

In [57]:

```

import pymc3 as pm
import numpy as np
import pandas as pd
import arviz as az
import theano
from scipy.stats import norm
from scipy.stats import t
import math
import itertools

from matplotlib import pyplot as plt
from pandas.plotting import scatter_matrix

%matplotlib inline

```

Configuration

In [49]:

```

remove_rows_not_cells      = True

tracesize                  = 50_000
h1_tune_size               = 1000 # default
h1_target_accept           = 0.8 # default
h2_tune_size               = 5000
h2_target_accept           = 0.95

#h1
h1_do_obs                  = True
h1_do_bern                 = True
resample_h1_obs            = False
resample_h1_bern           = False
folderName_h1_obs          = "h1_obs.trace"
folderName_h1_bern         = "h1_bern.trace"

#h2
h2_do_linear               = True
h2_do_quadratic            = True
resample_h2_linear         = False
resample_h2_quadratic      = True
folderName_h2_linear       = "h2_linear.trace"
folderName_h2_quadratic    = "h2_quadratic.trace"

describeData               = False

h1_ropes                   = list(itertools.product(["diff_μ"], [(-4, -0), (-4, -1), (-4, -2)]))
h1_bern_ropes              = list(itertools.product(["diff_μ"], [(0, 0.5), (0, ((4-1.0)/4.0)*0.5), (
var_names_h1_notRope       = ['log10_v', 'μ', 'σ', 'diff_σ', 'eff_size', "eff_size2"]
var_names_h1_all           = var_names_h1_notRope.copy().extend([name for name, rope in h1_ropes])

```

Helperfunctions

In [3]:

```

def flatten(lst):
    res = []
    for inner in lst:
        for v in inner:
            res.append(v)
    return res

```

```
In [4]: def getTrace(folder_name, model_name, resample, tune_size, target_accept):
    with model_name:
        if (resample):
            trace = pm.sample(tracesize, chains=4, tune=tune_size, cores=1, step=pm.NUTS(target_ac
            pm.save_trace(trace, folder_name, overwrite=True)
            trace = pm.load_trace(folder_name)
            return trace

def getInferenceData(trace, model_name):
    with model_name:
        return az.from_pymc3(trace, model = model_name)

def standardize(data, m, sd):
    return (data-m)/sd
```

```
In [5]: def plot_trace_method1(trace_inferencedata, var_names, ropes):
    az.plot_posterior(trace_inferencedata, var_names=var_names, kind='hist', figsize=(8,6)
        , point_estimate='mean', hdi_prob=0.95);
    for rope_vals in ropes:
        if len(rope_vals) == 2:
            (name, rope) = rope_vals
            plot_rope(trace_inferencedata, name, rope, 8, 2.5)
        else:
            (name, rope, height, width) = rope_vals
            plot_rope(trace_inferencedata, name, rope, height, width)

def plot_rope(trace_inferencedata, name, rope, width, height):
    az.plot_posterior(trace_inferencedata, var_names=[name], kind='hist', figsize=(width,height)
        , point_estimate='mean', hdi_prob=0.95, ref_val=0, rope=rope)

def plot_trace_method2(trace, model, var_names):
    az.plot_trace(az.from_pymc3(trace,model=model), var_names=var_names);

def plot_trace_scatter(trace, varnames):
    scatter_matrix(pm.trace_to_dataframe(trace, varnames=varnames), figsize=(20, 10));

def plot_all_data(f_x):
    fig,ax = plt.subplots(figsize=(25,20))
    xprime = np.linspace(1,5,80)
    for i in np.random.randint(0,len(trace_h2_linear),100):
        ax.plot(xprime, f_x(xprime, i), color='lightsteelblue')

    # Define spectrum of colors
    number_of_plots=len(communities)
    colormap = plt.cm.nipy_spectral
    colors = [colormap(i) for i in np.linspace(0, 1,number_of_plots)]
    ax.set_prop_cycle('color', colors)

    [ax.plot(get_relevant_h2(com, getIndexV29())[1], get_relevant_h2(com, getIndexV31())[1], "--",

    plt.legend(loc='best')
    plt.show()
```

```
In [6]: def plot_com_reg_data(com_id, trace, num_ppc, ax, f_x):
    V29_to_plot = np.array(get_relevant_h2(communities[com_id], getIndexV29())[1])
    xprime = np.linspace(1,5,len(V29_to_plot))

    # Plot hdi
    az.plot_hdi(xprime,
        [t.rvs(df=trace[i]['v'],
            loc=f_x(xprime, i, com_id),
            scale=trace[i]['o'])
            for i in np.random.randint(low=0, high=len(trace), size=num_ppc)],
        color='lightblue',
        hdi_prob=0.95,
        ax=ax)

    for i in np.random.randint(0,len(trace_h2_linear),num_ppc):
```

```

        ax.plot(xprime, f_x(xprime, i, com_id), color='lightgreen')

    ax.plot(get_relevant_h2(communities[com_id], getIndexV29())[1], get_relevant_h2(communities[com_id],
        marker='o', linestyle=None, color='black', lw=0,
        label=communities[com_id]))

    ax.set_xlim(1,5)
    ax.set_ylim(-1,5)
    ax.set_title(communities[com_id])

def plot_individual(trace, f_x):
    fig, axs = plt.subplots(nrows=3,ncols=5, figsize=(20,12))
    flatten_axs = axs.ravel()
    [plot_com_reg_data(com_id=com_id,trace=trace,num_ppc=100,ax=ax,f_x=f_x) for (com_id,ax) in zip
    [flatten_axs[i].axis('off') for i in range(len(com_ids),len(flatten_axs))]]
    plt.show()

```

load data

In [7]:

```

df = pd.read_csv('pseudonymized-data.csv')
df = df.rename(columns={df.columns[0]: 'id'})

df = df[df["Community"] != "-1"]
df_h1 = df[["id", "Community", "V33"]]
df_h2 = df[["id", "Community", "V29", "V31"]]

def getIndexV29(): return 0
def getIndexV31(): return 1
def getIndexV33(): return 0

def remove_rows_not_cells(df):
    for col in df.iloc[:,2:].columns:
        df = df[df[col] != -1]
    return df

if remove_rows_not_cells:
    df_h1 = remove_rows_not_cells(df_h1)
    df_h2 = remove_rows_not_cells(df_h2)

```

In [8]:

```

def removeNoAnswer(lst):
    return lst if remove_rows_not_cells else [i for i in lst if i!=-1]

communities = df.Community.unique();

def process_data(df):
    data = []
    for com in communities:
        columns = []
        for question in df.iloc[:,2:].columns:
            columns.append(removeNoAnswer(df[df.Community == com][question].to_numpy()))
        positive = [[0.5 if d==3 else int(d<=3) for d in v] for v in columns]

        N = [len(v) for v in columns]
        μ = [np.mean(v) for v in columns]
        σ = [np.std(v) for v in columns]

        N_bern = [len(v) for v in positive]
        μ_bern = [np.mean(v) for v in positive]
        σ_bern = [np.std(v) for v in positive]
        all = (com, columns, positive, N, μ, σ, N_bern, μ_bern, σ_bern)
        data.append(all)
    return data

data_h1 = process_data(df_h1)
data_h2 = process_data(df_h2)

```

```
def get_relevant(com, dataIndex, data):
    (com, columns, positive, N,  $\mu$ ,  $\sigma$ , N_bern,  $\mu$ _bern,  $\sigma$ _bern) = next(filter(lambda lst : lst[0]==c
    return (com, columns[dataIndex], positive[dataIndex], N[dataIndex],  $\mu$ [dataIndex],  $\sigma$ [dataIndex])

def get_relevant_h1(com, dataIndex):
    return get_relevant(com, dataIndex, data_h1)

def get_relevant_h2(com, dataIndex):
    return get_relevant(com, dataIndex, data_h2)
```

```
In [9]: df_h1.head() if describeData else None
```

```
In [10]: df_h2.head() if describeData else None
```

```
In [11]: df_h1.iloc[:,2:].describe() if describeData else None
```

```
In [12]: df_h2.iloc[:,2:].describe() if describeData else None
```

```
In [13]: if describeData:
    df_h1.hist(column=df_h1.columns[1:], bins=50, figsize=(20,3), layout=(1,3))
    df_h2.hist(column=df_h2.columns[1:], bins=50, figsize=(20,3), layout=(1,3))
    plt.show()
```

H1

The Coala Community is more lenient than the Linux Kernel Community.

The decision rules for the hypothesis that the Coala Community is more lenient than the Linux Kernel Community is as follows:

The Likert scale value of Coala community is lower than that of Linux Kernel Community for question V33. 2 models have been created one comparing the unaltered data and one where data have been converted to a scale where 1,2 =0, 3=0.5 and 4,5=1.

```
In [ ]: (com_coala, obs_coala, bern_coala, N_coala_obs,  $\mu$ _coala_obs,  $\sigma$ _coala_obs, N_coala_bern,  $\mu$ _coala_bern,  $\sigma$ _coala_bern) = get_relevant_h1('coala', 0)
        (com_linux, obs_linux, bern_linux, N_linux_obs,  $\mu$ _linux_obs,  $\sigma$ _linux_obs, N_linux_bern,  $\mu$ _linux_bern,  $\sigma$ _linux_bern) = get_relevant_h1('linux', 0)

        if describeData:
            print("com: ", com_coala, com_linux)
            print("obs: ", obs_coala, obs_linux)
            print("N: ", N_coala_obs, N_linux_obs)
            print(" $\mu$ : ",  $\mu$ _coala_obs,  $\mu$ _linux_obs)
            print(" $\sigma$ : ",  $\sigma$ _coala_obs,  $\sigma$ _linux_obs)
            print("p: ", bern_coala, bern_linux)
            print("N: ", N_coala_bern, N_linux_bern)
            print(" $\mu$ : ",  $\mu$ _coala_bern,  $\mu$ _linux_bern)
            print(" $\sigma$ : ",  $\sigma$ _coala_bern,  $\sigma$ _linux_bern)
```

H1 Model description

```
In [15]: def makeModel(data_coala, data_linux, data_ $\mu$ _coala, data_ $\mu$ _linux, data_ $\sigma$ _coala, data_ $\sigma$ _linux):
    data_ $\sigma$ _coala = np.max([1/1000, data_ $\sigma$ _coala])
    data_ $\sigma$ _linux = np.max([1/1000, data_ $\sigma$ _linux])
    with pm.Model() as model_h1:
         $\mu$ _noData = pm.Normal('mu_noData', mu=1, sigma=100*1, shape=2)
         $\mu$  = pm.Deterministic('mu',  $\mu$ _noData*[data_ $\mu$ _coala, data_ $\mu$ _linux])
         $\sigma$ _noData = pm.Uniform('sigma_noData', lower=1/1000, upper=1*1000, shape=2)
```

```

σ      = pm.Deterministic('σ', σ_noData*[data_σ_coala, data_σ_linux])
v_minus_one = pm.Exponential('v_minus_one', lam=1/29)
v = pm.Deterministic('v', v_minus_one+1)

# for plotting/comparison purposes
log10_v = pm.Deterministic('log10_v', np.log10(v))
eff_size = pm.Deterministic('eff_size', (μ-100)/σ)

eff_size2 = pm.Deterministic('eff_size2', ((μ[0]-μ[1])/np.sqrt((σ[0]**2+σ[1]**2)/2)))

#likelihood
obs_coala = pm.StudentT('obs_coala', nu=v, mu=μ[0], sd=σ[0], observed=data_coala)
obs_linux = pm.StudentT('obs_linux', nu=v, mu=μ[1], sd=σ[1], observed=data_linux)

#differences
diff_μ = pm.Deterministic('diff_μ', μ[0]-μ[1])
diff_σ = pm.Deterministic('diff_σ', σ[0]-σ[1])
return model_h1

```

```

In [16]: model_h1_obs = makeModel(obs_coala, obs_linux, μ_coala_obs, μ_linux_obs, σ_coala_obs, σ_linux_obs)
model_h1_bern = makeModel(bern_coala, bern_linux, μ_coala_bern, μ_linux_bern, σ_coala_bern, σ_linux_bern)

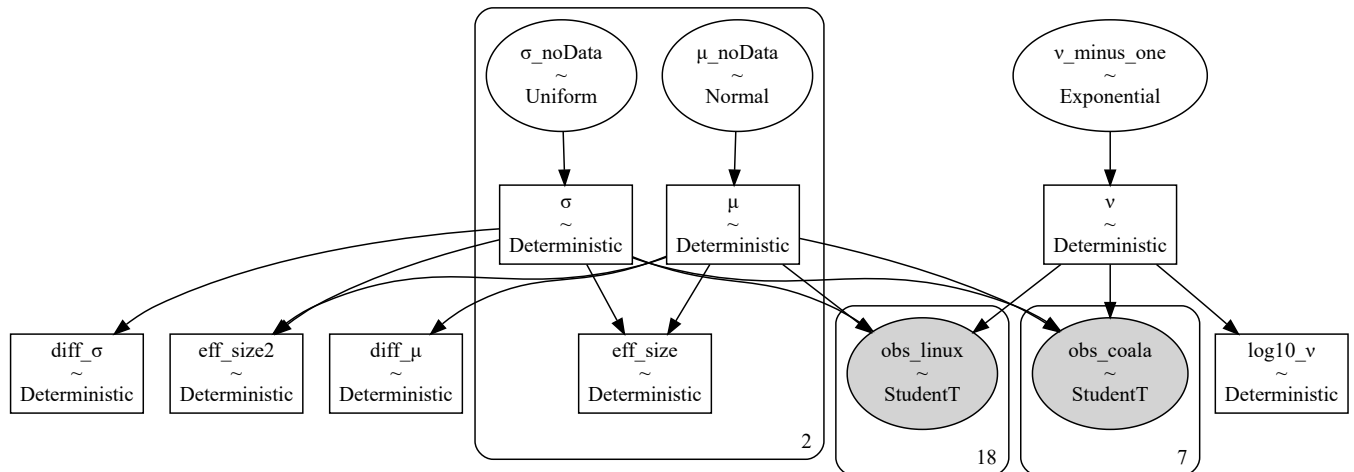
```

```

In [17]: pm.model_to_graphviz(model_h1_obs) if h1_do_obs else None

```

Out[17]:

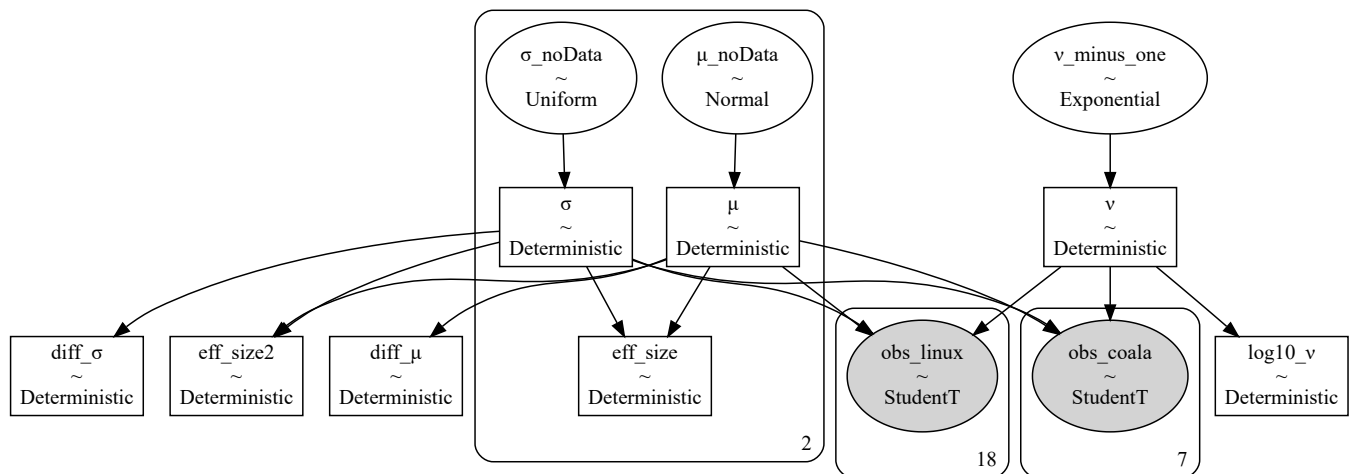


```

In [18]: pm.model_to_graphviz(model_h1_bern) if h1_do_bern else None

```

Out[18]:



Model arguments

The model consists of 3 things we wish to observe. The mean of both questions, the scale of both questions and the value of the normalizer.

