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# **Advanced** Programming

**State Monad** 

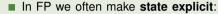




#### **Does FP Eliminate State?**

Picture: you after three weeks of ADPRO

- Variables and fields are state
- Program **stack**&heap are state
- Databases are state
- Program counter is state!
- Variable assignments set state
- Variable accesses read state
- Loops must change state
- Exceptions modify program counter and stack
- We have disallowed almost all of these?



- Converted loops to recursive functions
- A function is a state transform
- Arguments are the state explicitly
- No other implicit, hidden state that can be changed by others
- Today, a pure pattern for state transforms:
  - Allows to bide the state way to encode state
    - Allows to hide the state, make it implicit like in imperative programming
  - Still the state is **encapsulated** in a well defined value
  - Still no other encapsulated state that can be changed by others



- RNG: a random integer generator; we maintain the state
- Rand[A]: a random A generator; we hide the RNG in the state
- State[S,A]: a general pattern for stateful computations producing A, where the state is of type S

## **AGENDA**

## A Typical Stateful Imperative API

```
1 var rng = new scala.Util.Random
2
3 // returns a random number form 0 to 5
4 def rollDie: Int = rng.nextInt(6)
```

- We call rollDie and observe a value 5
- Mentimeter: What is the result of rollDie + rollDie?
- What does it tell us about referential transparency of rollDie?
- rng is an external, implicit state, that can be changed by others
- To make rollDie referentially transparent, make the state explicit

### **Converting RNG to explicit state**

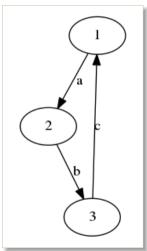
```
■ We had: RNG.nextInt: () =>Int■ Lets return new state explicitly, instead of modifying old (RT)
```

```
trait RNG { def nextInt: (Int, RNG) }
object RNG{
  def nextInt (rng: RNG) : (Int, RNG) = rng.nextInt
}
```

- In general a function: State =>(Output, State)
- Wrap this as case class State[S,+A] (run: S =>(A,S) )
- So RNG becomes State[RNG,Int] { run =RNG.nextInt }
- Intuition 1: Automaton or Transition would be better names than State
- Intuition 2: step would be a better name than run

### **Consider a Simple Automaton**

#### Stateful by definition



```
var state = 1
while (true)
  state match {
    case 1 => { print "a"; state = 2 }
    case 2 => { print "b"; state = 3 }
    case 3 => { print "c"; state = 1 }
```

```
def step (State: Int): (String,Int) = state match {
case 1 = > ("a", 2)
case 2 = > ("b", 3)
case 3 = > ("c", 1)
```

- We need a simple **recursive loop** to run the step like above
- One general general loop for the State type
- This automaton as an **instance of** State: State[Int,String] (step)

#### **Exercise**

Use 5 minutes to write down an instance of State implementing this imperative code

```
x=0
while (true) {
 println (x)
 x+=1
```

## Anything stateful maps to the state pattern

Recap

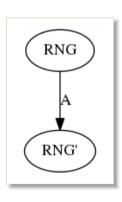
- Random number generators (state: RNG seed)
- Websites with modality (session state)
- Database backed applications (DB state)
- Communication protocols (protocol state)
- etc.

#### Random Number Generator as an Instance of State

type Rand[A] =State[RNG,A]

- RNG is the state of the random generator (usually some large number encapsulated)
- The textbook gives a simple implementation of RNG based on multiplication with large primes module 64 bits
- Rand[A] is a computation that we can run, then it will produce a random A and a new state RNG
- Another useful intuition: Rand[A] is a generator of random A's
- Or even just a "random A"
- Question:

What stream can we unfold from State[RNG, Int] (\_.nextInt)?



## How do I use this generator of random numbers?

```
type Rand[A] =State[RNG.A]
val r : Rand[Int] =SimpleRNG (42)
val(r1.i) = r.run
```

- Simplering is the book's concrete implementation of the RNG trait
- 42 is the initial seed (state)
- (r1,i) is a new state and a random number
- **Question:** How do I get the next random number?
- Question: What happens if I call r.run again?

#### What can we do with Automata/State?

State is a monad, similar key operations as for List, Option, and Stream

```
def map[S.A.B] (s: State[S,A]) (f: A =>B): State[S,B]
```

Can use this to generate even numbers:

```
val even: Rand[Int] =map[Int] (r) (n =>n * 2)
```

## Automata can be composed [1/2]

flatMap can be used to compose generators:

```
def flatMap[S,A,B] (s: State[S,A]) (f : A =>State[S,B]): State[S,B]
```

In our context of generators:

```
def flatMap[A,B] (r :Rand[A]) (f =>Rand[B]) : Rand[B] =
  flatMap[A,B] (r: State[RNG,A]) (f :State[RNG,B]) :State[RNG,B]
```

flatMap can compose generators (compute a random size list of random even integers):

```
val int :Rand[Int] = ... (assume vou have it)
val ints: Int =>Rand[List[Int]] =... (assume creates a random list of given length)
val ns :Rand[List[Int]] =int.flatMap( x =>ints(x).map (xs =>xs.map ( *2))
```

the state RNG passed implicitly; size generated with different state than each number

## Automata can be composed [2/2]

The map2 function can compute a zipping of two automata over the same state space for us:

```
map2 [S,A,B,C] (sa: State[S,A]) (sb: State[S,B]) (f: (A,B)=>C) :State[S,C]
```

Could be used to create a product automaton

- interleaving computations, then C is Either[A,B]
- synchronizing two computations, then c is (A,B)

More fun in exercises :)

#### Next week

- Next week we will design a parallel computation library, in purely functional style
- This shows (a bit) how Akka is implemented
- In two weeks, we will use the generators of random numbers to implement a modern testing framework
- So: keep reading the chapters and solve the exercises!