Fully connected networks

In the previous notebook, you implemented a simple two-layer neural network class. However, this class is not modular. If you wanted to change the number of layers, you would need to write a new loss and gradient function. If you wanted to optimize the network with different optimizers, you'd need to write new training functions. If you wanted to incorporate regularizations, you'd have to modify the loss and gradient function.

Instead of having to modify functions each time, for the rest of the class, we'll work in a more modular framework where we define forward and backward layers that calculate losses and gradients respectively. Since the forward and backward layers share intermediate values that are useful for calculating both the loss and the gradient, we'll also have these function return "caches" which store useful intermediate values.

The goal is that through this modular design, we can build different sized neural networks for various applications.

In this HW #3, we'll define the basic architecture, and in HW #4, we'll build on this framework to implement different optimizers and regularizations (like BatchNorm and Dropout).

CS231n has built a solid API for building these modular frameworks and training them, and we will use their very well implemented framework as opposed to "reinventing the wheel." This includes using their Solver, various utility functions, and their layer structure. This also includes nndl.fc_net, nndl.layers, and nndl.layer_utils. As in prior assignments, we thank Serena Yeung & Justin Johnson for permission to use code written for the CS 231n class (cs231n.stanford.edu).

Modular layers

This notebook will build modular layers in the following manner. First, there will be a forward pass for a given layer with inputs (x) and return the output of that layer (out) as well as cached variables (cache) that will be used to calculate the gradient in the backward pass.

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
    return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
    """

Receive derivative of loss with respect to outputs and cache,
    and compute derivative with respect to inputs.
    """

# Unpack cache values
    x, w, z, out = cache

# Use values in cache to compute derivatives
    dx = # Derivative of loss with respect to x
    dw = # Derivative of loss with respect to w

return dx, dw
```

```
In [1]:
         ## Import and setups
         import time
         import numpy as np
         import matplotlib.pyplot as plt
         from nndl.fc net import *
         from cs231n.data utils import get CIFAR10 data
         from cs231n.gradient check import eval numerical gradient, eval numer
         from cs231n.solver import Solver
         #import os
         #alias kk os. exit(0)
         %matplotlib inline
         plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of pl
         plt.rcParams['image.interpolation'] = 'nearest'
         plt.rcParams['image.cmap'] = 'gray'
         # for auto-reloading external modules
         # see http://stackoverflow.com/questions/1907993/autoreload-of-module
         %load ext autoreload
         %autoreload 2
         def rel error(x, y):
           """ returns relative error """
           return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(x)))
In [2]:
         # Load the (preprocessed) CIFAR10 data.
         data = get CIFAR10 data()
         for k in data.keys():
           print('{}: {} '.format(k, data[k].shape))
        X_train: (49000, 3, 32, 32)
        y train: (49000,)
        X val: (1000, 3, 32, 32)
        y_val: (1000,)
        X test: (1000, 3, 32, 32)
        y_test: (1000,)
```

Linear layers

In this section, we'll implement the forward and backward pass for the linear layers.

The linear layer forward pass is the function affine_forward in nndl/layers.py and the backward pass is affine_backward.

After you have implemented these, test your implementation by running the cell below.

Affine layer forward pass

Implement affine_forward and then test your code by running the following cell.

```
In [3]:
         # Test the affine forward function
         num inputs = 2
         input shape = (4, 5, 6)
         output dim = 3
         input_size = num_inputs * np.prod(input_shape)
         weight size = output dim * np.prod(input shape)
         x = np.linspace(-0.1, 0.5, num=input size).reshape(num inputs, *input
         w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_sha
         b = np.linspace(-0.3, 0.1, num=output dim)
         out, _ = affine_forward(x, w, b)
         correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                                 [ 3.25553199, 3.5141327, 3.77273342]])
         # Compare your output with ours. The error should be around 1e-9.
         print('Testing affine forward function:')
         print('difference: {}'.format(rel error(out, correct out)))
```

Testing affine_forward function: difference: 9.769849468192957e-10

Affine layer backward pass

Implement affine_backward and then test your code by running the following cell.

