

$$1. [(A \wedge B) \rightarrow C] \wedge B \wedge C' \rightarrow (A \rightarrow C)$$

$$[(A \wedge B) \rightarrow C] \wedge B \wedge C' \quad \text{by hyp.}$$

$$(A \rightarrow B \rightarrow C) \wedge B \wedge C' \quad \text{by ded.}$$

$$A \rightarrow (B \rightarrow C) \wedge B \wedge C' \quad \text{by asso}$$

$$A \rightarrow (C \wedge C') \quad \text{by m.p}$$

$$A \rightarrow 0 \quad \text{by neg.}$$

$$A \rightarrow (C \wedge 0) \quad \text{by dom}$$

$$A \rightarrow C \quad \text{by Simp.}$$

$$2. C(x) \Rightarrow x \text{ is a cat}$$

$$A(x) \Rightarrow x \text{ is an animal}$$

$$F(x) \Rightarrow x \text{ is fuzzy}$$

$$S(x) \Rightarrow x \text{ is something}$$

$$E(x) \Rightarrow x \text{ means cats.}$$

$$(\forall x)[C(x) \rightarrow (E(x) \wedge A(x))] \wedge (\exists x)[S(x) \wedge F(x)] \wedge (\forall x)[F(x) \rightarrow C(x)] \\ \wedge (\forall x)[E(x) \rightarrow S(x)] \rightarrow (\forall x)(A(x))$$

$$4. a) A = \{5, 8, 11, 14, 17, 20, 23, 26, 29, 32, 35, 38\}$$

$$b) B = \{-3, 2, 1, 2\}$$

$$c) C = \{1, 2, 3, 4, 5, 6, 8, 9, 10, 12, 15, 16, 18, 20, 24, 30, 36, 40, 45, 48, 60, 72, 80, 90, 120, 144, 180, 240, 360, 720\}$$

$$6. S = \{1, 2, 3, \dots, 29, 30\}$$

$$A = \{1, 2, 3, \dots, 30\} - \{9, 18, 27\}$$

$$B = \{5, 10, 15, 20, 25, 30\}$$

$$C = \{3, 6, 9, 12, 15, 18, 21, 24, 27, 30\}$$

$$a) |P(A)| = 2^{27}$$

$$b) |A \cup B \cup C| = 30$$

$$c) |(B \cup C) - (B \cap C)|$$

$$B \cup C = \{3, 5, 6, 9, 10, 12, 15, 18, 20, 21, 24, 25, 27, 30\}$$

$$|B \cup C| = 14$$

$$|B \cap C| = 2$$

$$14 - 2 = 12$$