The prior on mean μ is chosen to be a normal placed in the middle of the data and its sigma got set to a large value such that the prior has minimal influence. For the prior on the standard deviation whereas a gamma prior could have been used we went with a broad uniform instead. Just like with the mean the values were chosen such that the prior has minimal effect on the posterior.

The likelihood was first decided to be done using a normal. However, a T estimation/student-t was used instead to add robust estimation. The T estimation uses a combined normalizer parameter was as the dataset is small and using the same for both makes the normality more stable for estimation.

The primary result is the `diff_μ` which is computed as the computed μ for the coalas - the μ for the linux community. Effective sample size of the difference was also added in order to better conclude any results.

```
In [19]: trace_h1_obs = getTrace(folderName_h1_obs, model_h1_obs, resample_h1_obs, h1_tune_size, h1_target)
         trace_h1_inferencedata_obs = getInferenceData(trace_h1_obs, model_h1_obs) if h1_do_obs else None
```

```
In [20]: trace_h1_bern = getTrace(folderName_h1_bern, model_h1_bern, resample_h1_bern, h1_tune_size, h1_target)
         trace_h1_inferencedata_bern = getInferenceData(trace_h1_bern, model_h1_bern) if h1_do_bern else None
```

H1 Sampling analysis

```
In [21]: az.summary(trace_h1_obs) if h1_do_obs else None
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\data\io_pymc3.py:87: FutureWarning: Using `from_pymc3` without the model will be deprecated in a future release. Not using the model will return less accurate and less useful results. Make sure you use the model argument or call from_pymc3 with in a model context.
  warnings.warn(
```

	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_mean	ess_sd	ess_bulk	ess_tail	r_hat
μ_noData[0]	1.011	0.152	0.727	1.292	0.001	0.000	85420.0	85420.0	103013.0	91984.0	
μ_noData[1]	1.003	0.081	0.852	1.160	0.000	0.000	131062.0	130211.0	132836.0	111985.0	
μ[0]	1.733	0.261	1.246	2.214	0.001	0.001	85420.0	85420.0	103013.0	91984.0	
μ[1]	2.899	0.235	2.460	3.352	0.001	0.000	131062.0	130211.0	132836.0	111985.0	
σ_noData[0]	1.359	0.607	0.558	2.427	0.002	0.002	72270.0	63817.0	56290.0	36818.0	
σ_noData[1]	1.078	0.217	0.706	1.487	0.001	0.000	113490.0	113490.0	108811.0	78999.0	
σ[0]	0.614	0.274	0.252	1.096	0.001	0.001	72270.0	63817.0	56290.0	36818.0	
σ[1]	0.943	0.190	0.618	1.301	0.001	0.000	113490.0	113490.0	108811.0	78999.0	
v_minus_one	35.291	30.418	0.146	90.174	0.078	0.055	153095.0	153095.0	69408.0	34160.0	
v	36.291	30.418	1.146	91.174	0.078	0.055	153095.0	153095.0	69408.0	34160.0	
log10_v	1.412	0.381	0.691	2.089	0.002	0.001	60570.0	60570.0	69408.0	34160.0	
eff_size[0]	-185.384	73.284	-303.177	-66.886	0.652	0.726	12639.0	5089.0	56293.0	36829.0	
eff_size[1]	-106.961	20.774	-144.920	-68.779	0.081	0.074	65285.0	38991.0	108844.0	79820.0	
eff_size2	-1.494	0.501	-2.431	-0.541	0.002	0.001	93463.0	64340.0	103168.0	94523.0	
diff_μ	-1.166	0.350	-1.827	-0.512	0.001	0.001	106406.0	96329.0	115411.0	106732.0	
diff_σ	-0.329	0.330	-0.916	0.273	0.001	0.001	91701.0	76028.0	109034.0	101789.0	

```
In [22]: az.summary(trace_h1_bern) if h1_do_bern else None
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\data\io_pymc3.py:87: FutureWarning: Using `from_pymc3` without the model will be deprecated in a future release. Not using the model will return less accurate and less useful results. Make sure you use the model argument or call from_pymc3 with
```

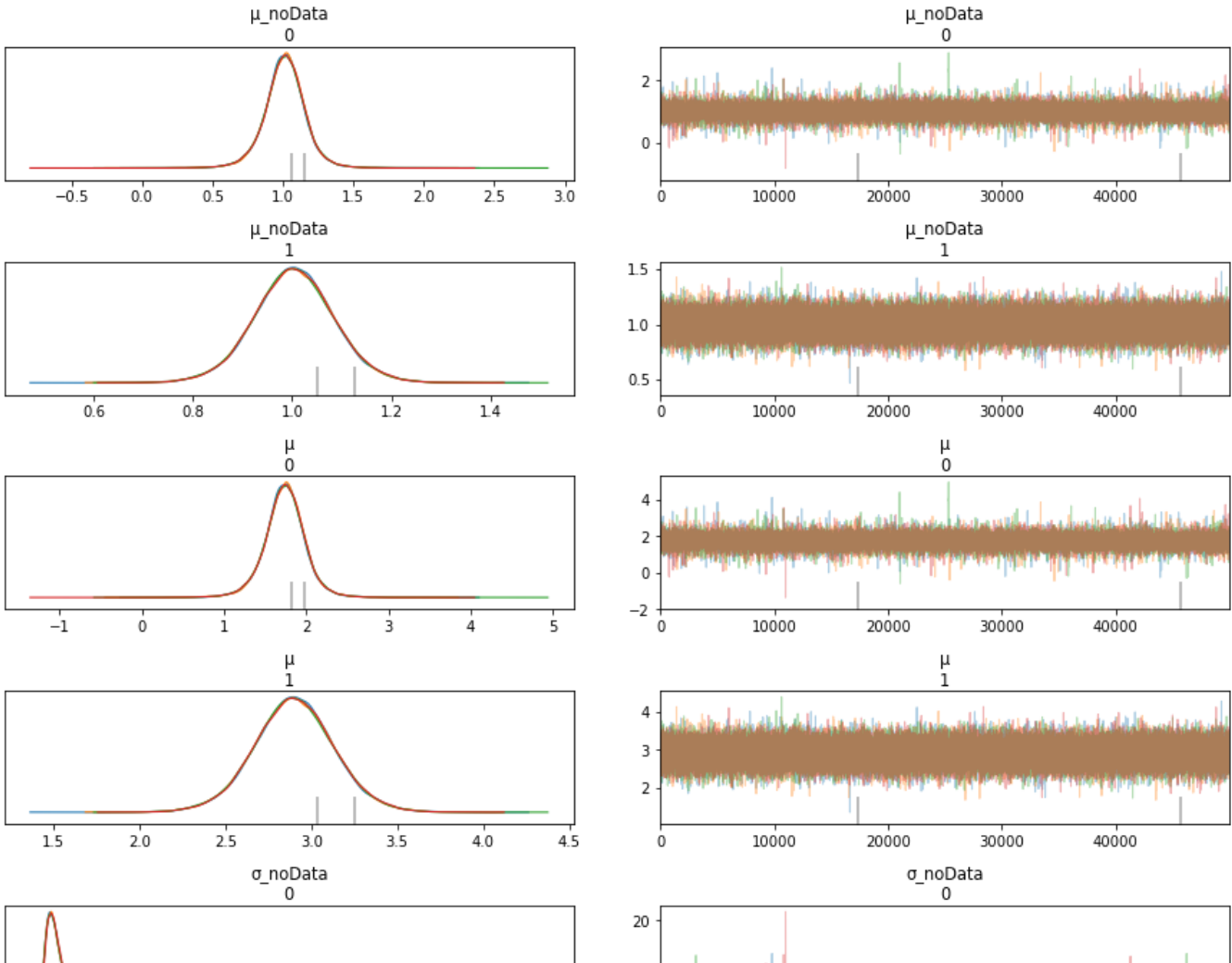
in a model context.
warnings.warn(

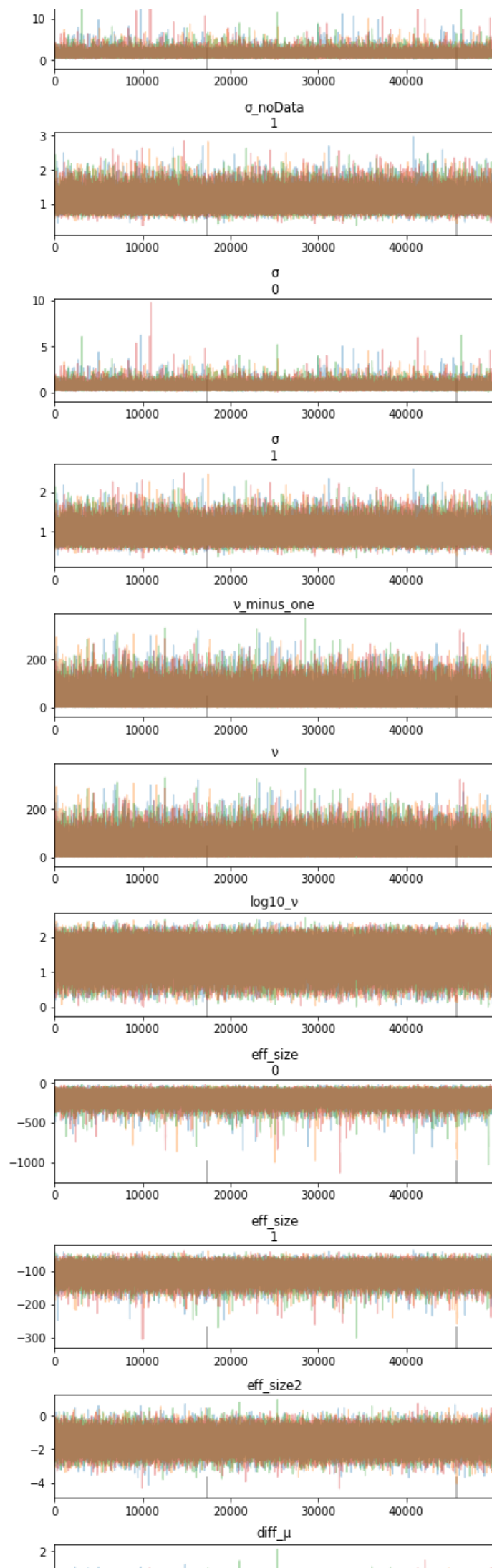
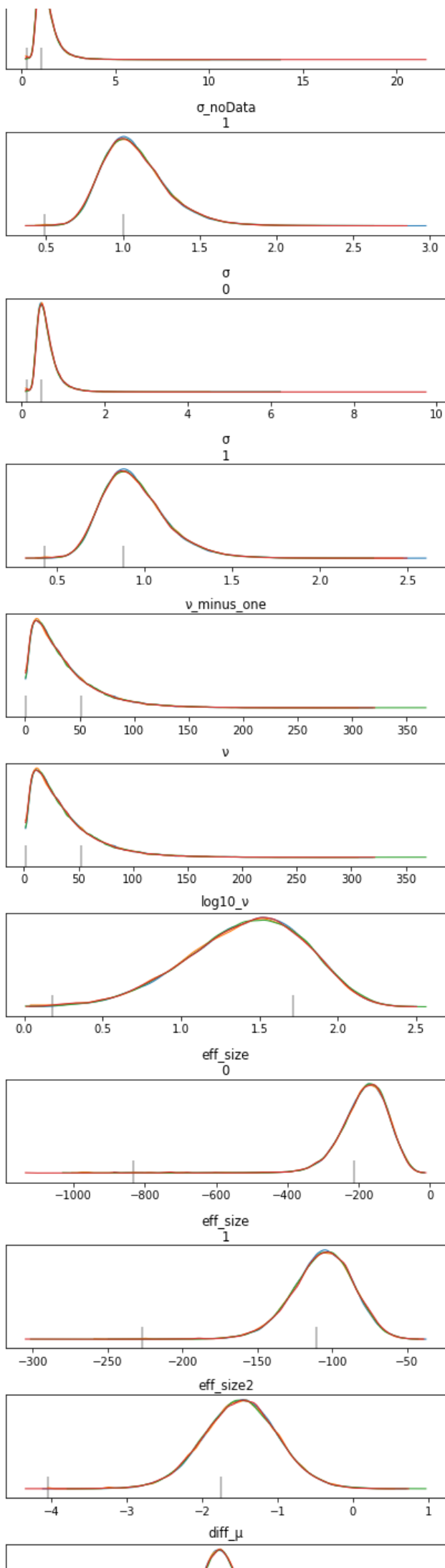
Out[22]:

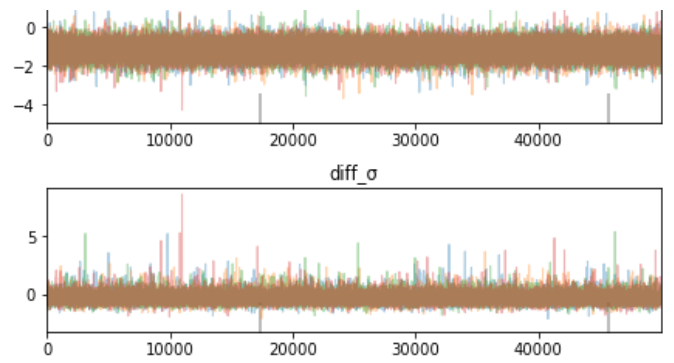
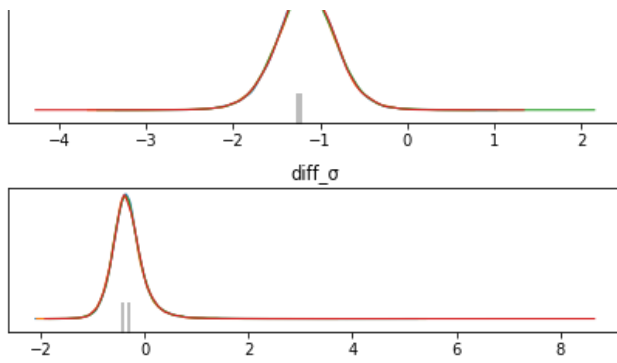
	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_mean	ess_sd
$\mu_{\text{noData}}[0]$	1.000000e+00	0.000000e+00	1.000000e+00	1.000000e+00	0.000	0.000	121715.0	121715.0
$\mu_{\text{noData}}[1]$	1.003000e+00	2.000000e-01	6.270000e-01	1.383000e+00	0.000	0.000	182554.0	177232.0
$\mu[0]$	1.000000e+00	0.000000e+00	1.000000e+00	1.000000e+00	0.000	0.000	121715.0	121715.0
$\mu[1]$	5.290000e-01	1.060000e-01	3.310000e-01	7.300000e-01	0.000	0.000	182554.0	177232.0
$\sigma_{\text{noData}}[0]$	1.000000e-03	0.000000e+00	1.000000e-03	2.000000e-03	0.000	0.000	103390.0	79187.0
$\sigma_{\text{noData}}[1]$	1.094000e+00	2.150000e-01	7.260000e-01	1.495000e+00	0.001	0.000	157936.0	145014.0
$\sigma[0]$	0.000000e+00	0.000000e+00	0.000000e+00	0.000000e+00	0.000	0.000	103390.0	79187.0
$\sigma[1]$	4.270000e-01	8.400000e-02	2.830000e-01	5.830000e-01	0.000	0.000	157936.0	145014.0
$v_{\text{minus_one}}$	3.819300e+01	3.085900e+01	1.149000e+00	9.409000e+01	0.071	0.053	187332.0	168594.0
v	3.919300e+01	3.085900e+01	2.149000e+00	9.509000e+01	0.071	0.053	187332.0	168967.0
$\log_{10} v$	1.465000e+00	3.490000e-01	8.030000e-01	2.093000e+00	0.001	0.001	155446.0	155446.0
$\text{eff_size}[0]$	-8.249509e+07	1.390605e+07	-9.899999e+07	-5.652645e+07	36282.613	25655.762	146896.0	146896.0
$\text{eff_size}[1]$	-2.417220e+02	4.495500e+01	-3.267640e+02	-1.590710e+02	0.106	0.075	178214.0	178214.0
eff_size2	1.616000e+00	4.570000e-01	7.680000e-01	2.482000e+00	0.001	0.001	198337.0	198337.0
$\text{diff_}\mu$	4.710000e-01	1.060000e-01	2.700000e-01	6.690000e-01	0.000	0.000	182554.0	180142.0
$\text{diff_}\sigma$	-4.270000e-01	8.400000e-02	-5.830000e-01	-2.830000e-01	0.000	0.000	157936.0	145014.0