```
In [4]:
         # Test the affine backward function
         x = np.random.randn(10, 2, 3)
         w = np.random.randn(6, 5)
         b = np.random.randn(5)
         dout = np.random.randn(10, 5)
         dx num = eval numerical gradient array(lambda x: affine forward(x, w,
         dw num = eval numerical gradient array(lambda w: affine forward(x, w,
         db num = eval numerical gradient array(lambda b: affine forward(x, w,
         , cache = affine forward(x, w, b)
         dx, dw, db = affine backward(dout, cache)
         # The error should be around 1e-10
         print('Testing affine backward function:')
         print('dx error: {}'.format(rel_error(dx_num, dx)))
         print('dw error: {}'.format(rel_error(dw_num, dw)))
         print('db error: {}'.format(rel_error(db_num, db)))
```

Testing affine_backward function: dx error: 8.965731101545999e-11 dw error: 6.440353621580692e-10 db error: 3.2757766509506992e-12

Activation layers

In this section you'll implement the ReLU activation.

ReLU forward pass

Implement the relu_forward function in nndl/layers.py and then test your code by running the following cell.

```
In [5]:
        # Test the relu forward function
        x = np.linspace(-0.5, 0.5, num=12).reshape(3, 4)
        out, _ = relu_forward(x)
        correct out = np.array([[ 0.,
                                              0.,
                                                          0.,
                                                                        0.,
                                              0.,
                                                          0.04545455,
                                [ 0.,
                                                                        0.13
                                [ 0.22727273, 0.31818182, 0.40909091,
                                                                        0.5,
        # Compare your output with ours. The error should be around 1e-8
        print('Testing relu forward function:')
        print('difference: {}'.format(rel_error(out, correct_out)))
```

Testing relu_forward function: difference: 4.999999798022158e-08

ReLU backward pass

Implement the relu_backward function in nndl/layers.py and then test your code by running the following cell.

```
In [6]:
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)

    dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0],
    _, cache = relu_forward(x)
    dx = relu_backward(dout, cache)

# The error should be around le-12
    print('Testing relu_backward function:')
    print('dx error: {}'.format(rel_error(dx_num, dx)))
```

Testing relu_backward function: dx error: 3.2756125268124612e-12

Combining the affine and ReLU layers

Often times, an affine layer will be followed by a ReLU layer. So let's make one that puts them together. Layers that are combined are stored in <code>nndl/layer_utils.py</code> .

Affine-ReLU layers

We've implemented affine_relu_forward() and affine_relu_backward in nndl/layer_utils.py . Take a look at them to make sure you understand what's going on. Then run the following cell to ensure its implemented correctly.

```
In [7]:
         from nndl.layer utils import affine relu forward, affine relu backwar
         x = np.random.randn(2, 3, 4)
         w = np.random.randn(12, 10)
         b = np.random.randn(10)
         dout = np.random.randn(2, 10)
         out, cache = affine_relu_forward(x, w, b)
         dx, dw, db = affine relu backward(dout, cache)
         dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(
         dw num = eval numerical gradient array(lambda w: affine relu forward(
         db num = eval numerical gradient array(lambda b: affine relu forward(
         print('Testing affine_relu_forward and affine_relu_backward:')
         print('dx error: {}'.format(rel_error(dx_num, dx)))
         print('dw error: {}'.format(rel error(dw num, dw)))
         print('db error: {}'.format(rel error(db num, db)))
        Testing affine relu forward and affine relu backward:
        dx error: 1.426314116653442e-10
        dw error: 1.3648105326402987e-09
        db error: 8.776606948204458e-12
```

Softmax and SVM losses

You've already implemented these, so we have written these in layers.py. The following code will ensure they are working correctly.

