$\mathcal{H}_N(t) = \sum C_i(t) \cdot \Phi_i(N) \quad \leftrightarrow \quad \mathcal{H}_{\text{VCN}}(N, \vec{\eta}) = \sum \eta_i \cdot \Phi_i(N)$

$$C_{1}(t) = \Pi_{A}(0, 1, t) \qquad \Phi_{1}(N) = J \sum_{l} \sum_{\substack{l^{+(x)} \\ \langle l^{+(x)} m \rangle}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{A}(l, m) | K \rangle$$

$$C_{2}(t) = \Pi_{B}(0, 1, t) \qquad \Phi_{2}(N) = J \sum_{l} \sum_{\substack{l^{+(x)} \\ \langle l^{+(x)} m \rangle}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{B}(l, m) | K \rangle$$

$$C_{3}(t) = \Pi_{C}(0, 1, t) \qquad \Phi_{3}(N) = J \sum_{l} \sum_{\substack{l^{+(x)} \\ \langle l^{+(x)} m \rangle}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{C}(l, m) | K \rangle$$

$$C_{3}(t) = \Pi_{C}(0, 1, t) \qquad \Phi_{3}(N) = J \sum_{l} \sum_{\substack{l < k(x) \\ (l < m)}} \sum_{K} \frac{\Psi_{N}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{C}(l, m) | K \rangle$$

$$C_{4}(t) = \Pi_{A}(1, 0, t) \qquad \Phi_{4}(N) = J \sum_{l} \sum_{\substack{l < k(x) \\ (l > m)}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{A}(l, m) | K \rangle$$

 $\Phi_{5}(N) = J \sum_{l} \sum_{\substack{l < N \\ \langle l > m \rangle}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{B}(l, m) | K \rangle$ $C_5(t) = \Pi_{\rm B}(1,0,t)$ $C_6(t) = \Pi_C(1, 0, t)$

$$\Phi_{6}(N) = J \sum_{l} \sum_{\substack{\langle l \to m \rangle \\ \langle l > m \rangle}} \sum_{K} \frac{\Psi_{K}}{\Psi_{N}} \langle N | \hat{\mathbf{F}}_{C}(l, m) | K \rangle$$

$$C_7(t) = \Pi_{\mathbf{A}}(0, M, t) \qquad \Phi_7(N) = J \sum_{l} \sum_{\substack{\langle l < m \rangle \\ \langle l < m \rangle}} \sum_{K} \frac{\Psi_K}{\Psi_N} \langle N | \hat{\mathbf{F}}_{\mathbf{A}}(l, m) | K \rangle$$