In [23]:

```
plot_trace_method2(trace_h1_obs, model_h1_obs, var_names_h1_all) if h1_do_obs else None
```

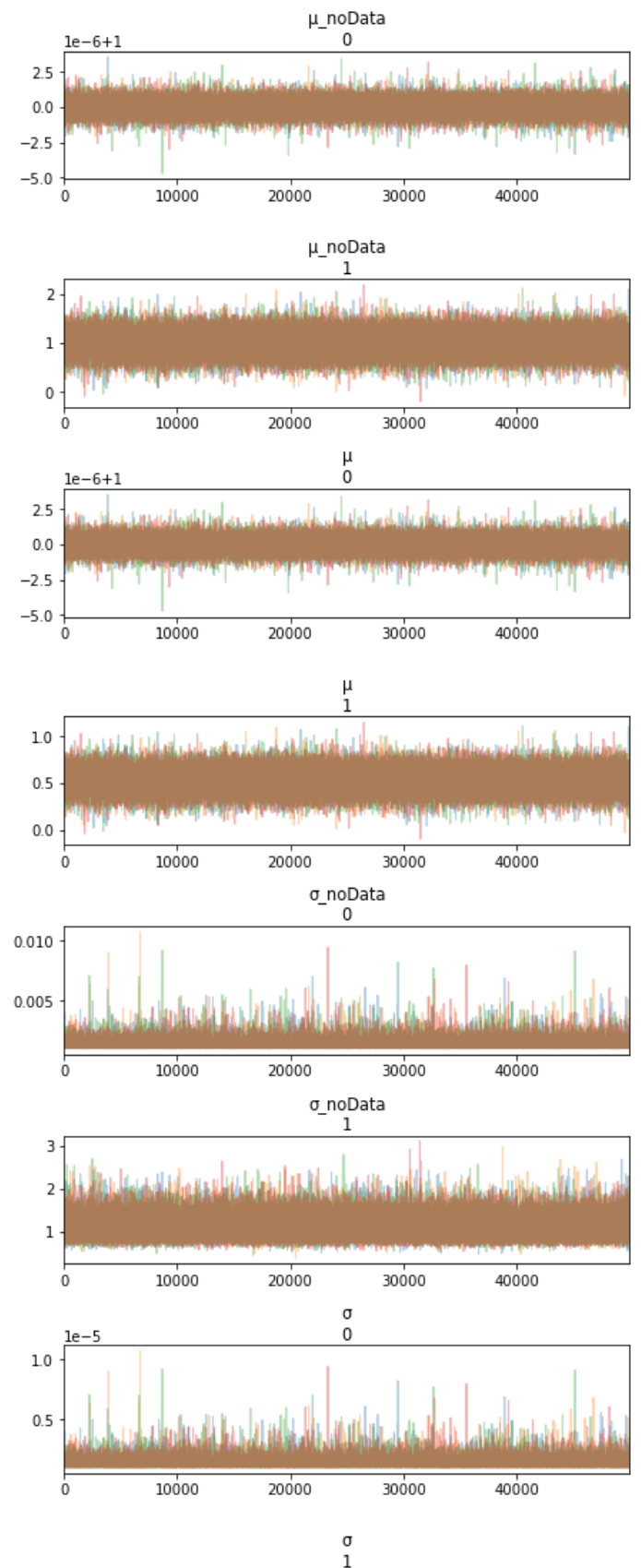
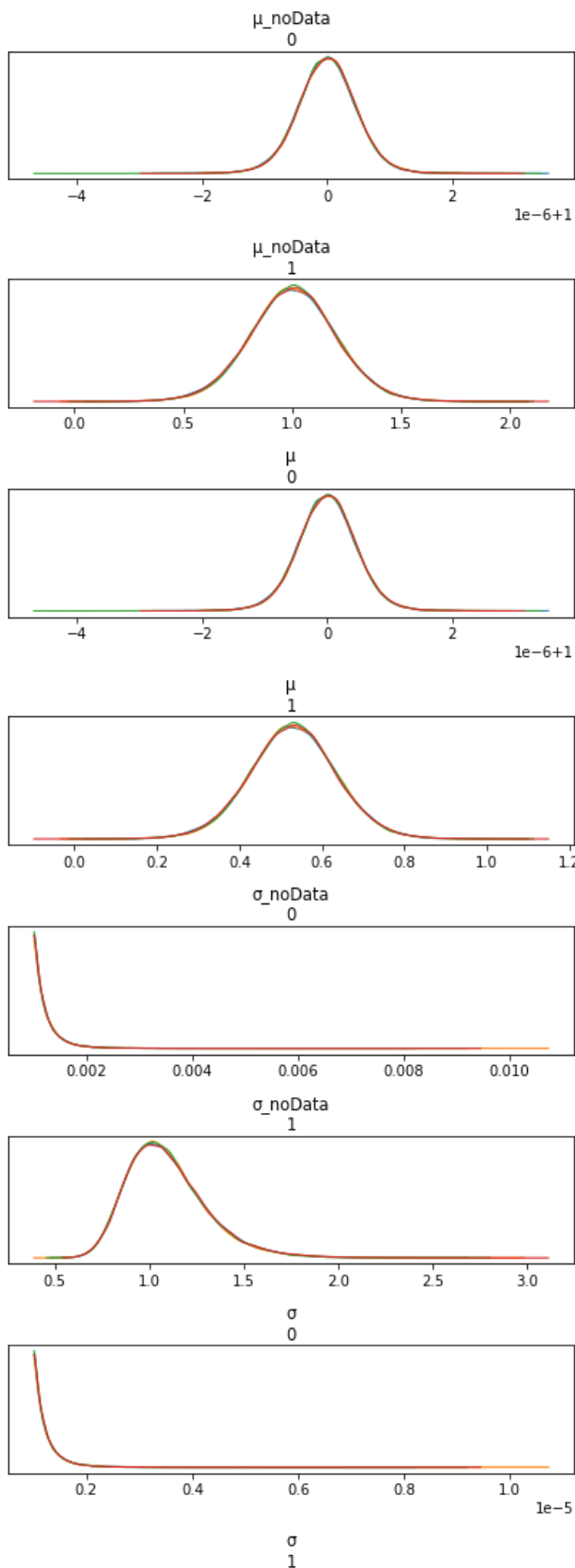


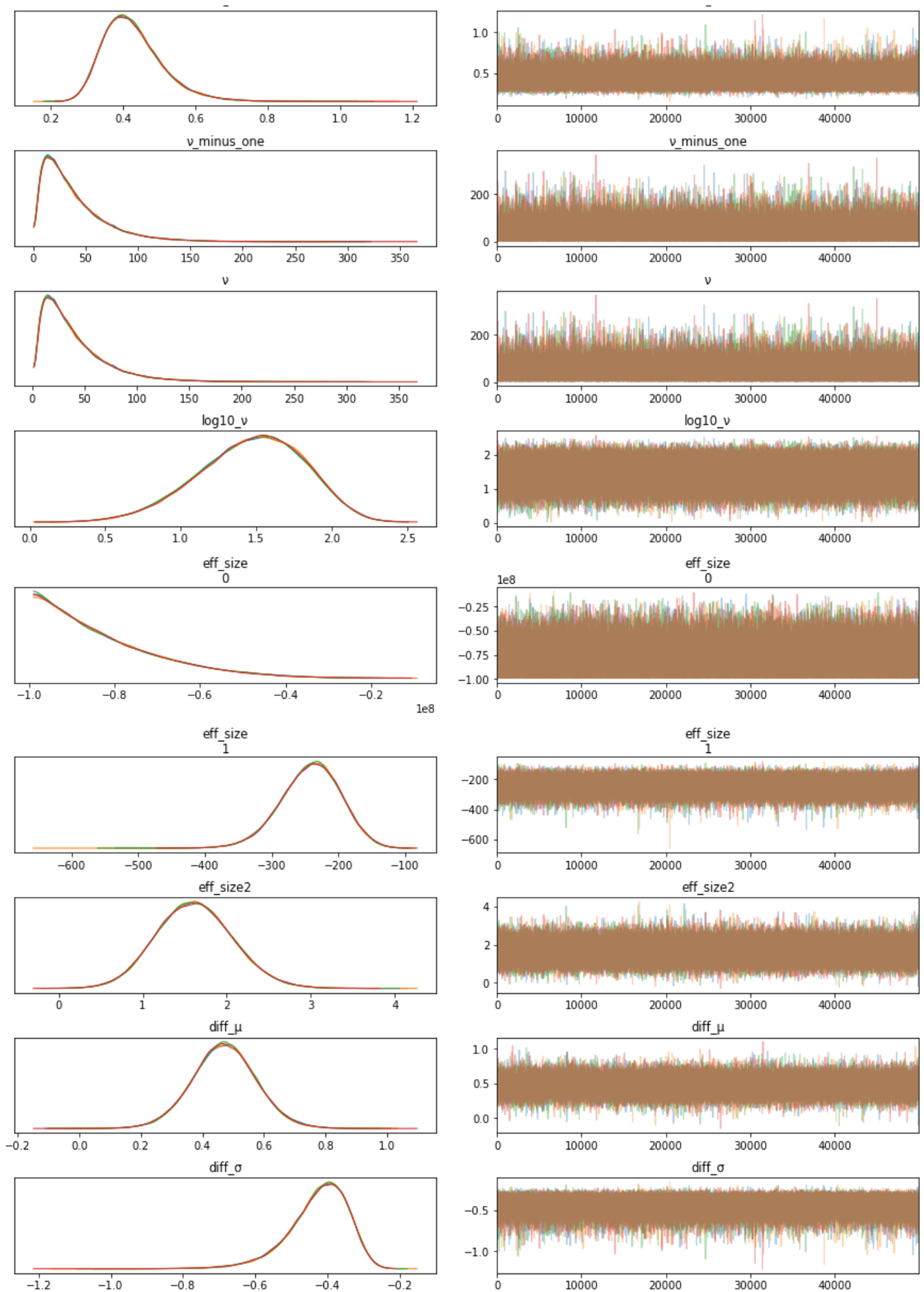




In [24]:

```
plot_trace_method2(trace_h1_bern, model_h1_bern, var_names_h1_all) if h1_do_bern else None
```





Sampling effectiveness

The tune used was the default 1000, and the number of cores was set to 1 as we otherwise observed many divergences.

The convergence diagnostic called \hat{r} is a generalization of the shrink factor / variance within the chain compared to variance between the chains. As it is 1 for both the original data and the transformed and not

above 1.05 there isn't a need to increase burn-in.

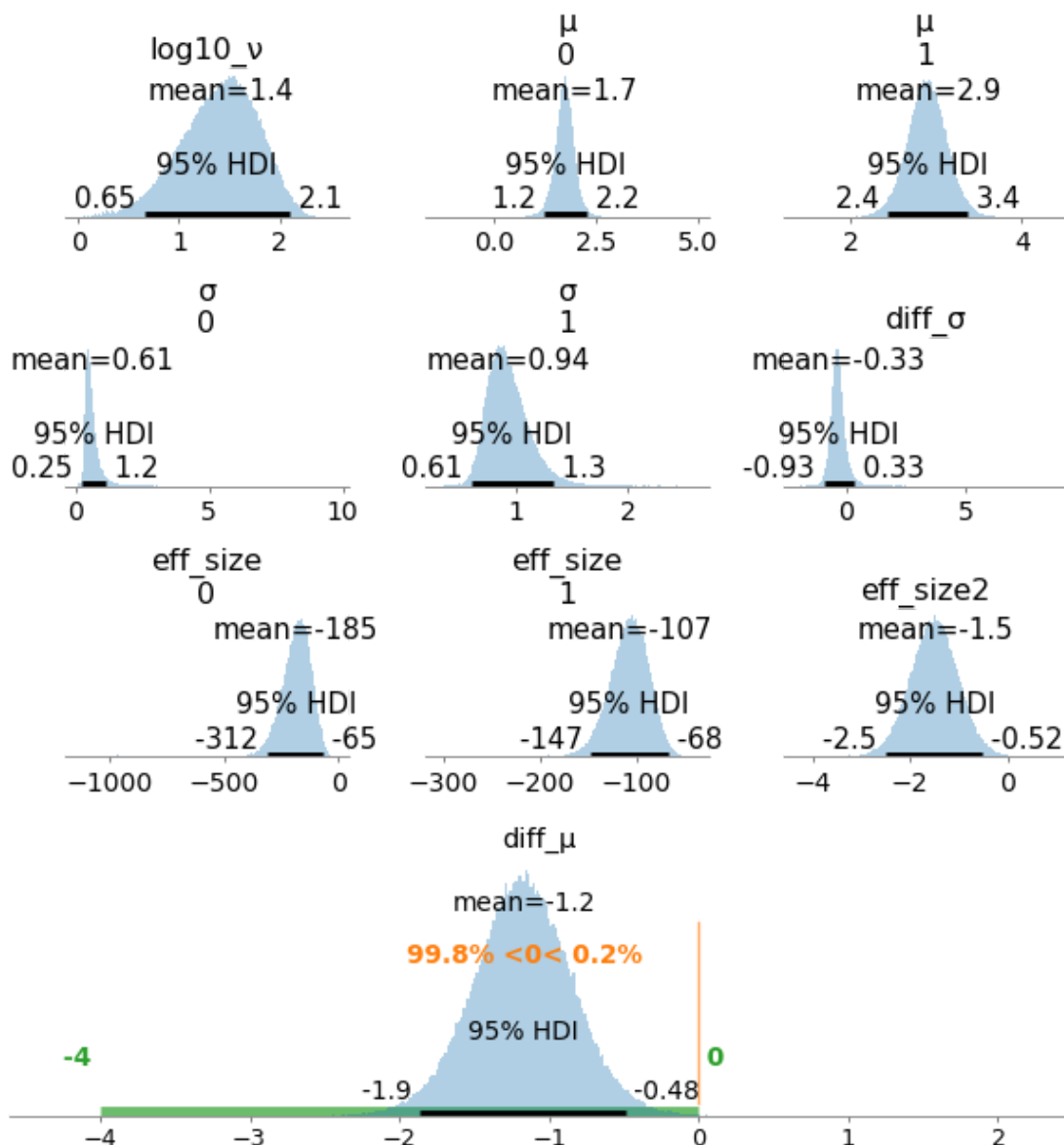
The visual check of convergence gotten with `az.plot_trace` method show that the chains are overlapping in the limit and that the densities are overlapping. As there are only 2 black rugplot for the original and 0 for the transformed, there aren't sufficient divergences present to cast doubt of the result.