```
In [8]:
         num classes, num inputs = 10, 50
         x = 0.001 * np.random.randn(num inputs, num classes)
         y = np.random.randint(num classes, size=num inputs)
         dx num = eval numerical gradient(lambda x: svm loss(x, y)[0], x, verb
         loss, dx = svm loss(x, y)
         # Test svm loss function. Loss should be around 9 and dx error should
         print('Testing svm loss:')
         print('loss: {}'.format(loss))
         print('dx error: {}'.format(rel_error(dx_num, dx)))
         dx num = eval numerical gradient(lambda x: softmax loss(x, y)[0], x,
         loss, dx = softmax loss(x, y)
         # Test softmax loss function. Loss should be 2.3 and dx error should
         print('\nTesting softmax loss:')
         print('loss: {}'.format(loss))
         print('dx error: {}'.format(rel_error(dx_num, dx)))
        Testing svm loss:
        loss: 9.001483824279473
        dx error: 3.038735505103329e-09
        Testing softmax loss:
        loss: 2.3027339369858155
```

Implementation of a two-layer NN

dx error: 7.998052176635476e-09

In nndl/fc_net.py , implement the class TwoLayerNet which uses the layers you made here. When you have finished, the following cell will test your implementation.

```
In [9]:
         N, D, H, C = 3, 5, 50, 7
         X = np.random.randn(N, D)
         y = np.random.randint(C, size=N)
         std = 1e-2
         model = TwoLayerNet(input dim=D, hidden dims=H, num classes=C, weight
         print('Testing initialization ...')
         W1 std = abs(model.params['W1'].std() - std)
         b1 = model.params['b1']
         W2_std = abs(model.params['W2'].std() - std)
         b2 = model.params['b2']
         assert W1 std < std / 10, 'First layer weights do not seem right'</pre>
         assert np.all(b1 == 0), 'First layer biases do not seem right'
         assert W2_std < std / 10, 'Second layer weights do not seem right'</pre>
         assert np.all(b2 == 0), 'Second layer biases do not seem right'
         print('Testing test-time forward pass ... ')
         model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
         model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
         model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
         model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
         X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
         scores = model.loss(X)
         correct scores = np.asarray(
           [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.571984
            [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.811491
            [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.050998
         scores diff = np.abs(scores - correct scores).sum()
         assert scores diff < 1e-6, 'Problem with test-time forward pass'
         print('Testing training loss (no regularization)')
         y = np.asarray([0, 5, 1])
         loss, grads = model.loss(X, y)
         correct loss = 3.4702243556
         assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time</pre>
         model.reg = 1.0
         loss, grads = model.loss(X, y)
         correct_loss = 26.5948426952
         assert abs(loss - correct loss) < 1e-10, 'Problem with regularization
         for reg in [0.0, 0.7]:
           print('Running numeric gradient check with reg = {}'.format(reg))
           model.reg = reg
           loss, grads = model.loss(X, y)
           for name in sorted(grads):
             f = lambda : model.loss(X, y)[0]
             grad_num = eval_numerical_gradient(f, model.params[name], verbose
             print('{} relative error: {}'.format(name, rel error(grad num, gr
```

```
Testing initialization ...

Testing test-time forward pass ...

Testing training loss (no regularization)

Running numeric gradient check with reg = 0.0

W1 relative error: 1.8336562786695002e-08

W2 relative error: 3.201560569143183e-10

b1 relative error: 9.828315204644842e-09

b2 relative error: 4.329134954569865e-10

Running numeric gradient check with reg = 0.7

W1 relative error: 2.5279152310200606e-07

W2 relative error: 7.976652806155026e-08

b1 relative error: 1.564679947504764e-08

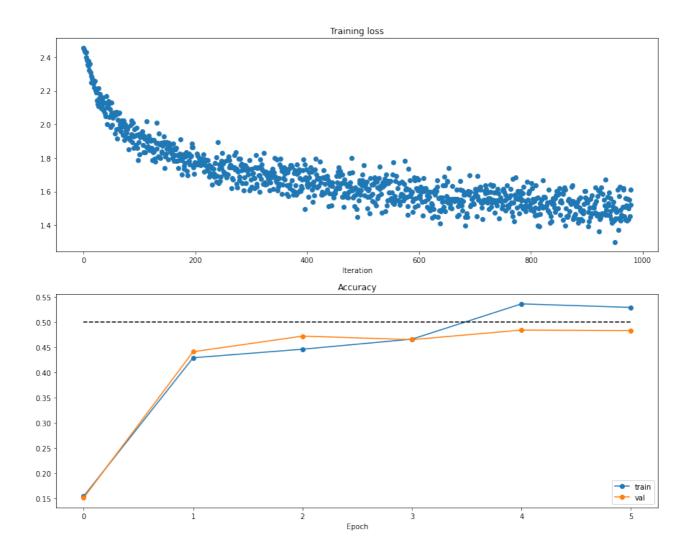
b2 relative error: 9.089617896905665e-10
```

Solver

We will now use the cs231n Solver class to train these networks. Familiarize yourself with the API in cs231n/solver.py. After you have done so, declare an instance of a TwoLayerNet with 200 units and then train it with the Solver. Choose parameters so that your validation accuracy is at least 40%.

