## **Lazy Streams**

The main file to work in this week is located in src/main/scala/adpro/Stream.scala. As usual solve the exercises in order, while executing the test suite. There are markings in the file where to place all the functions that I ask for.

The test suite and the exercise template assume that you are using Scala standard library immutable lists; not the lists implemented the last week. The test suite is weaker this week, but it should be sufficiently good to develop and test answers to the questions below. We will develop a proper test suite for this set of exercises in a later homework. For some exercises, the tests suites are missing, because it was impossible to write them without revealing the interface that you need to design. Feel free to add these tests, but do not hand them in.

Hand in: src/main/scala/adpro/Stream.scala

**Exercise 1.** Define functions from and to that generate streams of natural numbers above (and below) a given natural number n. The function from should create a stream producing all numbers larger than n, starting from n, increasing. The function to should create a stream producing all numbers smaller than n, starting from n, decreasing. In the source file, this exercise is in the very bottom, in the companion object of Stream.

```
def from (n: Int): Stream[Int]
def to (n: Int): Stream[Int]
```

Use from to create a value naturals: Stream[Int] representing all natural numbers in order.

**Exercise 2.** Write a function to convert a Stream to a List, which will force its evaluation and let you look at it in the REPL. You can convert to the regular List type in the standard library. You can place this and other functions that operate on a Stream inside the Stream trait.

```
def toList: List[A]
```

Test this function using the factory of streams to build finite streams and converting the to lists (to see whether they yield expected lists). Then create a few finite streams of integers using to (n) from the previous exercise, and convert them to lists.<sup>1</sup>

Exercise 3. Write the function take(n) for returning the first n elements of a Stream, and drop(n) for skipping the first n elements of a Stream.

```
def take (n: Int): Stream[A]
def drop (n: Int): Stream[A]
```

For fluency, try the following test case in REPL (should terminate with no memory exceptions and very fast). Why does it terminate without exception? Answer this question as a comment in the Scala file under the same exercise number.

```
naturals.take (100000000).drop (41).take (10).toList
```

**Exercise 4.** Write the function takeWhile (p) for returning all starting elements of a Stream that match the given predicate p. Use pattern matching to implement it.

```
def takeWhile(p: A => Boolean): Stream[A]
```

<sup>&</sup>lt;sup>1</sup>Exercise 5.1 [Chiusano, Bjarnason 2014]

Test your implementation on the following test case:

```
naturals.takeWhile { \_ < 1000000000 }.drop (100).take (50).toList
```

It should terminate very fast, with no exceptions thrown. Why?<sup>2</sup>

**Exercise 5.** Implement forAll (p), which checks that all elements in this Stream satisfy a given predicate. Terminate the traversal as soon as it encounters a non-matching value.

```
def forAll(p: A => Boolean): Boolean
```

We use the following test case for forAll: naturals.forAll ( < 0)

If we used this one, it would be crashing: naturals.forAll ( >=0). Explain why.

Recall that exists has already been implemented before (in the book). Both forAll and exists are a bit strange for infinite streams; you should not use them unless you know the result; but once you know the result there is no need to use them. They are fine to use on finite streams. Why?<sup>3</sup>

Exercise 6[+]. Use foldRight to implement takeWhile. Reuse the test case from Exercise 4.4

**Exercise 7.** Implement headOption using foldRight.

**Exercise 8[+].** Implement the following functions. The task involves designing their types. Implement map, filter, append, and flatMap using foldRight. The append method should be non-strict in its argument.<sup>5</sup>

- 1. map (f), using an analogous signature to the one from lists

  Test case: naturals.map (\_\*2).drop (30).take (50).toList
- 2. filter (p)

Test case: naturals.drop (42).filter (\_%2 ==0).take (30).toList

append (that)

This one requires sorting out the variance of type parameters carefully. You may find it easier to implement it as a function in the companion object first.

```
Test case: naturals.append (naturals) (useless, but should not crash)
```

Test case: naturals.take(10).append(naturals).take(20).toList

4. flatMap

```
Test case: naturals.flatMap (to _).take (100).toList
Test case: naturals.flatMap (x =>from (x)).take (100).toList
```

There are no automatic tests for this exercise—because the types are not already present in the template file, the test suite would be failing to compile, if we wrote them. This would make the test suite useless for the earlier exercises.

Exercise 9[+]. The book presents the following implementation for find:

```
def find (p :A => Boolean) :Option[A]= this.filter(p).headOption
```

Explain why this implementation is suitable (efficient) for streams and would not be optimal for lists.

```
<sup>2</sup>Exercise 5.3 [Chiusano, Bjarnason 2014]
```

<sup>&</sup>lt;sup>3</sup>Exercise 5.4 [Chiusano, Biarnason 2014]

<sup>&</sup>lt;sup>4</sup>Exercise 5.5 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>5</sup>Exercise 5.7 [Chiusano, Bjarnason 2014]

Exercise 10[+]. Compute a lazy stream of Fibonacci numbers fibs: 0, 1, 1, 2, 3, 5, 8, and so on. It can be done with functions available so far. Test it be translating to List a finite prefix of fibs, or a finite prefix of an infinite suffix.<sup>6</sup> Again, no ready-made tests, because the types are not prescribed.

**Exercise 11.** Write a more general stream-building function called unfold. It takes an initial state, and a function for producing both the next state and the next value in the generated stream.

```
def unfold[A, S] (z: S) (f: S => Option[(A, S)]): Stream[A]
```

If you solve it *without* using pattern matching, then you obtain a particularly concise solution, that combines aspects of this and last week's material.

You can test this function by unfolding the stream of natural numbers and checking whether its finite prefix is equal to the corresponding prefix of naturals.<sup>7</sup>

The exercise is placed in the companion object of Stream, in the bottom of Stream.scala.

## Exercise 12. Write fib and from in terms of unfold. Use these test cases:

```
from(1).take(1000000000).drop (41).take(10).toList ==
from1(1).take(100000000).drop (41).take(10).toList and
fibs1.take(100).toList ==fibs.take(100).toList,
```

where identifiers suffixed with 1 refer to the new versions of the functions.<sup>8</sup> At the tests to StreamSpec.scala following how other tests are implemented in the same file.

## Exercise 13. Use unfold to implement map, take, takeWhile, and zipWith.<sup>9</sup>

You can reuse test-cases from earlier exercises, or devise new ones. Remember to test with infinite streams. Infinite streams are a good way whether your implementations are indeed non-strict.

This is a good test case for zipWith:

```
naturals.zipWith[Int,Int] (_+_) (naturals).take(200000000).take(20).toList
```

Note that there is a choice whether the operation used by zipWith is strict or not. The lazy (by-name) is more general as it allows using efficiently functions that ignore the first (or the second) operand if the other one is a special case (so if you zip with || or &&). On the other hand, I experienced some trouble using strict functions in this context. You can choose yourself, what you implement.

What should be the result of this?

```
naturals.map (_%2==0).zipWith[Boolean,Boolean] (_||_) (naturals.map (_%2==1))
take(10).toList
```

Don't get tricked into just running this and seeing the result. There might be a bug in your implementation, so convince yourself, what the results of these two test cases should be.

<sup>&</sup>lt;sup>6</sup>Exercise 5.10 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>7</sup>Exercise 5.11 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>8</sup>Exercise 5.12 [Chiusano, Bjarnason 2014]

<sup>&</sup>lt;sup>9</sup>Exercise 5.13 [Chiusano, Bjarnason 2014]