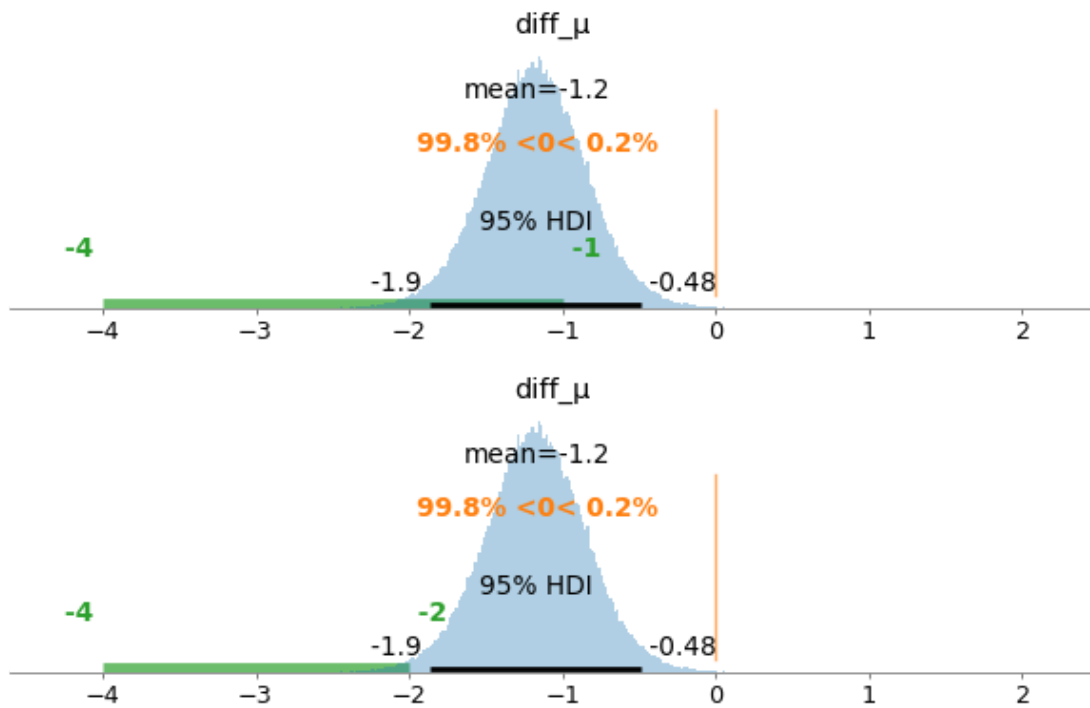
The effective sample size, which should be close to the sample size `tracesize` times number of chains, is for all variables larger than 55_000 and therefore also the 10_000 recommended for 95% HDI inference. For the transformed data the ESS is even greater and is between 100_000 and 200_000. The Monte Carlo standard error / MCSE which indicates the standard deviation of the chain / $\sqrt{\text{ESS}}$, is also low indicating an effective sampling.

When testing which sampler to use the best was the no U-turn sampler or the NUTS sampler. The samplers were tested with a `tracesize` of 10_000, 4 chains and their ESS was compared. For the metropolis, `step=pm.Metropolis()`, some variables had an ESS lower than 10_000 and for almost all it was lower than 30_000. For the Hamiltonian monte carlo, `step=HamiltonianMC()`, the ESS was for all variables lower than 20_000. The tune size was set by plotting the values over iterations and observing when it starts to flatten out.

H1 Finds

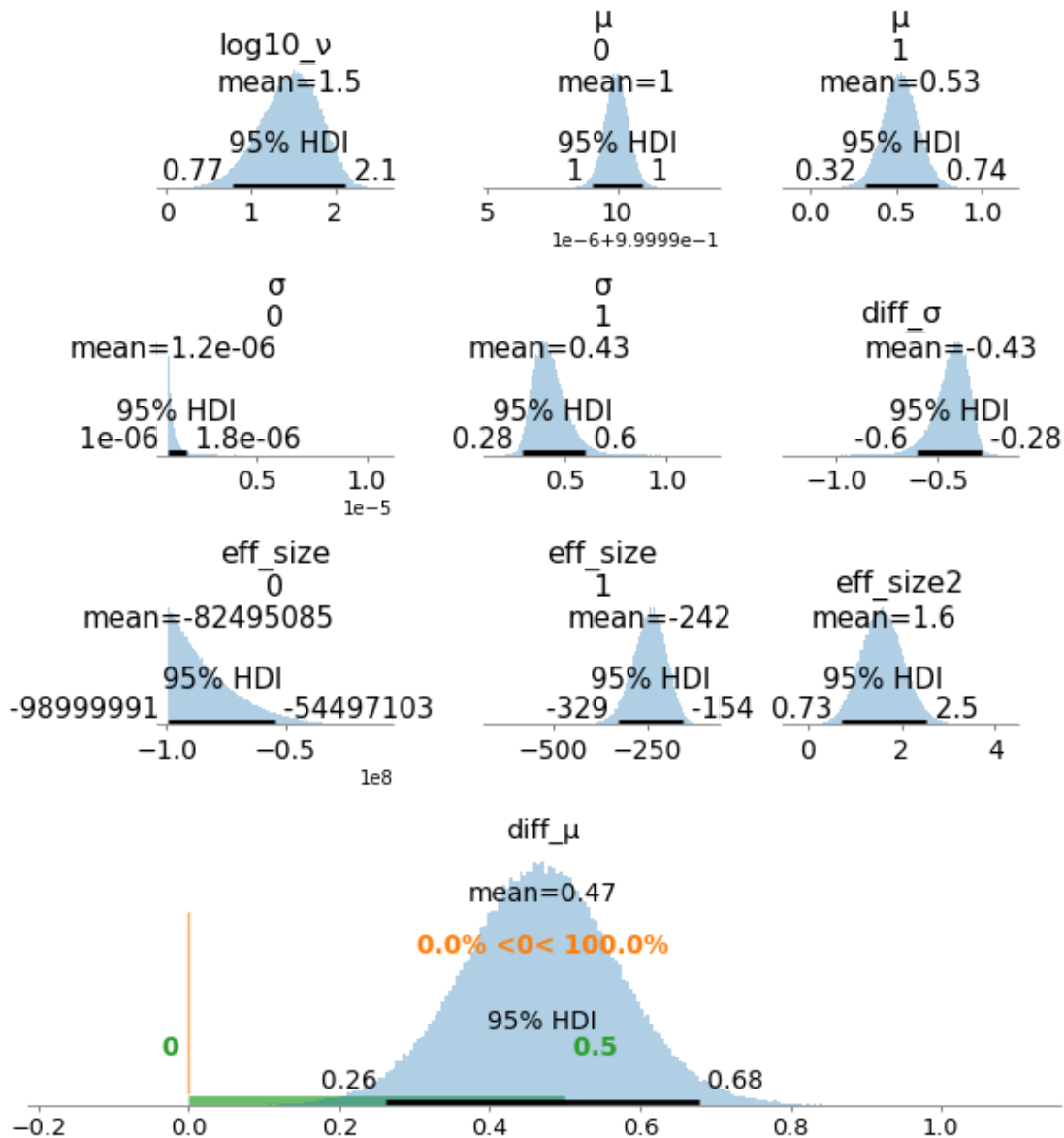
In [25]: `plot_trace_method1(trace_h1_inferencedata_obs, var_names_h1_notRope, h1_ropes) if h1_do_obs else`

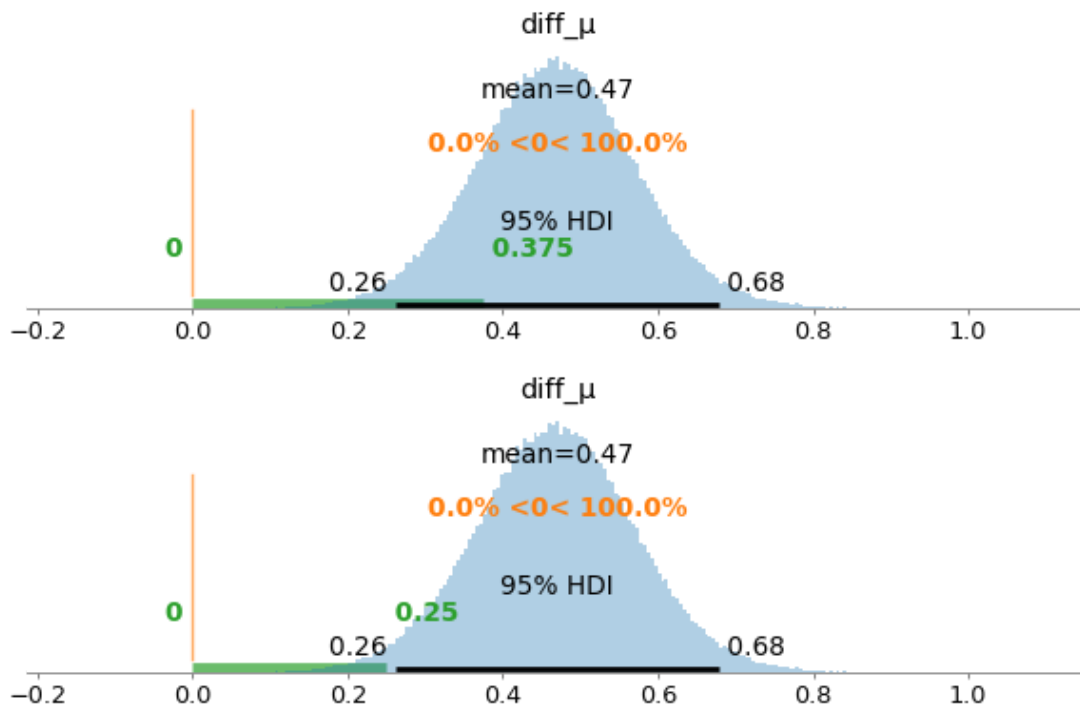




In [26]:

```
plot_trace_method1(trace_h1_inferencedata_bern, var_names_h1_notRope, h1_bern_ropes) if h1_do_bern
```





```
In [27]: # plot_trace_scatter(trace_h1_obs, ['μ_noData', 'μ', 'diff_μ'])
```

```
In [28]: # plot_trace_scatter(trace_h1_bern, ['μ_noData', 'μ', 'diff_μ'])
```

Summary of finds

For both the original and the transformed model, the normalizer v is less than 50. This indicates that in the dataset there are multiple outliers present and the t distribution thus differs from the normal it you have been if no outliers were present.

The means fro the Coala is as expected 1 for the transformed and for the original the 95% HDI is between 1.2 and 2.2. For the original data of the Linux the 95% HDI is between 2.4 and 3.4 and for the transformed it is between 0.32 and 0.74.

H1 acceptance / rejection

To clarify vagueness 3 hypotheses have been created.

- The bare minimum hypothesis says that the V33 for Coala community is less than or equal to the Linux community. Since the difference can be between 0 and 4 the rope for is between -4 and 0.
- The lax hypothesis we decided that the Coala is at least one less than the Linux community. The value 1 was chosen because the amount of observed data is quite low and the accepted range difference should be higher to accommodate this (~25% of the scale). Thus, the rope for the lax hypothesis is between -4 and -1.
- The stricter hypothesis we decided that the Coala is at least 2 less than the Linux community. The value 2 was chosen as it covers (~50% of the scale) and shows a clearer undeniable difference is present.

The hypothesis will be accepted if the HDI of difference is within the ROPE, else it will be deemed inconclusive if they overlap and rejected if the rope is entirely within the 95% HDI.

For both the data and the effective sample size of the data and the transformed data the 95% HDI is entirely within the rope from -4 to 0 and thus it can be concluded that the bare minimum hypothesis of Coala being lower or equal to the Linux community is accepted. Both 95% HDIs however crosses the rope from -4 to -1 and thus from the current data it is inconclusive when going with the definition of "more lenient" meaning a difference of always larger or equal to 1.

The stricter hypothesis of more lenient referring to a difference of at least 2 is however rejected since the rope

from -4 to -2 falls completely outside the 95% HDI. This hypothesis is however inconclusive in regard to the standard the effect size. Since effect size is the difference of means relative to the average scale, the standard deviation in the data is large, which could be a reason to not yet exclude the hypothesis.

H2

All communities show either a protective or equitable style of governance for pull requests (so for each community answers to V29 and V31 are different)

We have created two models: a linear and a quadratic to model the relationship between the answers to V29 and V31.

The quadratic model was introduced to counteract skewed results around the neutral values of 3. It was deemed needed considering cases where if one answer 3 for V29 any answer between 5 and 1 for V31 would still be acceptable for this hypothesis, considering is neither positive or negative. While a cubic function would have been more effective at displaying the ignorance of the middle values it was decided that with that few data points it would become a case of overfitting.

Standardize data

```
In [29]: V29_norm = flatten([get_relevant_h2(com, getIndexV29())[1] for com in communities])
V31_norm = flatten([get_relevant_h2(com, getIndexV31())[1] for com in communities])
idxs = flatten([[i for v in get_relevant_h2(com, getIndexV29())[1]] for (i,com) in enumerate(commu
com_ids = range(len(communities))
m_29 = np.mean(V29_norm)
m_31 = np.mean(V31_norm)
sd_29 = np.std(V29_norm)
sd_31 = np.std(V31_norm)
V29 = standardize(V29_norm, m_29, sd_29)
V31 = standardize(V31_norm, m_31, sd_31)
```

Linear Model

```
In [30]: with pm.Model() as model_h2_linear:
    # Prior
    ζ0_group_μ = pm.Normal('ζ0_group_μ', mu=0, sigma=10)
    ζ1_group_μ = pm.Normal('ζ1_group_μ', mu=0, sigma=10)
    ζ0_group_σ = pm.Uniform('ζ0_group_σ', lower=1/1000, upper=1000)
    ζ1_group_σ = pm.Uniform('ζ1_group_σ', lower=1/1000, upper=1000)

    ζσ = pm.Uniform('ζσ', lower=1/1000, upper=1000)
    v_minus_one = pm.Exponential('v_minus_one', lam=1/29)
    v = pm.Deterministic('v', v_minus_one+1)

    ζ0 = pm.Normal('ζ0', mu=ζ0_group_μ, sigma=ζ0_group_σ, shape=len(communities))
    ζ1 = pm.Normal('ζ1', mu=ζ1_group_μ, sigma=ζ1_group_σ, shape=len(communities))

    pm.StudentT('obs',
                nu=v,
                mu=ζ0[idxs]+ζ1[idxs]*V29,
                sigma=ζσ,
                observed=V31)

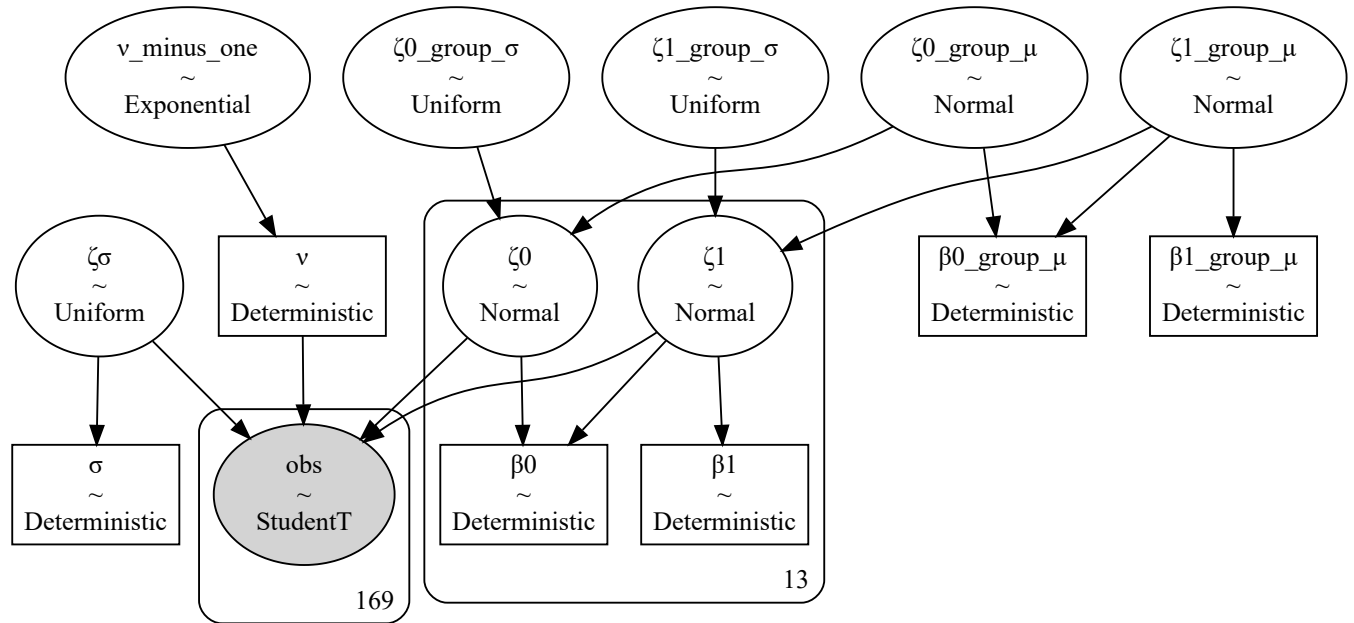
    #transforming data back
    β0 = pm.Deterministic('β0', (ζ0*sd_31) + m_31 - (ζ1*m_29*sd_31/sd_29))
    β1 = pm.Deterministic('β1', ζ1*sd_31/sd_29)

    β0_group_μ = pm.Deterministic('β0_group_μ', (ζ0_group_μ*sd_31) + m_31 - (ζ1_group_μ*m_29*sd_31/sd_29))
    β1_group_μ = pm.Deterministic('β1_group_μ', ζ1_group_μ*sd_31/sd_29)

    σ = pm.Deterministic('σ', ζσ)
```

```
pm.model_to_graphviz(model_h2_linear)
```

