$$\mathcal{H}_0 = U \cdot \sum_{l} \hat{\mathbf{n}}_{l,\uparrow} \hat{\mathbf{n}}_{l,\downarrow} + \sum_{l,\sigma} \underbrace{\left(\vec{E} \cdot \vec{r}_l\right)} \hat{\mathbf{n}}_{l,\sigma}$$



 $\mathcal{H} = \mathcal{H}_0 + \hat{V}$ 

 $\hat{\mathbf{V}} = -J \cdot \sum_{\langle l, m \rangle, \sigma} \left( \hat{\mathbf{h}}_{l, \sigma}^{\dagger} \hat{\mathbf{h}}_{m, \sigma} + \hat{\mathbf{h}}_{m, \sigma}^{\dagger} \hat{\mathbf{h}}_{l, \sigma} \right)$ 

