iter: 1750

Cost: 0.412553608417511

Iter: 2000

Cost: 0.26275649666786194

Iter: 2250

Cost: 0.481355220079422

4.10. Test

In [21]:

```
test_x, test_y = mnist.test.next_batch(100)
my_pred = sess.run(pred, feed_dict={x : test_x})
my_pred = np.argmax(my_pred, axis=1)

labels = np.argmax(test_y, axis=1)

accr = np.mean(np.equal(my_pred, labels))
print("Accuracy : {}%".format(accr*100))
```

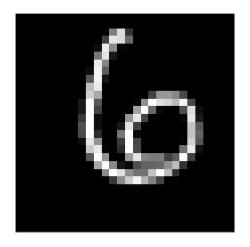
Accuracy: 96.0%

In [22]:

```
test_x, test_y = mnist.test.next_batch(1)
logits = sess.run(tf.nn.softmax(pred), feed_dict={x : test_x})
predict = np.argmax(logits)

plt.imshow(test_x.reshape(28,28), 'gray')
plt.xticks([])
plt.yticks([])
plt.show()

print('Prediction : {}'.format(predict))
np.set_printoptions(precision=2, suppress=True)
print('Probability : {}'.format(logits.ravel()))
```



Prediction: 6

Probability: [0.01 0.01 0.07 0. 0.01 0.01 0.89 0. 0.01 0.]

In [1]:

```
%%javascript
```

\$.getScript('https://kmahelona.github.io/ipython_notebook_goodies/ipython_notebook_toc.js')