Out[30]:



Model arguments

The linear model represents the relationship between the protective and equitable style of governance for pull requests for individual communities and a group of the communities. The linear model is defined with equation $V29 = \beta_0 + \beta_1 * V31$. The equation contains the metric predicted $V29$, metric predictor $V31$, the intercept β_0 and the slope β_1 .

Similar to H1, the prior distribution of the mean is chosen to be normal for mean per community and group. The scale parameter is set to a large uniform, so it has little relevance. The likelihood function also uses student-T for robust distribution.

The parameters: scale (σ) and normalizer (v) is common for all communities.

The observed data passed to the likelihood function are standardized. It was done to improve the performance of the sampling by making it easier for the algorithm to explore the parameter space. The mean and standard deviation of the data is shifted and shrunk to be close to 0. The results are transformed back to the original scale with a deterministic distribution. The standardization is done by having

$$(y - M_y)/SD_y = z_y = \zeta_0 + \zeta_1 * z_x$$

$$z_x = (x - M_x)/SD_x$$

Solving for y gives:

$$y = \beta_0 + \beta_1 x$$

$$\beta_0 = \zeta_0 SD_y + M_y - \zeta_1 M_x * SD_y / SD_x$$

$$\beta_1 = \zeta_1 SD_y / SD_x$$

$\beta_0_group_mu$ and $\beta_1_group_mu$ are the parameters used to make a decision on the hypothesis regarding general trends. β_0 and β_1 are the parameters to evaluate to test if the hypothesis works on all communities.

H2 Linear model, sampling

In [31]:

```
trace_h2_linear = getTrace(folderName_h2_linear, model_h2_linear, resample_h2_linear, h2_tune_size)
trace_h2_inferencedata_linear = getInferenceData(trace_h2_linear, model_h2_linear) if h2_do_li
```

Sequential sampling (4 chains in 1 job)

NUTS: [ζ_1 , ζ_0 , v_minus_one , $\zeta\sigma$, $\zeta_1_group_sigma$, $\zeta_0_group_sigma$, $\zeta_1_group_mu$, $\zeta_0_group_mu$]

100.00% [55000/55000 03:59<00:00 Sampling chain 0, 1,228 divergences]

100.00% [55000/55000 04:19<00:00 Sampling chain 1, 1,178 divergences]

divergences]

100.00% [55000/55000 04:47<00:00 Sampling chain 2, 710

divergences]

100.00% [55000/55000 04:29<00:00 Sampling chain 3, 439

divergences]

Sampling 4 chains for 5_000 tune and 50_000 draw iterations (20_000 + 200_000 draws total) took 1056 seconds.

There were 1228 divergences after tuning. Increase `target_accept` or reparameterize.

There were 2406 divergences after tuning. Increase `target_accept` or reparameterize.

There were 3116 divergences after tuning. Increase `target_accept` or reparameterize.

There were 3555 divergences after tuning. Increase `target_accept` or reparameterize.

The number of effective samples is smaller than 10% for some parameters.

```
In [32]: az.summary(trace_h2_linear) if h2_do_linear else None
```

C:\ProgramData\Miniconda3\lib\site-packages\arviz\data\io_pymc3.py:87: FutureWarning: Using `from_pymc3` without the model will be deprecated in a future release. Not using the model will return less accurate and less useful results. Make sure you use the model argument or call from_pymc3 with in a model context.

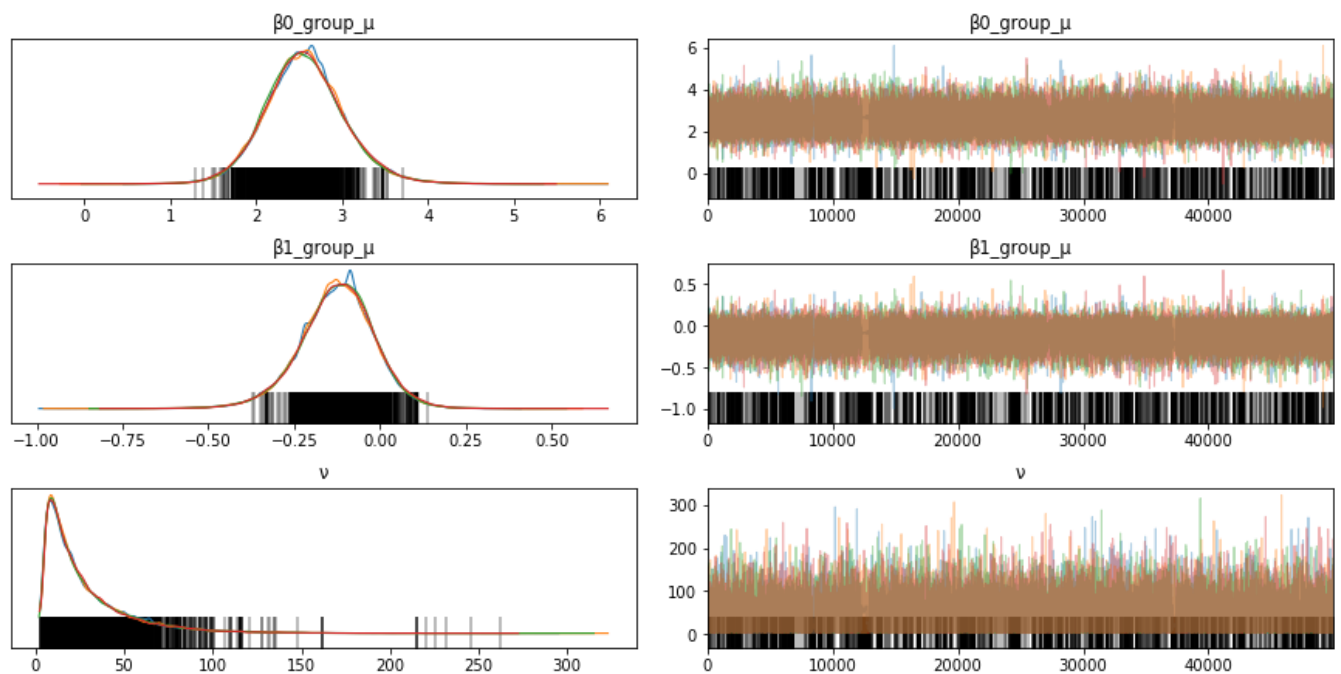
warnings.warn()

	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_mean	ess_sd	ess_bulk	ess_tail	r_hat
$\zeta_0_group_μ$	-0.005	0.154	-0.301	0.282	0.001	0.001	41733.0	41733.0	41398.0	27215.0	1.0
$\zeta_1_group_μ$	-0.135	0.118	-0.361	0.086	0.001	0.000	50147.0	50147.0	48506.0	79028.0	1.0
$\zeta_0[0]$	-0.374	0.169	-0.692	-0.058	0.001	0.000	70999.0	70999.0	71062.0	79830.0	1.0
$\zeta_0[1]$	0.097	0.176	-0.230	0.435	0.001	0.000	115470.0	83560.0	114983.0	128338.0	1.0
$\zeta_0[2]$	0.012	0.273	-0.514	0.519	0.001	0.001	66709.0	52107.0	65859.0	41698.0	1.0
...
$\beta_1[11]$	-0.088	0.200	-0.488	0.303	0.001	0.001	128144.0	47465.0	117682.0	85412.0	1.0
$\beta_1[12]$	-0.172	0.193	-0.560	0.182	0.001	0.001	58313.0	46201.0	58330.0	81724.0	1.0
$\beta_0_group_μ$	2.566	0.466	1.715	3.474	0.002	0.001	55134.0	54648.0	53829.0	56089.0	1.0
$\beta_1_group_μ$	-0.125	0.110	-0.336	0.080	0.000	0.000	50147.0	50147.0	48506.0	79028.0	1.0
σ	0.876	0.073	0.734	1.011	0.000	0.000	56711.0	56711.0	56792.0	60054.0	1.0

62 rows × 11 columns

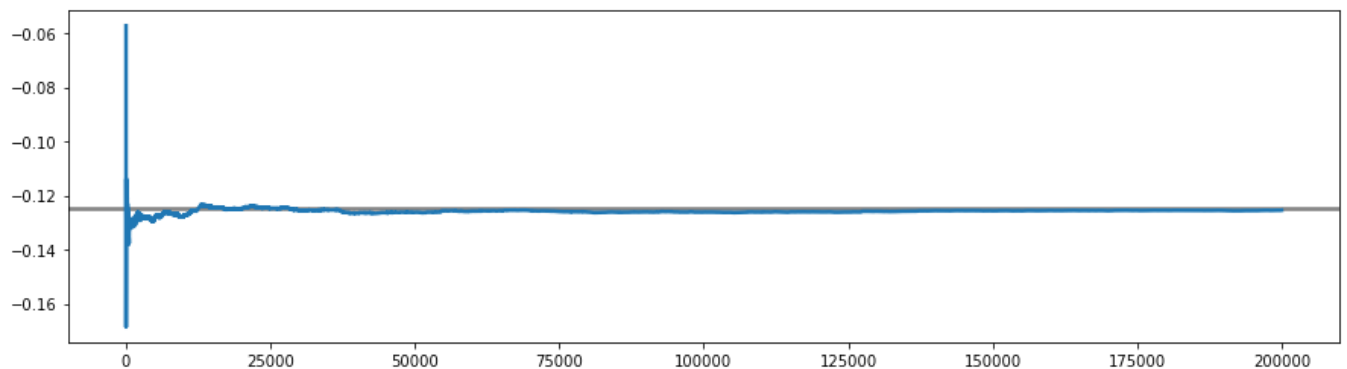
```
In [33]: var_names_h2_linear=['β0_group_μ', 'β1_group_μ', 'v']
rope_h2_linear = [("β1_group_μ", (-1.5, -0.65)), ("β1", (-1.5, -0.65), 15, 10)]
```

```
In [34]: plot_trace_method2(trace_h2_linear, model_h2_linear, var_names_h2_linear)
```

```
In [35]: logtau = trace_h2_linear["beta1_group_mu"]
mlogtau = [np.mean(logtau[:i]) for i in np.arange(1, len(logtau))]
plt.figure(figsize=(15, 4))
plt.axhline(-0.125, lw=2.5, color="gray")
plt.plot(mlogtau, lw=2.5)
```

Out[35]: [



Sampling effectiveness

R_{hat} was higher than 1 at ~ 1.02 , but it was fixed by adding tuning steps and higher trace size.