```
In [10...
      model = TwoLayerNet()
      solver = None
      # ----- #
      # YOUR CODE HERE:
         Declare an instance of a TwoLayerNet and then train
      #
        it with the Solver. Choose hyperparameters so that your validation
      #
        accuracy is at least 40%. We won't have you optimize this furthe
      #
        since you did it in the previous notebook.
      model = TwoLayerNet(input dim=3*32*32, hidden dims=200,reg = 0.5)
      solver = Solver(model, data,
                 update rule='sgd',
                 optim_config={
                    'learning rate': 1e-3,
                 },
                 lr decay=0.95,
                 num epochs=5, batch size=250,
                 print every=100)
      solver.train()
      # END YOUR CODE HERE
      # ----- #
```

```
(Iteration 1 / 980) loss: 2.456303
        (Epoch 0 / 5) train acc: 0.154000; val acc: 0.151000
        (Iteration 101 / 980) loss: 1.821681
        (Epoch 1 / 5) train acc: 0.429000; val acc: 0.441000
        (Iteration 201 / 980) loss: 1.764685
        (Iteration 301 / 980) loss: 1.628573
        (Epoch 2 / 5) train acc: 0.446000; val acc: 0.472000
        (Iteration 401 / 980) loss: 1.641078
        (Iteration 501 / 980) loss: 1.656095
        (Epoch 3 / 5) train acc: 0.466000; val acc: 0.465000
        (Iteration 601 / 980) loss: 1.571873
        (Iteration 701 / 980) loss: 1.615997
        (Epoch 4 / 5) train acc: 0.536000; val acc: 0.484000
        (Iteration 801 / 980) loss: 1.490272
        (Iteration 901 / 980) loss: 1.542056
        (Epoch 5 / 5) train acc: 0.529000; val acc: 0.483000
In [11...
        # Run this cell to visualize training loss and train / val accuracy
         plt.subplot(2, 1, 1)
         plt.title('Training loss')
         plt.plot(solver.loss history, 'o')
         plt.xlabel('Iteration')
         plt.subplot(2, 1, 2)
         plt.title('Accuracy')
         plt.plot(solver.train_acc_history, '-o', label='train')
         plt.plot(solver.val_acc_history, '-o', label='val')
         plt.plot([0.5] * len(solver.val acc history), 'k--')
         plt.xlabel('Epoch')
         plt.legend(loc='lower right')
         plt.gcf().set size inches(15, 12)
         plt.show()
```



Multilayer Neural Network

Now, we implement a multi-layer neural network.

Read through the FullyConnectedNet class in the file nndl/fc_net.py .

Implement the initialization, the forward pass, and the backward pass. There will be lines for batchnorm and dropout layers and caches; ignore these all for now. That'll be in assignment #4.

print('{} relative error: {}'.format(name, rel_error(grad_num, gr

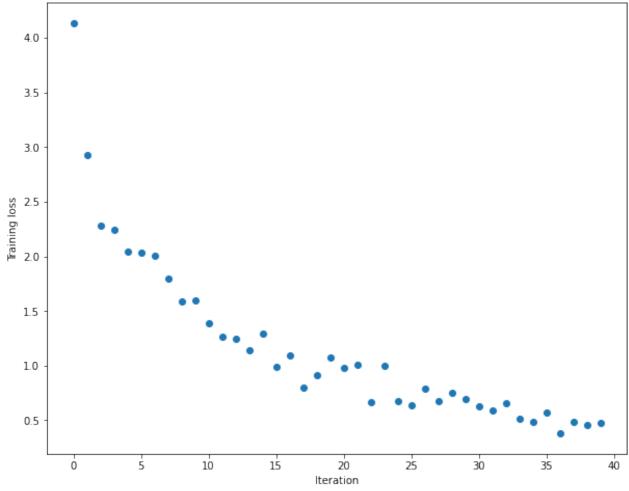
```
Running check with reg = 0
Initial loss: 2.3077984547761137
W1 relative error: 5.134769598521644e-07
W2 relative error: 1.4554668087059132e-06
W3 relative error: 5.7722430343791486e-08
b1 relative error: 3.518884117993465e-08
b2 relative error: 1.6453371658822287e-08
b3 relative error: 8.269075472305977e-11
Running check with reg = 3.14
Initial loss: 7.002026785468826
W1 relative error: 7.682583768481872e-09
W2 relative error: 2.0662916299162052e-08
W3 relative error: 1.1814138063807273e-08
b1 relative error: 9.649522856269296e-09
b2 relative error: 2.2935812804672787e-08
b3 relative error: 1.6410905141390848e-10
```

