MAT257 PSET 14—Question 1

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We know that if $f:\mathbb{R}^n \to \mathbb{R}$ is a 0-form, $\mathrm{d} f = \sum_i \frac{\partial f}{\partial x^i} \mathrm{d} x_i$. Since f,g,fg are 0-forms,

$$d(fg) = \sum_{i} \frac{\partial (fg)}{\partial x^{i}} dx_{i}$$

$$= \sum_{i} \frac{\partial f}{\partial x^{i}} g + f \frac{\partial g}{\partial x^{i}} dx_{i}$$

$$= g \sum_{i} \frac{\partial f}{\partial x^{i}} dx_{i} + f \sum_{i} \frac{\partial g}{\partial x^{i}} dx_{i}$$

$$= f dg + g df$$