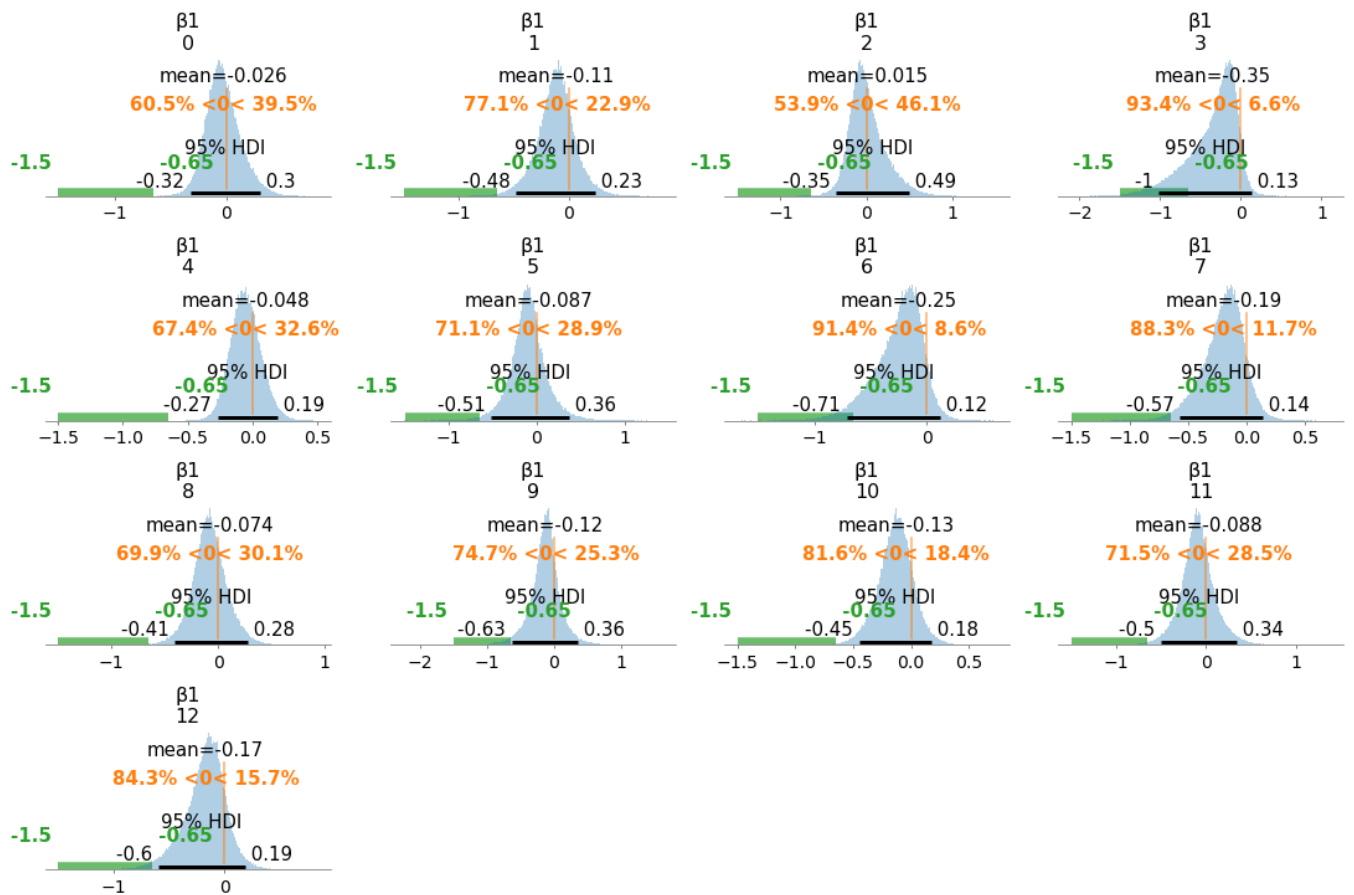
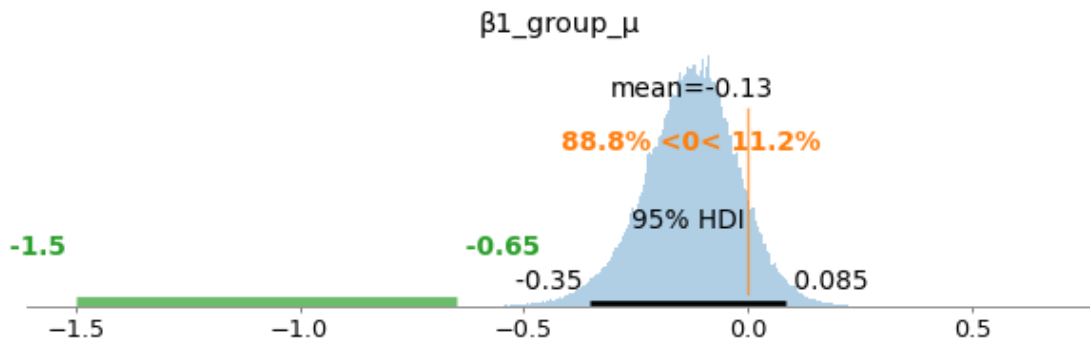
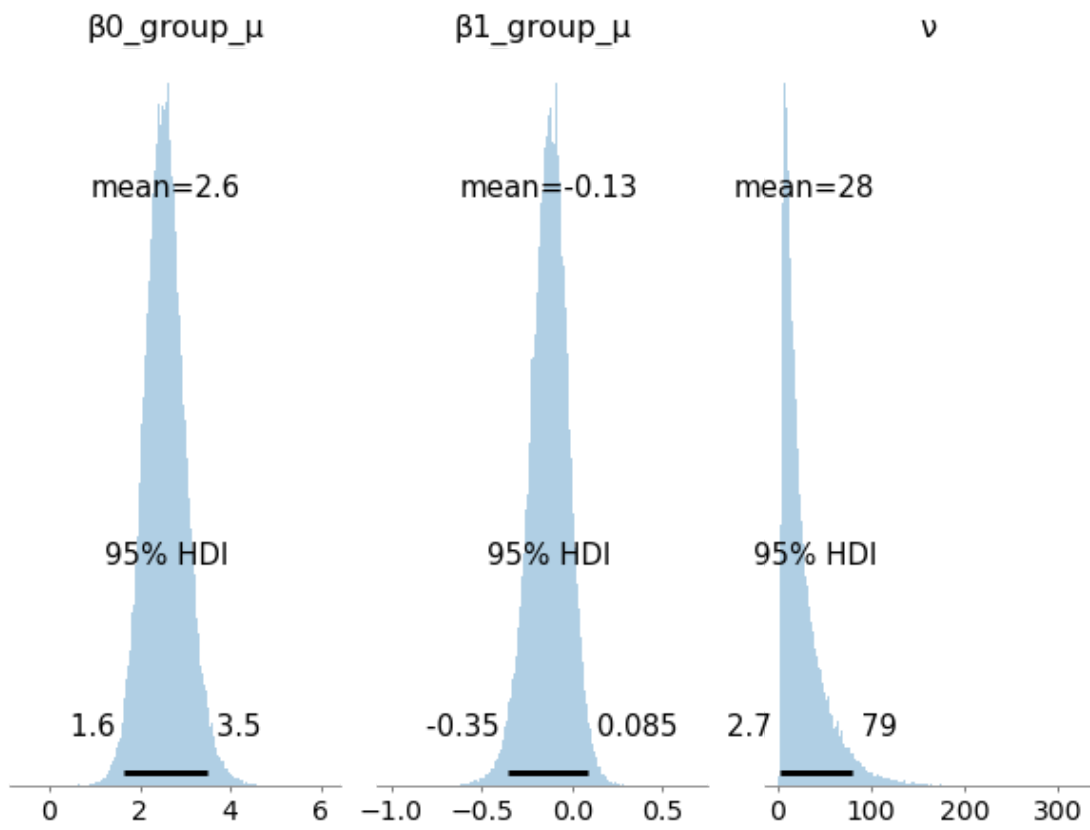
The effective sample size is quite low for many parameters including the slope and intercept of the group. Ess bulk / 200,000:

- $B0_{\text{group}_\mu}$ - 53829
- $B1_{\text{group}_\mu}$ - 48506 The mcse is consistently low indicating an effective sampling.

The visual check of convergence gotten with `az.plot_trace` method show that the chains are mostly overlapping with with only small differences around the highest density. As there many black rugplot then there are divergences present. Some steps we have taken to reduce the impact of the divergences include increasing ammount tuned, increasing sample size and trying with an acceptance rate of 0.95 as `pymc3` recommends and 0.99 when that didn't work well enough. Other efforts included decreasing and increasing the `step_size` which unfortunately only had negative effects on ammount of divergences.

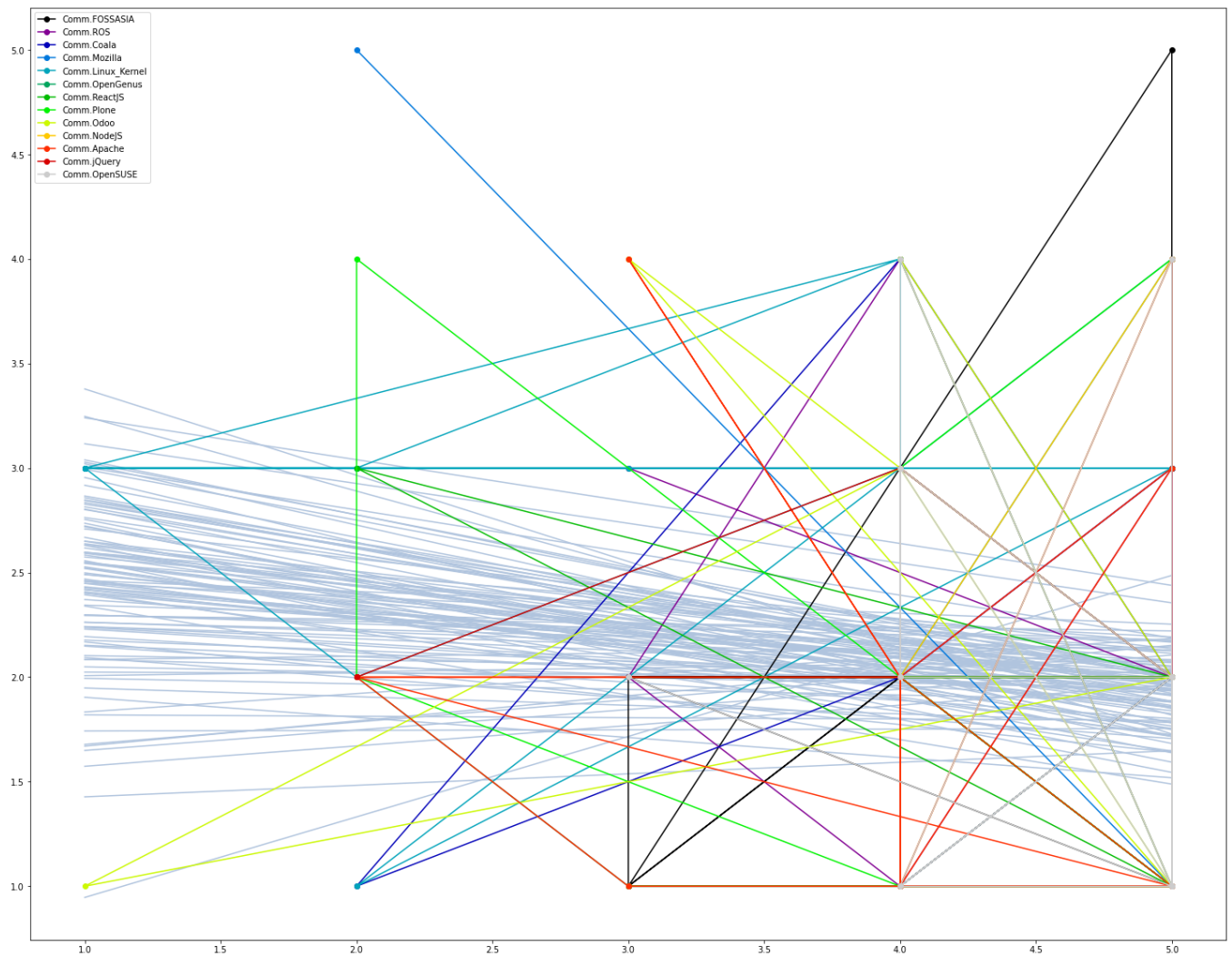
H2 linear model finds

```
In [36]: plot_trace_method1(trace_h2_inferencedata_linear, var_names_h2_linear, rope_h2_linear)
```



```
In [37]: #plot_trace_scatter(trace_h2_linear, [' $\beta_0$ _group_μ', ' $\beta_1$ _group_μ'], 8, 5)
```

```
In [38]: linFunction = lambda xprime, i: trace_h2_linear[i][' $\beta_0$ _group_μ']+trace_h2_linear[i][' $\beta_1$ _group_μ']*  
plot_all_data(linFunction)
```



```
In [39]: linFunction = lambda xprime, i, com_id: trace_h2_linear[i][' $\beta_0$ '][com_id]+trace_h2_linear[i][' $\beta_1$ ']  
plot_individual(trace_h2_linear, linFunction)
```

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

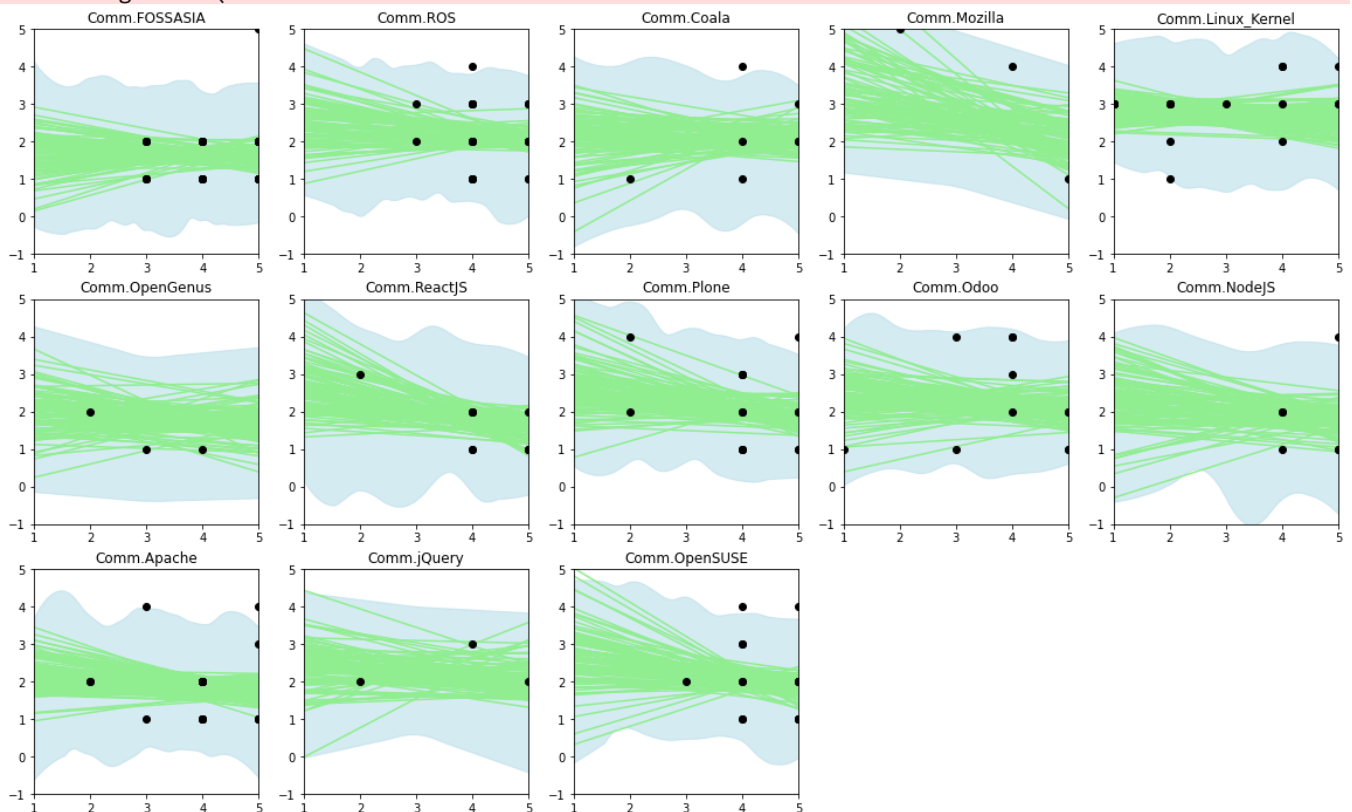
warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for

```
warnings.warn(
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently
interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for
coherence with other functions
    warnings.warn(
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently
interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for
coherence with other functions
    warnings.warn(
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently
interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for
coherence with other functions
    warnings.warn(
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently
interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for
coherence with other functions
    warnings.warn(
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently
interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for
coherence with other functions
    warnings.warn(
```



The decision rules for the acceptance is that the mean of answers for V29 and V31 should be highly negatively correlated.

- The 95% HDI of the slope value for the group lies between -0.34 and 0.096, meaning it rejects the rope from -inf to -0.65 and thus there isn't a big enough linear dependency to accept the hypothesis.
- For almost every community the 95% HDI lies completely outside the rope. For the 2 that don't completely reject

it the result is inconclusive as the 95% HDI and the rope have a minor overlap. Therefore it can be accepted that all communities don't show either a protective or equitable style of governance for PRs.

The acceptance/rejection only matters if the model actually captures the data, which the large model for all the communities seem indicate it does poorly. Looking at the individual models the data points does appear to be mostly inside the blue ranges, so it does appear to be a general trend line with some predictive capabilities. The range of the models are however very thick and thus isn't precise when predicting. The uncertainty of the models could be related to the few datapoints present in the data set. When looking at some of the green traces predicted many of the data points aren't being represented.