```
In [13...
         # Use the three layer neural network to overfit a small dataset.
         num train = 50
         small data = {
           'X_train': data['X_train'][:num_train],
           'y_train': data['y_train'][:num_train],
           'X_val': data['X_val'],
           'y val': data['y val'],
         }
         #### !!!!!!
         # Play around with the weight scale and learning rate so that you can
         # Your training accuracy should be 1.0 to receive full credit on this
         weight scale = 2e-2
         learning rate = 1e-3
         model = FullyConnectedNet([100, 100],
                       weight_scale=weight_scale, dtype=np.float64)
         solver = Solver(model, small data,
                         print every=10, num epochs=20, batch size=25,
                         update rule='sgd',
                         optim_config={
                            'learning_rate': learning_rate,
         solver.train()
         plt.plot(solver.loss history, 'o')
         plt.title('Training loss history')
         plt.xlabel('Iteration')
         plt.ylabel('Training loss')
```

plt.show()

```
(Iteration 1 / 40) loss: 4.136696
(Epoch 0 / 20) train acc: 0.120000; val acc: 0.116000
(Epoch 1 / 20) train acc: 0.140000; val acc: 0.122000
(Epoch 2 / 20) train acc: 0.240000; val acc: 0.131000
(Epoch 3 / 20) train acc: 0.300000; val acc: 0.149000
(Epoch 4 / 20) train acc: 0.400000; val_acc: 0.150000
(Epoch 5 / 20) train acc: 0.540000; val acc: 0.149000
(Iteration 11 / 40) loss: 1.386106
(Epoch 6 / 20) train acc: 0.680000; val acc: 0.163000
(Epoch 7 / 20) train acc: 0.720000; val acc: 0.168000
(Epoch 8 / 20) train acc: 0.780000; val acc: 0.167000
(Epoch 9 / 20) train acc: 0.780000; val acc: 0.159000
(Epoch 10 / 20) train acc: 0.780000; val acc: 0.163000
(Iteration 21 / 40) loss: 0.980530
(Epoch 11 / 20) train acc: 0.860000; val acc: 0.159000
(Epoch 12 / 20) train acc: 0.840000; val acc: 0.181000
(Epoch 13 / 20) train acc: 0.900000; val acc: 0.171000
(Epoch 14 / 20) train acc: 0.940000; val acc: 0.167000
(Epoch 15 / 20) train acc: 0.940000; val acc: 0.160000
(Iteration 31 / 40) loss: 0.632296
(Epoch 16 / 20) train acc: 0.980000; val acc: 0.171000
(Epoch 17 / 20) train acc: 0.940000; val acc: 0.182000
(Epoch 18 / 20) train acc: 1.000000; val acc: 0.172000
(Epoch 19 / 20) train acc: 1.000000; val acc: 0.174000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.178000
                              Training loss history
```





In []:			