

$$L = \lfloor \log_d(1 - s(1 - d)) \rfloor$$

$$E = s - \frac{1 - d^L}{1 - d}$$

$$R = d^L + E - \left\lceil \frac{E}{d} \right\rceil$$

where  $d$  is the number of dimensions (branching factor),  $s$  is the total number of nodes,  $R$  gives the maximum total number of roots. ( $d$  must be an integer greater than 1;  $s$  is an integer)