Quadratic Model

In [40]:

```
with pm.Model() as model_h2_quadratic:
    ζ0_group_μ = pm.Normal('ζ0_group_μ', mu=0, sigma=10)
    ζ1_group_μ = pm.Normal('ζ1_group_μ', mu=0, sigma=10)
    ζ2_group_μ = pm.Normal('ζ2_group_μ', mu=0, sigma=10)

    ζ0_group_σ = pm.Uniform('ζ0_group_σ', lower=1/1000, upper=1000)
    ζ1_group_σ = pm.Uniform('ζ1_group_σ', lower=1/1000, upper=1000)
    ζ2_group_σ = pm.Uniform('ζ2_group_σ', lower=1/1000, upper=1000)

    ζσ = pm.Uniform('ζσ', lower=1/1000, upper=1000)

    v_minus_one = pm.Exponential('v_minus_one', lam=1/29)
    v = pm.Deterministic('v', v_minus_one+1)

    ζ0 = pm.Normal('ζ0', mu=ζ0_group_μ, sigma=ζ0_group_σ, shape=len(communities))
    ζ1 = pm.Normal('ζ1', mu=ζ1_group_μ, sigma=ζ1_group_σ, shape=len(communities))
    ζ2 = pm.Normal('ζ2', mu=ζ2_group_μ, sigma=ζ2_group_σ, shape=len(communities))

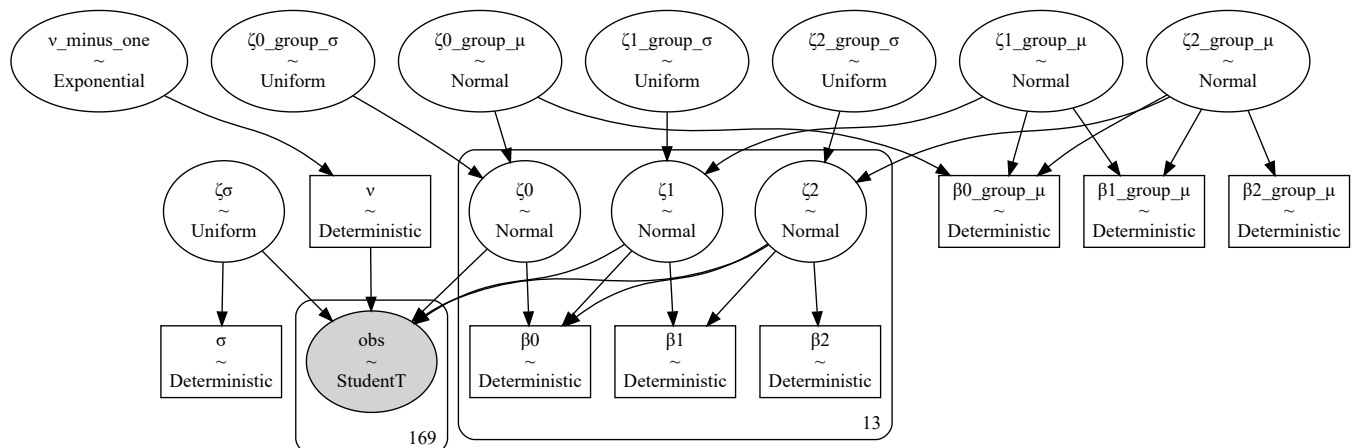
    pm.StudentT('obs',
                nu=v,
                mu=ζ0[idxs]+ζ1[idxs]*V29+ζ2[idxs]*V29**2,
                sigma=ζσ,
                observed=V31)

# Transform Data
β2 = pm.Deterministic('β2', ζ2*sd_31/(sd_29**2))
β1 = pm.Deterministic('β1', ζ1*sd_31/sd_29 - 2*ζ2*m_29*sd_31/(sd_29**2))
β0 = pm.Deterministic('β0', ζ0*sd_31+m_31-ζ1*m_29*sd_31/sd_29+ζ2*(m_29**2)*sd_31/(sd_29**2))

β2_group_μ = pm.Deterministic('β2_group_μ', ζ2_group_μ*sd_31/(sd_29**2))
β1_group_μ = pm.Deterministic('β1_group_μ', ζ1_group_μ*sd_31/sd_29 - 2*ζ2_group_μ*m_29*sd_31/(sd_29**2))
β0_group_μ = pm.Deterministic('β0_group_μ', ζ0_group_μ*sd_31+m_31-ζ1_group_μ*m_29*sd_31/sd_29+ζ2_group_μ*(m_29**2)*sd_31/(sd_29**2))

σ = pm.Deterministic('σ', ζσ*sd_31)
pm.model_to_graphviz(model_h2_quadratic)
```

Out[40]:



Model Arguments

The quadratic models express the relationship of the style with a quadratic equation.

$$V29 = \beta_0 + \beta_1 * V31 + \beta_2 * (V31)^2$$

It introduces an additional parameter, the quadratic coefficient β_2 and when this coefficient is 0, it can also fit what the linear model can. The distributions used here are the same ones used in the linear model.

The data from the model is standardized by: solving for y in the formula:

$$(y-M_y)/SD_y = z_y = \zeta_0 + \zeta_1 * z_x + \zeta_2 * (z_x)^2$$

$$z_x = (x-M_x)/SD_x$$

H2 quadratic model, sampling

In [50]:

```
trace_h2_quadratic = getTrace(folderName_h2_quadratic, model_h2_quadratic, resample_h2_quadratic,
trace_h2_inferencedata_quadratic = getInferenceData(trace_h2_quadratic, model_h2_quadratic)
```

Sequential sampling (4 chains in 1 job)

NUTS: [ζ_2 , ζ_1 , ζ_0 , $v_{\text{minus_one}}$, $\zeta\sigma$, $\zeta_2_{\text{group_}\sigma}$, $\zeta_1_{\text{group_}\sigma}$, $\zeta_0_{\text{group_}\sigma}$, $\zeta_2_{\text{group_}\mu}$, $\zeta_1_{\text{group_}\mu}$, $\zeta_0_{\text{group_}\mu}$]

100.00% [55000/55000 06:56<00:00 Sampling chain 0, 2,179 divergences]

100.00% [55000/55000 15:45<00:00 Sampling chain 1, 2,038 divergences]

100.00% [55000/55000 10:07<00:00 Sampling chain 2, 1,018 divergences]

100.00% [55000/55000 11:06<00:00 Sampling chain 3, 1,381 divergences]

Sampling 4 chains for 5_000 tune and 50_000 draw iterations (20_000 + 200_000 draws total) took 26 37 seconds.

There were 2179 divergences after tuning. Increase ``target_accept`` or reparameterize.

The acceptance probability does not match the target. It is 0.9051967529080067, but should be close to 0.95. Try to increase the number of tuning steps.

There were 4217 divergences after tuning. Increase ``target_accept`` or reparameterize.

There were 5235 divergences after tuning. Increase ``target_accept`` or reparameterize.

There were 6616 divergences after tuning. Increase ``target_accept`` or reparameterize.

The number of effective samples is smaller than 10% for some parameters.

In [51]:

```
az.summary(trace_h2_quadratic) if h2_do_quadratic else None
```

C:\ProgramData\Miniconda3\lib\site-packages\arviz\data\io_pymc3.py:87: FutureWarning: Using ``from_pymc3`` without the model will be deprecated in a future release. Not using the model will return less accurate and less useful results. Make sure you use the model argument or call `from_pymc3` with in a model context.

warnings.warn(

Out[51]:

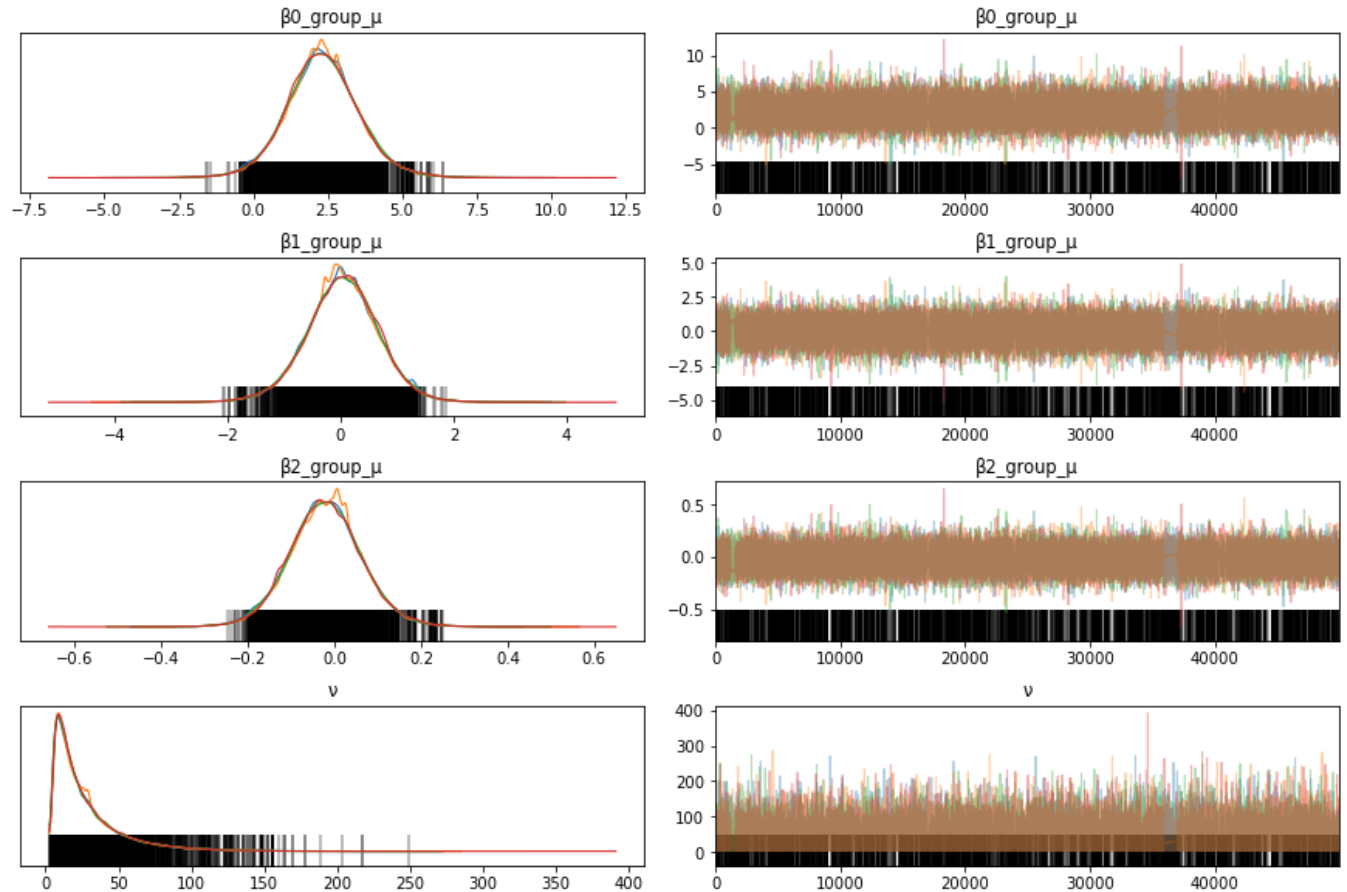
	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_mean	ess_sd	ess_bulk	ess_tail	r_hat
$\zeta_0_{\text{group_}\mu}$	0.020	0.171	-0.303	0.345	0.001	0.001	25779.0	25779.0	25582.0	25019.0	1.0
$\zeta_1_{\text{group_}\mu}$	-0.157	0.138	-0.418	0.100	0.001	0.001	30329.0	30329.0	29641.0	59413.0	1.0
$\zeta_2_{\text{group_}\mu}$	-0.025	0.098	-0.209	0.160	0.001	0.000	29039.0	29039.0	28274.0	39730.0	1.0
$\zeta_0[0]$	-0.359	0.188	-0.718	-0.008	0.001	0.001	51326.0	51326.0	51113.0	80206.0	1.0
$\zeta_0[1]$	0.106	0.189	-0.238	0.473	0.001	0.001	38643.0	35144.0	39081.0	42829.0	1.0
...
$\beta_0[12]$	2.009	2.603	-3.119	6.990	0.010	0.008	64889.0	58518.0	53498.0	78889.0	1.0
$\beta_2_{\text{group_}\mu}$	-0.022	0.085	-0.181	0.139	0.000	0.000	29039.0	29039.0	28274.0	39730.0	1.0
$\beta_1_{\text{group_}\mu}$	0.025	0.644	-1.167	1.267	0.003	0.002	33950.0	33950.0	32752.0	44663.0	1.0
$\beta_0_{\text{group_}\mu}$	2.333	1.232	0.012	4.694	0.006	0.004	46504.0	46504.0	44332.0	52001.0	1.0

	mean	sd	hdi_3%	hdi_97%	mcse_mean	mcse_sd	ess_mean	ess_sd	ess_bulk	ess_tail	r_hat
σ	0.869	0.074	0.728	1.007	0.000	0.000	44496.0	44496.0	44360.0	72149.0	1.0

91 rows × 11 columns

In [52]:

```
var_names_h2_quadratic=['β0_group_μ', 'β1_group_μ', 'β2_group_μ', 'v']
rope_h2_linear_quadratic = [("β2_group_μ", (-0.05, 0.05)), ("β2", (-0.05, 0.05), 15, 10)]
plot_trace_method2(trace_h2_quadratic, model_h2_quadratic, var_names_h2_quadratic)
```



Sampling effectiveness

Like with the sampling for the linear model the r_{hat} and $mcse$ is small indicating an effective sampling.

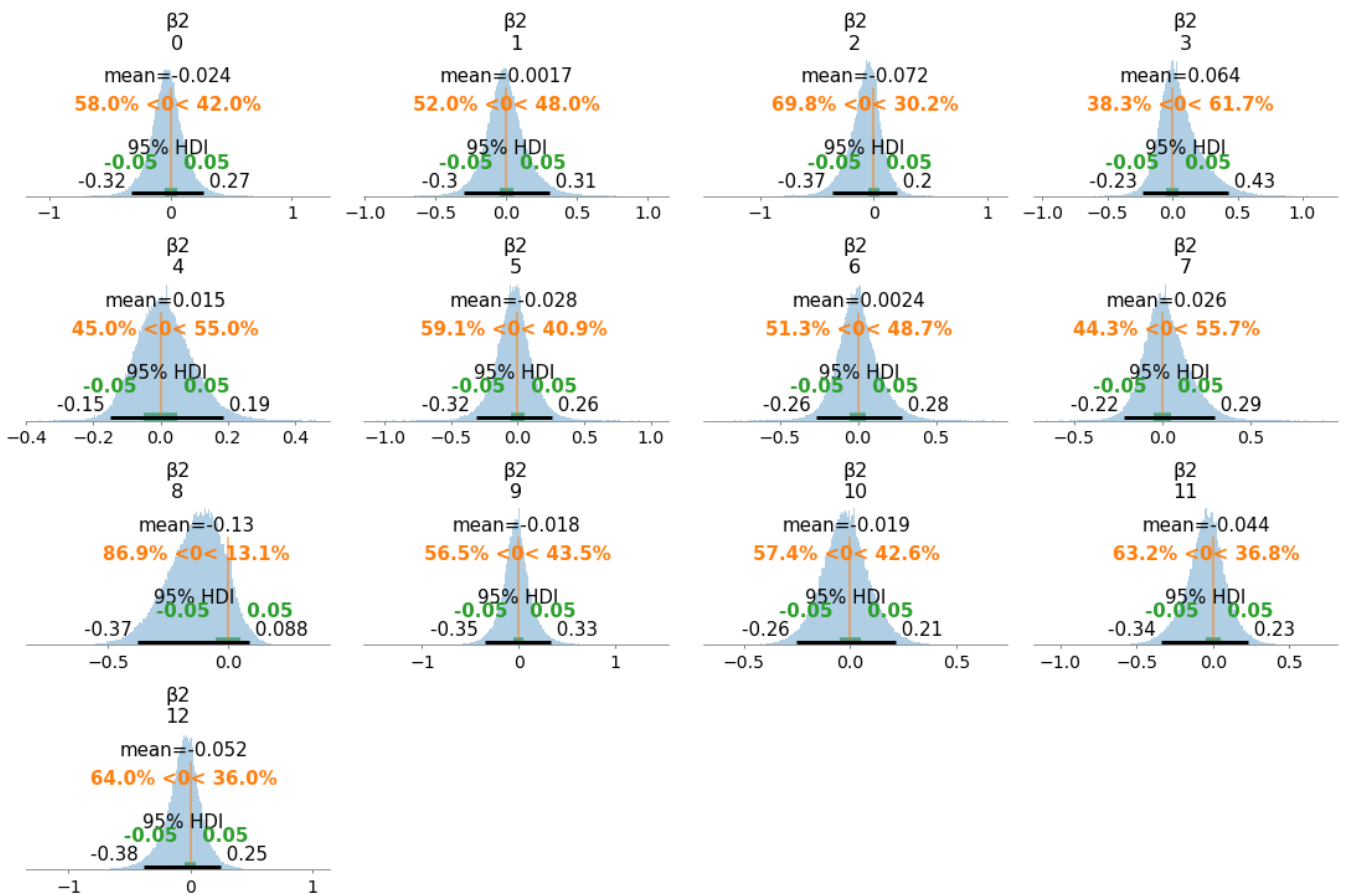
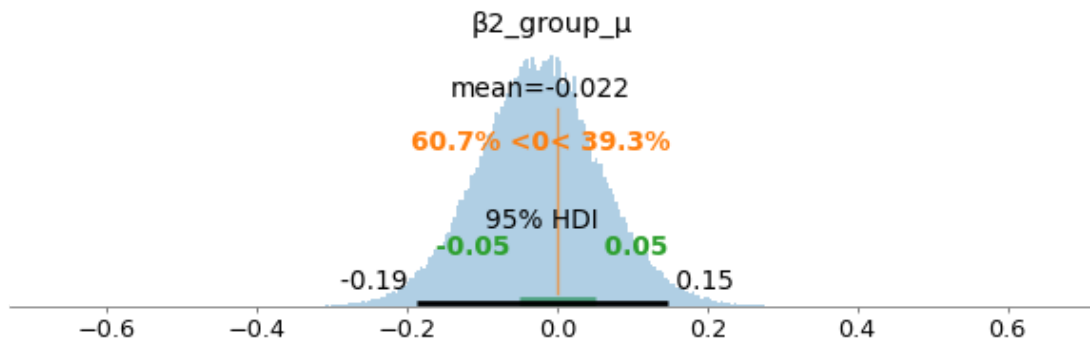
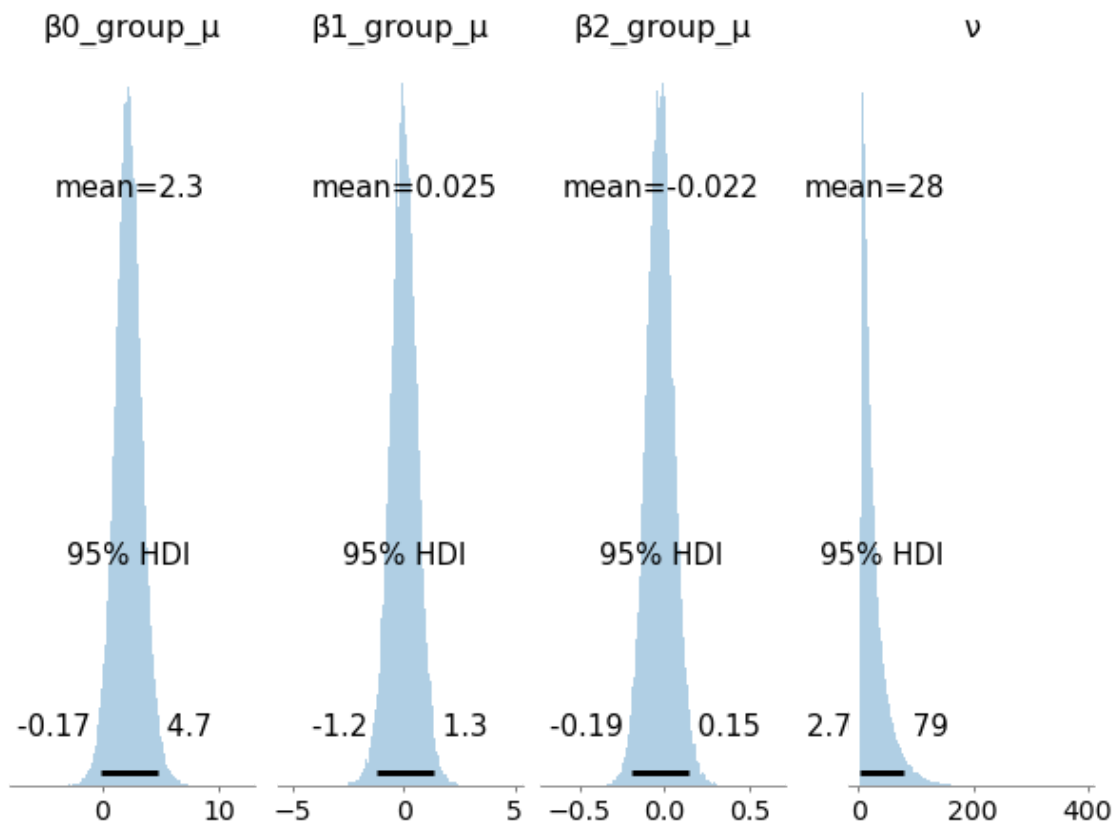
The effective sample size is still high being above 80_000 for the most of the variables. for the 3 coefficients for the group, despite being smaller, they are still all above 28_000.

Unfortunately the divergences for this sampling is quite high being above 1_000 for all chains. Visually, despite some few spikes, the chains appear to be overlapping nicely.

H2 quadratic model finds

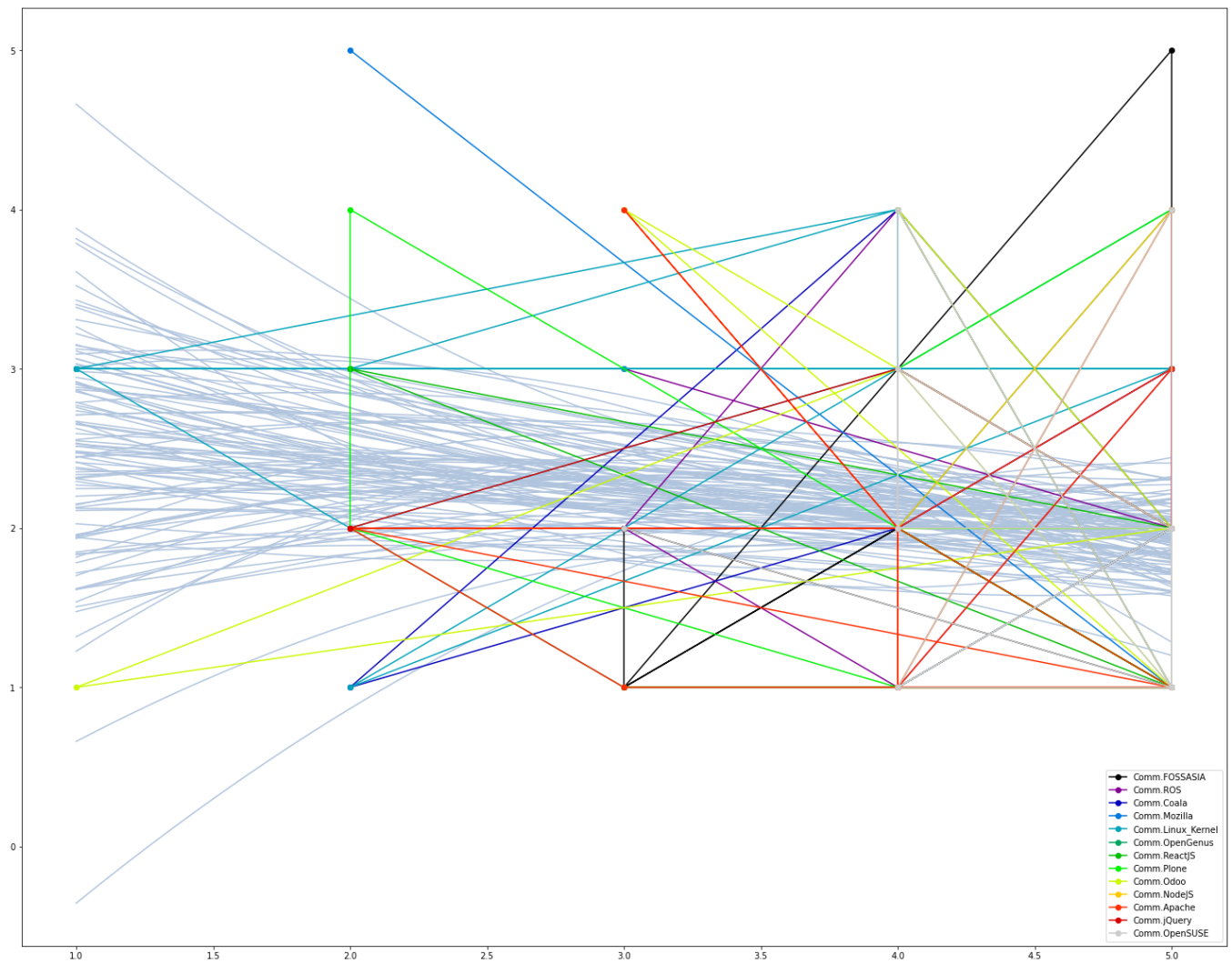
In [53]:

```
plot_trace_method1(trace_h2_inferencedata_quadratic, var_names_h2_quadratic, rope_h2_linear_quadra
```




```
In [54]: #plot_trace_scatter(trace_h2_quadratic, ['θ0_group_μ', 'θ1_group_μ', 'θ2_group_μ'], 8, 5)
```

```
In [55]: quadraticFunction = lambda xprime, i: trace_h2_quadratic[i]['β0_group_μ']+trace_h2_quadratic[i]['β1_group_μ']*xprime[0]+trace_h2_quadratic[i]['β2_group_μ']*xprime[1]  
plot_all_data(quadraticFunction)
```



```
In [56]: quadraticFunction = lambda xprime, i, com_id: trace_h2_quadratic[i]['β0_group_μ']+trace_h2_quadratic[i]['β1_group_μ']*xprime[0]+trace_h2_quadratic[i]['β2_group_μ']*xprime[1]  
plot_individual(trace_h2_quadratic, quadraticFunction)
```

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

warnings.warn(

C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions

coherence with other functions

```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

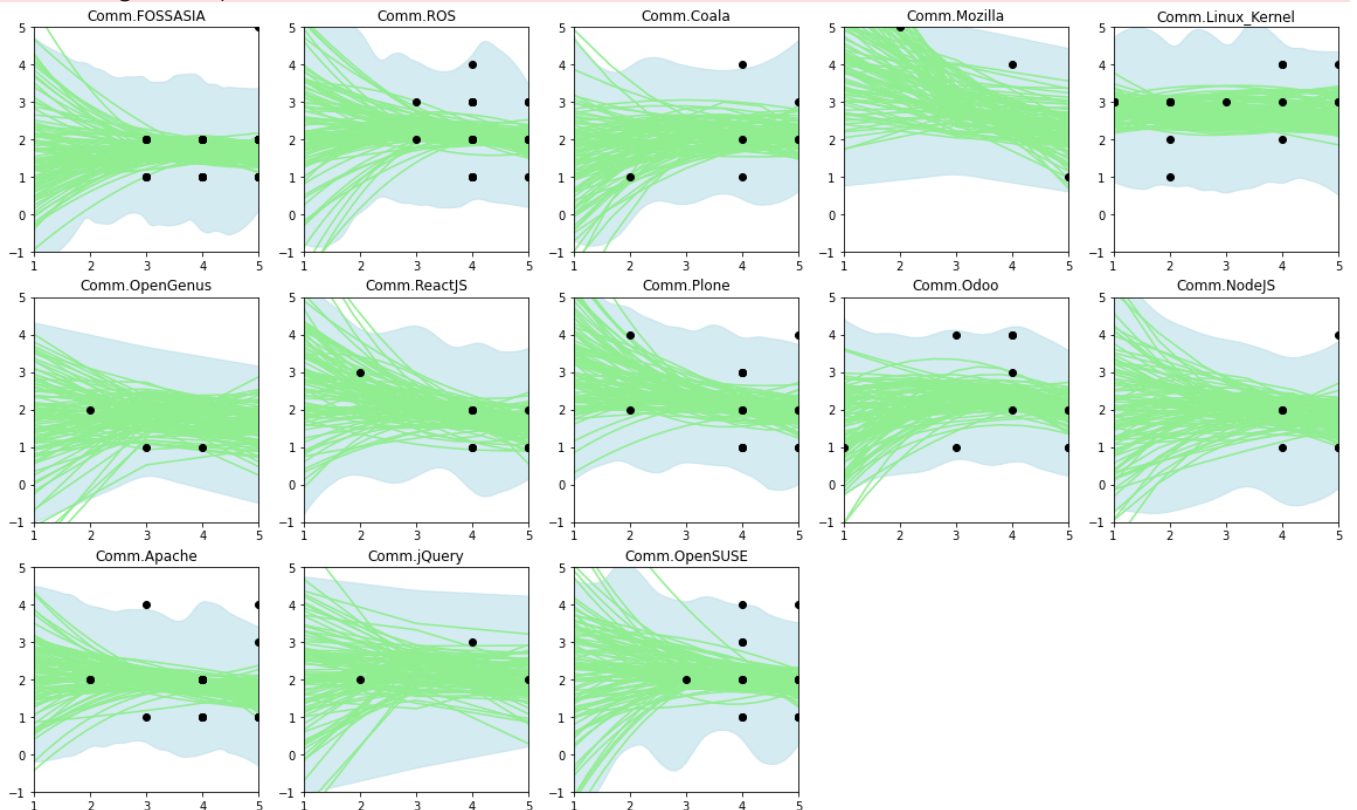
```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

```
warnings.warn(
```

```
C:\ProgramData\Miniconda3\lib\site-packages\arviz\stats\stats.py:484: FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
```

```
warnings.warn(
```



H2 quadratic model - Acceptance / Rejection

If the credible values β_2 in posterior are not close to 0, then we can conclude that the linear model was not adequate. For this the rope chosen was 0 ± 0.05 , as it then at least have an effect of 1, $1 = (25 * 0.05) - (1 * 0.05)$. This means that if the rope is accepted, then the quadratic model provides an insignificant amount of more information.

For the group coefficient $B2_group_mu$ and the individual coefficients $B2$ it can be observed that the entire rope is within the 95% HDI, and thus it can be rejected that the quadratic provides only an insignificant amount of more information.

Visual:

Looking at the individual models the data points appear to be mostly inside the blue ranges, so it does appear to be a general trend line. Although the range of the models have become a little more narrow thus more

precise when predicting, it is still broad and imprecise. When comparing which datapoints the quadratic trace can predict with what the linear is able to, it becomes clear that it doesn't represent the data to a larger extent than what the linear model is capable of doing.

Even when adding the more precise quadratic model there still doesn't appear to be a negative slope which would be needed to conclude the hypothesis.

Warnings

sampling related

- There were 2 divergences after tuning. Increase 'target_accept' or reparameterize.
This problem as described above have been mitigated by increasing trace size, increasing tuning, and adding higher value to the 'target_accept' parameter. Higher 'target_accept' leads to smaller 'step_size' and also increases sampling time.
- There were 11436 divergences after tuning. Increase 'target_accept' or reparameterize.
The acceptance probability does not match the target. It is 0.85120956111205, but should be close to 0.95. Try to increase the number of tuning steps.
The number of effective samples is smaller than 10% for some parameters.
Setting the tuning size to a high amount like 20_000 removed most of the disjoint peaks in the trace graphs, but the ESS was halved. Thus, the number of tuning steps was reduced back to 5_000.

Plotting

- FutureWarning: Using 'from_pymc3' without the model will be deprecated in a future release. Not using the model will return less accurate and less useful results. Make sure you use the model argument or call from_pymc3 within a model context.
This is just a warning for future versions, but making the suggested change didn't suppress the warning.
- FutureWarning: hdi currently interprets 2d data as (draw, shape) but this will change in a future release to (chain, draw) for coherence with other functions
This is also a warning for future version, and it doesn't suggest a way to suppress it.

Division of group work

The vast majority of the code was made in full collaboration, with only a few plots and restructuring done individually. In regard to analyzing and arguing for models, sampling and so on the different sections was at first split up, but after rewriting and going through it would be erroneous to declare one had more responsibility than the other.

In []: